

# Finite element analysis of concrete filled lean duplex stainless steel columns

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## Abstract

In recent years, a new low nickel content stainless steel (EN 1.4162) commonly referred as 'lean duplex stainless steel' has been developed, which has over two times the tensile strength of the more familiar austenitic stainless steel but at approximately half the cost. This paper presents the finite element analysis of concrete filled lean duplex stainless steel columns subjected to concentric axial compression. To predict the performance of this form of concrete filled composite columns, a finite element model was developed and finite element analyses were conducted. The finite element model was validated through comparisons of the results obtained from the experimental study. A parametric study was conducted to examine the effect of various parameters such as section size, wall thickness, infill concrete strength, etc. on the overall behaviour and compressive resistance of this form of composite columns. Through both experimental and numerical studies, the merits of using lean duplex stainless steel hollow sections in concrete filled composite columns are highlighted. In addition, a new formula based on the Eurocode 4 is proposed to predict the cross-section capacity of the concrete filled lean duplex stainless steel composite columns subjected to axial compression.

**Keywords:** *Lean duplex stainless steel; composite columns; axial compression; finite element model; cross-section capacity; Eurocode 4*

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## 1. Introduction

Concrete filled steel tubes (CFSTs) have been used for high-rise buildings and bridges throughout the world. This increase is due to their advantages in constructability and superiority in strength. CFST columns consist of steel and concrete materials acting together contributed to the higher stiffness and load bearing capacity of these columns. [1]

Austenitic stainless steel is most widely used in the construction industry, however, a recently developed 'lean duplex' stainless steel which contains only 1.5% nickel offers a cheaper alternative. The particular grade used in this study is EN 1.4162, which is generally less expensive than the austenitic counterpart but offers higher strength, while maintaining a reasonable corrosion resistance. Numerous examples of lean duplex used in the construction could be found. Theofanous and Gardner [2] carried out experimental and

numerical studies on the behaviour of lean duplex stainless steel square hollow sections (SHS) and rectangular hollow sections (RHS) subjected to axial compression, to investigate the effects of the sectional shape and wall thickness to the ultimate axial capacity. It was found that lean duplex sections offer superior strength when comparing to the austenitic counterparts, which in turn, provided a significant saving to the material cost.

Huang and Young [3] conducted finite element analysis (FEA) on cold-formed lean duplex stainless steel with square and rectangular hollow sections. An accurate finite element model has been created to simulate the pin-ended cold-formed lean duplex stainless steel short columns. The results showed that Eurocode 3 [4] and the Australian / New Zealand Standard [5] are relatively conservative in predicting the axial capacity of these form of hollow sections. Even though a significant number of researchers had conducted research

on the lean duplex stainless steel sections, there is little research had been carried out on CFST columns with lean duplex stainless steel tubes.

Lam and Giakoumelis [6] evaluated CFST columns under a variety of loading conditions with load applied: 1) on the steel and concrete simultaneously, 2) on the concrete alone and 3) on the concrete and steel with greased interface. The steel grades of S275 and S355 were used and the concrete strength varied from 30 to 100MPa. Results shown when the concrete and steel were loaded concurrently, the tube provided less confinement by comparison to the specimens that were only loaded to the concrete core, similar findings are also reported by Sakino *et al.* [7].

Studies on concrete filled carbon steel rectangular hollow section (RHS) composite columns have shown that width to thickness ratio of the steel elements and the constraining factor have significant influence to the compressive axial capacity and ductility of the concrete filled columns. [8-13] Research into CFST columns with high strength concrete infill has shown that high strength concrete infill provided enhancement in strength but led to reduction in ductility. [14-16] In terms of concrete filled composite columns with stainless steel sections, Uy *et al.* [17] tested 72 stub and 24 slender concrete filled stainless steel columns, with concrete strength varied between 20 to 75MPa, results on the stub column tests have shown that CFST with stainless steel tube has higher residual strength and ductile behaviour when compared to the carbon steel counterpart. An investigation into the behaviour of circular concrete filled lean duplex stainless steel tube using the finite element package ABAQUS [18] was reported by Hassanein *et al.* [19]. However, the FE model was validated using experimental studies on austenitic stainless steel columns carried out by Chang *et al.* [20] and the behaviour especially at the section capacity is quite different. It can be seen that previous research into lean duplex composite columns is relatively limited, little experimental study has been made on concrete filled composite columns with lean duplex stainless steel sections. [21] In the present study, a finite element model is developed and validated against the test results. Parametric studies were carried out over a range of concrete grades and steel thicknesses. The results of the parametric

studies were used and compared with the existing design rule given in Eurocode 4 [22]. On the basis of the comparison, a new design expression based on the Eurocode 4 is proposed.

## 2. Finite element model

### 2.1. General

In this paper, finite element package ABAQUS 6.14 (RIKS method) is used to simulate the concrete filled lean duplex stainless steel stub column tests conducted by Lam *et al.* [21]. Geometry of the columns, materials, interactions, meshes, loading and boundary conditions of the FE model are defined accordingly and are described in the following sections.

The column specimens were subjected to concentric axial compression. Measured dimensions of the specimens are summarized in Table 1, where  $t_f$ ,  $t_c$  denote the wall thickness at flat and corner portions of the stainless steel tube. Note that the tested concrete cube strength is 35.1 MPa, 61.2MPa and 81.0 MPa for the C30, C60 and C80 concrete specified in Table 1, respectively. SC1, SC2 and SC3 refer to square columns with steel tube dimensions of 60×60×3, 80×80×4 and 100×100×4 (unit: mm), respectively.

Table 1. Summarized measured stub column specimens dimensions in paper [21] (mm).

Column ID	$B \times H \times t_f \times t_c \times L$
SC1-C30	60.18×60.49×3.34×3.47×183.5
SC1-C60	59.96×60.34×3.41×3.68×184.5
SC1-C80	59.90×60.27×3.12×3.56×184.5
SC2-C30	80.27×80.16×3.82×4.19×243.5
SC2-C60	80.30×80.10×3.86×3.94×244.5
SC2-C80	80.19×80.42×3.73×4.05×244.5
SC3-C30	102.68×102.72×4.26×4.47×304.5
SC3-C60	102.93×102.52×3.99×4.42×304.5
SC3-C80	102.85×102.60×4.05×4.47×305.0

### 2.2. Steel material

The stress-strain model used for both the flat and corner regions of the lean duplex stainless steel tube in the FE model included of two parts. The first part is linear and up to the proportional limit stress with the measured elastic modulus  $E_0$  (listed in Table 2, Poisson's ratio 0.3). The second part is a converted true stress-strain curve based on tested data, e.g.

0.2% ( $\sigma_{0.2}$ ), 1% proof stresses ( $\sigma_{1.0}$ ), the ultimate stress ( $\sigma_u$ ) and the strain at fracture ( $\epsilon_f$ ) by using Eqs. (1) and (2).

$$\sigma_{true} = \sigma_{nom}(1 + \epsilon_{nom}) \quad (1)$$

$$\epsilon_{ln}^{pl} = \ln(1 + \epsilon_{nom}) - \frac{\sigma_{true}}{E} \quad (2)$$

where  $\sigma_{true}$  and  $\sigma_{nom}$  represent the true and engineering stress, respectively, and  $\epsilon_{ln}^{pl}$  and  $\epsilon_{nom}$  are the logarithmic plastic strain and engineering strain, respectively. The corner properties was extended to a distance of  $2t$  beyond the curved portions of the stainless steel cross-sections, as suggested by Gardner and Nethercot [23].

Table 2. Measured steel material properties.

Section ID	$E_0$ (MPa)	$\sigma_{0.2}$	$\sigma_{1.0}$	$\sigma_u$	$\epsilon_f$ (%)
S1 <sub>flat</sub>	209800	755	819	839	44
S1 <sub>corner</sub>	212400	885	1024	1026	22
S2 <sub>flat</sub>	199900	679	736	773	42
S2 <sub>corner</sub>	210000	731	942	959	24
S3 <sub>flat</sub>	198800	586	632	761	47
S3 <sub>corner</sub>	206000	811	912	917	32

### 2.3. Concrete material

The Drucker–Prager model available in ABAQUS material library was adopted to simulate the behavior of concrete core.

A three-part constitutive model was used to define the material. The first part is assumed as an elastic part up to the proportional limit which is defined as  $0.5f_c$  (concrete cylinder strength, assumed as 0.8 times of the cube strength). The initial modulus of elasticity  $E_c$  is calculated by the empirical equation ACI Committee 318 [24] as given in Eq. (3). Poisson's ratio of concrete is taken as 0.2. The corresponding strain ( $\epsilon_c$ ) is taken as 0.003 [23].

$$E_c = 4700\sqrt{f_c} \quad (3)$$

The second part starts from the proportional limit stress ( $0.5f_c$ ) to the concrete strength ( $f_c$ ). The equation proposed by Saenz [25] was adopted shown as follows (Eq. 4).

$$f = E_c \epsilon / [1 + (R + R_E - 2) \left(\frac{\epsilon}{\epsilon_c}\right) - (2R - 1) \left(\frac{\epsilon}{\epsilon_c}\right)^2 + R \left(\frac{\epsilon}{\epsilon_c}\right)^3] \quad (4)$$

$$\text{where } R_E = \frac{E_c \epsilon_c}{f_c}, R = \frac{R_E(R_\sigma - 1)}{(R_E - 1)^2} - \frac{1}{R_E},$$

$$R_\sigma = R_E = 4 \text{ [26].}$$

The third part is linear and starts from  $f_c$  to  $rkf_c$  while the corresponding strain is  $11\epsilon_c$ . The value of  $r$  is taken as 1.0 and 0.5 for concrete with cube strength of 30MPa and 100MPa, respectively, while linear interpolation is used for cube strength between 30 and 100MPa [16]. The value of  $k$  can be calculated from an empirical equation given by Hu *et al.* [27] in Eq. (5).

$$k = 0.000178 \left(\frac{B}{T}\right)^2 - 0.02492 \left(\frac{B}{T}\right) + 1.2722 \quad (5)$$

for  $17 \ll B/T \ll 70$

### 2.4. Meshes and interfaces

Three-dimensional 8-node solid elements (C3D8) were employed to discretize the concrete-filled square stainless steel stub column models. Generally, a mesh size equals to the tube wall thickness was adopted in the flat portions of the steel columns, while minimum of 3 elements along curvature was used at corners. For concrete core, a mesh size of two times of the wall thickness was used. Two layers of meshes were used in the tube wall thickness direction.

A surface-to-surface based interaction was adopted for the contact between steel tube (slave surface) and concrete core (master surface). In the direction tangential to the surface, the 'penalty' friction with a coefficient of friction equal to 0.3 was used, while 'hard contact' was used for the normal direction. End plates were included in the model to replicate the tests. The concrete was treated as slave surface in the interactions with the end plates.

### 2.5. Loading and boundary conditions

Load was applied axially through a reference point coupled to the top end plate by displacement control method. Both ends of the stub columns were restrained against all degrees of freedom, except for the displacement in the loading direction at the top. To reduce the calculation cost, a quarter model was simulated with symmetry boundaries in two directions.

## 3. Validation of the FE model

The FE model was validated with the load vs. displacement curves, ultimate capacities and failure modes of the concrete-filled lean duplex stainless steel columns tested. The comparison of the test and FEA curves is given in Fig. 1.

The column capacities recorded from tests and extracted from FEA is compared in Table 3. The average ratio of capacities  $N_{Test}/N_{FEA}$  is 0.98, with the standard deviation of 0.04 and the coefficient of variation (COV) of 0.044. The value of  $N_{Test}/N_{FEA}$  ranges from 0.88 to 1.02, within a satisfactory error of 12%. The failure modes observed from tests and predicted from FEA are shown in Fig. 2. It can be seen from the failure shapes and mode of failure (outwards local buckling), acceptable agreement was achieved. The developed FE model is deemed to be capable of predicting both the ultimate compressive strength and failure mode of the concrete-filled lean duplex stainless steel stub columns tested by Lam *et al.* [21].

Table 3. Comparison of test and FEA results.

Column ID	$N_{Test}$ (kN)	$N_{FEA}$ (kN)	$N_{Test}/N_{FEA}$
SC1-C30	739	761	0.97
SC1-C60	759	808	0.94
SC1-C80	790	898	0.88
SC2-C30	1105	1079	1.02
SC2-C60	1160	1143	1.01
SC2-C80	1220	1193	1.02
SC3-C30	1394	1414	0.99
SC3-C60	1493	1519	0.98
SC3-C80	1599	1614	0.99
Average			0.98
Standard Deviation			0.04
Coefficient of Variation			0.044

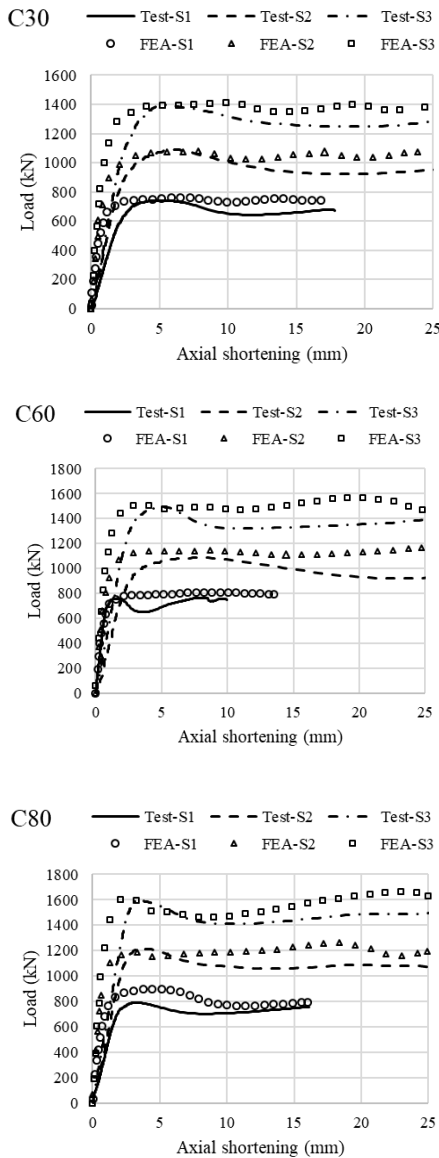


Fig. 1. Comparisons of load vs. displacement curves between test and FEA.

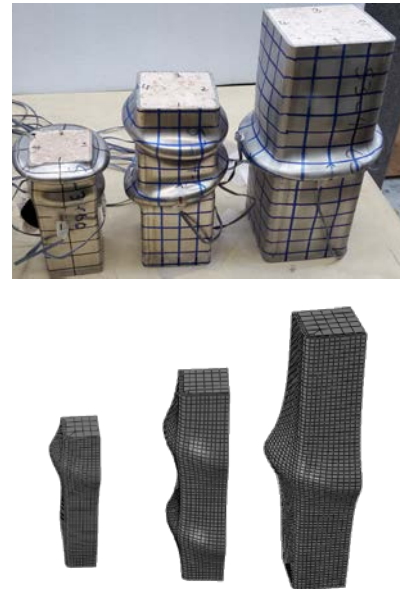


Fig. 2. Local buckling observed in both test and FEA results.

## 4. Parametric study

### 4.1. Parameters

A preliminary parametric study was carried out by using the validated FE model. A total of 24 stub column models were considered to assess the effect of concrete cylinder strength and steel tube cross-sectional geometry on the overall behaviour of the concrete-filled lean duplex stainless steel stub columns.

Table 4 summarizes the characteristics of the models. Overall 8 cross-sections were selected, ranging from  $60 \times 60 \times 3$  to  $150 \times 150 \times 5$ , among which the ratio of outer width to tube wall thickness ( $B/t_f$ ) varies from 20 to 40. The length of all the stub columns was equal to  $3B$ .

Adopted concrete cylinder strength is 30MPa, 60MPa and 80MPa for each cross-section. In the parametric study, steel properties given in Table 2 for S1, S2 and S3 were used for cross-sections 60×60×3, 80×80×4 and 100×100×4, respectively. The properties of S1 were also used for cross-sections 100×100×3 and 120×120×3, and S3 for 120×120×4 and 150×150×5

Table 4. Details of concrete-filled lean duplex stainless steel stub columns considered in the parametric study.

Model ID	Concrete	$B/t_r$	$N_{sc}$ (kN)
60×60×3	C30/60/80	20	682/748/784
80×80×4	C30/60/80	20	1114/1231/1299
100×100×3	C30/60/80	33.3	1217/1443/1601
100×100×4	C30/60/80	25	1306/1500/1634
100×100×5	C30/60/80	20	1593/1818/1970
120×120×3	C30/60/80	40	1472/1837/2087
120×120×4	C30/60/80	30	1606/1937/2170
150×150×5	C30/60/80	30	2510/3027/3390

#### 4.2. Effect of concrete cylinder strength and section size

Fig. 3 shows the axial capacities of the columns increased with the increasing of concrete cylinder strength. The bigger the section size, the higher the increment. In other words, the capacity enhancement was more significant for the cross-section 120×120×3 than 60×60×3. This phenomenon resulted from the contributions of both the enlarged cross-sectional area of the tube and the amount of concrete infill.

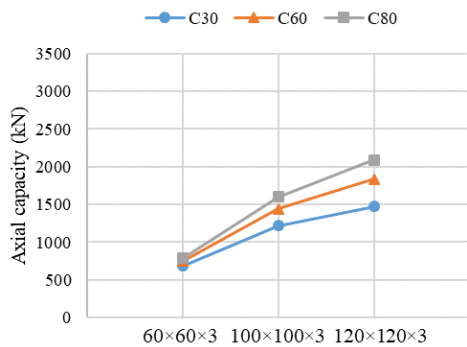


Fig. 3. Effect of cylinder strength and section size on axial compressive capacities of concrete-filled lean duplex stainless steel stub columns.

#### 4.3. Effect of tube wall thickness

By maintaining the section size, the effect of tube wall thickness on the ultimate capacities of

the columns was revealed, as shown in Fig. 4. The axial compressive capacity of the columns appeared to rise with the increasing of the tube wall thickness. The increase of the column capacity was more notable after the tube wall thickness was thicker than, i.e. 4mm in this case.

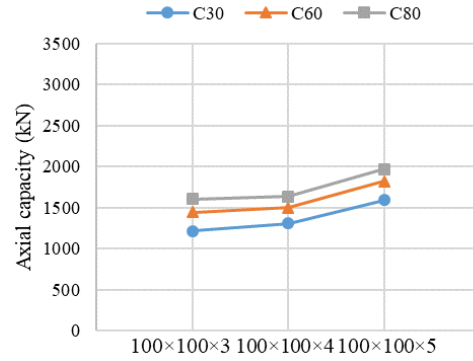


Fig. 4. Effect of tube wall thickness on axial compressive capacities of concrete-filled lean duplex stainless steel stub columns.

### 5. Prediction of axial compacity

The design equation, Eq. (6), provided in Eurocode 4 for concrete-filled carbon steel tube columns was firstly used to calculate the axial compressive capacities of the columns analyzed in the parametric study. The results showed that Eq. (6) for concrete filled carbon steel tube columns underestimated the axial capacity of the composite concrete filled columns with lean duplex stainless steel sections. Eq. (7) was then proposed for the prediction of the axial compressive capacity of concrete-filled lean duplex stainless steel columns. Eqs. (6)-(7) are given as follows,

$$N_{EC4} = A_s f_y + A_c f_{ck} \quad (6)$$

where

- $A_s$  is the cross section area of the steel section;
- $f_y$  is the yield stress of the steel section;
- $A_c$  is the cross section area of the concrete;
- $f_{ck}$  is the cylinder strength of the concrete.

$$N_{prop} = A_s \sigma_{1.0} + \varphi A_c f_{ck} \quad (7)$$

where

- $\sigma_{1.0}$  is the steel strength at 1.0% strain;
- $\varphi$  is the confinement coefficient for the infilled concrete.

In this study, the confinement coefficient ( $\varphi$ ) for the concrete infill is taken as 1.1 for simplicity. Table 5 shows the comparison of the parametric results vs. the new proposed design equation. The average ratio of capacities  $N_{para}/N_{prop}$  is 1.00, with the standard deviation of 0.05 and COV of 0.053. The average value of (for each cross-section with different concrete strengths)  $N_{sc}/N_{prop}$  ranges from 0.93 to 1.08, within a satisfactory average error of 8%.

Table 5. Comparison of parametric results vs. proposed design equation.

Model ID	$N_{prop}$ (kN)	$N_{sc}/N_{prop}$
60×60×3	637/733/797	1.02
80×80×4	1035/1206/1320	1.03
100×100×3	1226/1517/1711	0.96
100×100×4	1224/1502/1688	1.01
100×100×5	1427/1693/1871	1.08
120×120×3	1559/1988/2274	0.93
120×120×4	1560/1974/2250	0.99
150×150×5	2438/3084/3515	0.99
Average		1.00
Standard Deviation		0.05
Coefficient of Variation		0.053

## 6. Conclusions

Finite element analysis of concrete filled lean duplex stainless steel columns subjected to concentric axial compressive load was conducted in this paper. A finite element model was developed and validated through comparisons of the results obtained from the experimental study. A parametric study was then carried out to examine the effect of concrete cylinder strength, section size and tube wall thickness on the compressive capacity of the composite columns. Through both experimental and numerical studies, the merits of using lean duplex stainless steel hollow sections in concrete filled composite columns are highlighted. A new formula based on the Eurocode 4 is proposed to predict the cross-section capacity of the concrete filled lean duplex stainless steel composite columns subjected to axial compression. The results showed that the proposed equation could predict the axial capacity of concrete filled lean duplex stainless steel columns.

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