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Additional Information

1 **COMPUTATIONAL INVESTIGATION OF DIESEL NOZZLE INTERNAL**
2 **FLOW DURING THE COMPLETE INJECTION EVENT**

3

4 **Salvador, F.J. (*), De la Morena, J., Bracho, G., Jaramillo, D.**

5 CMT-Motores Térmicos. Universitat Politècnica de València, Spain

6 (*) Corresponding author:

7 Dr. F. Javier Salvador, fsalvado@mot.upv.es

8 CMT-Motores Térmicos, Universitat Politècnica de València

9 Camino de Vera s/n, E-46022 Spain.

10 Telephone: +34-963879658

11 FAX: +34-963877659

12

13 **ABSTRACT**

14 Currently, diesel engines are calibrated using more and more complex multiple injection
15 strategies. Under these conditions, the characteristics of the flow exiting the fuel injector
16 are strongly affected by the transient interaction between the needle, the sac volume and
17 the orifices, which are not yet clear. In the current paper, a methodology combining a
18 1D injector model and 3D-CFD simulations is proposed. First, the characteristics of the
19 nozzle flow have been experimentally assessed in transient conditions by means of
20 injection rate and momentum flux measurements. Later, the 3D-CFD modeling
21 approach has been validated at steady-state fixed lift conditions. Finally, a previously
22 developed 1D injector model has been used to extract the needle lift profiles and
23 transient pressure boundary conditions used for the full-transient 3D-CFD simulations,

24 using Adaptive Mesh Refinement (AMR) strategies to be able to simulate the
25 complete injection rate starting from 1 micrometer lift.

26

27 **KEYWORDS:** nozzle, modelling, Diesel, dynamic, moving-mesh

28 **NOMENCLATURE**

A Constant for discharge coefficient vs. Reynolds equation

A_{eff} Effective area

A_o Geometrical area

C_a Area coefficient

C_c Contraction coefficient

C_d Discharge coefficient

$C_{d,max}$ Maximum value of discharge coefficient vs. Reynolds

C_v Velocity coefficient

D_o Geometrical nozzle diameter

\dot{m} Mass flow

\dot{M} Momentum flux

P_{back} Discharge pressure

P_{inj} Injection pressure

u_o Outlet nozzle orifice velocity

u_{th} Theoretical outlet orifice velocity, $u_o = \sqrt{\frac{2 \cdot (P_{inj} - P_{back})}{\rho_f}}$

Greek Symbols

ΔP	Pressure drop, $\Delta P = P_{inj} - P_{back}$
ρ_f	Fuel density
ν_f	Kinematic viscosity
λ	Flow coefficient or theoretical Reynolds number

29

30 **1. INTRODUCTION.**

31 The design of modern Diesel engines is focused on the reduction of pollutant emissions
 32 as well as fuel consumption due to the strict emission standards and global
 33 environmental awareness [1, 2] . Both aspects are related to the fuel-air mixing and
 34 combustion processes. In particular, several studies have observed how the formation of
 35 soot particles, which are one of the most critical pollutants in diesel engines, is directly
 36 related to the equivalence ratio at the lift-off length, which is an indicator of the fuel-air
 37 mixing efficiency [3–5]. Furthermore, brake thermal efficiency and combustion
 38 efficiency are also strongly impacted by the spray characteristics [6, 7].

39 Fuel-air mixing and spray formation depend on the fuel injector design. R. Payri et al.
 40 [8] showed that the injector technology affects spray formation and combustion
 41 performance, with piezoelectric actuated injectors being characterized by shorter
 42 evaporation time and ignition delay. Similar results were obtained by Park et al. [9],
 43 linking also the use of piezoelectric injectors to a more efficient spray atomization. Most
 44 of these effects are linked to the different dynamic behavior of these injector
 45 technologies, which affect the transient evolution of the needle lift, known to impact the
 46 internal flow and near-nozzle spray features in both diesel and gasoline direct injection
 47 systems [10–12]. Additionally, the internal geometry of the nozzle, and in particular of
 48 the discharge holes, is also critical in spray formation [13–15].

49 As a consequence of their relevance into the engine development process, different
50 modeling approaches have been investigated over the years to predict the different
51 physical phenomena related to fuel injection. Payri et al. [16] have used 1D-modeling
52 tools to simulate the transient needle lift and mass flow rate of injectors, allowing to
53 evaluate the effects of different fuel temperatures. Similar tools have been used by other
54 authors to predict the effect of the injector technology on the instantaneous mass flow
55 rate [17, 18]. Desantes et al. [19] evaluated a 1D-model based on momentum flux data
56 to assess local velocity and mass fraction distribution inside the spray. Different authors
57 have also analyzed the influence of the nozzle geometry on the internal flow, and in
58 particular the eventual cavitation formation, through experimental and computational
59 tools [20–24]. Internal nozzle flow simulations can also be coupled with spray models
60 to have the complete picture of all the related phenomena [25].

61 To approach coupled internal flow and spray simulations in realistic engine conditions,
62 it is necessary first to develop internal flow models working at transient needle lift
63 conditions. This implies the usage of moving mesh techniques. Traditionally, these
64 strategies are based on stretching a set of pre-defined cells [26, 27]. For diesel injector
65 applications, if the mesh is configured to provide meaningful resolution at high needle
66 lifts, then very narrow cells with high skewness factors appear when the needle is close
67 to its seat, inducing numerical instabilities and affecting the model predictability. This
68 has limited the minimum needle lift for transient simulations to a value between 10 and
69 20 μm [28, 29]. Nevertheless, the nozzle internal flow behaves in a significantly
70 different way at very low needle positions due to the different flow direction induced
71 [13, 30], which influences end-of-injection related phenomena like fuel dribble, linked
72 to higher smoke and hydrocarbon emissions [7]. Battistoni et al. [31] performed a

73 coupled internal flow and spray simulation with moving mesh for a single-hole nozzle.
74 In their work, the minimum lift was set to 2.5 μm for the injection rate opening and 10
75 μm for the needle closure, after which, a transition strategy to a fully close needle
76 simulation was developed. These two stages of the injection event were characterized in
77 two different simulations, in order to maintain a reasonable computational time. Such
78 methodology allowed the study of the spray dynamics in a more realistic way, even
79 though some of the internal flow characteristics at very low needle lifts could not be
80 captured.

81 In the current paper, an Adaptive Mesh Refinement (AMR) methodology implemented
82 in CONVERGE [32] has been evaluated for internal nozzle flow modeling of a diesel
83 injector. The strategy has been applied to both fixed and moving needle conditions. At
84 fixed lifts, this methodology has the potential to reduce computational time by
85 automatically refining the mesh only in the areas of the domain where needed according
86 to velocity gradients. When computing a transient injection event with moving needle
87 conditions, AMR has the advantage of being able to create new layers of cells as the
88 needle moves up, which improves the modeling capability and stability at very low lifts
89 (1 μm for the current paper).

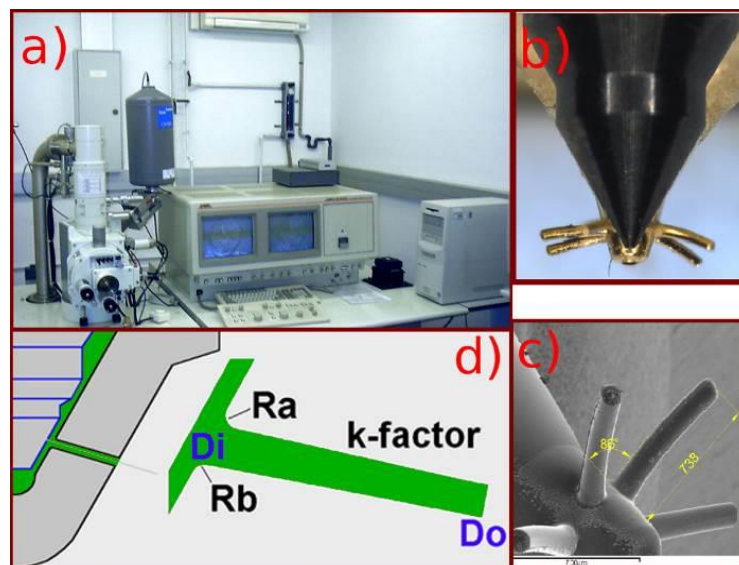
90 The paper is divided in 6 sections. Section 2 presents the experimental tools used to
91 characterize the hydraulic behavior of the injector used in this research. The results of
92 this characterization, used to validate the CFD model, are summarized in Section 3. The
93 outcomes of the modeling approach are detailed in two sections: one for the steady state
94 lift simulations (4), and a second one that analyzes the transient injection event (5).
95 Finally, the main conclusions of the study are drawn in Section 6.

96

97 **2. EXPERIMENTAL TOOLS.**

98 **2.1 Injection system, nozzle description and fluid properties.**

99 In this research, a common-rail fuel injection system able to reach up to 180 MPa is
100 used. This system includes a solenoid-driven Bosch injector mounting a seven-orifices
101 microsac nozzle. To perform the numerical investigations summarized in sections 4 and
102 5, the nozzle geometry has been obtained using a silicone mold technique explained in
103 [33]. This technique is based on the imaging of the molds using an electron microscope
104 (Figure 1.a). The mold is analyzed with different levels of resolution to detect the
105 geometrical features of the nozzle sac and orifices (Figure 1.b). The post-processing of
106 the orifices allows to determine all the critical parameters, such as the rounding radii or
107 the inlet and outlet diameters, with an accuracy of $\pm 2 \mu\text{m}$ (Figure 1.c and 1.d). The
108 orifice length has been directly set to 1 mm according to the nozzle nominal dimensions
109 provided by the fuel injector manufacturer.



110

111

Fig. 1. Nozzle geometry determination by the silicone molding technique.

112 The specific values of these parameters for the nozzle of study are given in Table 1. The
 113 nozzle conicity degree is evaluated by means of the *k-factor*, which is defined as:

$$k - factor = \frac{D_i - D_o}{10} \quad (1)$$

114 Table 1. Geometrical parameters of the nozzle.

R_a [μm]	R_b [μm]	R [μm]	D_i [μm]	D_m [μm]	D_o [μm]	k-factor	Length [μm]
29 \pm 8	22 \pm 6	25.5 \pm 7	143 \pm 2.3	130 \pm 1.4	124 \pm 2.2	1.9 \pm 0.2	715 \pm 15

115

116 As can be seen from the table, *k-factor* is 1.9, meaning that the nozzle orifices have a
 117 relatively high degree of convergence. Thus, according to previous experiences in the
 118 literature, low (or null) cavitation is *a priori* expected [34, 35].

119 The value of *R* in Table 1, is the rounding radius at the inlet orifice, which together the
 120 *k-factor* are the most important factors having influence on cavitation phenomena [36,
 121 37]. It can be determined either for the upper part of the orifice inlet, *R_a*, or for the
 122 bottom part of the orifice inlet, *R_b*. Again, the values obtained indicate the low
 123 probability for cavitation formation inside the nozzle orifices.

124 As far as the fluid used for the experiments is concerned, it was a Repsol Diesel CEC
 125 RF-06-99 fuel. Its most important physical properties were characterized in a previous
 126 work [38]. In particular, the correlations available for the fuel density and viscosity as a
 127 function of pressure and temperature are:

$$\rho_f = 830.6 - 1.021(T - 298) + 1.53 \cdot 10^{-3}(T - 298)^2 + 0.566(P - 0.1) - 6.4 \cdot 10^{-4}(P - 0.1)^2 + 0.013(P - 0.1)(T - 298) \quad (2)$$

$$\mu_f = \mu_0 \cdot 10^{\left[(-1.48+5.86\mu_0^{0.181})\left(\frac{P-0.1013}{1000}\right)\right]} \quad (3)$$

$$\mu_0 = 3.4571 \cdot \exp[-0.0283(T - 298)] \quad (4)$$

128 Where ρ_f is the fuel density in kg/m^3 , μ_f is the fuel dynamic viscosity in $\text{mPa}\cdot\text{s}$, μ_0 is the
 129 fuel dynamic viscosity at 0.1 MPa of pressure (also in $\text{mPa}\cdot\text{s}$), P is the fuel pressure in
 130 MPa and T is the fuel temperature in K.

131 **2.2 Injection rate meter and spray momentum test rig.**

132 A wide experimental hydraulic characterization was made based on mass flow rate and
 133 momentum flux measurements. The first were carried out by means of an Injection Rate
 134 Discharge Curve Indicator system based on Bosch method [39]. The measuring
 135 principle consists in measuring the pressure increase when injecting into a fuel-filled
 136 tube. This pressure increase is related to the injected mass flow rate through the fuel
 137 sound speed, among others factors. The registered signals should be processed in order
 138 to filter a cumulative phenomenon deemed to be important especially for long
 139 injections, following the procedure described in [40]. The uncertainty in the actual
 140 injection rate when using the previously described methodology has been estimated in
 141 $\pm 1.5\%$.

142 As far as the momentum flux test rig is concerned, with this device it is possible to
 143 measure the spray momentum flux by capturing the impact force of the spray on a
 144 surface. The force is transmitted to a piezo-electric pressure sensor previously calibrated
 145 with an accelerometer. The uncertainty of this measurement is approximately $\pm 1.8\%$.
 146 Details of the measuring principle and a picture of this test rig are given in [41]. This

147 kind of measurement, combined with the mass flow rate results, can be used as a tool to
148 assess the orifice-to-orifice dispersion in a nozzle, and also for determining the effective
149 injection velocity and other non-dimensional flow parameters, which help describing
150 the characteristics of the inner nozzle flow.

151 **2.3 Test matrix.**

152 In order to have a complete hydraulic characterization at different injection conditions,
153 i.e., different values of the Reynolds number, a wide test matrix has been used. Table 2
154 reports the operating conditions in terms of injection pressures and backpressures
155 (discharge pressure). Each of them has been tested for three energizing times of 1ms,
156 1.5 ms and 2 ms. All the possible combinations lead to a total of 108 points.

157 Table 2. Test matrix for the mass flow rate and momentum flux measurements.

Injection Pressure [MPa]	Back Pressures [MPa]
30-80-130-180	0.5 – 1 – 3 – 5 – 7 – 9 – 11 – 13 - 15

158

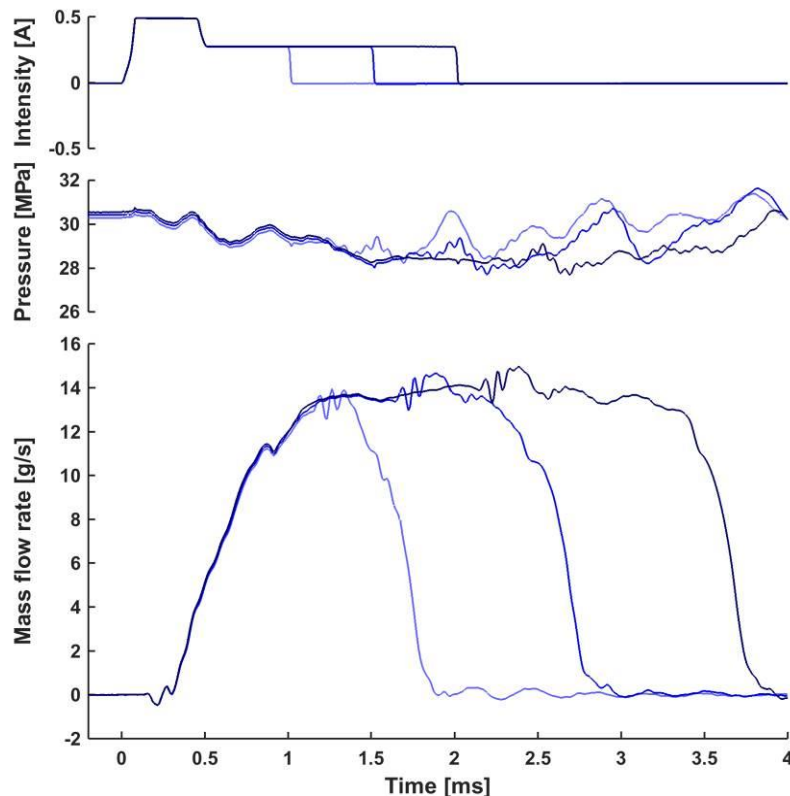
159 **3. HYDRAULIC CHARACTERIZATION RESULTS.**

160 In this section, the results of the hydraulic characterization are reported and analyzed.

161 **3.1 Mass flow rate results.**

162 In Figure 2, the mass flow rate results for $P_{inj}=30$ MPa and $P_{back}= 3$ MPa are plotted for
163 three different values of Energizing Time (1 ms, 1.5 ms and 2 ms). As expected, the
164 mass flow rates are identical at the beginning of the injection during the needle opening,
165 and they show the same steady mass flow rate. The small perturbation observed in the
166 different registered signals is related to the electrovalve closing. As can be seen in the

167 upper part of the figure, where the intensity of the energizing electrical current is
168 plotted, this perturbation coincides with the instant at which the current intensity ceases.
169 The pressure in the line feeding the injector is also represented in the middle part of
170 Figure 2, and, again, the differences between them are due to the different energizing
171 time of each injection.



172

173 Fig. 2 Mass flow rate for $P_{inj}= 30$ MPa, $P_{back}= 3$ MPa and different Energizing Times.

174 In Figure 3, the mass flow rates measurements for the injection pressure of 30 MPa and
175 nine different backpressures are displayed. The points correspond to the energizing time
176 of 2 ms. The main differences between the curves are related to the maximum mass
177 flow value and the end of injection time. According to equation (5), the mass flow at
178 steady-state conditions is directly proportional to the square root of the pressure drop
179 along the injector:

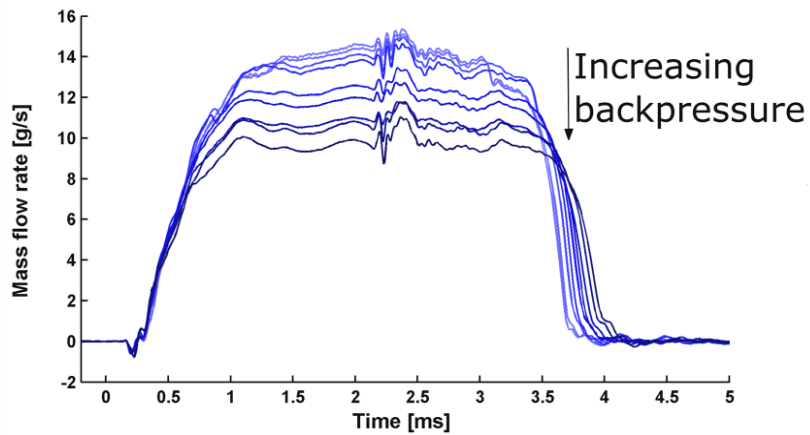
$$\dot{m} = \rho_f \cdot A_{eff} \cdot u_{eff} = \rho_f \cdot C_a \cdot A_o \cdot C_v \cdot u_{th} = C_d \cdot A_o \cdot \sqrt{2\Delta P \cdot \rho_f} \quad (5)$$

180 Being ΔP the pressure drop defined as $\Delta P = P_{inj} - P_{back}$; A_o and A_{eff} the geometrical and
 181 effective outlet sections of the nozzle orifices, respectively; u_{th} the theoretical outlet
 182 velocity according to Bernoulli's equation and C_d , C_v and C_a are the discharge, velocity
 183 and area coefficients, defined as:

$$C_d = \frac{\dot{m}}{\dot{m}_{th}} = \frac{\dot{m}}{\rho_f \cdot A_o \cdot u_{th}} \quad (6)$$

$$C_v = \frac{u_{eff}}{u_{th}} = \frac{u_{eff}}{\sqrt{2\Delta P / \rho_f}} \quad (7)$$

$$C_a = \frac{A_{eff}}{A_o} = \frac{C_d}{C_v} \quad (8)$$



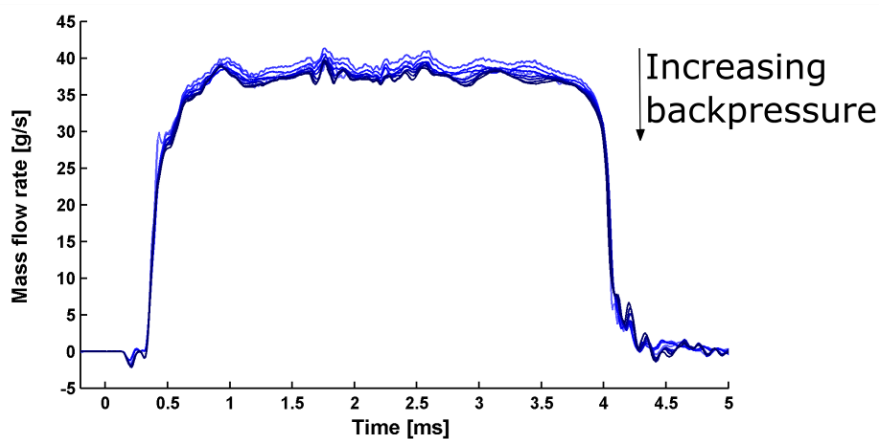
184

185 Fig. 3. Mass flow rates for $P_{inj}= 30$ MPa and different backpressures (0.5-15 MPa).

186 Apart from the effect seen on the maximum mass flow, increasing the backpressure also
 187 leads to slower needle dynamics, which results in a longer delay from the end of the
 188 electrical signal to the hydraulic closing of the injector. This is mainly due to the
 189 stronger force that opposes to the needle motion when the backpressure is higher. At the
 190 start of the injection event, the control volume is at pressure levels close to the injection
 191 pressure, and the contribution of the control pressure to the needle dynamics is small.

192 When the electrovalve stops being energized and the needle starts closing, both the
193 control volume and the needle are at similar pressure values, and the weight of the
194 backpressure force is more significant, resulting in the longer injection duration for
195 higher backpressure previously mentioned.

196 Figure 4 shows the same kind of results for $P_{inj} = 180$ MPa. In this case, being the
197 injection pressure much higher, the weight of the backpressure variation on the pressure
198 drop value is small, and consequently the injection rate curves are very close one to
199 another. Additionally, the effect of the backpressure on the needle dynamics, and
200 consequently on the opening and closing slopes of the injection rate, are minimal.

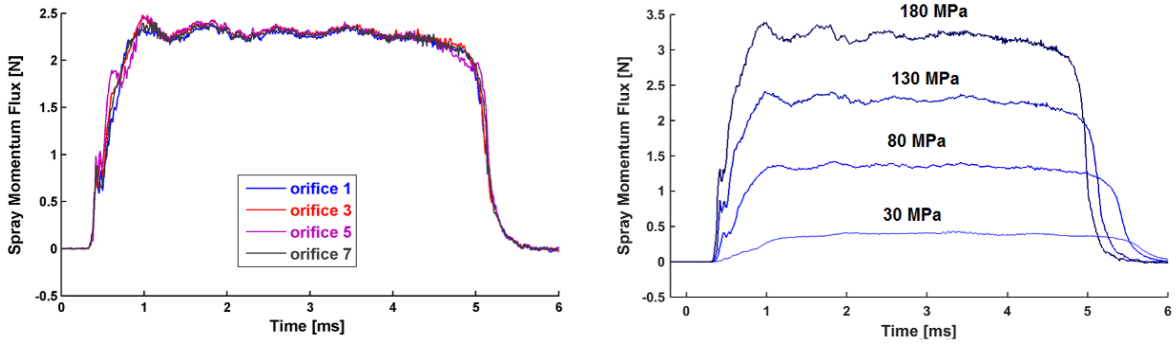


201

202 Fig. 4. Mas flow rates for $P_{inj}= 180$ MPa and different backpressures (0.5-15 MPa).

203 3.2 Momentum flux results.

204 Figure 5 summarizes the momentum flux results obtained for $P_{back}= 5$ MPa conditions.
205 The left hand side of the figure represents the momentum flux from four of the seven
206 discharge orifices of the nozzle for $P_{inj}= 130$ MPa, showing that there is small hole-to-
207 hole dispersion in the injector of study, which will allow performing the numerical
208 simulations for just one of the nozzle orifices. The right hand side of the figure shows
209 the evolution of the momentum flux as a function of the injection pressure.



210

211 Fig. 5. Left: momentum flux for $P_{inj}=130$ MPa, $P_{back}=5$ MPa for different orifices. Right:
 212 momentum flux for $P_{back}=5$ MPa and different injection pressures

213 The main difference among them relates to their maximum value (at steady-state
 214 conditions), which can be evaluated assuming steady-state conditions according to
 215 equation (9):

$$\dot{M} = \dot{m} u_{eff} = \rho_f \cdot A_{eff} \cdot u_{eff}^2 = \rho_f \cdot C_a \cdot A_o \cdot C_v^2 \cdot u_{th}^2 = C_M \cdot A_o \cdot 2\Delta P \quad (9)$$

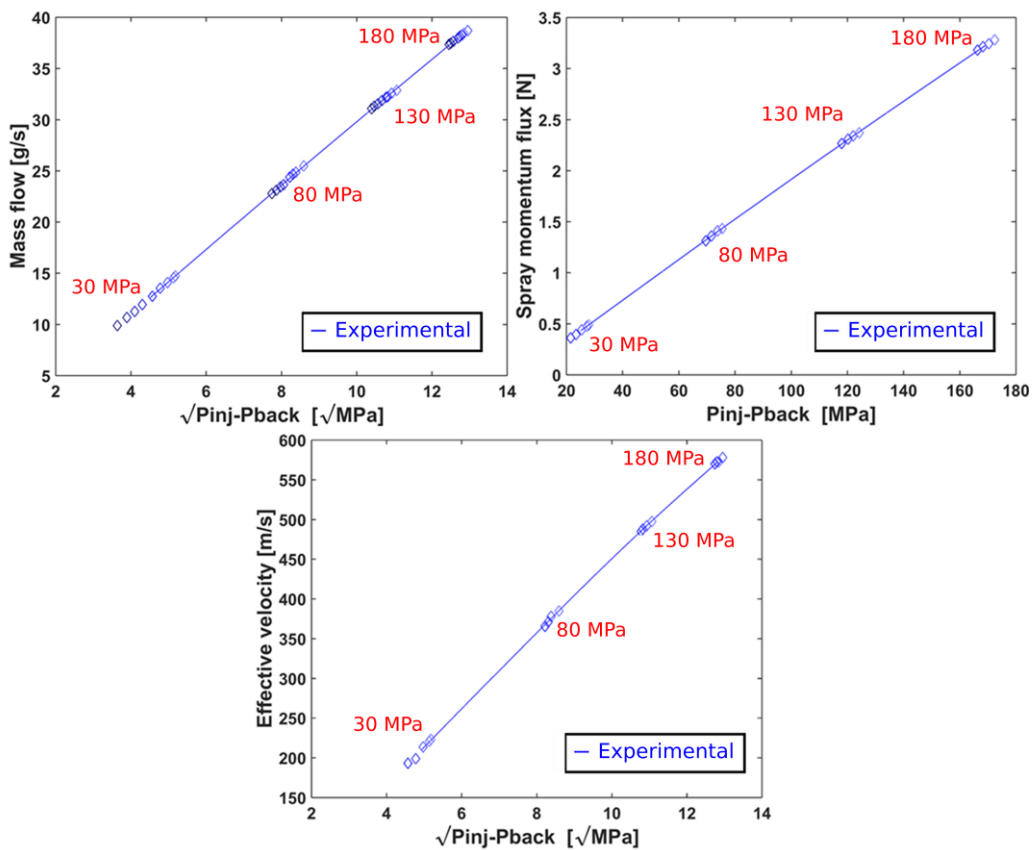
216 Thus, the stationary momentum flux grows linearly with the pressure drop along the
 217 injector, which is consistent with the results previously observed. Regarding the
 218 dynamic behavior of this parameter, it is evident again that higher values of ΔP lead to
 219 faster injection dynamics and shorter hydraulic durations for the same energizing time,
 220 as it was already observed when analyzing the injection rate data.

221 3.3 Flow coefficients behavior.

222 From the analysis introduced in equation (9), it can be immediately seen that the
 223 effective outlet velocity of the flow can be obtained from the combination of the
 224 stationary mass flow and momentum flux results:

$$u_{eff} = \frac{\dot{M}}{\dot{m}} \quad (10)$$

225 Figure 6 depicts the steady-state conditions values of mass flow, momentum flux and
 226 effective velocity obtained from the previous measurements. Stationary mass flow
 227 grows linearly with the square root of the pressure drop, consistently with the analysis
 228 performed in equation (5) and the fact that no cavitation occurs inside the nozzle
 229 orifices, as it was expected from their geometry. Similar result is obtained in terms of
 230 the spray momentum, but considering in this case the pressure drop, consistently with
 231 equation (9). Being the effective velocity the ratio among the two, its evolution is also
 232 linear with the square root of ΔP , with values ranging approximately 200-600 m/s.



233

234

Fig. 6. Steady mass flow rate, spray momentum and effective velocity.

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236

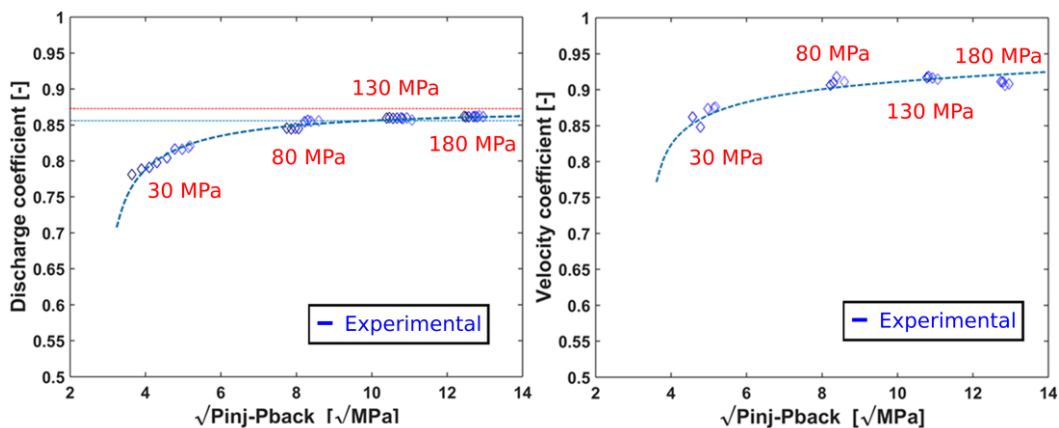
Apart from the effective velocity, it is also possible to determine the main flow coefficients (i.e., the discharge coefficient $-C_d-$ and the velocity coefficient C_v-) from the

237 combined analysis of mass flow and momentum flux, using equations (6) and (7). The
 238 values finally reached are depicted in Figure 7.

239 The discharge coefficient shows an asymptotic increase behavior with the square root of
 240 the pressure drop, with a maximum value of approximately 0.87. This is due to the
 241 different turbulent characteristics of the flow. At low values of ΔP (i.e., low values of
 242 outlet velocity), the characteristic Reynolds number at the outlet of the nozzle is low,
 243 and consequently the turbulence intensity is moderate, characteristic of a
 244 laminar/transitional regime. At these conditions, the discharge coefficient tends to grow
 245 with the Reynolds number according to the expression [42]:

$$C_d = C_{d,max} - \frac{A}{\sqrt{Re}} \quad (11)$$

246 With $C_{d,max}$ and A being coefficients depending on the geometrical and hydraulic
 247 characteristics of the nozzle. For the conditions along the study, the Reynolds number
 248 defined from the geometrical and the velocity calculated from Bernoulli's equation
 249 ranges approximately 10900-37700.



250

251

Fig. 7. Non-dimensional flow parameters: C_d and C_v .

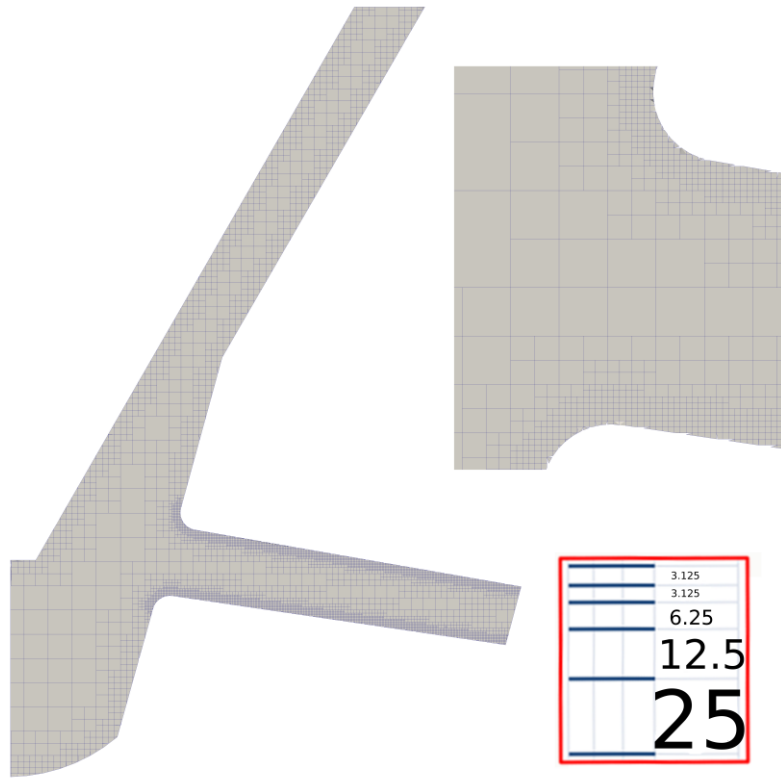
252 As the pressure drop increases, the outlet Reynolds number also grows, and the
253 turbulent regime is already developed; therefore, the discharge coefficient becomes
254 almost independent from the Reynolds number. In the case of the velocity coefficient,
255 the behavior is analogous to the one already described for the discharge coefficient,
256 since the nozzle shows no cavitation and the area coefficient is almost constant.

257 **4. NOZZLE SIMULATION IN STEADY-STATE (MAXIMUM LIFT).**

258 In the current section, the simulation work at fixed needle lift conditions will be
259 discussed. First, the characteristics of the mesh used for such study and the main
260 simulation settings are described. Later on, the conditions at the nozzle orifice outlet
261 obtained through these computations are validated against the flow coefficients obtained
262 from the hydraulic characterization results.

263 **4.1 Mesh construction and simulations setup.**

264 For the computational study a sector geometry of 51.4° of the nozzle, representing one
265 of the seven orifices of the nozzle, will be considered. This approach can be considered
266 acceptable taking into account the low hole-to-hole dispersion already observed during
267 the momentum flux measurements. As stated during the introduction, an Adaptive Mesh
268 Refinement technique, for which the mesh is automatically refined in the areas needed
269 according to the information from the velocity fields at every time step, has been
270 selected in CONVERGE. Such strategy allows reducing the total amount of cells
271 compared to a static mesh approach, saving CPU time for the simulations.



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Fig. 8. Geometry and sample mesh for the simulation (cell size in μm)

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Figure 8 shows the detail of the geometry and an image of the final mesh used for the study at the initial time step. The inlet and outlet boundary conditions in the domain have been set as constant pressure, and equal to the values of injection and discharge pressure used during the experimental activities. It ought to be considered that these pressures are not measured exactly in the location of the boundary conditions, which induces some uncertainties for the validation process. Nevertheless, in the case of the injection pressure, previous experiences show that the pressure losses from the rail up to the needle seat are low compared to those occurring in the needle seat itself [43]. For the nozzle and needle walls, a non-slip boundary condition (i.e. the fluid velocity is the same as the velocity of the solid boundary) has been set. About turbulence, Renormalization Group (RNG) k-epsilon model has been chosen over the standard k-epsilon because the modelization of the effective viscosity makes possible a better

286 handling of low Reynolds numbers and near-wall flows according to previous
287 experiences from diesel internal nozzle flow simulations [44]. For the fluid properties,
288 the values of density and viscosity have been computed using equations (2-4),
289 particularized for the outlet pressure and a temperature level of 40°C. All simulations
290 assume incompressible and isothermal conditions, which means that the fluid properties
291 are constant along the complete computational domain.

292 During the initial stages of the investigation, preliminary simulations have been carried
293 out to select the most appropriate combination of numerical schemes for the
294 discretization of the Navier-Stokes equations and the mesh size parameters. In terms of
295 the numerical schemes, both first order (upwind) and second order (central) approaches
296 have been explored. In any case, PISO algorithm combined with Successive Over-
297 Relaxation (SOR) method has been used for solving the transport equations.

298 Regarding the mesh sizing, in the AMR methodology available in CONVERGE, it is
299 based on two parameters: the base cell size (dx_{base}), representing the maximum size in
300 the domain, and the embed-scale parameter (emb), which is related to the minimum size
301 of the cells close to the walls (dx_{min}), according to the following expression:

$$dx_{min} = \frac{dx_{base}}{2^{emb}} \quad (12)$$

302 For the current case, 3 levels for the base cell size (40, 50 and 60 μm) and three levels
303 for the embed-scale parameter inside the nozzle orifice (2, 3 and 4) have been explored
304 on a single case ($P_{inj} = 80 \text{ MPa}$, $P_{back} = 7 \text{ MPa}$) to explore the effects of these
305 parameters on the model accuracy. Additionally, different number of layers at the initial
306 cell size have been considered, starting at a minimum value of 2.

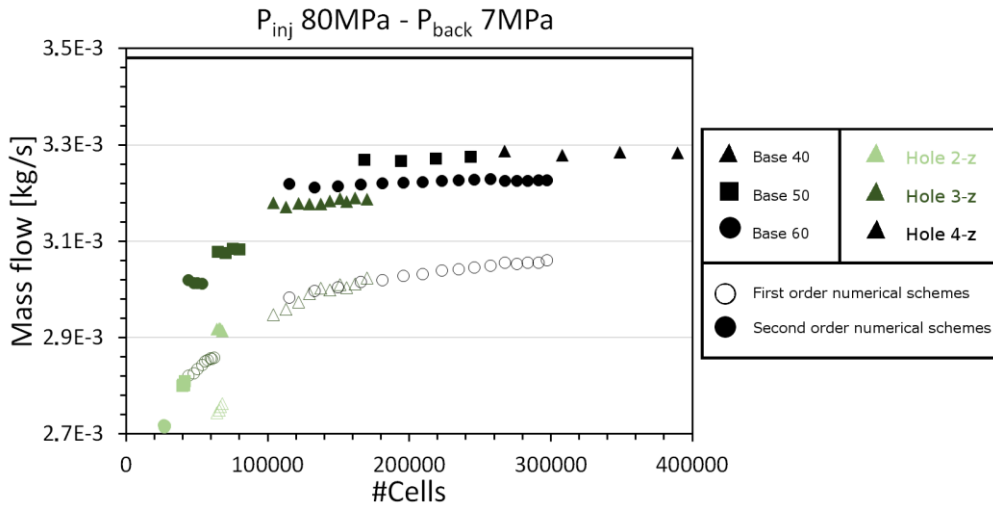


Fig. 9. Mesh sensitivity study.

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308

309 In Figure 9, the solid black line represents the experimental value of mass flow through
310 the nozzle orifice at these operating conditions; void symbols are used for the first order
311 numerical schemes, while solid symbols indicate that second order schemes are selected
312 (in both cases, upwind schemes are used); the kind of symbol is linked to the base cell
313 size value and, finally, the color is related to the value of the embed-scale parameter
314 inside the orifice. For each combination of numerical scheme, base size and embed-
315 scale parameter, different configurations with different number of layers at the
316 minimum cell size, starting at a value of 2, have been screened. As the number of layers
317 gets higher, the total number of cells increases significantly. For example, in the case of
318 the Base 60, second order schemes, embed-scale parameter 4, the total number of cells
319 in the computational domain increase from ~115000 to ~300000 when changing the
320 number of layers from 2 to 16.

321 Looking at the results, the first conclusion that can be drawn is that the first order
322 scheme shows very significant sensitivity to number of layers, while the second order
323 scheme is almost insensitive to this variable. For this reason, the number of layers will
324 be set to 2 in order to reduce the computational effort. For the cell parameters, it can be

325 observed how the combination of a base size of 40 μm and an embed-scale value of 4 is
 326 providing the closer results to the experimental results, with an accuracy of
 327 approximately 5% in terms of the mass flow. Nevertheless, it can be seen that the values
 328 are very close to those achieved for the 50 μm and an embed-scale value of 4 (only
 329 0.3% accuracy improvement), while the total number of cells (and consequently the
 330 computational effort) can be significantly reduced. Thus, these values will be used for
 331 the rest of the study. Other settings of the model are reported in Table 3.

332 Table 3. Tolerances and relaxation factors for the main physical parameters in CFD.

Parameter	Tolerance	Relaxation Factor
Velocity	10^{-6}	0.5
Pressure	10^{-8}	1
Density	10^{-6}	0.5
Turbulent kinetic energy	10^{-3}	0.5
Turbulent dissipation	10^{-3}	0.5

333

334 Figure 10 shows the maximum, mean and minimum y^+ values calculated in the cells
 335 inside the nozzle orifice, where the higher flow velocities and turbulent levels are
 336 reached. As it can be seen the values achieved are rather low, with a mean value lower
 337 than 0.5. This is consistent with the very low minimum cell size used along the
 338 simulations (3.125 μm), and can be seen as another indicator of the consistency of the
 339 mesh characteristics previously chosen during the mesh sensitivity study. Thanks to the
 340 high level of refinement used, no particular wall functions were necessary for these
 341 simulations.

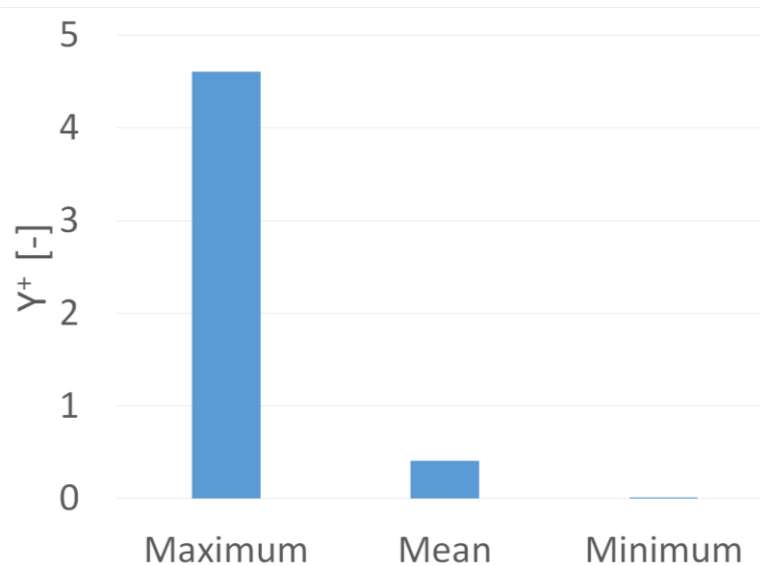
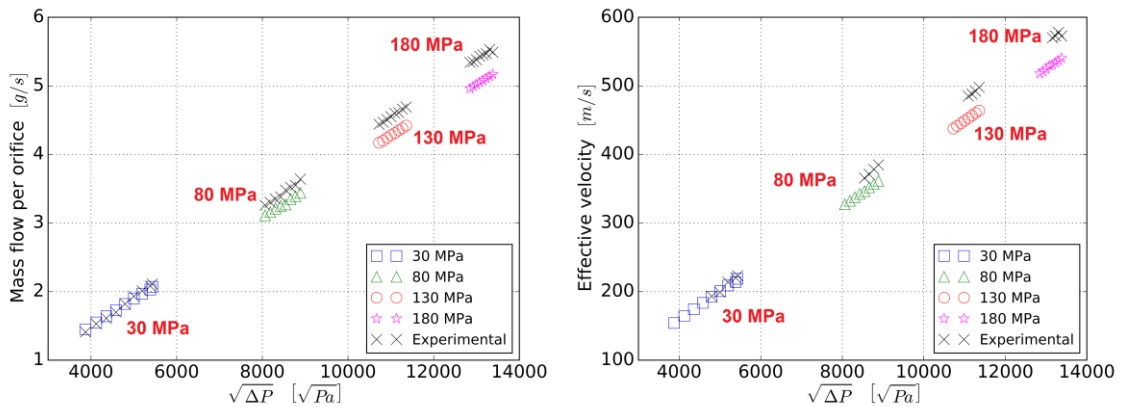


Fig. 10. Computed y^+ values inside the orifice

4.2 Validation of results in steady-state conditions.

Figure 11 shows the results of the validation of the stationary AMR simulations at maximum needle lift. In particular, the left hand side of the figure shows the comparison of experimental vs. computations for the stationary mass flow rate, while on the right hand side the effective velocity values are depicted. As it can be observed, the results of the simulation are almost overlapped with the experiments at low injection pressure level (30 MPa, $\Delta P^{1/2} \approx 5500 Pa$), while the simulations tend to deviate from the experimental results as the injection pressure gets high, with a maximum of 10% at 180 MPa ($\Delta P^{1/2} \approx 13000 Pa$). It has to be noted that, while the fluid properties have been considered constant, in reality both density and viscosity tend to increase together with the fuel pressure. Since density and viscosity have been computed at the backpressure conditions, there is an underestimation of these properties, especially in the areas corresponding to the needle seat, the sac and the inlet section of the orifice. While higher viscosities would tend to reduce the nozzle permeability thanks to the increase of

358 the viscous friction losses, the effect of density and viscosity on the local Reynolds
 359 number and the turbulence characteristics could partially explain the behavior of the
 360 simulation results. Another potential cause of the differences between experiments and
 361 simulations is related to the uncertainties in the nozzle geometry determination, which
 362 are related to the standard deviation values provided in Table 1. This subject will be
 363 analyzed in more details in the next section for the transient simulations results.



364

365

Fig. 11. Numerical results validation for mass flow rate and effective velocity.

366

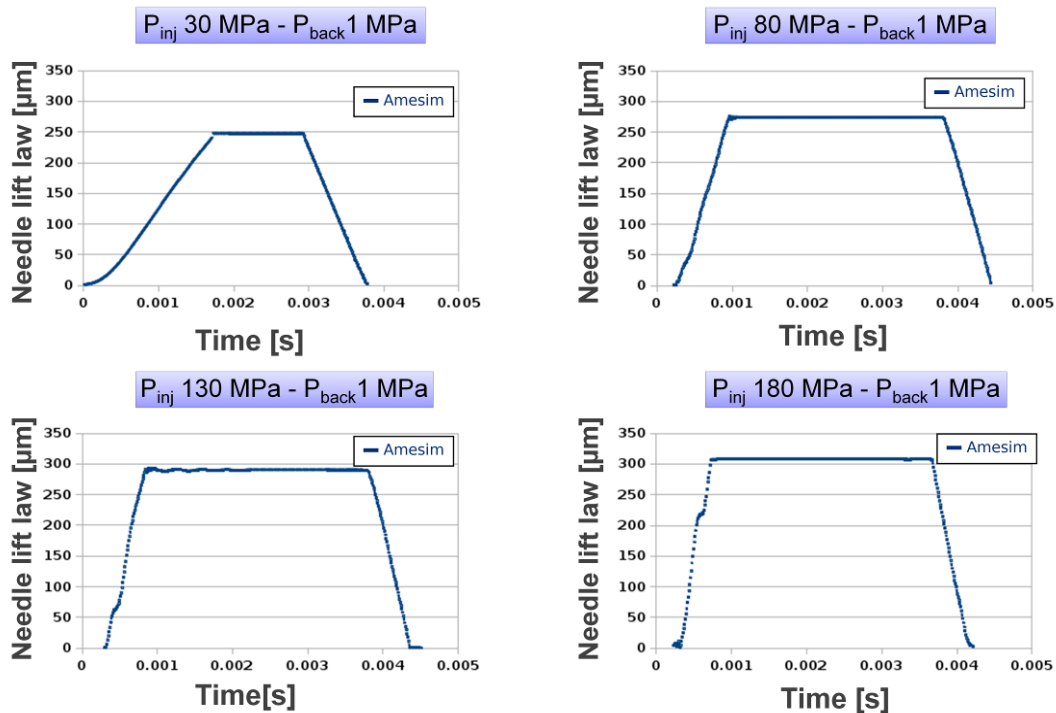
367 5. NOZZLE SIMULATION IN TRANSIENT CONDITIONS.

368 In the next lines, the procedure used to perform the moving needle lift simulations and
 369 the consequent injection rate results are analyzed.

370 5.1 Needle lift law derivation from 1D Modelling.

371 One of the most critical aspects of performing transient internal nozzle flow simulations
 372 is how to impose the needle lift law itself, since this information is generally not
 373 available experimentally. The proposal used in this study has been to obtain the needle
 374 lift profiles from a 1D model of the injector, previously developed in Amesim [45],

375 which is a multidisciplinary 1D-model platform based on Bond Graph technique. The
 376 needle lift profiles obtained through the 1D model are then imposed as boundary
 377 conditions for the 3D moving-mesh model. It has to be noted that the 3D simulations do
 378 not start at a completely closed needle condition. Indeed a minimum needle lift of 1 μm
 379 has been set



380

381

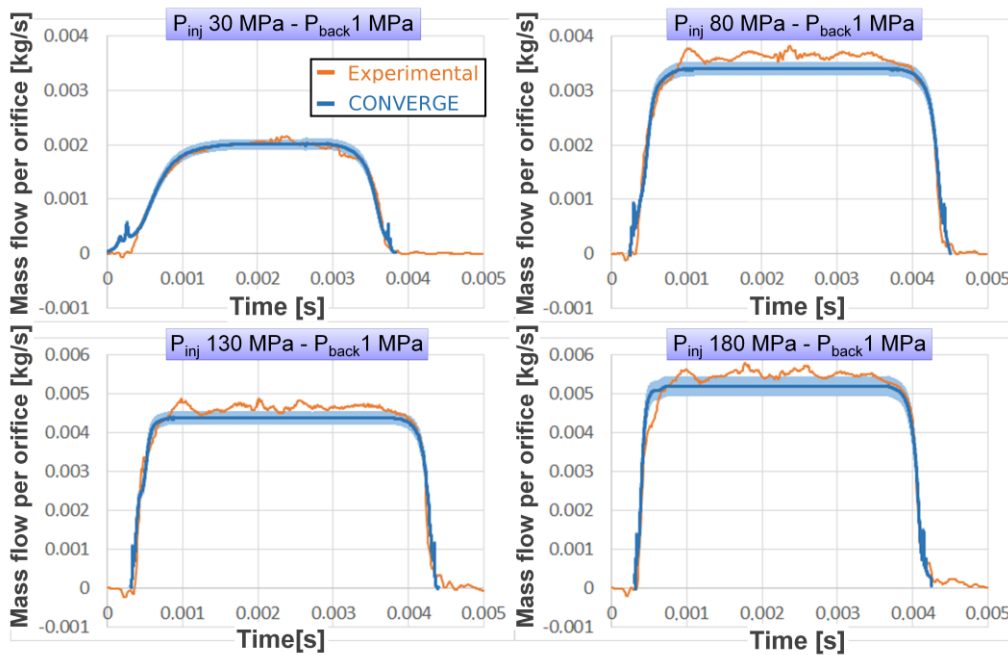
Fig. 12. Needle lift laws used for the transient internal flow simulations

382 The 1D injector model includes all the geometrical, mechanical and hydraulic
 383 information of the internal elements of the injector, extracted from a throughout
 384 characterization of each of them. The details of the model build-up and validation are
 385 available in [46]. The corresponding needle lift laws are shown in Figure 12. The
 386 different maximum lift achieved for each condition is linked to the higher deformation
 387 of the needle and piston as the pressure inside the injector increases.

388

389 **5.2 Numerical results in transient conditions.**

390 For the dynamic internal flow simulations, the position of the needle lift obtained from
391 the Amesim model (starting at 1 μm lift) has been directly introduced into the 3D-CFD
392 code, so that the simulation starts and finishes when the needle is at its closed position.
393 The rest of the boundary conditions, together with the configuration parameters
394 (turbulence model, cell size, numerical schemes, etc.) are maintained equal to the ones
395 already explained for the fixed lift simulations. Figure 13 shows the results of these
396 simulations for the four different levels of injection pressure used along the study (30,
397 80, 130 and 180 MPa) with a backpressure of 1 MPa.



398

399

Fig. 13. Mass flow rate profiles: experiments vs modelling.

400 In this graph, the continuous line represents computed injection rate for the nominal
401 geometry (same as previously used for the steady-state analysis). The shaded area
402 shows the sensitivity of the results to the main nozzle geometry parameters. In this
403 sense, the upper boundary of the shaded area corresponds to a geometry where the inlet

404 rounding radii and the outlet diameter are equal to the average values plus the standard
405 deviation obtained from the silicone molds methodology, and reported on Table 1. This
406 results in values of $R_a=37\ \mu\text{m}$ and $D_o=126.2\ \mu\text{m}$. On the contrary, the bottom boundary
407 of the shaded area is obtained with geometrical parameters equal to the average values
408 minus the standard deviation (*i.e.*, $R_a=21\ \mu\text{m}$ and $D_o=121.8\ \mu\text{m}$). In the steady state
409 region, this results in a sensitivity of approximately $\pm 5\%$ with respect to the nominal
410 geometry in terms of mass flow rate.

411 As it can be observed, there is a good overall agreement between the numerical and
412 experimental injection rate results for all the cases studied. This is especially clear for
413 the opening and closing phases of the injection event, where the nozzle mass flow is
414 mostly controlled by the needle position, since the most of the pressure drop along the
415 nozzle is found in the needle seat region. Nevertheless, two regions of interest can be
416 identified in the simulation:

- 417 • At very low needle lift conditions (start and end of the injection event), a small
418 bump is observed in the mass flow results, especially at low injection pressure.
419 This is related to positions at which only one or two layers of cells with the
420 minimum cell size (approximately $3.2\ \mu\text{m}$) appear in the needle seat region. This
421 low cell resolution together with the high pressure and velocity gradients
422 appearing in the flow in this area are the source of numerical instabilities, which
423 produce the effect previously described. The fact that this effect is more visible
424 at 30 MPa is related to the slower needle dynamics at this injection pressure,
425 which results in a longer time to achieve the needle lift necessary to overcome
426 this phenomenon. According to a previous work by Battistoni et al. [31], the
427 mass flow at very low needle lifts, and especially during the opening phase of

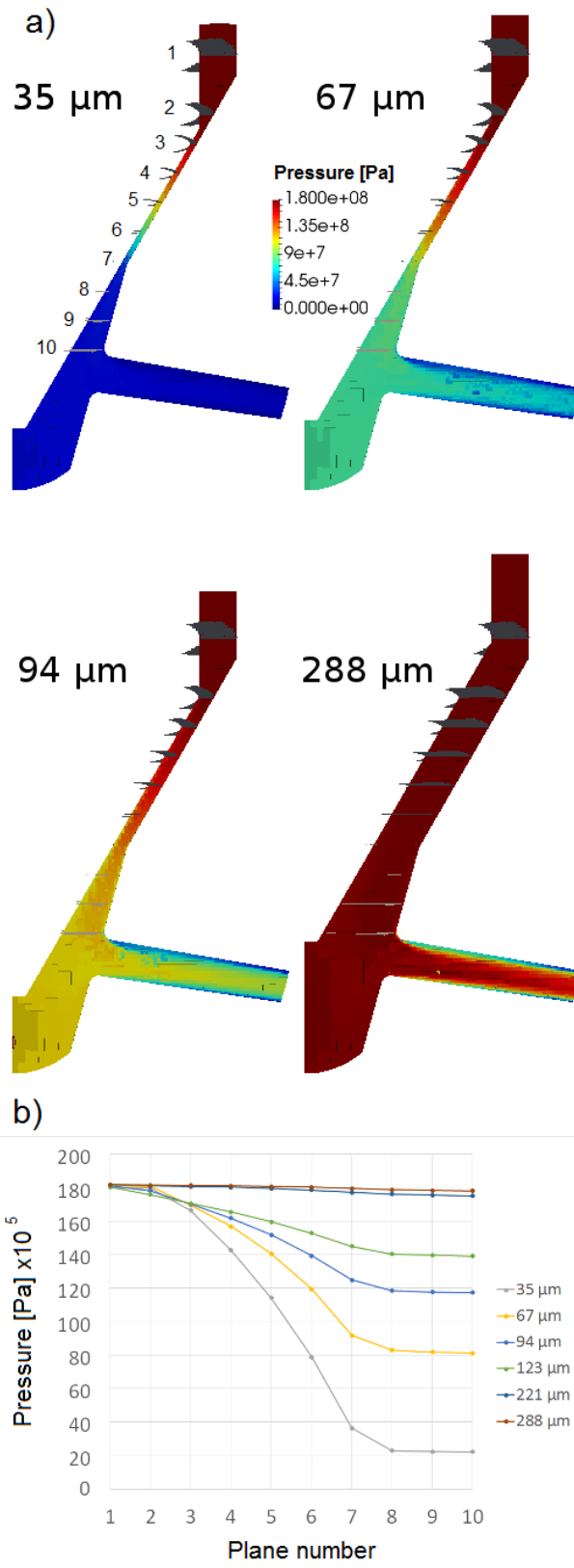
428 the injection, is also affected by the fact that the fluid domain in the sac is
429 initialized with pressurized liquid fuel. In fact, they noticed that when
430 initializing the sac volume with a pressurized gas, as it would be realistic for a
431 spray simulation, the instabilities almost disappeared. Nevertheless, for the
432 current study a pressurized liquid condition was chosen since it is representative
433 of the conditions during the injection rate measurements. It has to be noted
434 anyway that the magnitude of the mass flow deviation induced by this instability
435 is reduced.

436 • At steady flow conditions, the simulation considering the nominal geometry
437 does not follow completely the experimental curve. The mass flow in this case is
438 slightly lower than the experimental, which was the trend already observed in
439 the steady-state simulations results (section 4). Closer results are observed when
440 using higher rounding radii and outlet diameter values, although some deviation
441 is still present for mid-to-high injection pressures. Additionally, all the
442 simulations show a flat mass flow in this region, while some oscillations appear
443 in the experimental data. These oscillations are induced by the pressure waves
444 traveling inside the injector during its dynamic behavior, which are not captured
445 in the CFD simulations since a constant pressure boundary condition has been
446 used, and no needle position or inlet pressure fluctuations have been considered.

447 Finally, the pressure information inside the domain can be seen in Figure 14 as a
448 function on the needle lift. In Figure 14.a, the pressure contours have been plotted in the
449 nozzle middle plane across the orifice for four intermediate needle positions: 35, 67, 94
450 and 288 μm (maximum needle lift). In this figure, it can be seen that for low needle lifts
451 the pressure drop is mostly located in the needle seat region. This means that the

452 pressure drop across the orifice is reduced, resulting in a low velocity and mass flow
453 condition, as previously seen in figure 13. On the contrary, as the needle moves up the
454 area where the pressure drop is concentrated transitions from the needle seat to the
455 orifice region. Indeed, at maximum needle lift (288 μm) the pressure upstream the
456 orifice is very close to the inlet pressure of the domain. Consequently, the mass flow
457 across the orifice is maximum. When this flow scenario is reached (no significant
458 pressure drop in the needle seat area), the nozzle outlet velocity and consequently the
459 mass flow become independent from the needle position, resulting in the steady-state
460 injection rate area previously analyzed.

461 This behavior can be seen in further details in Figure 14.b, where the average pressure
462 values along several transversal planes in the needle seat region are detailed. The
463 numbers of the planes are related to the positions highlighted in the 35 μm contour of
464 figure 14.a, being 1 the plane positioned just after the inlet and 10 the plane just before
465 the orifice. Additionally, this information is represented for different needle positions,
466 including the four previously analyzed. According to this figure, the pressure just before
467 the orifice goes as low as 20 MPa for the 35 μm lift, while it is almost equal to the inlet
468 pressure for the last two lifts (221 and 288 μm).



469

470 Fig. 14. Pressure data as a function of the needle lift for $P_{inj}=180$ MPa. a) Contours in the

471 middle plane. b) Average values in different planes across the needle seat region.

472 **6. CONCLUSIONS.**

473 In the current paper, the transient hydraulic performance of a diesel injector during a
474 complete injection event has been evaluated using 3D-CFD simulations. For this
475 purpose, a production solenoid-driven multihole injector has been widely characterized
476 prior to carry out the simulations. In particular, a silicone mold technique has been
477 employed to obtain the geometry of the nozzle sac and orifices, needed to construct the
478 3D model. Additionally, experiments to determine the injection rate and momentum
479 flux at the nozzle outlet have been done at different boundary conditions, allowing to
480 obtain enough data for a wide validation of the model.

481 The simulation methodology, including Adaptative Mesh Refinement (AMR) has been
482 first studied and validated on fixed-lift stationary conditions (computed at maximum
483 needle position). A wide parameterization of the numerical schemes for the equations
484 discretization, as well as the cell size parameters, has been performed to find the optimal
485 configuration for the study. Then, some of the main nozzle outlet hydraulic parameters,
486 such as the stationary mass flow rate or the effective velocity, have been computed and
487 compared to the experiments, showing a maximum deviation lower than 10%, which is
488 consistent with previous results without AMR.

489 Later on, AMR has been used to compute internal nozzle flow at transient needle lift.
490 The needle lift profiles imposed in the 3D-CFD study had been obtained from a
491 previously developed and validated 1D model of the same injector used for the
492 experiments. In these conditions, the methodology used in this study has shown its
493 suitability to compute the flow delivery at very low lifts, which would not be possible
494 with other moving mesh strategies without severe convergence issues. The results show
495 also a good consistency between the experimental and computational injection rates

496 (especially in the opening and closing phases), with maximum deviations similar to the
497 ones obtained at stationary needle lifts. These deviations can be significantly diminished
498 when increasing the orifice inlet rounding radii and outlet diameter within the
499 uncertainty boundaries of the silicone molds methodology. Finally, it is seen that the
500 pressure drop along the domain is strongly related to the needle position, resulting in
501 different velocity and mass flow through the discharge orifices.

502

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514 **References**

- 515 1. Hall CAS, Lambert JG, Balogh SB (2014) EROI of different fuels and the
516 implications for society. *Energy Policy* 64:141–152. doi:
517 10.1016/j.enpol.2013.05.049
- 518 2. Lujan JM, Tormos B, Salvador FJ, Gargar K (2009) Comparative analysis of a
519 DI diesel engine fuelled with biodiesel blends during the European MVEG-A
520 cycle: Preliminary study (I). *Biomass and Bioenergy* 33:941–947. doi:
521 10.1016/j.biombioe.2009.02.004
- 522 3. Pickett LM, Siebers DL (2004) Soot in diesel fuel jets: Effects of ambient
523 temperature, ambient density, and injection pressure. *Combust Flame* 138:114–
524 135. doi: 10.1016/j.combustflame.2004.04.006
- 525 4. Dec JE (1997) A Conceptual Model of DI Diesel Combustion Based on Laser-
526 Sheet Imaging. SAE Tech. Pap. 970873
- 527 5. Wang X, Huang Z, Zhang W, et al (2011) Effects of ultra-high injection pressure
528 and micro-hole nozzle on flame structure and soot formation of impinging diesel
529 spray. *Appl Energy* 88:1620–1628. doi: 10.1016/j.apenergy.2010.11.035
- 530 6. Sayin C, Gumus M, Canakci M (2013) Influence of injector hole number on the
531 performance and emissions of a di diesel engine fueled with biodiesel-diesel fuel
532 blends. *Appl Therm Eng* 61:121–128. doi: 10.1016/j.applthermaleng.2013.07.038
- 533 7. Mohan B, Yang W, Chou SK (2013) Fuel injection strategies for performance
534 improvement and emissions reduction in compression ignition engines—A
535 review. *Renew Sustain Energy Rev* 28:664–676. doi: 10.1016/j.rser.2013.08.051

- 536 8. Payri R, Salvador FJ, Gimeno J, De la Morena J (2011) Influence of injector
537 technology on injection and combustion development, Part 1: Hydraulic
538 characterization. *Appl Energy* 88:1068–1074. doi:
539 <http://dx.doi.org/10.1016/j.apenergy.2010.10.012>
- 540 9. Park SW, Kim JW, Lee CS (2006) Effect of Injector Type on Fuel-Air Mixture
541 Formation of High-Speed Diesel Sprays. *Proc Inst Mech Eng Part D J Automob*
542 *Eng* 220:647–659. doi: 10.1243/09544070D20304
- 543 10. Moon S, Komada K, Sato K, et al (2015) Ultrafast X-ray study of multi-hole GDI
544 injector sprays: Effects of nozzle hole length and number on initial spray
545 formation. *Exp Therm Fluid Sci* 68:68–81. doi:
546 [10.1016/j.expthermflusci.2015.03.027](http://dx.doi.org/10.1016/j.expthermflusci.2015.03.027)
- 547 11. Powell CF, Kastengren AL, Liu Z, Fezzaa K (2010) The Effects of Diesel
548 Injector Needle Motion on Spray Structure. *J Eng Gas Turbines Power*
549 133:12802. doi: 10.1115/1.4001073
- 550 12. Huang W, Moon S, Ohsawa K (2016) Near-nozzle dynamics of diesel spray
551 under varied needle lifts and its prediction using analytical model. *Fuel* 180:292–
552 300. doi: 10.1016/j.fuel.2016.04.042
- 553 13. Sun Z-Y, Li G-X, Chen C, et al (2015) Numerical investigation on effects of
554 nozzle's geometric parameters on the flow and the cavitation characteristics
555 within injector's nozzle for a high-pressure common-rail DI diesel engine.
556 *Energy Convers Manag* 89:843–861. doi: 10.1016/j.enconman.2014.10.047
- 557 14. Devassy BM, Habchi C, Daniel E (2015) Atomization Modelling of Liquid Jets

- 558 using a Two-Surface Density Approach. *At Sprays* 25:47–80.
- 559 15. Moon S, Gao Y, Park S, et al (2015) Effect of the number and position of nozzle
560 holes on in- and near-nozzle dynamic characteristics of diesel injection. *Fuel*
561 150:112–122. doi: 10.1016/j.fuel.2015.01.097
- 562 16. Payri R, Salvador FJ, Carreres M, De la Morena J (2016) Fuel temperature
563 influence on the performance of a last generation common-rail diesel ballistic
564 injector. Part II: 1D model development, validation and analysis. *Energy Convers*
565 *Manag* 114:376–391. doi: 10.1016/j.enconman.2016.02.043
- 566 17. Plamondon E, Seers P (2014) Development of a simplified dynamic model for a
567 piezoelectric injector using multiple injection strategies with biodiesel/diesel-fuel
568 blends. *Appl Energy* 131:411–424. doi: 10.1016/j.apenergy.2014.06.039
- 569 18. Postrioti L, Malaguti S, Bosi M, et al (2014) Experimental and numerical
570 characterization of a direct solenoid actuation injector for Diesel engine
571 applications. *Fuel* 118:316–328. doi: 10.1016/j.fuel.2013.11.001
- 572 19. Desantes JM, Salvador FJ, Lopez JJ, De la Morena J (2011) Study of mass and
573 momentum transfer in diesel sprays based on X-ray mass distribution
574 measurements and on a theoretical derivation. *Exp Fluids* 50:233–246. doi:
575 10.1007/s00348-010-0919-8
- 576 20. De la Morena J, Neroorkar K, Plazas AH, et al (2013) Numerical analysis of the
577 influence of diesel nozzle design on internal flow characteristics for 2-valve
578 diesel engine application. *At Sprays* 23:97–118. doi:
579 10.1615/AtomizSpr.2013006361

- 580 21. Duke DJ, Schmidt DP, Neroorkar K, et al (2013) High-resolution large eddy
581 simulations of cavitating gasoline-ethanol blends. *Int J Engine Res* 14:578–589.
582 doi: 10.1177/1468087413501824
- 583 22. Mitroglou N, McLorn M, Gavaises M, et al (2014) Instantaneous and ensemble
584 average cavitation structures in Diesel micro-channel flow orifices. *Fuel*
585 116:736–742. doi: 10.1016/j.fuel.2013.08.060
- 586 23. Wang X, Li K, Su W (2012) Experimental and numerical investigations on
587 internal flow characteristics of diesel nozzle under real fuel injection conditions.
588 *Exp Therm Fluid Sci* 42:204–211. doi:
589 <http://dx.doi.org/10.1016/j.expthermflusci.2012.04.022>
- 590 24. Sou A, Pratama RH (2016) Effects of Asymmetric Inflow on Cavitation in Fuel
591 Injector and Discharged Liquid Jet. *At Sprays* 26:939–959. doi:
592 10.1615/AtomizSpr.2015013501
- 593 25. Xue Q, Battistoni M, Powell CF, et al (2015) An Eulerian CFD model and X-ray
594 radiography for coupled nozzle flow and spray in internal combustion engines.
595 *Int J Multiph Flow* 70:77–88. doi: 10.1016/j.ijmultiphaseflow.2014.11.012
- 596 26. Castilla R, Gamez-Montero PJ, Ertrk N, et al (2010) Numerical simulation of
597 turbulent flow in the suction chamber of a gearpump using deforming mesh and
598 mesh replacement. *Int J Mech Sci* 52:1334–1342. doi:
599 10.1016/j.ijmecsci.2010.06.009
- 600 27. Parlak Z, Engin T (2012) Time-dependent CFD and quasi-static analysis of
601 magnetorheological fluid dampers with experimental validation. *Int J Mech Sci*

- 602 64:22–31. doi: 10.1016/j.ijmecsci.2012.08.006
- 603 28. Chiatti G, Chiavola O, Palmieri F (2009) Spray Modeling for Diesel Engine
604 Performance Analysis. SAE Tech Pap 2009-01-0835. doi: 10.4271/2009-01-0835
- 605 29. Marcer R, Audiffren C, Viel A, et al (2010) Coupling 1D System AMESim and
606 3D CFD EOLE models for Diesel Injection Simulation Renault. In: ILASS - Eur.
607 2010, 23rd Annu. Conf. Liq. At. Spray Syst. pp 1–10
- 608 30. Desantes JM, Salvador FJ, Carreres M, Martínez-López J (2014) Large-eddy
609 simulation analysis of the influence of the needle lift on the cavitation in diesel
610 injector nozzles. Proc Inst Mech Eng Part D J Automob Eng 229:407–423. doi:
611 10.1177/0954407014542627
- 612 31. Battistoni M, Xue Q, Som S (2016) Large-Eddy Simulation (LES) of Spray
613 Transients : Start and End of Injection Phenomena. Oil Gas Sci Technol - Rev
614 d'IFP Energies Nouv 71:24. doi: <http://dx.doi.org/10.2516/ogst/2015024>
- 615 32. CONVERGE is a trade mark of Convergent Science <https://convergecf.com>.
- 616 33. Macian V, Bermúdez V, Payri R, Gimeno J (2003) New technique for
617 determination of internal geometry of a Diesel nozzle with the use of silicone
618 methodology. Exp Tech 27:39–43. doi: 10.1111/j.1747-1567.2003.tb00107.x
- 619 34. Dabiri S, Sirignano W a., Joseph DD (2007) Cavitation in an orifice flow. Phys
620 Fluids 19:72112. doi: 10.1063/1.2750655
- 621 35. Mohan B, Yang W, Chou SK (2014) Cavitation in Injector Nozzle Holes - A
622 Parametric Study. Eng Appl Comput Fluid Mech 8:70–81.

- 623 36. Salvador FJ, Hoyas S, Novella R, Martinez-Lopez J (2011) Numerical simulation
624 and extended validation of two-phase compressible flow in diesel injector
625 nozzles. *Proc Inst Mech Eng Part D J Automob Eng* 225:545–563. doi:
626 10.1177/09544070JAUTO1569
- 627 37. Som S, Longman DE, Ramirez AI, Aggarwal S (2012) Influence of Nozzle
628 Orifice Geometry and Fuel Properties on Flow and Cavitation Characteristics of a
629 Diesel Injector. In: *Fuel Inject. Automot. Eng.* pp 112–126
- 630 38. Desantes JM, Salvador FJ, Carreres M, Jaramillo D (2015) Experimental
631 Characterization of the Thermodynamic Properties of Diesel Fuels Over a Wide
632 Range of Pressures and Temperatures. *SAE Int J Fuels Lubr* 8:2015-01–0951.
633 doi: 10.4271/2015-01-0951
- 634 39. Bosch W (1966) The Fuel Rate Indicator: a New Measuring Instrument for
635 Display of the Characteristics of Individual Injection. *SAE Pap.* 660749
- 636 40. Payri R, Salvador FJ, Gimeno J, Bracho G (2008) A new methodology for
637 correcting the signal cumulative phenomenon on injection rate measurements.
638 *Exp Tech* 32:46–49. doi: 10.1111/j.1747-1567.2007.00188.x
- 639 41. Payri F, Payri R, Salvador FJ, Martínez-López J (2011) A contribution to the
640 understanding of cavitation effects in Diesel injector nozzles through a combined
641 experimental and computational investigation. *Comput Fluids* 58:88–101. doi:
642 10.1016/j.compfluid.2012.01.005
- 643 42. Lichtarowicz AK, Duggins RK, Markland E (1965) Discharge coefficients for
644 incompressible non-cavitating flow through long orifices. *J Mech Eng Sci* 7:210–

- 645 219. doi: 10.1243/JMES_JOUR_1965_007_029_02
- 646 43. Lopez JJ, Salvador FJ, De la Garza OA, Arrègle J (2012) Characterization of the
647 pressure losses in a common rail diesel injector. Proc Inst Mech Eng Part D-
648 Journal Automob Eng 226:1697–1706. doi: 10.1177/0954407012447020
- 649 44. Salvador FJ, Carreres M, Jaramillo D, Martínez-López J (2015) Comparison of
650 microsac and VCO diesel injector nozzles in terms of internal nozzle flow
651 characteristics. Energy Convers Manag 103:284–299. doi:
652 10.1016/j.enconman.2015.05.062
- 653 45. LMS (2010) Imagine.Lab AMESim v.10. User’s manual.
- 654 46. Payri R, Salvador FJ, Martí-Aldaraví P, Martínez-López J (2012) Using one-
655 dimensional modeling to analyze the influence of the use of biodiesels on the
656 dynamic behavior of solenoid-operated injectors in common rail systems:
657 Detailed injection system model. Energy Convers Manag 54:90–99. doi:
658 10.1016/j.enconman.2011.10.007
- 659