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Additional Information

## Stability and accuracy of deterministic project duration forecasting methods in Earned Value Management

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1	Stability and accuracy of deterministic project duration
2	forecasting methods in Earned Value Management

#### **3** Structured abstract

4 Purpose: Earned Value Management (EVM) is a project monitoring and control technique
5 that enables the forecasting of a project's duration. Many EVM metrics and project duration
6 forecasting methods have been proposed. However, very few studies have compared their
7 accuracy and stability.

8 Design/methodology/approach: This paper presents an exhaustive stability and accuracy 9 analysis of 27 deterministic EVM project duration forecasting methods. Stability is measured 10 via Pearson's, Spearman's, and Kendall's correlation coefficients; while accuracy is 11 measured by Mean Squared and Mean Absolute Percentage Errors. These parameters are 12 determined at ten percentile intervals to track a given project's progress across 4,100 artificial 13 project networks with varied topologies.

Findings: Findings support that stability and accuracy are inversely correlated for most
forecasting methods, and also suggest that both significantly worsen as project networks
become increasingly parallel. However, the *AT+PD-ES<sub>min</sub>* forecasting method stands out as
being the most accurate and reliable.

Originality: Unlike previous research comparing EVM forecasting methods, this one
includes all deterministic methods (classical and recent alike) and measures their
performance in accordance with several parameters. Activity durations and costs are also
modelled akin to those of construction projects.

Practical implications: Implications of this study will allow construction project managers to resort to the simplest, most accurate and most stable EVM metrics when forecasting project duration. They will also be able to anticipate how the project topology (i.e. the network of

activity predecessors) and the stage of project progress can condition their accuracy andstability.

*Keywords:* Earned Value Management; construction projects; project duration; deterministic
forecasting; metrics stability; time estimates accuracy.

29 *Article classification:* Research article.

30 Introduction

Earned Value Management (EVM) is a deterministic project monitoring and control technique widely adopted in many industries, including construction (Batselier and Vanhoucke, 2015a). EVM can measure whether a project is behind (or ahead) of schedule and whether it is costing more (or less) than planned. These applications are extremely useful for project managers taking corrective actions to bring the project back on track (Vanhoucke, 2010). Another common application of EVM metrics is generating forecasts of when the project will finish and how much it will cost by the time it is completed.

EVM has been included in the Project Management Body of Knowledge (PMBOK) 38 Guide since its first edition in 1987. However, EVM has also been adopted by many other US 39 government agencies [e.g. the National Aeronautics and Space Administration (NASA) and 40 41 the United States Department of Energy]. More recently, EVM has also been standardized in other regions such as Australia (e.g. AS 4817-2003 and AS 4817-2006) and Europe (ISO 42 43 21508:2018). In parallel with its adoption by governments, practitioners, certification and 44 professional bodies, EVM has also received extensive research attention (Vanhoucke, 2011, 2013). 45

46 Due to its relative simplicity, EVM also allows conveying in simple terms to top
47 management how the project is performing. To do this, it relies on a series of *metrics* whose
48 values can be updated whenever the *actual* activity durations, costs and percentages of

49 completion are measured. These measurements should take place at approximately regular
50 time intervals during project execution and are commonly known as *tracking periods*.

The present study will focus on project *duration* methods. These are commonly 51 52 known in EVM as Estimated time At Completion or just EAC(t). EAC(t) methods have 53 received much less research attention than their cost counterpart (Batselier and Vanhoucke, 54 2015b). Yet, many EVM metrics and EAC(t) expressions have been proposed over the last 20 years. Earlier EAC(t) expressions mostly resorted either directly to classical EVM metrics 55 [Planned Value (PV), Actual Cost (AC) and Earned Value (EV)] or their derived indicators 56 [the Schedule Performance Index (SPI) or the Schedule Cost Index (SCI)]. In 2003, though, a 57 58 fourth metric named Earned Schedule (ES) was proposed by Lipke (2003). Several EAC(t) expressions have used the ES metric since, also in combination with its derived performance 59 indicators [e.g. the SPI(t) or the SCI(t)]. Finally, and much more recently, other EAC(t) 60 61 expressions have been proposed based on exponential smoothing and further reformulations of the ES metric (e.g. ES(e), ES<sub>min</sub>, ES<sub>max</sub>) (Ballesteros-Pérez et al., 2019). 62 Among recent variants of EAC(t) methods, some have not been intrinsically 63 deterministic [e.g. (Acebes et al., 2015; Elshaer, 2013; Nadaf et al., 2019)]. However, this 64 study will focus on *deterministic* methods. Deterministic methods are the most common 65 nowadays in the EVM framework and they are also simpler and easier to use (Vanhoucke, 66 2013). These make deterministic EVM quite appealing to most construction practitioners. 67 Apart from EVM project duration forecasting methods, other more advanced 68 techniques have also been proposed (e.g. fuzzy logic, neural network analysis, Bayesian 69 70 inference, Monte Carlo simulation, statistical learning and artificial intelligence methods, 71 Kalman filter algorithms, and endless variants of PERT) (Bai et al., 2020; Ballesteros-Pérez, Cerezo-Narváez, et al., 2020). However, most of these techniques are also more computer 72

73 demanding and/or data-intensive than the EVM deterministic expressions analyzed here.

Hence, this paper will perform a stability and accuracy performance comparison of all 74 deterministic EVM project duration forecasting methods found in the literature. We 75 understand by use of the term accuracy that this refers to the capability of an EAC(t) method 76 77 to anticipate the final project duration before the project is actually completed. Similarly, stability is defined here as the ability of an EAC(t) method to experience low volatility (as the 78 project progresses and new information comes in), while showing a high correspondence 79 80 between the current (forecast) and eventual (actual) project duration values. Both indicators -accuracy and stability-will be numerically defined later within the Research methods. A 81 82 representative artificial projects' dataset will be used to measure the performance of both indicators for all EAC(t) methods. 83 We will analyze both stability and accuracy because, among the few studies that have 84 compared EAC(t) expressions so far, most have neglected the stability criterion and/or have 85 86 resorted to an *ad hoc* definition that cannot be easily generalized. Similarly, most 87 comparative studies have resorted to a single parameter for measuring accuracy (generally the Mean Absolute Percentage Error, MAPE), which does not necessarily gauge the occasional 88 existence of significant deviations (unlike the Mean Squared Error, MSE). 89

#### 90 Literature review

Before continuing, the 27 EAC(t) methods to be compared are presented in Table 1.
Due to the large number of metrics and variables involved, further details on all methods'
variables are provided as *Supplemental material* (see Table S1).

94

#### < Insert Table I here >

Table 1 classifies the project duration forecasting expressions by authors [e.g.
(Anbari, 2004; Ballesteros-Pérez et al., 2019; Batselier and Vanhoucke, 2017a; Jacob, 2003;
Khamooshi and Golafshani, 2014; Lipke, 2003, 2011)], and type of formula. The formulae

are all numbered on the first column for easier reference in the upcoming sections.

#### 99 Broadly speaking, most of these methods (but not all) resort to one of these three standard EAC(t) formula configurations: PD/PF, MAX(PD, AT)/PF or $AT+(PD-ES_x)/PF$ . 100 Where: *PD* is the project Planned Duration (before it starts); *AT* is the Actual (current) Time; 101 MAX( $\cdot$ ) is the maximum of two variables; *ES<sub>x</sub>* is one of the variants of the Earned Schedule 102 metric (e.g. ES, ED, ES(e), ES<sub>min</sub>, etc.); and PF is a Performance Factor that can be 1 or 103 another indicator such as SPI, SPI(t), SPI(t)(e), SPI(t)<sub>ESmin</sub>, SPI(t)<sub>ESmax</sub>, SCI, SCI(t), SCI(t)(e), 104 $SCI(t)_{ESmin}$ , $SCI(t)_{ESmax}$ , even an exponential smoothing factor (e.g. $T_{t,SPI(t)}$ , $T_{t,AT}/T_{t,ES}$ or $T_{t,EDI}$ ). 105 Previous research comparing EAC(t) methods' accuracy 106 The first comparison of EAC(t) project duration methods was performed by 107 Vanhoucke (2010). He compared methods 1-9 from Table 1. In his comparison, method 7 108 was the most accurate but considering Mean Absolute Performance Errors (MAPE) only. 109 Five years later, Batselier and Vanhoucke (2015b) compared the same methods 1-9, 110 but this time with 23 real projects. Again, method 7 turned out to be the most accurate. In the 111 present study we will not use real projects, though. This is because *stability* calculations 112 113 require multiple realizations of the same project (which can only be obtained by simulation). Then, Batselier and Vanhoucke (2015c) compared methods 7, 15, 16 and some of Eslhaer's 114 (2013) non-deterministic EAC(t) expressions. Again, method 7 was the most accurate. 115 116 In 2017, Khamooshi and Abdi (2017) compared methods 10-13, 22 and 24 with another 19-real-project dataset. In their analyses, methods 22 and 24 were the top performers. 117 Both methods 22 and 24 were proposed by the authors and resorted to exponential 118 smoothing. In the same year, Batselier and Vanhoucke (2017b) proposed method 20, which 119 120 was also coincidentally based on exponential smoothing. However, they only compared it against method 9, observing just a marginal accuracy improvement. 121

122	Also in 2017, de Andrade and Vanhoucke (2017) compared methods 7 and 15 on a
123	14-real-project subset extracted from Batselier and Vanhoucke's (2015b) dataset. Method 7
124	was again the top performer (regarding accuracy as measured by MAPEs only).

More recently, Ballesteros-Pérez et al. (2019) compared methods 1-22 and 25. In his study, method 22 was the best but very closely followed by methods 7, 14, 16 and 25. This study, however, omitted methods 23, 24, 25 and 27, and neglected the stability analysis. Also, it only calculated the MAPEs (not the MSEs), nor did it use activity durations and costs similar to those of real construction projects.

As can be seen, no previous study has compared all EVM project duration methods, 130 nor used activity durations and cost representations of real construction projects. These 131 132 aspects justify the current comprehensive comparative analysis. Additionally, our analysis will include measurements of the methods' Mean Squared Errors (MSEs) besides MAPEs 133 (the only error metric previously reported). This is relevant as MSEs allow for the detection 134 135 of sporadic but significant deviations from the project duration estimates. Namely, MSEs, on measuring *quadratic* deviations instead of *absolute*, grow quicker when significant deviations 136 appear and are more difficult to dilute in error averages. MAPEs, on the other hand, tend to 137 *blur* sporadic deviations as long as the method is accurate most of the time. 138

#### 139 Previous research comparing EAC(t) methods' stability

Regarding the stability of EAC(t) methods within the temporal dimension,
significantly fewer studies can be found in the literature. Stability of the cost dimension, on
the other hand, was defined early on as the time point in the project life-cycle at which the
Cost Performance Index (CPI) is already deemed to be accurate and constant (De Koning and
Vanhoucke, 2016). Several formative studies referred to a rule of thumb which suggested
that, from approximately the 20% stage of project completion onwards, cost estimates do not

differ much from final project costs (Sato *et al.*, 2017). However, later studies have

147 consistently denied the existence of such a putative point (Henderson and Zwikael, 2008;

148 Khafri et al., 2018; Kim et al., 2019; Petter et al., 2015).

Among those studies that addressed cost stability, a few also included a description of 149 the variability that some EVM time indicators experience during project execution. The SPI 150 and the SPI(t) were the commonly preferred indicators [e.g. (Henderson and Zwikael, 2008; 151 De Koning and Vanhoucke, 2016; Ladeeda and Jeevan, 2020; De Marco et al., 2016; Petter 152 et al., 2015)]. In those studies, researchers determined whether these indicators remained 153 within an arbitrary interval (e.g.  $\pm 0.1$  or  $\pm 0.2$ ) from a given point until the end of the project 154 155 execution (Khafri et al., 2018; Petter et al., 2015). Most of them also resorted to real projects, rather than artificial ones which, as stated earlier, remains the only way of assessing multiple 156 potential outcomes of the same project (Kim, 2016; Ladeeda and Jeevan, 2020). However, 157 158 some of these studies did focus on specific project factors potentially influencing stability: namely project duration and budget, project network topology, the S-curve of the project's 159 baseline, and so forth. Some of their results have been at least partially inconclusive 160 (Henderson and Zwikael, 2008; De Koning and Vanhoucke, 2016), but they did find that 161 project duration and budget do not seem to influence project stability in real projects. They 162 also suggested that the steeper the project expenditure S-curve line was in the middle, the 163 more likely the expected stability of the CPI, SPI, and SPI(t) later in the project. 164

We can only find three studies focusing on the time stability of EAC(t) methods. The first was Wauters and Vanhoucke (2015) who compared 12 EAC(t) methods' stability and accuracy. The methods' accuracy was measured with MAPEs, whereas stability was measured with an ad-hoc *Mean Lags* estimator. This *Mean Lags* estimator was similar to the MAPE in the sense that it measured the differences in the EAC(t) estimates from one tracking period to the next in absolute percentage values. The authors claimed that their estimator had

the advantage of being independent of each method's accuracy. That is indeed true, but that is 171 not the only way of detaching stability from accuracy. In this regard, an EAC(t) method that 172 173 consistently claimed that project duration equals the Planned Duration (PD) would be perfectly stable, but utterly useless for project managers. Additionally, it seems more 174 advisable comparing the possible EAC(t) estimates at one tracking period, not with the next 175 tracking period's, but with the actual project durations, that is, with the final set of possible 176 177 Real Duration (RD) values. We are of course assuming a probabilistic approach here as, by definition, it is the only way of assessing the stability of multiple possible project realizations. 178 179 This is, as mentioned earlier, the very reason why this study cannot resort to a real projects dataset to perform the EAC(t) methods stability analysis. 180

The other two studies which compared some EAC(t) methods' stability (but this time 181 not their accuracy) were Batselier and Vanhoucke's (2017a) and de Andrade et al.'s (2019). 182 183 They proposed a Regularity Index (RI) which measured deviations in the project value accrued during execution. Namely, this index measured the Planned Value (PV) curve's 184 degree of closeness to a perfectly linear curve. However, this RI indicator conceives the 185 evolution of the PV as linear, when indeed it is usually closer to an S-shaped curve in most 186 construction projects (Hürol et al., 2020). This is because, in most construction projects, more 187 activities are being performed (and therefore generating associated costs) in the middle stages 188 of the project as compared to the initial and final stages (Narbaev and De Marco, 2017). Also, 189 this RI indicator conflates accuracy with stability. 190

Hence, due to the limitations highlighted in the three previous studies mostly
regarding their ad hoc stability indicators, our study will resort to parametric order correlation
coefficients (e.g. Spearman's and Kendall's) for measuring EAC(t) methods' stability. These
order correlation coefficients are also more statistically robust, and their interpretation easier.

195

To serve as a summary of the works reviewed in this section, Table II is included.

This table summarizes the scope and limitations of previous studies, comparing some EVMproject duration forecasting methods.

198

#### < Insert Table II here >

#### **199** Research methods

#### 200 Artificial project networks dataset

In our study, we use an artificial projects dataset which boasts 4,100 activity-on-node 201 networks with varied topologies (different configurations of activities' predecessors). Each 202 203 project has 30 activities plus two dummy activities (zero cost and duration) indicating the start and end of each project. This dataset was generated with RanGen2, a robust random 204 network generator validated in previous research (Demeulemeester et al., 2003; Vanhoucke 205 206 et al., 2008). This same dataset has been used by other studies on EVM (e.g. (Ballesteros-Pérez, Sanz-Ablanedo, et al., 2019; Batselier and Vanhoucke, 2015c; Colin and Vanhoucke, 207 2014; 2010, 2011)). The complete project dataset is currently curated by the Ghent University 208 Operations Research & Scheduling Research Group. All project files can be downloaded at: 209 https://www.projectmanagement.ugent.be/research/data (MT set). For each project, a file 210 211 containing all activities' predecessors information can be found. Files also contain information on resource allocation that will not be used in this study. 212 More precisely, these 4,100 projects were generated by setting staggered values of the 213

Serial-Parallel (SP) indicator. The SP indicator measures how close a project is to a serial
network (SP=1) or a parallel network (SP=0). The SP is calculated as:

216

$$SP = \frac{q-1}{n-1} \tag{1}$$

217 Where q is the number of activities in the path with the highest number of activities 218 (which is not necessarily the longest in duration), and n is the total number of (non-dummy) 219 activities in the network (30 in our case for all projects).

This way our project dataset contains networks with SP={7%, 17%, 28%, 38%, 48%, 59%, 69%, 79%, 90%}. More rounded values (e.g. SP=10%, 20%,30%...) were not possible due to the fixed amount of activities within each network (30). Also, we did not consider perfectly serial (SP=100%) or parallel (SP=0) projects, as those configurations are not representative of real construction projects [see some average SP values of building, civil engineering, industrial and services projects in Ballesteros-Pérez et al. (2020), Table 9].

Finally, while the 4,100 projects were generated by increasing values of the SP 226 indicator, other topological indicators were also calculated. They can be found in the Excel 227 file of the Supplemental material for each network. These other indicators are the Coefficient 228 of Network Complexity (CNC), the Order Strength (OS), the Activity Distribution (AD), the 229 Length of Arcs (LA), and the Topological Float (TF). Further details on the meaning and 230 calculations of these topological indicators can be found in Vanhoucke (2010). However, we 231 232 will not refer to them anymore as our analyses did not find any significant stability nor accuracy correlation with any of them. 233

#### 234 Activity durations and costs

235 Despite previous studies having assumed different distributions for modeling activity durations and costs, we use correlated Lognormal distributions whose variability resembles 236 that of real construction projects. Several studies support, in fact, that the distribution of 237 activity durations and costs closely resembles Lognormal distributions in real construction 238 projects (Colin and Vanhoucke, 2016; Trietsch et al., 2012; Vanhoucke, 2015). Furthermore, 239 a recent analysis of construction activities also measured that the activities' duration-cost 240 correlation can vary between 0 (no correlation whatsoever) and 100% (perfect correlation) 241 242 (Ballesteros-Pérez, Sanz-Ablanedo, et al., 2020).

243

Hence, we generate Lognormally-distributed activity duration and cost values with

some partial correlation between both values. Mathematical details on how these durationsand values are generated are included in the *Appendix*.

Additionally, when calculating the project schedules, all activities are scheduled to start as soon as possible (ASAP scheduling). Activity preemption is not allowed.

#### 248 Accuracy and stability measurement

For measuring the *accuracy* of the 27 EAC(t) project duration forecasting methods we calculate the Mean Squared Errors (MSEs) and Mean Absolute Percentage Errors (MAPEs) at 10% of project progress tracking intervals (respect the Real project Duration RD). Namely, for each EAC(t) method and tracking interval (AT), we calculate:

253 
$$MSE_{AT} = \frac{1}{M} \sum_{m=1}^{M} \left\{ \frac{1}{K} \sum_{k=1}^{K} \frac{\left( RD_{mk} - EAC(t)_{AT} \right)^2}{RD_{mk}} \right\}$$
(2)

254 
$$MAPE_{AT} = \frac{1}{M} \sum_{m=1}^{M} \left\{ \frac{1}{K} \sum_{k=1}^{K} \frac{|RD_{mk} - EAC(t)_{AT}|}{RD_{mk}} \right\}$$
(3)

255 Where:

- 256 *M* is the total number of projects analyzed (M=4100) and m=1, 2...4100.
- 257 *K* is the total number of simulation runs per project (K=100) with k=1, 2...100.
- 258  $RD_{mk}$  is project *m*'s Real Duration in simulation run *k*.

259  $EAC(t)_{AT}$  is the project duration estimate at tracking period AT=10%, 20%...100% of  $RD_{mk}$ .

For the sake of simplicity, though, we will not use an extra subscript to refer to each of the 27

- $261 \quad EAC(t) \text{ forecasting methods.}$
- As justified earlier, the MAPE allows us to directly anticipate the order of magnitude

of our errors when we use EAC(t) methods in real contexts. The MSE, on the other hand,

- allows detecting occasional, but significant errors of the EAC(t) methods.
- 265 For measuring the methods' *stability*, we resort to three correlation coefficients:

Pearson's linear correlation (*R*), Spearman's rank correlation ( $\rho$ ), and Kendall's rank

267 correlation ( $\tau$ ). The use of Spearman and Kendall's coefficients was justified in the *Literature* 

*review* section. Pearson's correlation calculations are only included for comparative purposes.

Namely, Pearson's *R* correlation of the EAC(t) estimates at every tracking period AT
with the final Real project Duration (RD) is calculated as:

271 
$$R_{AT} = \frac{1}{M} \sum_{m=1}^{M} \left\{ \frac{\sum_{k=1}^{K} \left( EAC(t)_{AT} - \overline{EAC(t)_{AT}} \right) \left( RD_{mk} - \overline{RD_{mk}} \right)}{\sqrt{\sum_{k=1}^{K} \left( EAC(t)_{AT} - \overline{EAC(t)_{AT}} \right)^2} \sqrt{\sum_{k=1}^{K} \left( RD_{mk} - \overline{RD_{mk}} \right)^2}} \right\}$$
(4)

272 Where  $\overline{EAC(t)_{AT}}$  represents the average of the EAC(t) estimates at tracking period 273 AT in the *K*=100 simulation runs; and  $\overline{RD_{mk}}$  represents the average of project *m*'s RD values 274 in the *K*=100 simulation runs.

Pearson's linear correlation coefficient R has the advantage of having a 275 276 straightforward interpretation, i.e., the higher R, the more (linearly) proportional RD values are expected to be respect to the EAC(t) estimates. However, it also has some important 277 limitations. First, it mixes accuracy and stability. Hence, it is useful as a combined indicator 278 but misleading for measuring stability only. Second, the relationship between EAC(t) and RD 279 is expected to be nonlinear, at least for early tracking periods. Third, Pearson's correlation 280 assumptions (that both variables are normally distributed, linearity and homoscedasticity) do 281 not seem realistic in our analysis. Hence, we propose using rank correlation coefficients. 282

283 Spearman's rank correlation coefficient 
$$\rho$$
 is calculated at every tracking period AT as:

284 
$$\rho_{AT} = \frac{1}{M} \sum_{m=1}^{M} \left\{ 1 - \left( 6 \sum_{k=1}^{K} d_{mk}^{2} / K \left( K^{2} - 1 \right) \right) \right\}$$
(5)

285 Where  $d_{mk}$  is the difference between the ranking (order) values of  $EAC(t)_{AT}$  and  $RD_{mk}$ 286 for project *m*, for the *K*=100 simulation runs and at a particular tracking period *AT*, that is,

287 
$$d_{mk} \equiv rank \left( EAC(t)_{AT}^{k} \right) - rank \left( RD_{mk} \right) \text{ for } k=1,2...K.$$

Spearman's correlation has the advantage of being parametric, thus, capable of
detecting nonlinear relationships among the EAC(t) estimates and the RD values.

Additionally, Spearman's correlation does not carry any assumptions about the distribution of the data and works very well with ordinal data (as in our analysis). The calculation of  $\rho$  is not computationally demanding either. However, Spearman's  $\rho$  is a little more sensitive to errors and less robust than Kendall's  $\tau$ .

That is why we also suggest the calculation of Kendall's  $\tau$  correlation coefficient for measuring the stability of the EAC(t) estimates at any tracking period AT:

296 
$$\tau_{AT} = \frac{1}{M} \sum_{m=1}^{M} \left\{ \frac{4P_m}{K(K-1)} - 1 \right\}$$
(6)

297 Where  $P_m$  represents the number of concordant pairs between the EAC(t) estimates 298 and the RD values for each project *m*, that is:

299 
$$P_{m} = \sum_{k=1}^{K-1} \sum_{\ell=k+1}^{K} \mathbf{1} \left\{ \left( EAC(t)_{AT}^{\ell} - EAC(t)_{AT}^{k} \right) \left( RD_{mk}^{\ell} - RD_{mk}^{k} \right) > 0 \right\}$$
(7)

300 Where  $\mathbf{1}(\cdot)$  is a binary operator that equals 1 when the condition is fulfilled and 0 301 when it is not.

Kendall's rank correlation coefficient is the more robust of all three correlation coefficients for measuring the methods' stability. However, its values tend to be lower than Spearman's and it also is much more computationally expensive. Particularly, the calculations involved in Kendall's  $\tau$  are proportional to  $K^2$ , that is, 10.000 assuming K=100. (number of simulation runs per project). However, since we are evaluating 4,100 projects, 27 EAC(t) methods and 10 tracking periods, the number of calculations quickly skyrockets ( $10^4 \cdot 4100 \cdot 27 \cdot 10 = \cdot 1.107 \cdot 10^{10}$ ). This is the reason why only 100 iterations were performed per project. Otherwise, for *K*=1000 simulation runs per project, for example, the computational
effort would have required months of computing time for an average computer.

Still, as the total number of simulations is circa half a million (4,100 projects 100 simulations/project= $0.41 \cdot 10^6$ ) this will provide us with enough accuracy up to the second decimal place in our results. The latter as the error of Monte Carlo estimates are proportional to  $1/\sqrt{n^\circ simul. runs} = 1/\sqrt{M \cdot K} = 1/\sqrt{0.41 \cdot 10^6} = 0.00156 < 1\%$  (Koehler *et al.*, 2009).

- Finally, for the sake of clarity, Figure 1 includes a graphical description of bothSpearman and Kendall's correlation coefficients interpretation.
- 317

#### < Insert Figure 1 here >

For the examples shown in Figure 1, Pearson's correlation coefficient would have turned out low values. This is because this coefficient measures relative numerical deviations between the EAC(t) estimates and the project's possible Real Duration RD outcomes.

However, both Spearman's  $\rho$  and Kendall's  $\tau$  coefficient values depend on relative 321 order differences, not on pairwise numerical differences. Hence, it does not matter whether 322 323 each pair of (EAC(t), RD) values is numerically close, nor whether their deviations follow a nonlinear relationship. What matters is the degree of coincidence between the relative orders 324 of both sets of values. If there is a good match, then EAC(t) estimates will remain in an 325 approximately constant percentile until the project finishes. This means each EAC(t) estimate 326 will point towards the correct RD value from that tracking period onwards. This calculation 327 becomes much more accurate of course, as we count on more data points. That is why we 328 329 used *K*=100 (iterations) points per project.

330 Results

331

Once the artificial projects dataset, the simulation framework and the analysis

332	variables have all been described, Figure 2 and 3 present the 27 EAC(t) project duration
333	forecasting methods' stability and accuracy results for the 4,100 artificial projects. As
334	justified earlier, the methods' stability is represented by three correlation coefficients
335	(Pearson's <i>R</i> , but mostly Spearman's $\rho$ and Kendall's $\tau$ ) at the top of both Figures 2 and 3.
336	The methods' accuracy, on the other hand, is measured by MSEs and MAPEs both at the
337	bottom left and center of Figures 2 and 3, respectively. The difference between Figures 2 and
338	3 lays in the performance results of each sub-table being classified by tracking period AT
339	(Figure 2) or by the value of the Serial-Parallel indicator SP (Figure 3). A performance
340	summary table is also included at the bottom right corner of Figures 2 and 3.
341	< Insert Figure 2 here >
342	< Insert Figure 3 here >
343	Interpretations of these two tables are rich but highly varied. We will focus on the
344	most relevant only. Further details presented by projects can be found as Supplemental
345	material.
346	EAC(t) methods stability
347	Comparatively speaking, the average results of the three correlation coefficients (see
348	summary tables at the bottom right corner of Figures 2 and 3) are not that different. However,
349	Kendall's $\tau$ correlation values are significantly lower and produce slightly different results.
350	As expected, the closer the tracking period is to the end of the project in Figure 2 (AT
351	values closer to 100% of RD), the higher the stability and accuracy of all EAC(t) methods.
352	This agrees with almost all existing research on both project duration and cost forecasting
353	(Henderson and Zwikael, 2008; De Marco et al., 2016; Warburton et al., 2017). It is worth
354	noticing, though, that AT=100%RD does not represent a finished project but a project that
355	has just less than one day left to finish. Otherwise, stability and accuracy results would have

been perfectly stable and accurate at AT=100%RD for most methods.

357 Analogously, but now in Figure 3, the higher the Serial-Parallel indicator (meaning more serial networks), the more stable and accurate all methods become. This echoes the 358 359 results of Vanhoucke (2010) and Ladeeda and Jeevan (2020). Particularly, R and  $\rho$  values are very high for projects with SP>80%. Conversely, for parallel projects with SP<30%, all 360 EAC(t) methods are quite unstable. In fact, among Kendall's  $\tau$  results, we can even find some 361 negative correlation values. This means EAC(t) methods produced estimates which are 362 reversed in order with the actual RD values. This can only be fully appreciated, though, in the 363 project-by-project results in the Supplemental material. Therein, it can be observed how for 364 projects with low SP values, almost all EAC(t) methods have negative correlation values 365 during the early stages of project execution (AT<30%RD). This renders all EAC(t) methods 366 useless at the early stages of a project when the project network is close to parallel. Thus, 367 368 EAC(t) methods may still be accurate, but lower EAC(t) estimates will point towards longer RD values, whereas higher EAC(t) estimates will end up in shorter project durations. 369 Regarding projects with SP values between 20% and 80%, we can find moderate 370 correlation coefficients in most cases (R,  $\rho$  and  $\tau$  values between 0.40 and 0.80). But it must 371 be borne in mind that these are *average* values for all tracking periods. That is, if a 372 correlation coefficient is, for example, 0.50, this means that it will probably have been close 373 to 0 at early tracking periods, but surely above 0.80 in later stages. Hence, for projects with 374 moderate SP values, most EAC(t) methods are sufficiently stable, but only once half of the 375 project execution has been exceeded. This is also in agreement with previous studies [e.g. (de 376 Andrade et al., 2019; Batselier and Vanhoucke, 2017a; Wauters and Vanhoucke, 2015)] and 377 can be better appreciated in the AT>50%RD columns presented within the three tables at the 378 top of Figure 2. 379

#### 380 *EAC(t) methods accuracy*

Regarding EAC(t) methods' accuracy (tables at the bottom half of Figures 2 and 3), we can find a similar pattern for both the MSEs and the MAPEs. Particularly, it is only from the middle of the project execution onwards (AT>50%RD in Figure 2) that the errors are relatively small (MSEs<1 and MAPEs<10%) for most EAC(t) methods. This agrees with the findings of Ballesteros-Pérez et al. (2019) who analyzed some EAC(t) methods using MAPEs.

When it comes to the influence of the network topology in Figure 3, most EAC(t) methods perform sufficiently well (MAPEs<10%) for projects with SP>50% (rather serial projects). The same happens with MSEs but only for projects whose SP>60%. This means that, halfway through the project execution, we can still find some sporadic but relevant estimation errors in most EAC(t) methods.

On the other side of the spectrum, Figure 2 shows that most EAC(t) methods seem to be very inaccurate during the first third of the project execution (AT<30%RD), even until much later in projects with SP<30%. This issue had not been identified within the extant literature on EVM, however, the results clearly indicate that, at this execution stage, MAPEs >> 10% and MSEs are usually above unity.

#### 397 Top-performing EAC(t) methods

In the two tables at the bottom right corner of Figures 2 and 3, we can find a summary of which methods perform well (\*) or excel (\*\*) in both stability and accuracy dimensions. Figure 2 depicts an average assessment considering that there are more possible network combinations of projects in the dataset with intermediate values of the SP indicator (as also happens in real projects). In Figure 2, methods 14 and 22 are the top performers, but methods 7, 12, 16, 20 and 25 are also good. It is worth highlighting that almost all of these EAC(t)

404 methods use the configuration  $AT+(PD-ES_x)/PF$  with a Performance Factor PF=1, that is, 405 one of the simplest mathematical configurations. Similar findings had also been reported by 406 Vanhoucke (2010) and Ballesteros-Pérez et al. (2019), although the authors compared fewer 407 EAC(t) methods.

However, when analyzing the summary performance results in Figure 3, we find some 408 409 unexpected results. When averaged by the SP indicator, most methods that are stable are not accurate, and vice versa. This was earlier suggested by Wauters and Vanhoucke (2015) but 410 could not be validated by Batselier and Vanhoucke (2017a) or de Andrade et al. (2019). 411 However, there is one method that is sufficiently stable and highly accurate (method 22). This 412 method uses the configuration AT+PD-ES<sub>min</sub>, where ES<sub>min</sub> is the Earned Schedule calculated 413 on the most delayed path during the project execution. Method 22 limits the quadratic errors 414 very early (AT>40%RD) compared to other methods, and from that point onwards we can 415 416 also expect project duration estimates to differ <10% from the final Real Duration RD.

Finally, it is worth noticing that among methods 22 to 27, there are several which are very stable and others which are very accurate. Since these six methods are quite similar to each other (they use variants of the same metrics  $ES_{min}$  and  $ES_{max}$  with different Performance Factors), future efforts might look for superior combinations of these metrics. This is left for future research, however, as it is not the intention of this paper to propose new EAC(t) methods.

#### 423 Discussion

Results have shown that in parallel projects (SP<25%), most EAC(t) methods are very</li>
inaccurate and unstable (MSEs>1, MAPEs>15% and correlation coefficients<40%). The</li>
opposite happens to serial projects (SP>60%) in which most EAC(t) methods are quite
accurate and stable (MSEs<0.5, MAPEs<10% and correlation coefficients>70%). In projects

with intermediate topologies (25%<SP<60%), we can expect most EAC(t) methods to</li>
become sufficiently accurate and stable too, but only approximately from the middle of the
project execution onwards.

431 A pertinent question is, how can real construction projects benefit from these 432 findings? Inevitably, when a project manager observes that the duration forecast anticipates a 433 project duration significantly longer than that originally envisaged, he or she may need to take action to bring the project back on track. The project manager will then either have to 434 allocate more resources to make the existing project(s) more efficient and/or make the 435 contractors work overtime. However, the specific nature of the systemic project changes 436 437 triggered by a likely late completion date falls beyond the remit of this work. However, a construction manager might ask 'which are the serial-parallel (SP) values of real construction 438 projects so that we can select the best project duration forecasting method?' 439

In this regard, serial projects tend to perform the most relevant activities one after the 440 441 other. Highway projects, pipelines, train tracks, and renewable energy projects are some examples of projects with high SP values (Ballesteros-Pérez, Sanz-Ablanedo, et al., 2020). 442 However, when they have enough resources, these projects' activities can also be partially 443 executed in parallel. Examples of parallel projects with low SP values are usually those that 444 involve several but simple and homogeneous construction units. Examples are residential 445 condominiums, quarry earthworks, off-site prefabrication, etc. (Ballesteros-Pérez, Sanz-446 Ablanedo, et al., 2020). In between, we can find most construction projects whose schedules 447 boast a mixture of series and parallel paths. Among them, we have most buildings, industrial 448 449 facilities, water treatment plants, etc.

Hence, when choosing a project duration forecasting method, the project manager will
need to consider the project seriality and/or the number of resources he/she counts on to
perform the project. If many parallel paths or lines of work are expected to be active

simultaneously, most EAC(t) methods will provide very inaccurate and unstable estimates, at
least until the end of the project is near. But probably by then, the project might be very
difficult to bring back on track if it was delayed and/or was too expensive. For these types of
projects, other suitable project control and duration forecasting alternatives would be
Schedule Risk Analysis (SRA) or Stochastic Network Analysis (SNA) (Ballesteros-Pérez,
Cerezo-Narváez, *et al.*, 2019).

Conversely, if the project has just a few parallel paths and/or few resource teams, 459 earned value management EAC(t) methods constitute a simpler yet accurate and stable 460 alternative for forecasting the project duration. For most construction projects with 461 30%<SP<100%, the EAC(t) methods described here will also be a good alternative. 462 However, apart from method 22 (which becomes reliable from 40% of the project execution 463 onwards), the others might need to wait until 50-60% of the project has been executed. Many 464 465 project managers may still find that this point as too late to take corrective actions (Ballesteros-Pérez, Elamrousy, et al., 2019), and it probably is. 466

#### 467 Conclusions

468 Earned Value Management (EVM) is a common project monitoring and control technique for measuring how a project is performing in both time and cost dimensions. Over 469 470 the last 20 years, many EVM-based project duration forecasting expressions (named EAC(t)) have been proposed. However, their accuracy and stability had not been exhaustively 471 measured. Among the very limited studies comparing EAC(t) methods' accuracy or stability, 472 none has included all recent EAC(t) expressions, most have used ad hoc indicators whose 473 results are difficult to generalize, and they did not simulate activities' variability according to 474 475 real construction projects.

476

This study has performed a comparison of all deterministic EAC(t) project duration

forecasting methods found in the literature (27 methods to date). The methods' stability has
been measured using three correlation coefficients (namely, Pearson's, Spearman's, and
Kendall's), whereas accuracy has been measured with Mean Squared Errors (MSEs) and
Mean Absolute Percentage Errors (MAPEs). Additionally, all of these parameters have been
evaluated and analyzed at 10% project progress intervals on a project dataset with 4,100
artificial networks with varied Serial-Parallel (SP) indicator values.

The most relevant results point out that almost all EAC(t) methods produce very inaccurate estimates until at least half of the project is completed. On the contrary, in the last third of the project, most methods are very accurate. Regarding stability, most EAC(t) methods are quite unstable in the early third of the project execution. However, in the last third, all EAC(t) methods become quite stable.

Regarding project topology, the results support that stability and accuracy are
inversely correlated for most EAC(t) methods, and that both significantly worsen as project
networks become more parallel (mostly for projects with SP<30%).</li>

Among the top-performing EAC(t) methods, method 22:  $AT+PD-ES_{min}$  is quite stable and highly accurate, even from the early stages of project progress. It also shows promise for further enhancing its accuracy and stability by combining it with other similar methods that use the *ES<sub>min</sub>* and *ES<sub>max</sub>* metrics. This is expected to be addressed in future research.

A comparison of current EVM project *cost* forecasting methods is expected to be
addressed in future research. This should be relatively straightforward once all cost-related
performance indicators have been parametrized and included within the calculation
framework developed for this paper. A performance comparison of deterministic *vs* nondeterministic project forecasting methods, incorporating both time and cost dimensions, will
also be developed. However, this will involve departing from the EVM framework and

501 implementing alternative calculation approaches (e.g. multivariate regression, statistical
502 learning, fuzzy logic, etc.)

Limitations of this study are mostly related to the size of the projects in the dataset 503 and the number of simulations performed in each project. Regarding the project size, all 504 networks had 30 (non-dummy) activities. Regarding the number of simulations, only 100 505 506 simulation runs per project were performed. The size and number of simulations were intentionally restricted to avoid the number of calculations from skyrocketing, especially 507 when it comes to calculating Kendall's rank correlation coefficient. However, considering the 508 analysis encompassed 4,100 different projects, we still expect our results to be sufficiently 509 510 representative of most real construction projects.

#### 511 Appendix

512 This appendix provides detailed explanations on how the activity durations and costs 513 were generated for each of the 4,100 artificial projects. Their activity duration and cost mean 514 values and dispersion values were generated so that they resembled those from real 515 construction project activities. Activity durations and costs were also correlated.

516 Namely, Lognormally-distributed activity durations  $(d_i)$  were generated in this study 517 for each activity *i* by means of these expressions:

519

$$d_i \sim e^{Normal(mean = \mu_i, st.dev. = \sigma_i)}$$
(8)

$$\mu_i \sim Normal \left(mean = 1, st. dev. = 0.25\right) \tag{9}$$

520 
$$\sigma_i \sim \mu_i \cdot Uniform(lower bound = 0.25, upper bound = 0.75)$$
 (10)

521 Where *e* is Euler's number; Normal(·) and Uniform (·) are the Normal and Uniform 522 distributions, respectively;  $\mu_i$  is the Normal distribution mean calculated according to 523 equation (9); and  $\sigma_i$  is the activity durations standard deviation according to equation (10). 524 The Normal distribution of  $d_i$  in equation (8) becomes Lognormal when exponentiated. The 525 Uniform distribution in equation (10) acts as the Coefficient of Variation ( $CV_i = \sigma_i / \mu_i$ ) whose 526 values are set to resemble those of real construction projects as measured by Ballesteros-527 Pérez et al. (2020).

528 Activity costs ( $c_i$ ) are also randomly generated for each project and activity *i*, but now 529 introducing a duration-cost correlation coefficient ( $\delta_i$ ):

530 
$$c_i \sim e^{\left(\mu'_i + \sigma'_i \cdot X_i\right)} \tag{11}$$

531 
$$\mu'_{i} \sim Normal(mean = 10, st. dev. = 1)$$
(12)

532 
$$\sigma'_{i} \sim \mu'_{i} \cdot Uniform(lower bound = 0.25, upper bound = 0.75)$$
(13)

533 
$$X_{i} \sim \delta_{i} \frac{LN(d_{i}) - \mu_{i}}{\sigma_{i}} + \sqrt{1 - \delta_{i}^{2}} \cdot Normal(mean = 0, st.dev. = 1)$$
(14)

534

$$\delta_i \sim Uniform(lower bound = 0.0, upper bound = 1.0)$$
 (15)

Where most variables are analogous to previous equations (8) to (10), but now some 535 of them with an apostrophe (') indicating that they refer to costs instead of durations. 536  $X_i$  refers to an auxiliary correlated Normally-distributed random variable. This variable helps 537 simplifying the mathematical expressions above and allows generating activity costs which 538 are correlated with the activity durations. Namely, the value of  $X_i$  is partially conditioned by 539 the  $d_i$  value obtained from equation (8), and the rest is randomly generated according to a 540 541 standard Normal distribution. Again, the values chosen in equations (13) and (15) are representative of real construction activities (Ballesteros-Pérez, Sanz-Ablanedo, et al., 2020). 542 Each project calculation involves variables  $\mu_i$ ,  $\mu'_i$ ,  $\sigma_i$ ,  $\sigma'_i$  and  $\delta_i$  being randomly 543 generated for each activity at the outset. These variables are forced to remain constant when 544 100 stochastic simulations are performed for each project. Hence, 100  $d_i$  and  $c_i$  values are 545 stochastically generated in these 100 projects simulations while keeping the other variables 546 constant. Only with this approach is it possible to ensure that each activity duration and cost 547 keeps the same average, dispersion, and correlation values across simulations. 548

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ID	Method	EAC(t)	Mathematical expression	Authors	Brief description
1	EVM	PVI	$EAC(t)_{EVM PVI} = PD(1 - (EV - PV)/BAC)$		Methods 1-3 adjust the Planned Project Duration (PD) by subtracting a
2	EVM	PV2	$EAC(t)_{EVM PV2} = PD/SPI$	(Anbari, 2004)	Time Variance factor $(TV=SV/PV_{rate}=(EV-PV)\cdot PD/BAC)$ in method 1; or by dividing <i>PD</i> by the Schedule Performance Index ( <i>SPI</i> ) or the
3	EVM	PV3	EAC(t) <sub>EVM PV3</sub> =PD/SCI		Schedule Critical Index ( <i>SCI</i> ) in methods 2 and 3, respectively.
4	EVM	ED1	$EAC(t)_{EVM ED1} = MAX(PD, AT) + AT(1-SPI)$		Methods 4 to 6 were originally expressed as a function of a metric
5	EVM	ED2	$EAC(t)_{EVM ED2} = MAX(PD, AT)/SPI$	(Jacob, 2003)	named Earned Duration ( $ED' = AT \cdot SPI$ ). $ED'$ has nothing to do with the $ED$ metric from methods 14 and 15. These $EAC(t)$ expressions, though,
6	EVM	ED3	$EAC(t)_{EVM ED3} = MAX(PD,AT)/SCI + AT(1-(1/CPI))$		have been worked out and skip the use of $ED'$ .
7	EVM	ES1	$EAC(t)_{EVM ESI} = AT + PD - ES$		Methods 7 to 9 follow the formula <i>AT</i> +( <i>PD-ES</i> )/ <i>PF</i> , where <i>ES</i> is the
8	EVM	ES2	$EAC(t)_{EVM ES2} = AT + (PD-ES)/SPI(t)$	(Lipke, 2003)	Earned Schedule and <i>PF</i> is a Performance Factor. <i>PF</i> equals 1 in method 7; $PF=SPI(t)=ES/AT$ in method 8, or $PF=SCI(t)=SPI(t)\cdot CPI$ in method
9	EVM	ES3	$EAC(t)_{EVM ES3} = AT + (PD-ES)/SCI(t)$		9.
10	EDM	PV1	$EAC(t)_{EDM PVI} = PD(1-(TED-TPD)/BAC(t))$		Methods 10 to 15 were proposed under the Earned Duration
11	EDM	PV2	$EAC(t)_{EDM PV2} = PD/EDI$		Management (EDM) framework. In EDM, the activity (planned and actual) costs are replaced by activity (planned and actual) durations.
12	EDM	ED1	$EAC(t)_{EDM EDI} = MAX(PD, AT) + AT(1-EDI)$	(Khamooshi and Golafshani,	Metric names change, but methods 10-15 are equivalent to 1,2, 4, 5, 7
13	EDM	ED2	$EAC(t)_{EDM ED2} = MAX(PD, AT)/EDI$	2014)	and 8, respectively. There are no counterparts of <i>CPI</i> and <i>SCI</i> in EDM, that is why methods 3, 6 and 9 do not have equivalent methods in EDM.
14	EDM	ES1	$EAC(t)_{EDMESI} = AT + PD - ED$		
15	EDM	ES2	$EAC(t)_{EDM ES2} = AT + (PD-ED)/DPI$		
16	ESM	ESM1	$EAC(t)_{ESM ESI} = AT + PD - ES(e)$		Methods 16 to 18 are similar to methods 7 to 9. However, these replace
17	ESM	ESM2	$EAC(t)_{ESM ES2} = AT + (PD-ES(e))/SPI(t)(e)$	(Lipke, 2011)	the Earned Schedule ( <i>ES</i> ) with the effective Earned Schedule ( <i>ES</i> ( <i>e</i> )). <i>ES</i> ( <i>e</i> ) represents the fraction of Earned Value ( <i>EV</i> ) performed according
18	ESM	ESM3	$EAC(t)_{ESM ES3} = AT + (PD - ES(e))/SCI(t)(e)$		to the original schedule, as measured by the p-factor (Lipke 2004).
19	XSM	XSM1	$EAC(t)_{XSM XSM1} = AT + (PD-ES)/T_{t,SPI(t)}$	(Khamooshi and Abdi, 2017)	Methods 22 to 24 apply exponential smoothing techniques so that they
20	XSM	XSM2	$EAC(t)_{XSM XSM2} = AT + (PD-ES)/(T_{t,AT}/T_{t,ES})$	(Batselier and Vanhoucke, 2017)	weight not just immediate (current) metrics progress, but also past information to some extent. Namely, methods 19 and 20 are the
21	XSM	XSM3	$EAC(t)_{XSM XSM2} = AT + (PD-ES)/T_{t,EDI}$	(Khamooshi and Abdi, 2017)	counterparts of method 7 with different smoothing factors $T$ ; whereas method 21 is the equivalent of method 14.
22	$\mathrm{ES}_{\min}$	ES1	$EAC(t)_{ESmin ESI} = AT + PD - ES_{min}$		Methods 22 to 24 are the counterparts of methods 7 to 9, respectively.
23	$ES_{\text{min}}$	ES2	$EAC(t)_{ESmin ES2} = AT + (PD - ES_{min})/SPI(t)_{ESmin}$		However, these methods replaced the Earned Schedule metric ( <i>ES</i> ) with the Earned Schedule min metric ( $ES_{min}$ ). $ES_{min}$ measures the project
24	$\mathrm{ES}_{\mathrm{min}}$	ES3	$EAC(t)_{ESmin ES3} = AT + (PD-ES_{min})/SCI(t)_{ESmin}$		progress as a function of its most delayed path.
25	$\mathrm{ES}_{\mathrm{max}}$	ES1	$EAC(t)_{ESmax ESI} = AT + PD - ES_{max}$	(Ballesteros-Pérez et al., 2019)	Methods 25 to 27 are equivalent to methods 7 to 9, respectively.
26	$\mathrm{ES}_{\mathrm{max}}$	ES2	$EAC(t)_{ESmax ES2} = AT + (PD - ES_{max})/SPI(t)_{ESmax}$		However, the former replaced the Earned Schedule metric ( <i>ES</i> ) with the Earned Schedule max metric ( $ES_{max}$ ) while the latter measure the project
27	$\mathbf{ES}_{max}$	ES3	$EAC(t)_{ESmax ES3} = AT + (PD - ES_{max})/SCI(t)_{ESmax}$		progress as a function of its most advanced path.

Table I. Project Duration forecasting methods EAC(t) (all variables and mathematical details can be found in the Supplemental material)

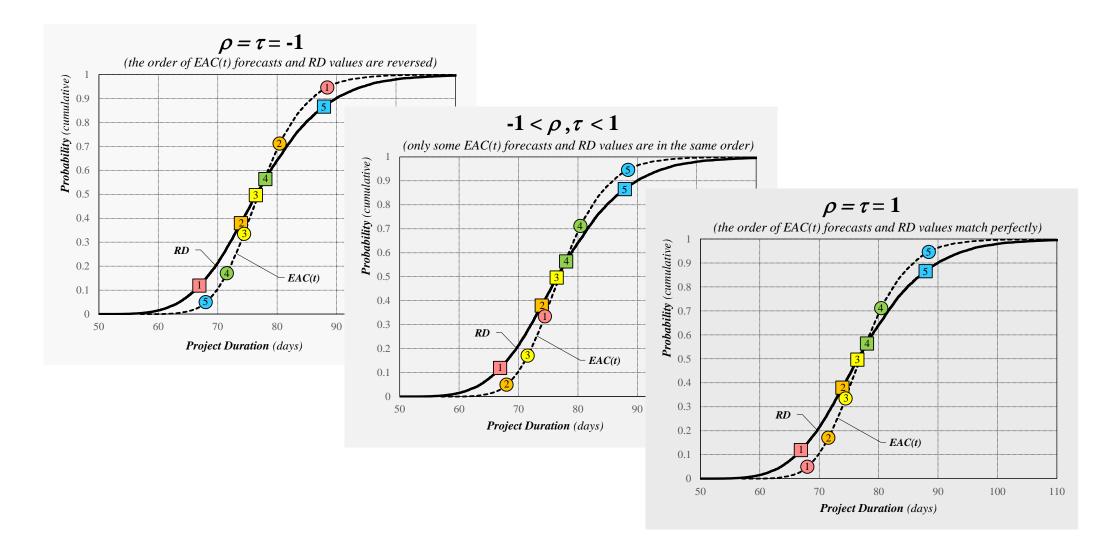
Study	Accu	racy	Stability	Project da	ıtaset	EAC(t) n	nethods
(Reference)	MAPE	MSE	Ad-hoc indicator	Nº simulated projects	N° real projects	Methods compared	Top performers
(Vanhoucke 2010)	~		-	4100	-	1-9	7
(Batselier and Vanhoucke 2015b)	~		-	-	23	1-9	7
(Batselier and Vanhoucke 2015c)	~		-	-	23	7, 15 & 16	7
(Khamooshi and Abdi 2017)		<b>√</b> *		-	19	10-13, 22 & 24	22 & 24
(Batselier and Vanhoucke 2017b)	~		-	-	23	9 & 20	9
(de Andrade and Vanhoucke 2017)	~		-	-	14	7 & 15	7
(Ballesteros-Pérez et al. 2019)	~		-	4100	23	1-22 & 25	22
(Wauters and Vanhoucke 2015)	~		Mean lags indicator	90	2	1-9**	7
(Batselier and Vanhoucke 2017a)	~		Regularity index	Not specified	23	1-9	7
(de Andrade et al. 2019)	~		Regularity index	-	57	7-9, 14 & 15	7 & 14
This study	✓	✓	<i>R</i> , $\rho$ and $\tau$ correlations	4100	_***	1-27	22

Table II. Summary of the relevant existing research on deterministic EVM project duration forecasting methods on accuracy and stability

\* Khamooshi and Abdi (2017) actually used the Root Mean Squared Error (RMSE) which is quite an unusual error metric.

\*\* Wauters and Vanhoucke also compared the performance of one non deterministic EVM method proposed by Elshaer (2013).

\*\*\* Due to the probabilistic approach adopted in this study to measure the EAC(t) methods stability, it is not possible to resort to real projects.



**Figure 1:** Interpretation of EAC(t) metrics stability through Spearman's  $\rho$  and Kendall's  $\tau$  parametric tests of rank correlation.

			Aver	age F	Pearso	on's F	2									Aver	age S	Spear	man's	r								Avera	age K	enda	<i>ll's</i> t								
Track	. per. (%	6RD) ►	0%	10%	20%	30%	40%	50	% 6	60%	70%	80%	90%	100%		0%	10%	20%	30%	40%	50%	60%	70%	80%	90%	100%		0%	10%	20%	30%	40%	50%	60%	70%	80%	90%	100%	
ID	Method	EAC(t)	0.00	0.29	0.40	0.50	0.58	0.6	66 (	0.73	0.80	0.86	0.90	0.92	Avg.	0.00	0.29	0.41	0.50	0.58	0.66	0.73	0.80	0.86	0.91	0.93	Avg.	0.00	0.09	0.20	0.28	0.35	0.41	0.47	0.53	0.59	0.65	0.67	Avg.
1	EVM	PV1	0.00	0.25	0.39	0.50	0.58	0.6	64 (	0.69	0.71	0.72	0.70	0.63	0.58	0.00	0.27	0.40	0.50	0.58	0.65	0.70	0.75	0.77	0.77	0.71	0.61	0.00	-0.02	0.13	0.23	0.30	0.36	0.40	0.43	0.43	0.36	0.10	0.27
2	EVM	PV2	0.00	0.27	0.37	0.46	0.53	0.5	59 (	0.65	0.69	0.71	0.70	0.63	0.56	0.00	0.31	0.40	0.49	0.57	0.63	0.69	0.74	0.77	0.77	0.71	0.61	0.00	0.14	0.21	0.28	0.33	0.38	0.42	0.44	0.44	0.37	0.10	0.31
3	EVM	PV3	0.00	0.20	0.28	0.35	0.41	0.4	15 (	0.48	0.49	0.47	0.42	0.35	0.39	0.00	0.23	0.30	0.37	0.42	0.46	0.49	0.51	0.50	0.46	0.37	0.41	0.00	0.11	0.17	0.21	0.25	0.28	0.30	0.31	0.30	0.26	0.20	0.24
4	EVM	ED1	0.00	0.25	0.39	0.51	0.60	0.6	58 (	0.75	0.82	0.88	0.94	0.98	0.68	0.00	0.28	0.40	0.50	0.59	0.66	0.73	0.80	0.87	0.95	0.99	0.68	0.00	-0.08	0.09	0.20	0.28	0.34	0.41	0.47	0.55	0.65	0.74	0.36
5	EVM	ED2	0.00	0.27	0.37	0.46	0.54	0.6	51 (	0.70	0.79	0.87	0.94	0.98	0.65	0.00	0.31	0.40	0.49	0.57	0.64	0.71	0.78	0.87	0.95	0.99	0.67	0.00	0.14	0.21	0.28	0.34	0.38	0.43	0.49	0.56	0.66	0.75	0.42
6	EVM	ED3	0.00	0.21	0.29	0.38	0.46	0.5	i3 (	0.63	0.73	0.84	0.93	0.98	0.60	0.00	0.24	0.33	0.41	0.49	0.56	0.63	0.72	0.81	0.92	0.98	0.61	0.00	0.12	0.18	0.24	0.29	0.34	0.39	0.46	0.54	0.65	0.75	0.40
7	EVM	ES1	0.00	0.28	0.44	0.56	0.65	0.7	13 (	0.80	0.86	0.92	0.97	1.00	0.72	0.00	0.27	0.41	0.52	0.61	0.69	0.76	0.83	0.90	0.96	1.00	0.70	0.00	-0.03	0.14	0.25	0.34	0.42	0.49	0.56	0.64	0.73	0.80	0.43
8	EVM	ES2	0.00	0.31	0.40	0.50	0.59	0.6	57 (	0.75	0.83	0.90	0.96	1.00	0.69	0.00	0.31	0.42	0.51	0.60	0.67	0.75	0.82	0.89	0.95	0.99	0.69	0.00	0.16	0.24	0.31	0.38	0.44	0.50	0.57	0.64	0.73	0.80	0.48
9	EVM	ES3	0.00	0.23	0.33	0.43	0.52	0.6	51 (	0.70	0.79	0.87	0.95	1.00	0.64	0.00	0.26	0.36	0.46	0.54	0.63	0.71	0.79	0.87	0.95	0.99	0.66	0.00	0.14	0.21	0.28	0.34	0.40	0.47	0.54	0.63	0.72	0.80	0.45
10	EDM	PV1	0.00	0.31	0.45	0.55	0.62	0.6	58 (	0.73	0.76	0.76	0.74	0.66	0.62	0.00	0.30	0.43	0.52	0.61	0.67	0.73	0.78	0.80	0.80	0.72	0.64	0.00	0.01	0.16	0.25	0.33	0.39	0.44	0.47	0.48	0.43	0.18	0.31
11	EDM	PV2	0.00	0.34	0.42	0.50	0.57	0.6	53 (	0.69	0.73	0.75	0.74	0.66	0.60	0.00	0.34	0.43	0.52	0.60	0.66	0.72	0.77	0.80	0.80	0.72	0.64	0.00	0.17	0.24	0.30	0.36	0.40	0.45	0.48	0.49	0.43	0.18	0.35
12	EDM	ED1	0.00	0.31	0.45	0.56	0.64	0.7	/1 (	0.79	0.85	0.91	0.96	0.99	0.72	0.00	0.30	0.42	0.52	0.61	0.68	0.75	0.83	0.90	0.96	1.00	0.70	0.00	-0.06	0.11	0.22	0.31	0.37	0.44	0.51	0.59	0.69	0.77	0.39
13	EDM	ED2	h00000000	0.34	0.42	0.50	0.58	0.6	5 (	0.74	0.82	0.90	0.96	0.99	0.69	0.00	0.34	0.43	0.52	0.60	0.66	0.74	0.81	0.89	0.96	1.00	0.69	0.00	0.17	0.24	0.30	0.36	0.41	0.46	0.52	0.60	0.69	0.77	0.45
14	EDM	ES1	0.00	0.31	0.46	0.57	0.66	0.7	4 (	0.81	0.87	0.93	0.97	1.00	0.73	0.00	0.30	0.45	0.53	0.62	0.70	0.77	0.84	0.91	0.96	1.00	0.71	0.00	-0.03	0.15	0.26	0.35	0.42	0.50	0.57	0.65	0.73	0.81	0.44
15	EDM	ES2	0.00		0.43	0.52	0.60	0.6	58 (	0.76	0.83	0.90	0.96	1.00	0.70	0.00	0.35		0.53	0.61	0.69	0.76	0.83	0.90	0.96	1.00	0.71	0.00	0.18	0.25	0.32	0.38	0.45	0.51	0.58	0.65	0.73	0.81	0.49
16	ESM	ES1	0.00		0.44	0.55	0.64	0.7	2 (	0.80	0.86	0.92	0.97	1.00	0.72	0.00	0.28	0.41	0.51	0.60	0.68	0.76	0.83	0.90	0.96	0.99	0.69	0.00	-0.03	0.14	0.25	0.33	0.41	0.49	0.56	0.64	0.72	0.80	0.43
17	ESM	ES2	0.00		0.38	0.48	0.57	0.6	66 (	0.74	0.82	0.89	0.96	1.00	0.68	0.00	0.27	0.39	0.49	0.58	0.66	0.74	0.82	0.89	0.95	0.99	0.68	0.00	0.14	0.22	0.30	0.37	0.43	0.50	0.57	0.64	0.73	0.80	0.47
18	ESM	ES3	0.00		0.31	0.41	0.51	0.6	60 (	0.69	0.78	0.87	0.95	1.00	0.63	0.00	0.24		0.44	0.53	0.62	0.70	0.79	0.87	0.95	0.99	0.65	0.00	0.12	0.20	0.27	0.33	0.40	0.47	0.54	0.62	0.72	0.80	0.45
19	XSM	XSM1		0.26	0.41	0.51	0.59	0.6	57 (	0.75	0.82	0.89	0.96	1.00	0.69	0.00	0.25	0.40	0.51	0.60	0.67	0.75	0.82	0.89	0.95	0.99	0.68	0.00	0.09	0.22	0.30	0.37	0.43	0.50	0.57	0.64	0.72	0.80	0.46
20	XSM	XSM2	0.00	0.30	0.45	0.55	0.63	0.7	0 0	0.76	0.83	0.90	0.96	1.00	0.71	0.00	0.28	0.42	0.52	0.61	0.68	0.75	0.82	0.89	0.95	0.99	0.69	0.00	0.06	0.20	0.29	0.37	0.43	0.50	0.57	0.64	0.73	0.80	0.46
21	XSM	XSM3	0.00	0.29	0.44	0.53	0.61	0.6	68 (	0.76	0.84	0.91	0.97	1.00	0.70	0.00	0.27	0.42	0.52	0.61	0.68	0.76	0.83	0.90	0.96	1.00	0.69	0.00	0.10	0.22	0.30	0.37	0.43	0.50	0.57	0.64	0.73	0.81	0.47
22	ESmin	ES1		0.34	0.47	0.58	0.67	0.7	5 (	0.82	0.88	0.93	0.97	1.00	0.74		0.32	0.45	0.55	0.64	0.71	0.79	0.85	0.91	0.96	1.00	0.72	0.00	0.06	0.19	0.29	0.37	0.44	0.51	0.58	0.66	0.74	0.81	0.46
23	ES <sub>min</sub>	ES2	0.00		0.42	0.52	0.60	0.6	59 (	0.77	0.84	0.91	0.96	1.00	0.70	0.00	0.34	0.45	0.54	0.63	0.70	0.77	0.84	0.91	0.96	1.00	0.71	0.00	0.20	0.27	0.34	0.40	0.46	0.53	0.59	0.66	0.74	0.81	0.50
24	ES <sub>min</sub>	ES3	0.00		0.37	0.45	0.54	0.6	53 (	0.72	0.80	0.89	0.96	1.00	0.66	0.00	0.31	0.40		0.58	0.66	0.74	0.81	0.89	0.95	1.00	0.68		0.18	0.25	0.31	0.37	0.43	0.50	0.57	0.64	0.73	0.81	0.48
25	ESmax	ES1	0.00		0.40	0.54	0.64	0.7	3 (	0.80	0.87	0.92	0.97	1.00	0.71	0.00			0.50		0.69	0.77	0.84	0.90	0.96	1.00	0.69			0.14	0.25	0.34	0.42	0.49	0.57	0.65	0.73	0.81	0.44
26	ESmax	ES2	0.00		0.45	0.54	0.62	0.7	0 0	0.77	0.84	0.91	0.96	1.00	0.72	0.00	0.38			0.63	0.70	0.77	0.83	0.90	0.96	1.00	0.72	0.00	0.19	0.26	0.33	0.40	0.46	0.52	0.58	0.65	0.73	0.81	0.49
27	ES <sub>max</sub>	ES3	0.00	0.30	0.37	0.47	0.55	0.6	64 (	0.72	0.81	0.89	0.96	1.00	0.67	0.00	0.32	0.41	0.50	0.58	0.66	0.73	0.81	0.89	0.95	1.00	0.68	0.00	0.17	0.23	0.30	0.36	0.42	0.49	0.56	0.64	0.73	0.81	0.47

				Avera	ige M	ISEs											Aver	age 1	MAP	Es									Sun	ımary	(top)	perfo	rmers j	for bo	oth sta	ıbility c	and a	ccura	cy)
Tra	ıck. pe	er. (%1	RD) 🕨	0%	10%	20%	30%	40%	50%	66	0%	70%	80%	90%	100%		0%	10%	20%	30%	40%	50%	609	% 70%	5 80%	% 90%	100%			Avg. w	alues 🕨		Stab	ility		Ac	curacy	i	Both
ID	Me	ethod l	EAC(t)	1.35	42.37	24.04	6.11	3.25	1.8	7 1	.13	0.75	0.49	0.32	0.25	Avg.	0.14	0.25	0.21	0.18	0.15	0.13	0.1	1 0.09	0.0	8 0.06	0.03	Avg.	ID	Metho	od EAC(t)	) <b>R</b>	r	t	(Best)	MSE M	IAPE (	(Best)	Best)
1	E	EVM	PV1	1.35	1.33	1.21	1.07	0.94	0.83	3 0	).75	0.71	0.74	0.85	1.08	0.95	0.14	0.14	0.13	3 0.13	0.12	0.11	0.1	0.10	0.1	0 0.10	0.12	0.12	1	EVN	4 PV1	0.58	0.61	0.27		0.95	0.12	*	
2	E	EVM	PV2	1.35	117.7	48.29	14.13	6.96	3.01	71	.65	1.17	0.92	0.89	1.08	19.58	0.14	0.29	0.24	0.20	0.17	0.15	0.1	3 0.1	0.1	0 0.11	0.12	0.16	2	EVN	4 PV2	0.56	0.61	0.31		19.58	0.16		
3	E	EVM	PV3	1.35	351.0	204.8								2.04	1.94	62.24	0.14		0.37	0.30	0.26	0.23	0.2	20 0.18	3 0.1	7 0.16	0.16	0.25	3	EVN	1 PV3	0.39	0.41	0.24		62.24	0.25		
4	E	EVM	ED1		1.47	1.30								0.32		0.82			0.14	0.13	0.12	0.11	0.1	0.10	0.0	8 0.07	0.04	0.10	4	EVN	4 ED1	0.68	0.68	0.36		0.82	0.10	**	
5	E	VM	ED2	1.35	117.7	48.29	14.13	6.96	3.08	8 1	.64	1.09	0.68	0.34	0.13	19.40	0.14	0.29	0.24	0.20	0.17	0.15	0.1	0.1	0.0	9 0.07	0.03	0.15	5	EVN	4 ED2	0.65	0.67	0.42		19.40	0.15		
6	E	VM	ED3	1.35	348.1	201.0	28.82	11.7	6 5.33	32	.33	1.42	0.81	0.37	0.13	60.00	0.14	0.44	0.34	0.26	0.22	0.18	0.1	4 0.12	2 0.0	9 0.07	0.03	0.19	6	EVN	4 ED3		0.61	0.40		60.00	0.19		
7	E	VM	ES1	1.35	1.30	1.14	0.97	0.81	0.65	5 0	.49	0.34	0.21	0.09	0.01	0.60	0.14	0.14	0.13	3 0.12	0.11	0.10	0.0	0.0	0.0	6 0.04	0.01	0.09	7	EVN	4 ES1		0.70		*	0.60	0.09	**	*
8	E	VM	ES2	1.35	6.84	5.08	3.37	2.26	5 1.49	9 0	.97	0.60	0.33	0.13	0.01	2.11	0.14	0.25	0.21	0.18	0.15	0.13	0.1	1 0.09	0.0	0.04	0.01	0.12	8	EVN	A ES2	0.69	0.69	0.48	*	2.11	0.12		
9	E	EVM	ES3	1.35	32.80	21.80	8.67	4.66						0.16	0.01	7.38	0.14	0.38	0.30	0.24	0.20	0.16	0.1	0.10	0.0	7 0.04	0.01	0.17	9	EVN	4 ES3	0.64	0.66	0.45		7.38	0.17		
10	E	DM	PV1	1.35		1.14						0.59	0.61	0.75	1.02	0.86	0.14				0.11	0.10	0.1	0.09	0.0	9 0.10	0.11	0.11	10		4 PV1	0.62	0.64	0.31		0.86	0.11	*	
11	E	DM	PV2	1.35	6.70	4.82	3.22	2.10	1.31	7 0	.91	0.68	0.61	0.73	1.02	2.22	0.14	0.22	0.19	0.16	0.14	0.12	0.1	0.10	) 0.0	9 0.09	0.11	0.13	11	EDN	1 PV2	0.60	0.64	0.35		2.22	0.13		
12	E	DM	ED1	1.35	1.31	1.17	1.02	0.87	0.73	3 0	0.59	0.46	0.31	0.17	0.09	0.67	0.14	0.14	0.13	3 0.12	0.11	0.11	0.1	0.09	0.0	0.05	0.03	0.10	12	EDM	4 ED1	0.72	0.70	0.39	*	0.67	0.10	**	*
13	E	DM	ED2	1.35		4.82	3.22	2.10	1.30	60	.88	0.58	0.34	0.16	0.07	2.02	0.14	0.22	0.19	0.16	0.14	0.12	0.1	1 0.09	0.0	7 0.05	0.03	0.12	13	EDM	4 ED2		0.69		*	2.02	0.12		
14		DM	ES1		1.29	1.13	0.96	0.80	0.64	4 0	.48	0.33	0.19	0.08	0.01	0.59	0.14	0.14	0.13	3 0.12	0.11	0.10	0.0	0.07	0.0	5 0.03	0.01	0.08	14	EDN		0.73	0.71	0.44	**	0.59	0.08	**	**
15		DM	ES2	1.35	6.38	4.84	3.23	******						0.11	0.01	1.99				0.17				1 0.09	0.0	6 0.04	0.01	0.12	15	EDN			0.71		**	1.99	0.12		
16		ESM	ES1	1.35	1.27	1.12	0.96	0.80	0.64	4 0	).49	0.35	0.21	0.09	0.01		0.14	0.14	0.13	3 0.12	0.11	0.10	0.0	0.01	0.0	6 0.04	0.01	0.09	16	ESM			0.69		*	0.59		**	*
17	E	ESM	ES2	1.35	7.95	5.68	3.70	2.46	1.6	1 1	.03	0.64	0.34	0.13	0.01	2.36	0.14	0.26	0.22	0.19	0.16	0.14	0.1	1 0.09	0.0	0.04	0.01	0.13	17	ESM	1 ES2	0.68	0.68	0.47	*	2.36	0.13		
18	E	ESM	ES3	1.35	35.76	23.26	9.34	4.99	2.93	31			0.48	0.17	0.01	7.96	0.14	0.39	0.31	0.25	0.21	0.17	0.1	4 0.10	) 0.0	8 0.04	0.01	0.17	18	ESM	1 ES3	0.63	0.65	0.45		7.96	0.17		
19			XSM1	1.35	4.19	4.25	3.16	2.18	1.40	6 0	.96	0.60	0.33	0.13	0.01	1.73	0.14	0.21	0.20	0.17	0.15	0.13	0.1	1 0.09	0.0	0.04	0.01	0.12	19			0.69	0.68		*	1.73	0.12		
20			XSM2	1.35	1.50	1.55	1.52	1.38	1.13	3 0	.86	0.59	0.36	0.13	0.01	0.90	0.14	0.15	0.14	0.14	0.13	0.12	0.1	0.08	3 0.0	6 0.04	0.01	0.10	20		4 XSM2			0.46	*		0.10	**	*
21			XSM3		3.97	3.94	2.89	1.95	1.2	7 C	0.80	0.48	0.25	0.09	0.01	1.56	0.14				0.14		0.1	0.08	3 0.0	6 0.04	0.01	0.11	21		4 XSM3			0.47	*		0.11	*	
22		$S_{min}$	ES1	1.35	1.24	1.07	0.90	0.74	0.59	9 0	).44	0.30	0.17	0.07	0.00	0.55				2 0.11	0.10	0.09	0.0	0.03	0.0	5 0.03	0.01	0.08	22	ES <sub>mi</sub>			0.72		**	0.55		**	**
23		$S_{min}$	ES2	1.35	9.96	6.48	4.07	2.58	1.6	1 0		0.57	0.29	0.10	0.01	2.66	0.14			0.20	0.16	0.13	0.1	0.08	3 0.0	6 0.04	0.01	0.13	23	ESmi				0.50	**		0.13		
24		Smin	ES3	~~~~~	36.93	23.74		~~~~~	2.88	8 1	.62	0.88	0.42	0.13	0.01	8.13	-	*****	~~~~~	~~~~	0.21	0.16	0.1	0.10	0.0	******		0.17	24	ESmi			0.68		*	8.13			
25		S <sub>max</sub>	ES1	1.35	1.46	1.33	1.15	0.96	0.78	8 0	0.59	0.41	0.24	0.09	0.01	0.70	0.14				0.12	0.11	0.1	0.08	3 0.0	6 0.04	0.01	0.09	25	ES <sub>ma</sub>			0.69		*	0.70		**	*
26		Smax	ES2		7.45	5.14	3.34	2.17	1.40	0 0		0.57	0.31	0.11	0.01	2.14	0.14				0.17			1 0.09	0.0	, 0.01		0.14	26	ES <sub>ma</sub>			0.72		**		0.14		
27	E	S <sub>max</sub>	ES3	1.35	30.55	20.58	7.99	4.22	2.49	9 1	.45	0.83	0.41	0.14	0.01	6.87	0.14	0.43	0.33	0.26	0.21	0.17	0.1	0.10	0.0	8 0.04	0.01	0.18	27	ES <sub>ma</sub>	IX ES3	0.67	0.68	0.47	*	6.87	0.18		

Figure 2: EAC(t) estimates' stability and accuracy by percentage of project progress (as %RD) (\*: Good performers, \*\*: Top performers).

			Aver	age P	earso	on's R							Aver	age S	pearn	nan's	r						Avere	age K	Cenda	<i>ll's</i> t						
Seria	l-Par. (%S	SP) ►	7%	17%	28%	38%	48%	59%	69%	79%	90%	_	7%	17%	28%	38%	48%	59%	69%	79%	90%		7%	17%	28%	38%	48%	59%	69%	79%	90%	
ID	Method	EAC(t)	0.30	0.41	0.48	0.57	0.66	0.74	0.82	0.88	0.93	Avg.	0.30	0.40	0.47	0.58	0.67	0.74	0.81	0.87	0.93	Avg.	-0.16	0.13	0.24	0.35	0.44	0.51	0.58	0.66	0.74	Avg.
1	EVM	PV1	0.23	0.39	0.47	0.57	0.67	0.73	0.80	0.85	0.86	0.62	0.22	0.38	0.45	0.57	0.67	0.73	0.80	0.87	0.91	0.62	-0.33	0.03	0.17	0.31	0.41	0.48	0.56	0.64	0.68	0.33
2	EVM	PV2	0.39	0.38	0.42	0.53	0.63	0.71	0.79	0.84	0.86	0.62	0.40	0.38	0.44	0.57	0.66	0.73	0.80	0.87	0.91	0.64	0.05	0.15	0.22	0.35	0.44	0.50	0.57	0.64	0.69	0.40
3	EVM	PV3	0.27	0.27	0.32	0.41	0.48	0.55	0.58	0.59	0.57	0.45	0.28	0.29	0.32	0.43	0.49	0.54	0.57	0.60	0.61	0.46	0.03	0.13	0.17	0.27	0.32	0.36	0.39	0.41	0.42	0.28
4	EVM	ED1	0.23	0.40	0.48	0.58	0.68	0.73	0.81	0.87	0.93	0.64	0.22	0.38	0.46	0.57	0.67	0.73	0.80	0.87	0.93	0.63	-0.51	-0.05	0.12	0.29	0.40	0.48	0.55	0.64	0.73	0.29
5	EVM	ED2	0.39	0.38	0.42	0.53	0.63	0.71	0.80	0.87	0.93	0.63	0.40	0.38	0.44	0.57	0.66	0.73	0.80	0.87	0.94	0.64	0.05	0.15	0.22	0.35	0.44	0.50	0.57	0.65	0.74	0.41
6	EVM	ED3	0.29	0.30	0.35	0.46	0.55	0.65	0.74	0.83	0.92	0.56	0.31	0.32	0.36	0.50	0.58	******	0.74	0.82	0.91	0.58	0.04	0.14	0.19	0.31	0.38	0.45	0.52	0.61	0.71	0.37
7	EVM	ES1	0.15	0.44	0.53	0.62	0.72	0.79	0.86	0.91	0.96	0.67	0.15	0.40		0.60	0.69	0.76	0.84	0.90	0.95	0.64	-0.53	0.03	0.22	0.34	0.44	0.52	0.60	0.68	0.77	0.34
8	EVM	ES2	0.36	0.41	0.46	0.57	0.68	0.76	0.84	0.90	0.96	0.66	0.34	0.40	0.47	0.59	0.69	0.77	0.84	0.90	0.95	0.66	0.01	0.19	0.28	0.38	0.46	0.54	0.61	0.69	0.77	0.44
9	EVM	ES3	0.28	0.34	0.42	0.51	0.61	0.71	0.79	0.87	0.95	0.61	0.28	0.35	0.43	0.55	0.64	0.72	0.79	0.87		0.62	0.02	0.17	0.25	0.35	0.43	0.50	0.57	0.66	0.76	0.41
10	EDM	PV1	0.28	0.47	0.52	0.61	0.71	0.77	0.84	0.89	0.89	0.66	0.24	0.44	0.49	0.60	0.68		0.83	0.89	0.93	0.65	-0.39	0.08	0.21	0.34	0.43	0.51	0.59	0.67	0.72	0.35
11	EDM	PV2	0.51	0.45	0.47	0.57	0.67	0.75	0.83	0.88	0.89	0.67	0.51	0.44	0.48	0.59	0.68	0.75	0.83	0.89	0.93	0.68	0.08	0.19	0.26	0.37	0.45	0.52	0.60	0.67	0.73	0.43
12	EDM	ED1	0.28	0.48	0.53	0.62	0.71	0.77	0.85	0.91	0.96	0.68	0.24	0.44	0.50	0.60	0.68	0.75	0.83	0.89	0.95	0.65	-0.57	-0.02	0.17	0.32	0.42	0.50	0.59	0.67	0.77	0.32
13	EDM	ED2	0.51	0.45	0.47	0.57	0.67	0.75	0.84	0.90	0.96	0.68	0.51	0.44	0.48	0.59	0.68	0.75	0.83	0.89		0.68	0.08	0.19	0.26	0.37	0.45	0.52	0.60		0.77	0.44
14	EDM	ES1	0.21	0.49	0.56	0.63	0.73	0.79	0.86	0.91	0.96	0.68	0.17		0.52	0.60	0.69	0.76	0.84	0.90	0.95	0.65	-0.59	0.04	0.24	0.34	0.45	0.52	0.60	0.68	0.77	0.34
15	EDM	ES2	0.47	0.47	0.50	0.58	0.68	0.76	0.84	0.91	0.96	0.69	0.46	0.45	0.50	0.60	0.69	0.77	0.84	0.90	0.95	0.69	0.05	0.22	0.30	0.39	0.47	0.54	0.61	0.69	0.77	0.45
16	ESM	ES1	0.23	0.44	0.52	0.62	0.72	0.79	0.86	0.91	0.96	0.67	0.21	0.40	0.48	0.59	0.69	0.76	0.83	0.90	0.95	0.65	-0.51	0.03	0.21	0.34	0.44	0.52	0.60	0.68	0.77	0.34
17	ESM	ES2	0.26	0.36	0.43	0.55	0.67	0.76	0.84	0.90	0.96	0.64	0.26	0.35	0.44	0.58	0.68	0.76	0.84	0.90	0.95	0.64	-0.03	0.16	0.26	0.37	0.46	0.54	0.61	0.69	0.77	0.43
18	ESM	ES3	0.22	0.30	0.39	0.50	0.61	0.70	0.79	0.87	0.95	0.59	0.23	0.32	0.40	0.54	0.64	0.72	0.79	0.87	0.94	0.61	0.00	0.15	0.24	0.34	0.43	0.50	0.57		0.76	0.41
19	XSM				0.49	0.56	0.67	0.75	0.84	0.90	0.96	0.64	0.13	0.39	0.48	0.59	0.68	0.76	0.83	0.89	0.95	0.63	-0.28	0.15	0.27	0.37	0.46	0.53	0.61	0.68	0.77	0.40
20	XSM	ASM2 XSM3		0.45	0.53	0.61	0.69	0.76	0.83	0.89	0.95	0.65	0.16	0.40	0.49	0.57	0.69	0.76	0.83	0.89	0.95 0.95	0.64	-0.42 -0.31	0.11	0.26	0.37	0.46	0.53	0.61	0.68	0.77	0.37
21 22	XSM ES <sub>min</sub>	ES1		0.48	0.52	0.58	0.67	0.76	0.84	0.90	0.96	0.66	0.17	0.45	0.51	0.59	0.08	0.76	0.83	0.89	0.95	0.65	-0.31	0.17	0.28	0.37	0.46	0.53	0.61	0.68	0.77	0.40 0.40
22	ES <sub>min</sub>	ES1 ES2	0.38	0.30	0.50	0.05	0.74	0.80	0.80	0.91	0.90	0.68	0.33	0.47	0.55	0.62	0.71	0.77	0.84	0.90	0.95	0.68	0.14	0.14	0.27	0.30	0.40	0.55	0.60	0.68	0.77	0.40
23		ES2 ES3	0.40	0.44	0.30	0.59	0.69	0.71	0.85	0.91	0.96	0.68	0.37	0.40	0.54	0.62	0.70	0.77	0.84	0.90	0.95	0.65	0.14	0.20	0.55	0.40	0.48	0.55	0.62		0.77	0.47
24	ES <sub>min</sub> ES <sub>max</sub>	ES5 ES1	-0.06		0.46	0.55	0.65	0.71	0.79	0.87	0.95	0.64	0.37	0.45	0.50	0.58	0.65	0.75	0.80	0.87	0.94	0.65	-0.40	0.24	0.51	0.37	0.44	0.51	0.58	0.68	0.78	0.45
25	ES <sub>max</sub> ES <sub>max</sub>	ES1 ES2	0.53	0.33	0.54	0.62	0.72	0.78	0.85	0.91	0.96	0.03	0.10	0.31	0.51	0.60	0.69	0.76	0.85	0.90	0.95	0.65	-0.40	0.01	0.24	0.34	0.43	0.52	0.60	0.68	0.77	0.36
20	ES <sub>max</sub>		0.33			0.59	0.69	0.70		0.91	0.90	0.65	0.30		0.50	0.62	0.70	0.77	0.84	0.90	0.93	0.70	0.00	0.23	0.34	0.40	0.47	0.54	0.57	0.69	0.76	0.40
21	Lio max	E-35	0.49	0.42	0.49	0.55	0.02	0.71	0.79	0.87	0.95	0.05	0.40	0.44	0.51	0.58	0.05	0.75	0.80	0.87	0.94	0.07	0.07	0.21	0.51	0.57	0.44	0.50	0.57	0.00	0.70	0.43

			Aver	age M	1SEs								Aver	age M	<i>IAPE</i>	Es							Sun	ımary	(top p	perform	mers	for be	oth sta	bility	and a	ccura	cy)
Ser	ial-Par. (%	(SP) ►	7%	17%	28%	38%	48%	59%	69%	79%	90%		7%	17%	28%	38%	48%	59%	69%	79%	90%			Avg. va	lues 🕨		Stal	bility		A	Accuracy	,	Both
ID	Method	EAC(t)	2.69	2.68	2.76	2.94	2.23	1.19	0.82	0.50	0.29	Avg.	0.34	0.22	0.18	0.15	0.12	0.09	0.07	0.05	0.04	Avg.	ID	Method	I EAC(t)	R	r	t	(Best)	MSE	MAPE	(Best)	(Best)
1	EVM	PV1	1.84	1.41	1.00	0.80	0.76	0.66	0.59	0.47	0.43	0.88	0.27	0.18	0.14	0.11	0.09	0.08	0.07	0.06	0.05	0.12	1	EVM	PV1	0.62	0.62	0.33		0.88	0.12	*	
2	EVM	PV2	2.5	3.97	4.46	4.86	4.04	1.94	1.40	0.78	0.54	2.72	0.34	0.22	0.19	0.17	0.14	0.11	0.09	0.07	0.05	0.15	2	EVM	PV2	0.62	0.64	0.40		2.72	0.15		
3	EVM	PV3	3.3	7.8	8.78	9.06	10.05	4.87	4.56	3.54	3.01	6.10	0.41	0.30	0.27	0.26	0.23	0.19	0.18	0.15	0.14	0.24	3	EVM	PV3	0.45	0.46			6.10	0.24		
4	EVM	ED1	1.75	1.50	1.03	0.82	0.82	0.80	0.68	0.50	0.36	0.92	0.26	0.18	0.14	0.11	0.10	0.09	0.08	0.06	0.05	0.12	4	EVM	ED1	0.64	0.63	0.29		0.92	0.12	*	1
5	EVM	ED2	2.5	3.97	4.46	4.86	4.08	1.95	1.42	0.77	0.45	2.71	0.34	0.22	0.19	0.17	0.14	0.11	0.09	0.07	0.05	0.15	5	EVM	ED2	0.63	0.64	0.41		2.71	0.15		
6	EVM	ED3	3.1	7.1	7.77	7.31	7.89	2.69	1.96	1.00	0.52	4.37	0.40	0.28	0.24	0.21	0.17	0.13	0.11	0.07	0.05	0.18	6	EVM	ED3	0.56	0.58	0.37		4.37	0.18		
7	EVM	ES1	1.77	1.39	0.93	0.69	0.60	0.46	0.32	0.20	0.09	0.72	0.26	0.18	0.13	0.10	0.08	0.07	0.05	0.04	0.03	0.10	7	EVM	ES1	0.67	0.64	0.34		0.72	0.10	**	
8	EVM	ES2	2.56	1.70	2.63	2.71	1.65	0.95	0.53	0.28	0.11	1.46	0.35	0.21	0.20	0.16	0.12	0.09	0.07	0.05	0.03	0.14	8	EVM	ES2	0.66	0.66	0.44	*	1.46	0.14		
9	EVM	ES3	3.21	3.19	4.28	5.90	3.25	1.60	0.95	0.47	0.16	2.56	0.40	0.27	0.25	0.21	0.16	0.11	0.08	0.06	0.03	0.17	9	EVM		0.61	0.62	0.41		2.56	0.17		
10	EDM	PV1	1.85	1.37	0.94	0.71	0.64	0.53	0.38	0.27	0.25	0.77	0.27	0.18	0.13	0.10	0.09	0.07	0.06	0.04	0.03	0.11	10	EDM	PV1	0.66	0.65	0.35		0.77	0.11	**	
11	EDM	PV2	2.55	1.75	1.56	2.09	1.46	0.99	0.53	0.31	0.23	1.28	0.35	0.19	0.16	0.15	0.11	0.09	0.07	0.05	0.03	0.13	11	EDM	PV2	0.67	0.68	0.43	*	1.28	0.13		
12	EDM	ED1	1.77	1.42	0.99	0.73	0.67	0.54	0.39	0.23	0.10	0.76	0.26	0.18	0.13	0.10	0.09	0.08	0.06	0.04	0.03	0.11	12		ED1	0.68		0.32		0.76	0.11	**	
13	EDM	ED2	2.55	1.75	1.56	2.09	1.47	0.99	0.53	0.29	0.11	1.26	0.35	0.19	0.16	0.15	0.11	0.09	0.07	0.05	0.03	0.13	13		ED2			0.44	*	1.26	0.13		
14	EDM	ES1	1.78	1.38		0.68	0.59	0.46	0.32	0.20	0.09	0.71				0.10	0.08	0.07	0.05	0.04	0.03	0.10	14	EDM		0.68				0.71	0.10	**	
15	EDM	ES2	2.62	1.49	2.29	2.45	1.60	0.95	0.52	0.28	0.11	1.37	0.36	0.19	0.19	0.16	0.12	0.09	0.07	0.05	0.03	0.14	15		ES2	0.69	0.69	0.45	**	1.37	0.14		
16	ESM	ES1	1.67	1.33	0.93	0.70	0.60	0.46			0.09	0.70	0.25	0.18	0.13	0.10	0.08	0.07	0.05	0.04	0.03	0.10	16	ESM	ES1	0.67	0.65			0.70	0.10	**	
17	ESM	ES2	1.89	1.97	3.45	3.14	1.73	0.97	0.53	0.29	0.11	1.56	0.28	0.22	0.23	0.17	0.12	0.09	0.07	0.05	0.03	0.14	17		ES2		0.64	0.43		1.56	0.14		
18	ESM	ES3	2.58	3.83	5.50	6.99	3.38	1.63		0.47	0.16	2.83	0.34	0.28	0.27	0.22	0.16	0.11	0.08	0.06	0.03	0.17	18	ESM		0.59		0.41					
19		XSM1	2.08	1.49	1.67	2.52	1.76	1.03	0.55		0.11	1.28	0.29	0.19	0.17	0.16	0.12	0.09	0.07	0.05	0.03	0.13	19		XSM1		0.63	0.40		1.28	0.13		
20		XSM2	1.82	1.28	0.98	1.13	1.20	0.95	0.65	0.39	0.12	0.95	0.26	0.17	0.14	0.12	0.11	0.09	0.07	0.05	0.03	0.12	20		XSM2		0.64	0.37		0.95	0.12	*	1
21		XSM3	2.09	1.46	1.23	1.83	1.49	0.92	0.50	0.28	0.10	1.10	0.29	0.19	0.15		0.11	0.09	0.06	0.05	0.03	0.12	21		XSM3		0.65			1.10	0.12	*	
22	ES <sub>min</sub>	ES1	1.62	1.25	0.84	0.65		0.44	0.32	0.20	0.09	0.67	0.25	0.17			0.08	0.07	0.05	0.04	0.03	0.10	22		ES1	0.71				0.67		**	*
23	ES <sub>min</sub>	ES2	2.60	3.78	4.17	3.02	1.60	0.93	0.52	0.28	0.11	1.89	0.33	0.28	0.22	0.16	0.12	0.09	0.06	0.05	0.03	0.15	23	ES <sub>min</sub>			0.68	0.47	**	1.89	0.15		
24	ES <sub>min</sub>	ES3	3.32	5.61	6.22	7.24	3.15	1.58	0.94	0.46	0.15	3.19	0.37	0.33	0.26		0.15	0.11	0.08	0.06	0.03	0.18	24	ES <sub>min</sub>				0.45	*	3.19	0.18		
25	ES <sub>max</sub>	ES1		1.84	1.06		0.61	0.46			0.09			0.21			0.08	0.07	0.05	0.04	0.03	0.12	25	ES <sub>max</sub>		0.63					0.12	**	1
26	ES <sub>max</sub>	ES2	7.05	3.35	1.92	1.98	1.49	0.93	0.52	0.28	0.11	1.96	0.67	0.33	0.19	0.15	0.12	0.09	0.07	0.05	0.03	0.19	26	ES <sub>max</sub>		0.70			**	1.96	0.19	ļ	1
27	ES <sub>max</sub>	ES3	7.41	4.10	2.84	3.64	2.91	1.54	0.93	0.46	0.15	2.67	0.69	0.36	0.23	0.20	0.15	0.11	0.08	0.06	0.03	0.21	27	ES <sub>max</sub>	ES3	0.65	0.67	0.43	*	2.67	0.21		

Figure 3: EAC(t) estimates' stability and accuracy by the Serial-Parallel (SP) indicator (SP=0 Parallel network, SP=1 Serial network).

### Supplemental online material

Results from the 4100 simulated projects can be downloaded here <u>https://bit.ly/3d8jRIl</u>. The link allows you to download a 87 MB Excel spreadsheet file. Please, be patient when downloading and opening it. A list of all abbreviations, variables and mathematical expressions used in the paper follows in Table S1.

# Table S1. List of major EVM-related abbreviations, variables and mathematical expressions used in the paper.

Variable	Unit	Description	Expression
AC	Money	(Project) Actual Cost (at tracking period AT)	$AC = \sum_{i \in N} AC_{i,AT}$
$AC_{i, AT}$	Money	Activity <i>i</i> 's Actual Cost (at tracking period <i>AT</i> )	_
AT	Time	Actual Time (current tracking period). Also named <i>AD</i> .	-
$AT_t$	Time	Ongoing (Project) duration at tracking period <i>t</i>	-
BAC	Money	(Project) Budget At Completion (planned total project cost estimate)	_
BAC(t)	Time	(Project) Duration At Completion (sum of all activities' <i>TPD</i> or planned $d_i$ at the end of the project)	$BAC(t) = \sum_{i \in N} d_i$
$BAC_i$	Money	Activity <i>i</i> 's total planned cost	-
C <sub>i</sub>	Money	Activity <i>i</i> 's cost	-
СРІ	1	(Project) Cost Performance Index (at tracking period <i>AT</i> )	$CPI = \frac{EV}{AC}$
$CV_i$	1	Activity i's Coefficient of Variation	$CV_i = \frac{\sigma_i}{\mu_i}$
$d_i$	Time	Activity <i>i</i> 's duration	-
$d_{mk}$	Ranks	Difference between the ranking (order) values of $EAC(t)_{AT}$ and $RD_{mk}$ for project $m$ , for the $K$ simulation runs at a particular tracking period AT.	$d_{mk} = rank \left( EAC(t)_{AT}^{k} \right) - rank \left( RD_{mk} \right)$ for k=1,2K.
DPI	1	<ul><li>(Project) Duration Performance Index</li><li>(EVM's <i>SPI(t)</i> counterpart in EDM) (at tracking period <i>AT</i>)</li></ul>	$DPI = \frac{ED}{AT}$
$EAC(t)_{AT}$	Time	Project Duration forecasting estimate at tracking period AT.	-
$EAC(t)_x$	Time	Project Duration forecasting method <i>x</i>	See Table 1
$\overline{EAC(t)_{AT}}$	Time	Average of the EAC(t) estimates at tracking period AT in the K simulation runs.	

Variable	Unit	Description	Expression
		(Project) Earned Duration (EVM's ES	
ED	Time	counterpart in EDM) (at tracking period $AT$ )	$ED = t + \frac{TED - TPD_t}{TPD_{t+1} - TPD_t}$
ED	Time	as formulated by Khamooshi and Golafshani	$TPD_{t+1} - TPD_t$
		(2014). Also named $ED(t)$	
ED'	Time	(Project) Earned Duration (at tracking period	$ED = AT \cdot SPI$
ED	Time	AT) as formulated by Jacob (2003)	$LD = AI \cdot SPI$
		(Project) Earned Duration Index (EVM's SPI	TED TED
EDI	1	counterpart in EDM) (at tracking period $AT$ )	$EDI = \frac{TED}{TPD}$
$EDI_t$	1	(Project) <i>EDI</i> at tracking period <i>t</i>	$EDI_{t} = \frac{TED_{t}}{TPD_{t}}$
EDM	-	Earned Duration Management	-
ES	Time	(Project) Earned Schedule (at tracking period $AT$ )	$ES = t + \frac{EV - PV_t}{PV_{t+1} - PV_t} \cdot (t+1-t)$
ES(e)	Time	(Project) Effective Earned Schedule (ES calculated with <i>EV(e)</i> ) (at tracking period <i>AT</i> )	$ES(e) = t + \frac{EV(e) - PV_t}{PV_{t+1} - PV_t}$
$ES_i$	Time	Activity <i>i</i> 's Earned Schedule (at tracking period <i>AT</i> )	$ES_i = SD_i + PC_i \cdot d_i$
ESM	-	Earned Schedule Management	-
ΓG		(Project) Maximum Earned Schedule (at	$ES = MAV(ES \cdot DC = (0.11 \text{ i } N))$
$ES_{max}$	Time	tracking period AT)	$ES_{max} = MAX \{ ES_i : PC_i \subset (0,1], i \in N \}$
ES <sub>min</sub>	Time	(Project) Minimum Earned Schedule (at tracking period <i>AT</i> )	$ES_{min} = MIN \{ ES_i + s_i : PC_i \subset [0,1), i \in N\}$
$ES_t$	Time	(Project) ES at tracking period t	_
EV	Money	(Project) Earned Value (at tracking period <i>AT</i> )	$EV = \sum_{i \in N} EV_{i,AT}$
EV(e)	Money	(Project) Effective Earned Value (at tracking period <i>AT</i> )	$EV(e) = \left[1 - \left(1 - p\right)\left(1 - PC \cdot e^{-\frac{1 - PC}{2}}\right)\right]EV$
EV <sub>i, AT</sub>	Money	Activity <i>i</i> 's Earned Value (at tracking period $AT$ )	-
$EV_{i,AT}$	Money	Activity <i>i</i> 's Earned Value at tracking period <i>AT</i>	-
EVM	-	Earned Value Management	-
$EV_t$	Money	(Project) Earned Value at tracking period t	$EV_t = \sum_{i \in N} EV_{i,t}$
i	-	Activity <i>i</i> (one of the activities of the project schedule with $i=1,2N$ )	-
k	-	Each of the simulation runs in the experiments ( $k=1,2,K$ in the paper)	-
K	Sim. Runs	Number of simulation runs in the experiments ( <i>K</i> =100 in the paper)	-
т	-	Project <i>m</i> (one of the 4100 simulated projects of the dataset)	-
М	-	Total number of projects (4100 in the dataset)	-
$MAPE_{AT}$	-	Mean Absolute Percentage Error at tracking period AT.	See eq. (3) in the paper

Variable	Unit	Description	Expression
MSE <sub>AT</sub>	-	Mean Squared Error Error at tracking period AT.	See eq. (2) in the paper
n	Activities	Total number of (non-dummy) activities scheduled in the ongoing project (30 in the projects dataset)	-
Ν	units	Total number of planned tracking periods of a project	-
р	1	(Project) Schedule adherence <i>p-Factor</i> (at tracking period <i>AT</i> )	$p = \frac{\sum_{i \in N} \min(PV_{i,ES}, EV_{i,AT})}{\sum_{i \in N} PV_{i,ES}}$
Pm	Concordant pairs	Number of concordant pairs between the EAC(t) estimates and the RD values for each project <i>m</i> .	See eq. (7) in the paper
PC	1	(Project) Percentage of Completion (at tracking period <i>AT</i> )	$PC = \frac{EV}{BAC}$
$PC_i$	1	Activity i's Percentage of Completion (at tracking period <i>AT</i> )	$PC = \frac{EV}{BAC}$ $PC_{i} = \frac{EV_{i}}{BAC_{i}}$
PD	Time	(Project) Planned Duration (total project duration estimate)	-
PF	-	Performance Factor that can be 1 or another indicator such as SPI, SPI(t), SPI(t)(e), SPI(t) <sub>ESmin</sub> , SPI(t) <sub>ESmax</sub> , SCI, SCI(t), SCI(t)(e), SCI(t) <sub>ESmin</sub> , SCI(t) <sub>ESmax</sub> , even an exponential smoothing factor (e.g. $T_{t,SPI(t)}$ , $T_{t,AT}/T_{t,ES}$ or $T_{t,EDI}$ )	-
PV	Money	(Project) Planned Value (at tracking period <i>AT</i> )	$PV = \sum_{i \in N} PV_{i,AT}$
PV <sub>i, AT</sub>	Money	Activity <i>i</i> 's Planned Value (at tracking period <i>AT</i> )	-
PV <sub>i,ES</sub>	Money	Activity <i>i</i> 's Planned Value at tracking period <i>ES</i>	_
PV <sub>rate</sub>	Money/ time	(Project) Planned Value rate (at tracking period <i>AT</i> )	$PV_{rate} = BAC/PD$
$PV_t$	Money	(Project) Planned Value at tracking period <i>t</i>	$PV_t = \sum_{i \in N} PV_{i,t}$
q	Activities	Number of activities in the path with the highest number of activities of a project (which is not necessarily the longest in duration)	-
$R_{AT}$	1	Pearson's linear correlation coefficient at tracking period AT.	See eq. (4) in the paper
RAC	Money	(Project) Real (budget) At Completion (only known once the project is completed)	-
RD	Time	(Project) Real Duration (only known once the project is completed)	-
$RD_{mk}$	Time	Real (Actual) Duration of project <i>m</i> in the simulation run <i>k</i> .	-
$\overline{RD_{mk}}$	Time	Average of project <i>m</i> 's Real Duration values in the <i>K</i> simulation runs.	

Variable	Unit	Description	Expression
SCI	1	(Project) Schedule Cost Index using original	$SCI = SPI \cdot CPI$
	1	EVM metrics (at tracking period <i>AT</i> )	501 - 511 011
SCI(t)	1	(Project) Schedule Cost Index using the ES	$SCI(t) = SPI(t) \cdot CPI$
	1	metric (at tracking period <i>AT</i> )	
SCI(t) <sub>ESmax</sub>	1	(Project) Schedule Cost Index using the $ES_{max}$	$SCI(t)_{ESmax} = SPI(t)_{ESmax} \cdot CPI$
		metric (at tracking period <i>AT</i> )	SCI(t)ESmax - SIII(t)ESmax + CIII
SCI(t) and $s$	1	(Project) Schedule Cost Index using the ES <sub>min</sub>	$SCI(t)_{ESmin} = SPI(t)_{ESmin} \cdot CPI$
SCI(t) <sub>ESmin</sub>		metric (at tracking period AT)	$SCI(l)ESmin - SFI(l)ESmin \cdot CFI$
SCI(t)(e)	1	(Project) Effective Schedule Cost Index (at	$SCI(t)(e) = SPI(t)(e) \cdot CPI$
		tracking period AT)	$SCI(i)(e) - SII(i)(e) \cdot CII$
CD.	Time	Activity <i>i</i> 's (Earliest) Start Date (at tracking	Critical path calculations (ASAP
$SD_i$		period AT)	schedule)
	Time	Activity <i>i</i> 's slack or float . Difference	
$S_i$		between each activity's earliest and latest	Critical path calculations
		Finish or Start.	
SP	1	Serial-Parallel topological indicator	<i>SP</i> =( <i>q</i> -1)/( <i>n</i> -1)
		(Project) Schedule Performance Index using	
SPI	1	original EVM metrics (at tracking period $AT$ )	$SPI = \frac{EV}{PV}$
		(Project) Schedule Performance Index using	
SPI(t)	1		$SPI(t) = \frac{ES}{AT}$
		the <i>ES</i> metric (at tracking period $AT$ )	AT
SPI(t) <sub>ESmax</sub>	1	(Project) Schedule Performance Index using	$SPI(t)_{ESmax} = ES_{max} / AT$
		the $ES_{max}$ metric (at tracking period $AT$ )	()
SPI(t) <sub>ESmin</sub>	1	(Project) Schedule Performance Index using	$SPI(t)_{ESmin} = ES_{min} / AT$
		the $ES_{min}$ metric (at tracking period $AT$ )	
SPI(t)(e)	1	(Project) Effective Schedule Performance	$SPI(t)(e) = \frac{ES(e)}{ES(e)}$
51 1(1)(C)		Index (at tracking period <i>AT</i> )	SIT(t)(c) = AT
	1	(Device) SDI(4) at two line period t	$SPI(t)(e) = \frac{ES(e)}{AT}$ $SPI(t)_{t} = \frac{ES_{t}}{t}$
$SPI(t)_t$		(Project) $SPI(t)$ at tracking period t	
		Integer tracking period such that:	
		$PV_t \leq EV < PV_{t+1}$ for ES calculations,	
t	Time	$TPD_t \leq TED < TPD_{t+1}$ for $ED$ calc.,	-
		$PV_t \leq EV(e) < PV_{t+1}$ for $ES(e)$ calc.,	
		or just $t=0,1,2n$ for the other calc.	
		(Project) Total Actual Duration (EVM's AC	$TAD - \sum TAD$
TAD	Time	counterpart in EDM) (at tracking period $AT$ )	$TAD = \sum_{i \in N} TAD_{i,AT}$
	Time	Activity <i>i</i> 's Actual Duration (at tracking	
$TAD_{i, AT}$		period AT)	-
	Time	(Project) Total Earned Duration (EVM's <i>EV</i>	$TED - \sum TED$
TED		counterpart in EDM) (at tracking period $AT$ )	$TED = \sum_{i \in \mathcal{N}} TED_{i,AT}$
	Time	Activity <i>i</i> 's Earned Duration (at tracking	1±1V
$TED_{i, AT}$		period <i>AT</i> )	-
		(Project) Total Earned Duration at tracking	
$TED_t$	Time	period t	$TED_t = \sum TED_{i,t}$
	Time		$TED_{t} = \sum_{i \in N} TED_{i,t}$ $TPD = \sum_{i \in N} TPD_{i,AT}$
TPD		(Project) Total Planned Duration (EVM's <i>PV</i>	$TPD = \sum TPD_{i,AT}$
		counterpart in EDM) (at tracking period $AT$ )	i∈N
TPD <sub>i, AT</sub>	Time	Activity <i>i</i> 's Planned Duration (at tracking	-
		period <i>AT</i> )	
$TPD_t$	Time	(Project) Total Planned Duration at tracking	$TPD_t = \sum TPD_{i,t}$
$\boldsymbol{\mu}$	1 1110	period t	$i \in N$

Variable	Unit	Description	Expression
$T_{t,AT}$	1	(Project) Trend of AT at tracking period t	$T_{t,AT} = \gamma \left( AT_t - AT_{t-1} \right) + \left( 1 - \gamma \right) T_{t-1,AT}$ with $T_{0,AT} = \frac{PD}{n}$
$T_{t,EDI}$	1	(Project) Trend of <i>EDI</i> at tracking period t	$T_{t,EDI} = \beta \cdot EDI_t + (1 - \beta)T_{t-1,EDI}$ with $T_{0,EDI} = 1$
$T_{t,ES}$	1	(Project) Trend of ES at tracking period t	$T_{t,ES} = \gamma \left( ES_t - ES_{t-1} \right) + \left( 1 - \gamma \right) T_{t-1,AT}$ with $T_{0,ES} = \frac{PD}{n}$
T <sub>t,SPI(t)</sub>	1	(Project) Trend of <i>SPI(t)</i> at tracking period <i>t</i>	$T_{t,SPI(t)} = \beta \cdot SPI(t)_t + (1 - \beta)T_{t-1,SPI(t)}$ with $T_{0,SPI(t)} = 1$
TV	1	(Project) Time Variance (at tracking period <i>AT</i> )	$TV = SV/PV_{rate}$
Xi	1	Activity <i>i</i> 's correlated Normally-distributed random variable whose variability is conditioned by the $d_i$ from equation (2) and the rest varies according to a st. Normal distrib.	See eq. (14) in the paper
β	1	Exponential smoothing constant (assumed here as 0.25 according to Khamooshi & Abdi (2016))	-
γ	1	Exponential smoothing constant (assumed here as 0.05 according to Batselier & Vanhoucke (2017))	-
$\delta_i$	1	Activity <i>i</i> 's duration-cost correlation	See eq. (15) in the paper
$\mu_i$	Log time	Activity <i>i</i> 's average log duration.	See eq. (9) in the paper
$\mu'_i$	Log money	Activity <i>i</i> 's average log cost.	See eq. (12) in the paper
$\sigma_i$	Log time	Activity <i>i</i> 's avg. log duration st. deviation.	See eq. (10) in the paper
$\sigma'_i$	Log money	Activity <i>i</i> 's average log cost st. deviation.	See eq. (13) in the paper
$\rho_{AT}$	1	Spearman's rank correlation coefficient at tracking period AT.	See eq. (5) in the paper
$ au_{AT}$	1	Kendall's rank correlation coefficient at tracking period AT.	See eq. (6) in the paper

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