In-plane omnidirectional magnetic field sensor based on Giant Magneto Impedance (GMI)

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\textbf{Abstract}

In this work the design and characterization of an omnidirectional in-plane magnetic field sensor are presented. The sensor is based on the Giant Magnetoimpedance (GMI) effect in glass-coated amorphous microwires of composition (Fe\textsubscript{6}Co\textsubscript{94})\textsubscript{72.5}Si\textsubscript{12.5}B\textsubscript{15}. For the first time, a circular loop made with a microwire is used for giving omnidirectional response. In order to estimate the GMI response of the circular loop we have used a theoretical model of GMI, determining the GMI response as the sum of longitudinal sections with different angles of incidence. As a consequence of the circular loop, the GMI ratio of the sensor is reduced to 15\% instead of 100\% for the axial GMI response of a microwire. The sensor response has been experimentally verified and the GMI response of the circular loop has been studied as function of the magnetic field, driven current, and frequency. First, we have measured the GMI response of a longitudinal microwire for different angles of incidence, covering the full range between the tangential and perpendicular directions to the microwire axis. Then, using these results, we have experimentally verified the decomposition of a microwire with circular shape as longitudinal segments with different angles of incidence. Finally, we have designed a signal conditioning circuit for the omnidirectional magnetic field sensor. The response of the sensor has been studied as a function of the amplitude of the incident magnetic field.

\textbf{Keywords}: Giant Magneto Impedance (GMI), amorphous microwire, magnetic field sensor.
1. Introduction

Glass coated amorphous microwires have been intensively studied due to its outstanding magnetic properties, as giant magnetotransportance (GMI) [1-9] or absorption properties at microwave frequencies [10-19]. The GMI effect is related to the change of the skin depth on the microwire due to strong changes of the dynamic circular permeability [20,21]. In particular, the microwires studied in this work are of composition (Fe₉Co₄₄)₇₂.₅Si₁₂.₅B₁₅ which has negative but close to zero magnetostriction ($\lambda_s=10^{-7}$) [22]. Due to the fabrication process, they present a shell of circular permeability with a “bamboo like” structure and an inner core with axial anisotropy [23]. Since the microwire is amorphous, the domain structure is a consequence of the shape and magnetoelastic anisotropies resulting from the stress caused by the fabrication process. The microwires with the aforementioned composition present a circular anisotropy characterized by an anisotropy field $H_a = 285$ A/m [24]. When an external magnetic field $H$ is applied in the axial direction of the microwire, the effective dynamic circular permeability reaches a maximum as the applied field approach to the anisotropy field. In this point the skin depth shows a minimum and therefore the impedance is maximized [20,25].

The GMI effect has special application in the development of highly sensitive magnetic sensors [5,6,26,27] and current sensors [28]. Mohri et al. have done a remarkable contribution in the development of electronic circuits for GMI sensors [29,30]. All GMI sensors reported in previous works were done with the microwire placed longitudinally, and therefore the sensibility of the GMI depends on the angle between the applied magnetic field and the axis of the microwire. In this paper, we present an in-plane omnidirectional magnetic field sensor based on a microwire in the shape of a circular loop (see Fig.6(a)), and we have done theoretical simulations, experimental measurements and the signal conditioning circuit.

The microwires employed in this work have been studied in a previous work of the authors [24], where GMI measurements were performed with AC current and frequency as parameters, and a signal conditioning circuit was developed in order to design a magnetic field sensor. In this work we extend this study to a circular loop geometry of the microwire. For a proper understanding of the proposed configuration, a phenomenological model for circular microwires is presented. The results obtained are supported by a set of experimental measurements and the development of a high-sensitivity sensor.

2. Theoretical approach for GMI in circular microwires

The magnetic domain structure of microwires is rather complex and hinders the development of precise theoretical models. This fact is basically due to the change of magnetization with the radius because of the shape and magnetoelastic anisotropies, the latter being due to the radial variation of the stress in the microwire. Such a stress is caused by the radial gradient of temperature during the fabrication process and the different expansion coefficient of the glass shield and the inner ferromagnetic core. Many efforts have been made to model the GMI effect in microwires and many remarkable works have been reported [5,20,21,25,31-33], but indeed any of them gets a perfect agreement with experimental measurements. The discrepancies are especially important at zero magnetic field, where low levels of impedance are predicted while experimental data show a value close to the values found in saturation (i.e. at high magnetic fields).

Our aim is to present a simple approach that models the behaviour of a circular microwire. For this purpose, we will assume the loop can be decomposed in a series of small sections of microwires excited at different angles with respect to the external magnetic field. Under this assumption, we can decompose the incident magnetic field in two orthogonal components, one axial to the wire and the other perpendicular, the latter playing a minor role in the impedance and therefore being negligible. Thereby the problem is reduced to the study of a straight microwire excited with an external magnetic field at a given angle.

The GMI in a microwire depends on the dynamics of the magnetization due to the interaction of the external magnetic field and the circular field produced inside the microwire due to the AC current flowing through it. The movement of the magnetization with an applied magnetic field along with the Maxwell equations are described by the Landau-Lifshitz-Gilbert (LLG) equation:

$$\frac{\partial \vec{m}}{\partial t} = -\mu_0 \gamma (\vec{M} \times \vec{H}) + \alpha (\vec{M} \times \frac{\partial \vec{M}}{\partial t})$$

(1)

where $\gamma$ is the gyromagnetic ratio, $\mu_0$ the permeability of free space, $\alpha$ a damping parameter, $\bar{M}$ the saturation magnetization, $\bar{H} = H_0 + h_{ac}$ the total magnetic field (static and
where $H_0$ is the external field, $H_a$ the anisotropy field (with $H_a = 2K/\mu_0M_S$, $K$ being the effective anisotropy constant) and $\theta$ the angle between the axis of the microwire and the magnetization direction (see Fig.1(a)). We suppose a circular transversal anisotropy in the microwire with a “bamboo like” domain structure ($\alpha = 90^\circ$) as illustrated in Fig.1(b). With the minimization of the energy two solutions are obtained: $\theta = 90^\circ$ for $H_0 \geq H_a$, and $\theta = \arccos(H_a/H_0)$ for $H_0 \leq H_a$. By solving the LLG equation and Maxwell equations we get the effective transverse susceptibility [30,31]:

$$ Z_{\text{eff}}(\omega) = \frac{(1+\beta)}{\delta} = (1-j) \sqrt{\frac{\pi f \mu_\phi \sigma}{\omega_1 - j \omega \sigma}} $$

$$ \omega_1 = \mu_0 \gamma [H_0 \cos \theta + H_a \cos 2(90 - \theta)] $$

$$ \omega_2 = \mu_0 \gamma [H_0 \cos \theta + H_a \cos 2(90 - \theta)] $$

$$ \omega_M = \mu_0 \gamma M_S $$

Applying the Maxwell’s equations and the boundary conditions we obtain the longitudinal impedance of the microwire, which for the high frequency regime has the form [20,31-33]:

$$ Z_{\text{zz}}(\omega) = \frac{(1+j)}{2 \pi a} \sqrt{\frac{\pi \mu_0 \sigma}{\omega_1 - j \omega \sigma} (\sin^2 \theta + \sqrt{(1 + \chi_{\text{eff}} \phi \cos^2 \theta})} $$

Nevertheless, this solution presents some discrepancies in the zone of zero magnetic field where the predicted impedance tends to very low values (see Fig. 2). This behaviour contrasts with measured data previously reported for this kind of microwires [24]. To overcome this issue, we consider a simple model based on the application of Eq. 2 with the susceptibility given by Eq. 7. It must be noted that Eq. 2 for the high frequency limit is equal to Eq.11 with $\theta = 0^\circ$. This can be understood considering that in the magnetic field around zero, the skin depth is big enough to consider that the high frequency
magnetic field is penetrating through all the wire, being the most important contribution to the impedance that of the inner core with axial magnetization. It is also important to remark that we take as an approximation the magnetic permeability as a scalar instead of a tensor [13].

As shown in Fig. 3, this simple approach gets a closer fit to the experimental measurements exposed in the next section. The error around zero magnetic field has been improved, getting the expected value of the experimental data. Figure 4 describes the response of the skin depth δ with the external magnetic field. As expected, the value of δ is minimized at certain values of magnetic field where the projection of the field reaches the anisotropy field $H_a$. Thus the impedance of the microwire is maximum at these points since the effective section of the microwire is constrained by the skin-depth effect. At higher fields δ increases and therefore the impedance is reduced. When its value is much higher than the radius of the microwire, the sample is saturated and its impedance experience small variations with the external field.

As previously introduced, the circular loop configuration of the microwire (see Fig.6(a)) can be thought as a superposition of longitudinal elements with different incident angles. The model previously introduced can be used to calculate the angular-dependent impedance $Z_{\theta}(\theta)$ of a microwire. Thus, the total impedance of a loop can be calculated by integrating the contribution of the different elements:

$$Z_{\text{Loop}} = \int_{0}^{2\pi} Z(\theta) d\theta$$  \hspace{1cm} (13)

In Fig.5 it is shown the impedance of a microwire with the shape of a circular loop. It has been calculated by taking linear segments of microwires with angular steps of 1°. It is found that the response of a circular microwire presents the characteristic shape with two peaks, although these peaks are wider than those found for the reference case of a straight sample and with an incident angle of 0°. In addition, the GMI ratio is lower and the position of the peaks are slightly higher.

Fig.2: Simulation of GMI with the solution in Eq.11., with parameters, $a=3.8\mu m$, $f=15\text{MHz}$, $l=3.3\text{cm}$, $\sigma=8.7\cdot10^5 \text{S/m}$, $\mu_0\text{Ms}=0.5 \text{T}$, $\alpha=0.15$, $H_a=285 \text{A/m}$ and $\gamma=19.36\cdot10^{10} \text{T}^{-1} \text{s}$.  

Fig.3: Impedance of a microwire calculated with Eqs. 2 and 7 and parameters $a=3.8\mu m$, $f=15\text{MHz}$, $l=3.3\text{cm}$, $\sigma=8.7\cdot10^5 \text{S/m}$, $\mu_0\text{Ms}=0.5 \text{T}$, $\alpha=0.15$, $H_a=285 \text{A/m}$ and $\gamma=19.36\cdot10^{10} \text{T}^{-1} \text{s}$.  

Fig.4: Simulation of the skin depth in a microwire with parameters $a=3.8\mu m$, $f=15\text{MHz}$, $l=3.3\text{cm}$, $\sigma=8.7\cdot10^5 \text{S/m}$, $\mu_0\text{Ms}=0.5 \text{T}$, $\alpha=0.15$, $H_a=285 \text{A/m}$ and $\gamma=19.36\cdot10^{10} \text{T}^{-1} \text{s}$.
3. Experimental results and analysis.

Figure 6(b) shows a SEM image of the microwires here employed, where the ferromagnetic core as well as the glass coat can be clearly distinguished. The characterization of the GMI phenomena in microwires is usually performed by measuring the change of impedance versus magnetic field for a given frequency and a constant AC amplitude of the driving current. The driving current generates a circular magnetic field into the sample that affects to its magnetization processes. The GMI effect is measured at constant current amplitude in order to keep a constant contribution of the AC magnetic field.

Figure 7 shows the impedance modulus of a longitudinal microwire of 3.3 cm as a function of the incident angle of the magnetic field ($\theta$), with a constant current of 1 mA and 15 MHz. The behaviour of the impedance with the incident angle can be understood as the superposition of the parallel and perpendicular projections of the magnetic field with respect to the microwire (see inset in Figure 8). Due to the negligible GMI response of the perpendicular projection, the displacement of the peak position ($H_k$) is mainly controlled by measure the in plane (x-y) omnidirectional magnetic field $H_0$. A straight sample of 3.3 cm has been experimentally characterized. Incident fields at different angles $\theta$ with respect to the axis of the sample have been applied. We have used the experimental setup previously employed in [24]. First, the impedance has been characterized for a constant AC current of 1 mA, frequency of 15 MHz and incident angles from $\theta = 0^\circ$ to $\theta = 90^\circ$ in a $15^\circ$ step. The experimental results are summarized in Fig. 7. When the magnetic field is parallel to the microwire ($\theta = 0^\circ$), the impedance response shows double-peak behaviour (typical response when the wire has circular anisotropy with two maxima appearing at the anisotropy field $H_a=285.4$ A/m). Similar results were obtained in [24] where the same microwire composition was employed. The position of the peak of GMI increases with the increase of the incident angle of the magnetic field. Note that the maximum value of the impedance presents small variations for a broad range of angles. However, when the magnetic field impinges perpendicular to the microwire direction ($\theta = 90^\circ$), the GMI response disappears.
the projection of the applied field in the axial direction of the microwire. Using this approach, the peak position can be determined by $H_k = H_a / \cos(\theta)$, where $H_a$ is the anisotropy field. Figure 8 shows a comparison between the measured values of $H_k$ and the prediction obtained using the projection of the field on the axial direction of the microwire.

Following this procedure, the complete GMI response at a certain incident angle can be obtained as the superposition of the parallel and perpendicular projections, i.e. $Z(\theta) = Z_0 \cos(\theta) + Z_{90} \sin(\theta)$, although the perpendicular contribution in the magnetic field range under study can be neglected. A particular case for $\theta = 45^\circ$ is calculated and represented in Figure 9. In this figure, we can see the comparison between the measured response at $45^\circ$ and the modelled response calculated using the aforementioned projection. As we obtain a good agreement in the comparison we are going to use this model for the simulation of the impedance of a microwire in the shape of a circular loop. In Fig.10 there is the comparison between the measured microwire in a circular loop and the impedance calculated by the sum of the GMI for angles between $0^\circ$ to $90^\circ$ in steps of $15^\circ$. As it can be seen in Fig.10 the model used fits very well with the experimental measurement for the circular loop sensor.

Figure 11 shows the measurements of the impedance of a microwire in the shape of a circular loop with 0.5cm of radius for different AC currents flowing through it. It is found that the anisotropy field increases with decreasing currents. The excitation of the microwire at lower currents leads to higher GMI peaks, although for currents below 5mA there is more noise due to the magnetization processes. The noise is probably due to wall movements that leads to Barkhausen jumps. With a current of 7mA the measurements exhibit lower levels of noise and a monotonous variation of impedance without perceptible Barkhausen jumps. Regarding these data, we conclude that the sensor presented in the next section should be excited at 7mA. This current reduces the noise and offers a high sensitivity in the low field region.

**Fig. 8:** Magnetic field where the maximum of impedance is found ($H_k$) as a function of the incident angle ($\theta$). Comparison with the theoretical value obtained by using the projection over the wire direction.

**Fig. 9:** Superposition model and comparison with the measurement results for $\theta = 45^\circ$ with a constant current of 1 mA and 15 MHz.

**Fig. 10:** Impedance response for the circular loop with a constant current of 7mA and 11MHz. Comparison between the measurement (dotted blue line) and the model based on measured longitudinal elements (solid red line). The model uses the measurements of GMI form $0^\circ$ to $90^\circ$ in steps of $15^\circ$. 
The impedance of the microwire as a function of the frequency is shown in Fig. 12. According to previous results [24], the GMI effect is stronger at higher frequencies. For this reason, the proposed sensor will operate at the maximum measured current, that is, 15MHz.

**4. Signal conditioning.**

The proposed conditioning circuit is shown in Fig. 13. First, a sinusoidal signal at 15MHz is generated in a Colpitts oscillator. This signal is buffered and driven to a current source that feeds the microwire with a constant AC current. The voltage of the microwire pass through an envelope detector in order to measure its AC amplitude. Finally, the resulting signal goes to an amplifier with a low pass filter and offset adjustment.

**Fig. 13:** Schematic of the signal conditioning circuit designed for the GMI sensor.
The circuit of Fig. 13 has been built and characterized. A photograph of the resulting board can be observed in Fig. 14. Its response to an external magnetic field is shown in Fig. 15 and exhibits a usable response in the range of ±200A/m. Since the response is monotonic within this range, it is suitable to be digitally corrected in order to get a linear response between magnetic field and output voltage. Note that, since the sensor is omnidirectional, it cannot distinguish the direction of the applied field but only the in-plane magnitude of the magnetic field.

Fig. 14: Image of the signal conditioning circuit whose schematic is shown in Fig. 13.

Fig. 15: Output voltage of the developed sensor as a function of the in-plane magnetic field.

5. Conclusion

We have designed and built an in-plane omnidirectional magnetic sensor based on a glass coated microwire. For this purpose, we have used a microwire with the shape of a circular loop. In order to model the sensor response, a simplified approach for the calculation of the impedance of a circular microwire is presented. This model is based on the sum of the contributions of small pieces of microwire with different angles with respect to the direction of the incident magnetic field. It is worth to note that this method allows the calculation of microwires with any shape, which paves the way to new sensor designs based on the shape of the microwire.

We have designed and built a signal conditioning circuit for the measurement of in-plane magnetic fields. The sensor presents a monotonic response in the range ±200A/m which can be easily linearized with a digital controller.

The extension to an omnidirectional sensor would consist of two of these circular loops placed perpendicularly, each one sensing the component of magnetic field laying in the plane of the loop.

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