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Additional Information

Automatic Bluefin Tuna Sizing using a Stereoscopic Vision System

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9 Abstract

This paper presents a non-invasive fully automatic procedure for Bluefin Tuna sizing, based on a stereoscopic vision system and a deformable model of the fish ventral silhouette. An image processing procedure is performed on each video frame to extract individual fish, followed by a fitting procedure to adjust the fish model to the extracted targets, adapting it to the bending movements of the fish. The proposed system is able to give accurate measurements of tuna Snout Fork Length (SFL) and widths at five predefined silhouette points without manual intervention. In this work, the system is used to study size evolution in adult Atlantic Bluefin Tuna (Thunnus Thynnus) over time in a growing farm. The dataset is composed of 12 pairs of videos, which were acquired once a month in 2015, between July and October, in three growout cages of tuna aquaculture facilities on the west Mediterranean coast. Each grow out cage contains between 300 and 650 fish on an approximate volume of 20000 m³. Measurements were automatically obtained for the four consecutive months after caging and suggest a fattening process: SFL shows an increase of just a few centimetres (2%) while the maximum width (A₁) shows a relative increase of more than 20%, mostly in the first two months in farm. Moreover, a linear relation (with coefficient of determination R²>0.98) between SFL and widths for each month is deduced, and a fattening factor (F) is introduced. The validity of the measurements is proved by comparing 15780 SFL measurements, obtained with our automatic system in the last month, versus ground truth data of a high percentage of the stock under study (1143 out of 1579), obtaining no statistically significant difference. This procedure could be extended to other species to assess the size distribution of stocks, as discussed in the paper.

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Keywords: Underwater stereo-vision; Computer vision; Fisheries management; Fish sizing; Biomass estimation; Automatic 3D measurements.

1. Introduction

The early detection of impacts from natural and anthropogenic activities is very important to the sustainability of the marine environment. Fishing, climate change and pollution have high implications for fish stocks. Reliable fish measurements like length, height and width can be a very important indicator of the health of wild fish stocks (Dunbrack, 2006), (Shortis *et al.*, 2013), (Rosen *et al.*, 2013), (Shafait *et al.*, 2017). Sampling methods to take fish measurements that involve capturing and handling live fish must be discarded, because they not only cause fish stress and possible death but also hinder the achievement of a large number of measurements.

Monitoring wild fish stock and inspection in aquaculture require extremely gentle handling of the target to avoid damage. Thus underwater computer vision systems have been frequently used, as reported in recent reviews (Zion, 2012), (Shortis *et al.*, 2013), (Mallet and Pelletier, 2014), (Boutros *et al.*, 2015), (Hao *et al.*, 2015), (Saberioon *et al.*, 2016),

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because it is a very appropriate non-intrusive method that permits work even when the fish are alive. In the particular case of using stereoscopic vision systems (two cameras in a side-by-side arrangement), the following applications have been achieved: fish sizing (Ruff et al., 1995), (Tillett et al., 2000), (Lines et al., 2001), (Harvey et al., 2003), (Costa et al., 2006), (Dunbrack, 2006), (Torisawa et al., 2011), (Letessier et al., 2015), (Williams and Lauffenburger, 2016); fish counting and sizing (Costa et al., 2009), (Rosen et al., 2013); fish sizing in combination with acoustic techniques (Sawada et al., 2009), (Espinosa et al., 2011), (Kloser et al., 2011); fish farm automation (Martinez-de Dios et al., 2003); wild fish stock assessment (Willis and Babcock, 2000), (Watson et al., 2009), (Harvey et al., 2012), (Langlois et al., 2012), (Seiler et al., 2012), (Smale et al., 2012), (Zintzen et al., 2012), (Wakefield et al., 2013), (Santana-Garcon et al., 2014), (McLaren et al., 2015).

 Nevertheless, vision sensors and image processing methods have to overcome limited visibility, temporal and spatial variations in lighting, varying distances and relative orientations between cameras and objects, motion and density of the monitored targets, and even lack of physical stability. All these conditions represent a very demanding challenge, which have limited the development of fully automatic commercial solutions. In fact, most of the aforementioned applications are manual or semi-automatic and require human intervention in some of their stages. In regard to biomass estimation, the most widely used commercial systems are AQ1 AM100 (Phillips *et al.*, 2009) and AKVAsmart, formerly VICASS (Shieh and Petrell, 1998), which belong to the semi-automatic category. In both systems, human operators must inspect the videos and select frames in which the fish is isolated and straight, to then manually mark fish snout and fork in both stereo images to estimate its length. The International Commission for the Conservation of Atlantic Tunas (ICCAT) establishes a catch reporting system which covers the full chain of Atlantic Bluefin Tuna (ABT) fishery from capture to marketing (Costa *et al.*, 2009). The use of a stereoscopic system to estimate catch quotas is established in (ICCAT, 2015). The number of individuals, counted during the transfer from tow to grow-out cages, is multiplied by the average weight of a subsample of the stock to derive the total biomass per tow cage. As mentioned before, current stereoscopic vision systems need human operation, making the process slow and laborious, and introduce the variability of manual measuring in the biomass estimation. Therefore, a vision-based automatic procedure for ABT biomass estimation is required.

One of the most significant aspects for farmers, biologists and researchers would be the definition of growing models for different species (Aguado-Gimenez and Garcia-Garcia, 2005), but periodic systematic monitoring is required. Aquaculture farms are a good environment for this purpose. Species such as tuna and salmon are most commonly farmed due to market acceptance and rapid growth (Shortis, 2015), (Sture *et al.*, 2016). Monitoring would provide information on abnormal growth so that the causes such as parasites, stress caused by environmental conditions and diseases could be tackled. Additionally, fish behaviour depending on size or seasonal habits could also be studied and feed regimens and harvest strategies in aquaculture could be optimized. As indicated in (Harvey *et al.*, 2003), collecting numerous, precise accurate data on length or age without the need to physically handle live fish has been identified as an urgent requirement for fisheries and aquaculture managers. Some authors, such as (Lines *et al.*, 2001), (Zion, 2012), (Shortis *et al.*, 2013), (Atienza-Vanacloig *et al.*, 2016), (Shafait *et al.*, 2017), highlight the need for fully automatic methods for underwater video processing.

The automatic identification of a single fish is an essential step in achieving a fully automatic process. However, body bending while free-swimming means the same individual is observed with very different shapes, sizes and orientations depending on the visualized frame. So, robust fish detection methods dealing with these variations are required (Lines *et al.*, 2001). In (Atienza-Vanacloig *et al.*, 2016) a deformable adaptive model based on computer vision methods that automatically fit the body ventral silhouette of Bluefin Tuna while swimming was proposed. This model achieved very high success rates (up to 90%) identifying individuals in complex images acquired in real conditions. The main advantages of using silhouette model fitting are the following: i) foreground fish in crowded images can be detected ii) fish can be

measured even in images with bad segmentation due to noise or variable lighting, and iii) fish direction and body bending can be deduced. When the target has been identified and characterized, 3D biometric measurements can be obtained from a calibrated stereo vision system. Moreover, the validity of any semi-automatic or automatic procedure must be demonstrated by comparing the results with ground truth measurements.

In this work, we present a fully automatic procedure based on a stereoscopic vision system and a deformable model of the Bluefin Tuna ventral silhouette to estimate length and widths. Our proposal can provide accurate measurements under real conditions and without human intervention, as shown by comparing the results with ground truth data. Furthermore, fish growing and fattening models are deduced analysing the data collected by us through systematic periodic acquisition for four consecutive months in grow-out cages. Although this paper is mainly focused on achieving good precision in biometric measurements of fish in cages, the work is currently being adapted so that biomass can be estimated during the fish transfer process.

2. Materials and methods

The computer vision algorithms involved in the process of fish sizing are described and summarized in Figure 1, as well as the offline manual and supervised operations we performed to check the goodness of our algorithms.

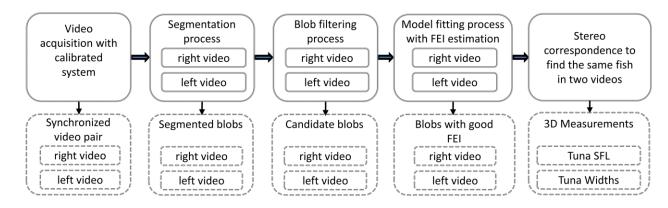


Figure 1. Sequence of processes performed automatically in our proposal, in the first row, and the results of each step, in the second row. Fitting Error Index (FEI) is a coefficient that represents the goodness of the model fitting.

2.1. Video acquisition

In order to study the evolution of the ABT dimensions, videos were acquired in three grow-out cages in the Grup Balfegó aquaculture facilities. The three grow-out cages are located next to each other and 2.5 miles off the port of l'Ametlla de Mar (Spain). The cages are cone shaped with a base of 50m of diameter in the water surface and 30 m high, that is an approximate volume of 20 000 m³. The recordings were taken using the AM100 stereovision system (www.aq1systems.com). It uses two Gigabit Ethernet cameras, with image resolution of 1360x1024 pixels and framerate of 12 fps. The cameras are mounted in an underwater housing, with a baseline of 80cm and an inward convergence of 6°. The system is rated to 40m deep and has an umbilical cable that supplies power to the cameras and transfers images to a logging computer, which generates synchronized left and right videos.

The recordings were taken once a month in 2015 between July and October for each grow-out cage, using the same AM100 stereovision system. The resulting dataset consists of 12 pairs of videos, one per month per cage, of 120 minutes duration each one, enough to extract a statistically representative amount of measurements. The cameras were positioned 15 m deep in the grow-out cages and looking towards the surface to obtain a ventral silhouette of the fish (Figure 2). This camera arrangement has three advantages: first, with this orientation, the sunlight acts like a backlight system so objects are always darker than water; second, in this set up, body bending can be clearly appreciated and dealt with; third, the

most reliable measurements are obtained when the fish are swimming in a plane orthogonal to the visual axis (Dunbrack, 2006). The acquired videos are processed automatically using the computer vision algorithms described.

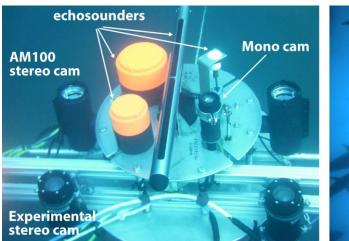




Figure 2. (a) Sensors platform in grow-out cages, including the AM100 stereoscopic vision system used for this study. (b) Snapshot of recordings with the AM100.

2.2. Stereo vision system calibration

 Images for calibration were acquired in a tank containing seawater at IEO (Spanish Oceanographic Institute) facilities in Mazarrón (Spain). A 1.40 x 1.10 m checkerboard pattern was guided from -45° to 45° with respect to the optical axis and moved between 1 and 10 m away from the cameras. The MATLAB® Stereo Calibration Application based on (Heikkila & Silven, 1997) and (Zhang, 2000) was used to estimate the calibration parameters. The diagonal length of the checkerboard pattern was computed in 5018 stereo images to analyse our calibration accuracy in terms of proportional error between true and measured lengths. 95.91% of the measurements fall within a margin of error of 1% and 100% of the measurements fall within a margin of error of 3% for all ranges. Measurements of a scale bar with known length (1.5 m) are done over a range of distances (2 to 10 m) before each recording to guarantee that the camera calibration is still valid.

2.3. Processing frames: segmentation, filtering and tuna model fitting

In the present paper, a variant of the tuna model presented in (Atienza-Vanacloig *et al.*, 2016) was implemented to achieve our objective of estimating biometric measurements.

2.3.1. Segmentation and filtering process

Image segmentation was implemented using local thresholding technique (Petrou and Petrou, 2011) to extract individual objects (fish) from video frames. Local thresholding examines statistically the intensity values of the local neighbourhood of each pixel assuming that illumination is approximately uniform in the neighbourhood. In our case, the pixel in i-th row and j-th column of the image is selected as foreground if its intensity value p_{ij} is below a local threshold M_{ij} . The local thresholding technique can be expressed as:

$$M_{ij} = \frac{1}{w*w} \sum_{l=i-\frac{w}{2}}^{i+\frac{w}{2}} \sum_{k=j-\frac{w}{2}}^{j+\frac{w}{2}} p_{lk} \quad ; \quad \begin{cases} p_{ij} \geq M_{ij}; \ p_{ij} \text{ is background} \\ p_{ij} < M_{ij}; \ p_{ij} \text{ is foreground} \end{cases} \quad ; \quad \forall \ p_{ij} \in F_t$$

where w=25 is the size of the neighbourhood, p_{lk} the intensity values of the neighbour pixels and F_t the video frame. Open, close and fill morphological operations complete the segmentation process. The segmented blobs are geometrically characterized and sifted using shape (aspect ratio), pixel density and dimensional filters. An edge detection algorithm is then applied and a fitting of the deformable model of the fish, defined as a nonlinear multivariable function, is obtained using a minimization algorithm.

2.3.2. Deformable tuna model and fitting process

Figure 3e shows the deformable model **M** of tuna fish defined in (Atienza-Vanacloig *et al.*, 2016) as a vector of five parameters $\mathbf{M} = [\mathbf{s}_x, \mathbf{s}_y, l, \alpha, \theta]$ where: \mathbf{s}_x and \mathbf{s}_y give the image location of the snout tip; l is the length of the vertebral column; α denotes the angle of the fish head in relation to the horizontal axis, and θ is the bending angle of the vertebral column. The capabilities of this fish model have been increased, from discrimination of individuals to accurate measuring: (i) the number of vertebral points has been increased from 16 to 18 and are now not equidistantly distributed along the fish length l, (ii) more points are concentrated in the tail, a crucial zone for length measurements, (iii) the area around the pectoral fin is not considered, as its many shapes can hinder model fitting, and (iv) a new width vector parameter w, containing a width coefficient for each vertebral point, has been added to already existing model parameters. While in the deformable model presented in (Atienza-Vanacloig *et al.*, 2016), the width is considered a function of length with constant coefficients, our model assigns a variable-bounded coefficient for each vertebral point.

This new model is defined as a vector of six parameters $\mathbf{M_w} = [s_x, s_y, l, \alpha, \theta, w]$ where w is a vector of coefficients for width fitting. The model is characterized by 18 vertebras $\mathbf{v_i} = (\mathbf{x_i^v}, \mathbf{y_i^v})$ distributed along the fish length, whose position is computed according to the parameters using the following equation:

where l_i is the length from the snout to the ith-vertebra and θ_i the bending angle of the ith-vertebra.

The model consists of 35 landmarks, 1 landmark for the snout tip and 17 landmarks for each side of the tuna body profile. The landmarks $k_i = (x_i^k, y_i^k)$ that configure the $\mathbf{M_w}$ model silhouette are obtained from the vertebral points v_i with the following expressions:

$$x_i^k = x_i^v \pm w_i l_i c_i \sin \theta_i; \quad y_i^k = y_i^v \pm w_i l_i c_i \cos \theta_i; \quad i = 1 ... n$$
 (3)

where the positive or negative sign depends on the side of the tuna body profile, while c_i is the ith-coefficient from a constant vector defining the distance from vertebras to landmarks and w_i is the width coefficient of ith-vertebra.

A Fitting Error Index (FEI), based on the quadratic distance between the model points and the target edges points, is computed to analyse the goodness of the fitting. FEI takes values in the [0..10] range, where FEI=0 denotes a perfect fit between the segmented blob and the theoretical model $\mathbf{M_w}$. Fittings with high values (FEI>6) are discarded. See (Atienza-Vanacloig *et al.*, 2016) for further details on the model definition and fitting procedure.

Figure 3a, b, c and d show the image processing steps. The model comprises from the fish snout to the end of the caudal peduncle keel, as the caudal fin cannot be modelled due to its great variability. A set of blobs with good FEI, that is, with good model fitting, is provided after the processing frames stage. Up to this point, the videos acquired by both cameras are processed independently, as can be seen in Figure 1.

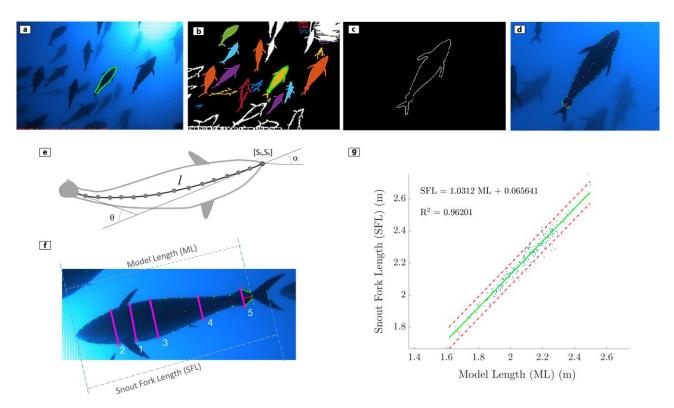


Figure 3. Image processing steps: (a) original image, (b) image segmentation, (c) edge detection, (d) deformable model fitting with the 18 non equidistant vertebral points in magenta and their respective profile points (landmarks) in green, (e) deformable tuna model presented in (Atienza-Vanacloig *et al.*, 2016), (f) graphical representation of the Model Length (ML), Snout Fork Length (SFL) and the five widths defined to study the fattening evolution, (g) polynomial fitting for the ML-SFL relation, the green line is the linear fitting and the red dashed lines are the 95% confidence interval.

2.4. Stereo correspondence

The results for left and right videos, obtained separately in Section 2.3, can be merged to calculate fish measurements if the same individuals can be identified in both videos. With the calibration described in Section 2.2 the relative position and orientation of the two cameras is known, so the following epipolar geometry restriction can be used: given two characteristic points of the fish model, like snout and tail, in one image, the matching points in the other image must lie on the epipolar line defined by the calibration parameters. The solution is not unique in the image plane so geometrical filters must be added to guarantee the correspondence. Only the samples with similar model parameters (length, orientations, bending and widths) are considered.

2.5. Length and Widths: 3D Measurements

When stereo correspondence has been guaranteed, the image plane information can be transformed to 3D measurements using the calibration matrices and 3D triangulation.

Fish are deformable due to the swimming motion and, consequently, measurements taken from a single frame may not be reliable (Shortis *et al.*, 2013). Two main options are used in the literature to reduce the effect of swimming motion on length measurement: i) take measurements in all frames and deduce straight body length from a sinusoid-like pattern (Shortis *et al.*, 2013); ii) account for body bending by adding contiguous linear segments (Williams and Lauffenburger, 2016). In our case, the swimming length problem is resolved using the tuna model bending angle θ , by identifying as valid samples the ones whose vertebral points form a straight line and discarding the others. Model Length (ML) is computed as the Euclidean distance between the 3D coordinates of the snout and tail fork model points.

As explained in Section 2.3 and as can be appreciated in Figure 3a and b, the caudal fin cannot be modelled due to its great variability, so a relation between SFL, usually used in the literature, and ML is needed. For this purpose, 279 samples

from within the automatic measurements were selected with the following requirements: the tail fork must be clearly identifiable and aligned with the snout and tail model points, as shown in Figure 3f. For these samples, the tail fork point was manually selected to have SFL. A polynomial fitting was done, resulting in an SFL-ML linear relation as shown in Equation 2 and Figure 3g.

$$SFL = 1.0312 \text{ ML} + 0.065641 \tag{4}$$

For the case of fish width measurements, the 3D coordinates of the model points that are symmetrically paired to the vertebral column could be used, see Figure 3d. However, these points are influenced more by the camera perspective because they are not extreme points in the silhouette. Triangulation may lead to major errors if the matching points in both images do not correspond to the same actual point.

Therefore, the proposal for width measurements differs from the one for SFL measurements. In this case, only the model with better FEI from the left or right image is considered. The pairs of characteristic model points defining the widths are transformed to the 3D space assuming each pair is at the same distance from the cameras. For this study, five fish widths A_i are considered, whose location in the model can be seen in Figure 3f.

The distance to the cameras Z_i for each width A_i is computed with the following expression:

$$Z_{i} = Z_{s} + \frac{l_{i}}{l}(Z_{t} - Z_{s})$$
 (5)

where Z_s and Z_t , are Z coordinates of snout and tail fork, l is model length, and l_i is length from the snout to the vertebral axis corresponding to A_i . Note that Equation 3 represents the equation of a line between Z_s and Z_t and the calculated distance depends on the position in the model of the pair of points associated to each width A_i . Once the points are in the 3D space, the Euclidean distances for each pair of points are selected as the fish 3D widths.

3. Results

The dataset was recorded with a stereoscopic system for four consecutive months immediately after caging, from July to October 2015, on three grow-out cages. Targets were extracted from a total of 12 pairs of videos of 120 minutes duration and around 100000 frames each. Our tuna model had a successful fitting, that is, good FEI, in individual images in more than 1.4 million blobs, and more than 100000 3D measurements where obtained after stereo correspondence. Redundant information in the statistical distribution is intrinsic to the case of grow-out cage monitoring due to sample repetition, but its impact decreases with the number of measurements. Moreover, the stock under study is considered almost constant, as the population only changes considerably in one cage and month (cage 1 in October). Table 1 summarizes the number of video frames, number of good model fitting samples, automatic 3D measurements, and number of fish in cages when the recordings were taken. The videos of cage 2 in August were corrupted, so no information can be extracted from them.

It should be noticed that this work focuses on obtaining as many samples as possible, so computing time is not an issue. The overall process shown in Figure 1, had a computing time of around 5 hours for each cage and month. As further work, both the code and the algorithms will be optimized to adapt the proposal to applications where computing time is important, like biomass estimation in transfers.

	NUMBER OF	GOOD MODEL FITTING		3D MEASUREMENTS / NUMBER OF FISH IN CAGES			
	FRAMES	LEFT	RIGHT	CAGE 1	CAGE 2	CAGE 3	TOTAL
JULY	648180	212562	231973	3923 / 646	20143 / 647	7651 / 647	31717 / 1940
AUGUST	324750	184316	192719	8180 / 636	- / 631	17209 / 626	25389 / 1893
SEPTEMBER	646220	199090	181340	3996 / 538	15208 / 625	12011 / 625	31215 / 1792
OCTOBER	650210	124712	129521	6706 / 326	3365 / 624	5709 / 624	15780 / 1579
TOTAL	2269360	720680	735553	22805	38716	42580	104101

Table 1. Number of video frames, number of good model fitting samples, automatic 3D measurements, and number of fish in cages when the recordings were taken. The study comprises three grow-out cages from July to October.

The data collected over four months have been processed using the computer vision algorithms described in Section 2, and the resulting 3D measurements of 104101 fish are analysed in this section with the following structure:

239 - SFL evolution.

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- 240 A_i evolution.
- SFL A₁ ratio evolution.
- Fattening factor.
- Measurements validation.

At least 3000 samples have been extracted for each cage and month, so the results are considered statistically significant. Measurements are validated by comparing ground truth data from harvests in October with automatic measurements in that month.

3.1. Snout Fork Length (SFL) evolution

Figure 4 shows normalized SFL frequency histograms and SFL means (\overline{SFL}) for each month and cage. Distributions are very similar for all months and \overline{SFL} variation for the four months is of only a few centimetres (2%). The great majority of the samples are located in the interval SFL ϵ [1.70,2.60]. The same results seems to apply to cage 2, despite the missing data in August.

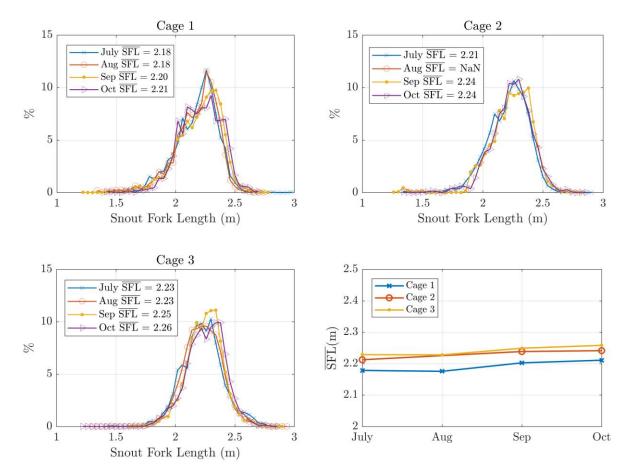


Figure 4. Normalized Snout Fork Length (SFL) frequency histograms and evolution of SFL means (SFL) for each month and cage under study.

3.2. Widths (A_i) evolution

The five fish widths defined in Figure 3f are considered. The normalized frequency histogram for each width A_i and month, and the evolution of the mean widths \overline{A}_i are shown in

Figure 5 for cages 1 and 3. It can be seen that the form of the distribution is similar over months and the evolution of the widths is different for each point: whereas A_2 and A_5 remain almost constant, A_1 , A_3 and A_4 show a clear fattening evolution. Moreover, those widths increase most in the first two months in the cages. Similar results apply to cage 2, although the representation of those results has been omitted due to the lack of information in August.

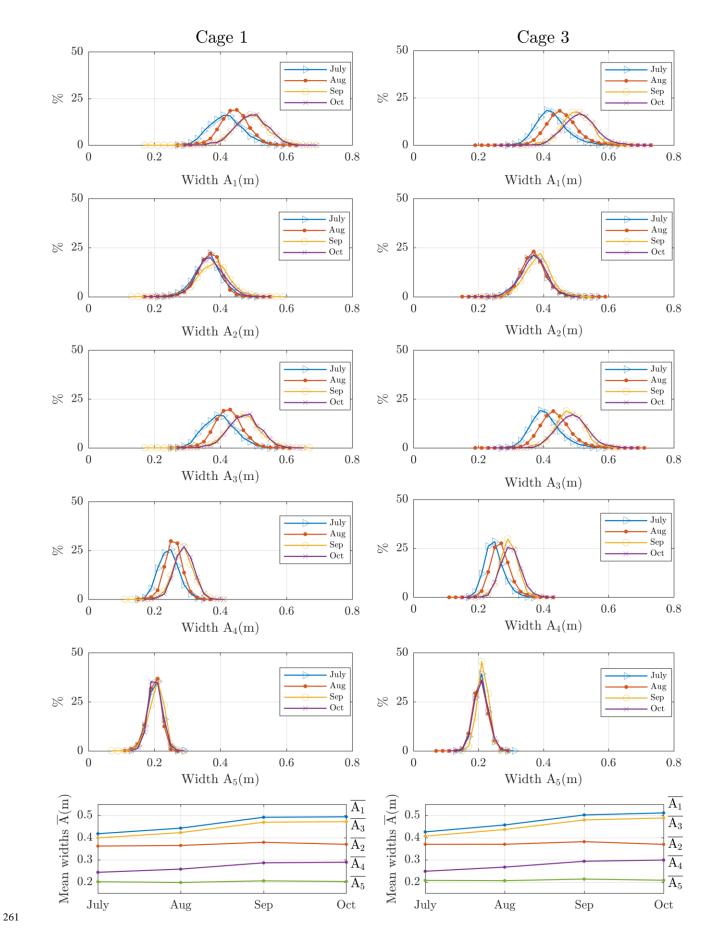


Figure 5. Normalized frequency histograms for each width A_i and evolution of mean widths \overline{A}_i over months for cages 1 and 3.

3.3. Snout Fork Length (SFL) - Maximum width (A_1) ratio evolution

The study of the SFL-widths ratio evolution is focused on the maximum width A_1 and for SFL ϵ [1.70,2.60], because the evolution is similar for all widths that vary over time and there are few samples outside that length interval. The relation between SFL and A_1 over months can be seen in Figure 6: on the left column, a scatter plot with the data of the first and last study months (July and October) is shown; on the right, SFL is split in intervals of 5 cm and the mean width for each interval is calculated. A strong linear relation can be observed for all months. The fitting to a linear model and the coefficient of determination R^2 is summarized in Table 2.

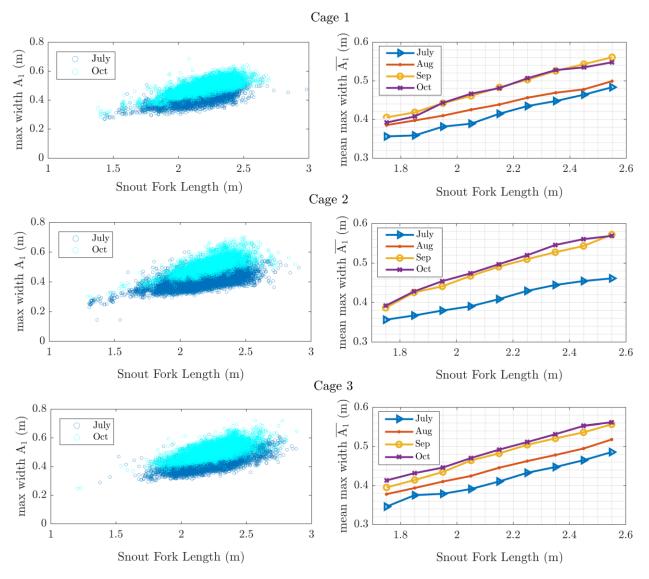


Figure 6. On the left, scatter plots of Snout Fork Length (SFL) and maximum width (A_1) for first and last study months. On the right, relation between SFL and $\overline{A_1}$ over months. SFL \in [1.70,2.60] is split in intervals of 5 cm and the mean width for each interval is calculated.

	JULY	AUG	SEP	OCT
CAGE 1	$A_1 = 0.164 \cdot SFL + 0.059$ $R^2 = 0.985$	$A_1 = 0.145 \cdot SFL + 0.125$ $R^2 = 0.996$	$A_1 = 0.194 \cdot SFL + 0.062$ $R^2 = 0.995$	$A_1 = 0.195 \cdot SFL + 0.060$ $R^2 = 0.981$
CAGE 2	$A_1 = 0.141 \cdot SFL + 0.106$ $R^2 = 0.988$	-	$A_1 = 0.218 \cdot SFL + 0.156$ $R^2 = 0.991$	$A_1 = 0.222 \cdot SFL + 0.015$ $R^2 = 0.985$
CAGE 3	$A_1 = 0.159 \cdot SFL + 0.069$ $R^2 = 0.990$	$A_1 = 0.175 \cdot SFL + 0.067$ $R^2 = 0.993$	$A_1 = 0.189 \cdot SFL + 0.071$ $R^2 = 0.998$	$A_1 = 0.188 \cdot SFL + 0.083$ $R^2 = 0.993$

Table 2. Linear fitting of the relation between Snout Fork Length (SFL) and maximum width (A₁) over months.

3.4. Fattening factor F

 As can be seen in Figure 7, the evolution over time of maximum width A_1 for different SFL is very similar, so a global fattening factor can be defined independently of SFL:

$$F = \frac{\overline{A_{1M}}}{\overline{A_{11}}} \tag{6}$$

where $\overline{A_{1M}}$ is the mean A_1 for each month, and $\overline{A_{1J}}$ mean A_1 in July. Its evolution over time can be seen on the last subplot in Figure 7: the fattening factor increases mostly, and almost linearly, in the first two months and less in the third month.

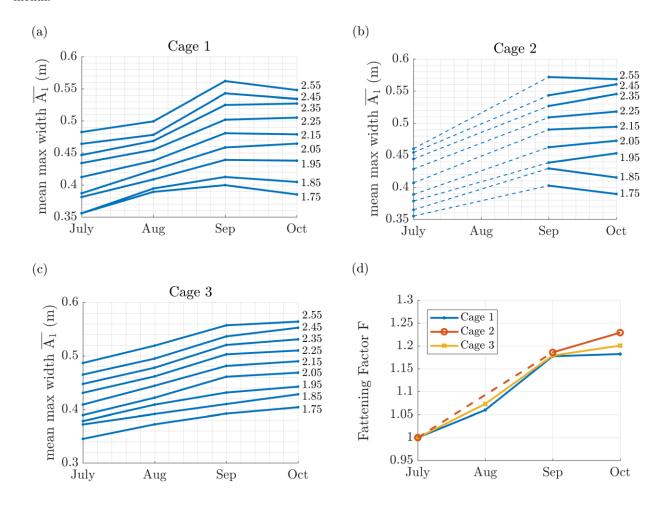


Figure 7. (a-c) Mean maximum width $(\overline{A_1})$ for Snout Fork Length (SFL) intervals over months. SFL \in [1.70,2.60] is split in intervals of 5 cm and the mean width for each interval is calculated. (d) Fattening factors over months. Line dashed to represent the missing data in August.

3.5. Measurements validation

 To validate the procedure, the system measurements and ground truth data are compared. The ground truth data is provided by Grup Balfegó, which measures SFL of the fish in the cages at harvesting. They are dated mostly between October and December, so it was decided to compare them with automatic measurements of the recordings in October. The analysis is also run on pooled data, although the fish in each cage constitute an independent stock and merging data from different stocks can lead to differences in distributions.

Figure 8 shows the normalized SFL frequency histograms of the automatic measurements and ground truth data, for each cage and with pooled data. Differences in SFL among harvests and automatic measurements were examined with analysis of variance tests. Since the two groups have unequal sample sizes and homoscedasticity (homogeneity of variance) cannot be ensured, Welch's ANOVA test (Welch, 1951) is used, as recommended in (Rasch *et al.*, 2011) and (McDonald, 2014). The differences in SFL frequency distributions are analysed with the Kolmogorov-Smirnov test (Massey, 1951).

As Table 3 shows, the tests for \overline{SFL} give p-values higher than the 5% significance level for each cage and with data pooled, and the tests for SFL distribution frequency give p-values higher than the 5% significance level, except when the cages are pooled. In conclusion, there is no statistically significant difference between ground truth and automatic measurements, thereby validating the measurements obtained with the proposed automatic system.

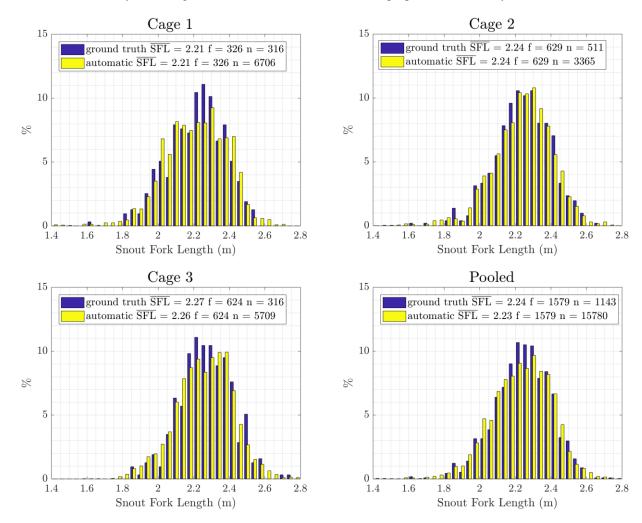


Figure 8. Normalized Snout Fork Length (SFL) frequency histograms. Ground truth in dark-blue and automatic measurements in light-yellow.

SFL, mean SFL; f, number of fish; n, number of samples.

	CAGE 1	CAGE 2	CAGE 3	POOLED
# fish	326	629	624	1579
# harvests (ground truth)	316	511	316	1143
# automatic measurements	6706	3365	5709	15780
Welch's ANOVA test p-value	0.9928	0.7793	0.4118	0.3884
Kolmogorov-Smirnov test p-value	0.3553	0.2944	0.3075	0.0183

Table 3. Automatic system measurements vs ground truth statistical comparison in the three grow-out cages and with data pooled.

4. Discussion

The need for a fully automatic system to accurately estimate the length of free swimming fish with a non-intrusive procedure has often been pointed out in recent years (Costa *et al.*, 2009), (Zion, 2012), (Shortis *et al.*, 2013), (Rosen et al. 2013), (Williams & Lauffenburger, 2016), (Shafait *et al.*, 2017). Fish length information is an important indicator of the health of wild fish stocks and for predicting biomass using length-weight relations (Lines *et al.*, 2001), (Martinez-de Dios *et al.*, 2003). The most common mathematical model between fish length (L) and mass (W) is W = aL^b, where a and b are parameters dependent on fish species (Zion, 2012) and on growth, in captivity or wild, (Aguado-Gimenez and Garcia-Garcia, 2005), (Katavić *et al.*, 2016). The total biomass of a fish stock is commonly determined by obtaining the mean length of a statistically representative number of fish and counting the number of fish (Costa *et al.*, 2009), (Shafait *et al.*, 2017).

The proposed automated system allowed us to process more than 2 million video frames, producing more than 100000 3D length and width measurements. Stereo-cameras were positioned 15 metres deep in the grow-out cages with fish measurements ranging from 3 to 10 m. The limitations of using computer vision, namely high turbidity in water and crowded fish situations, were revealed and the videos in November were dismissed because of poor water visibility. The results demonstrate highly accurate SFL estimation and validate the automatic procedure. As Figure 8 and Table 3 show, there is no statistically significant difference between ground truth and automatic measurements.

The periodicity of our recordings on the same individuals and the large number of samples collected, more than 3000 per cage and month, enables us to analyse evolution over time (four months) of the length and width measurements. This analysis may be of use for solving some paradigms of interest regarding Atlantic Bluefin Tuna for farmers, biologists and researchers such as:

- How does SFL evolve over time? The obtained SFL variation presents an increase of only 2% from first to last month (Figure 4).
- How do widths A_i evolve over time? The obtained evolution differs depending on the fish body section considered: whereas no increasing is shown in head and caudal peduncle keel sections (A_2, A_5) , sections between the pectoral fin and caudal peduncle keel (A_1, A_3, A_4) show clear increasing, mostly in the first two months (Figure 5).
- Is there any relation between SFL and A_1 ? A strong linear relation has been observed: high coefficients of determination R^2 for linear model fitting have been obtained for all months (Figure 6, and Table 2).
- Can a fattening factor for tuna in grow-out cages be established? Fattening factor F, defined as the relative increase over time of maximum width A_1 , shows a fattening evolution that increases almost linearly in the first two months and less in the third month (Figure 7) for SFL ϵ [1.70,2.60]. A simulation of fattening evolution according to fattening factor F is shown in Figure 9.

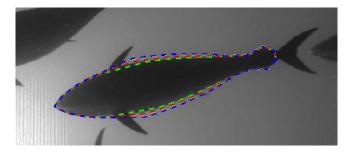


Figure 9. Bluefin Tuna fattening evolution according to the calculated fattening factor. The image corresponds to a fish in July, the green line is the model fitting in that month, and the red, yellow and blue dashed lines are the simulation of the evolution over months.

Automatic extraction of a large number of silhouettes, precise tuna model fitting and accurate 3D measurements were a priority in our developments, without paying much attention to processing time. Working with tuna in cages has the advantage of being able to record the time necessary to obtain a good statistical representation of the stock. Thus, on a two hours recording, the automatic system estimates on average about 10000 fish measurements (SFL and five widths A_i) with a computational cost of five hours (1.38 seconds per sample). We are sure it will be possible to improve the processing time, but currently it is obviously much lower than the time necessary to obtain the same measurements with a manual or semiautomatic application.

The whole fully automatic process is the main difference of this work with respect to other studies with similar goals. Also the following aspects should be highlighted:

- i) Our measurements have been validated with a large number of measurements (15780), a large amount of ground truth data (1143 harvests out of 1579 fish), and wide measuring range (from 3 to 10 metres). Other authors obtained good results measuring fish lengths with stereovision systems, but their proposals have one or several of the following common limitations: measurements are not extracted fully automatically, measurements are taken in a narrow range, the number of measurements is relatively small, or the ground truth comprises only a few samples. In fact, (Lines *et al.*, 2001) reported that the linear dimension of salmon in sea cages could be extracted automatically with a mean error below 10%, but they work with only 60 images of 17 fish and measure in a range from 1 to 2 metres. (Harvey *et al.*, 2003) predicted the SFL of Southern Bluefin Tuna (SBT) inside a cage with a relative error of 0.16% (with SFL from 830 to 1412 mm), but harvesting only 54 SBT from thousands in the cage and measuring in a range of about 1 meter. (Shafait *et al.*, 2017) present a semiautomatic method for estimating the fish lengths of 22138 SBT in transfers in a range from 1 to 4 metres, but it is not fully automatic and the results are compared with manual measurements and not ground truth data.
- ii) <u>Fully automatic estimation of five widths in addition to SFL</u>. Recent studies attempt to show that biomass can be better estimated if fish measurements in dimensions other than length, like width and depth, are available (Aguado-Gimenez and Garcia-Garcia, 2005), (Harvey *et al.*, 2003). Nevertheless, as stated in (Harvey *et al.*, 2003), measuring the width of a fish is relatively subjective due to the lack of defined points in the fish silhouette. Those authors use simple cursor positioning and mouse clicks to measure Maximum Body Depth (MBD). Instead, we use our tuna model features to obtain the maximum width (equivalent to MBD but in width) in the body section close to the pectoral fin (Figure 3f). Our automatic system can produce a lot of SFL and maximum width measurements in a relatively short time, so a statistical distribution with a high number of samples can be obtained, which would allow better biomass estimation.
- <u>iii)</u> Videos are acquired in real world conditions without using any background screen, contrast element or reference object, as it is done for example in (Shafait *et al.*, 2017).
- iv) The acquisition configuration meets the requirements for automatic sizing and counting of tuna in transfers according to (ICCAT, 2015). The stereo-videos were recorded from 15 m deep in grow-out cages with a measuring range from 3 to 10 m. This position and range were selected, as a first approach, to be able to apply this method to fish transfers,

where tuna have to pass from transport to grow-out cages through a 10 x 10 m door between cages. Although measuring fish at higher range to the cameras should lead to greater measurement error, the results prove that our automatic system is able to give accurate measurements in that range interval. The present regulations for ABT establish the use of stereoscopic vision systems to estimate catch quotas when the fish are transferred from tow cages to grow-out cages. But the current systems need human operation, making the process slow and laborious, and introduces the variability of manual measuring into the biomass estimation. Therefore, the proposed vision-based fully automatic procedure for Bluefin Tuna individual biomass estimation makes a necessary and valuable contribution. To complete the system and be able to estimate total biomass in transfer operations, an automatic counting procedure is currently under development.

5. Conclusions and further work

The proposed procedure might be a significant contribution towards a commercial system for fully automatic Bluefin Tuna biomass estimation. The authors consider this system a potential tool to ensure the reliable accomplishment of catch quotas following ICCAT recommendations and to support farmers, biologists and researchers in important aspects of fish growth and marine environment. It is also reasonable to think that better biomass estimation could be achieved using more dimensions of the tuna than just SFL. Our system estimates SFL and five widths in different sections of the fish silhouette which can be used to compute biomass.

As further work, we plan to improve the robustness of the method by adding a time-dependent analysis, as well as other developments, such as: improved segmentation procedures, accurate measurements in bended fish and accurate measurements from other perspectives (not only ventral silhouette) some aspects of the model to provide accurate 3D measurements of bent fish and to fit the tuna silhouette from other views in addition to the ventral one. Moreover, we want to combine this computer vision procedure with echosounder information to estimate biomass in more complex situations, such as wild environments and transfers from tow to grow-out cages.

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