

## Modelling performance management measures through statistics and system dynamics-based simulation

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### Abstract

The objective of this paper is to establish a methodology that combines performance measurement, a statistical record of measures to identify any relations among them, and system dynamics-based simulation modeling with the aim of supporting operations decision systems. This methodology intends to provide the comprehensive analysis of performance in such a way that it also analyzes the sensitivity and optimization of certain metrics according to requirements in each case. In the literature, this appears as a poorly developed research area. Some relevant studies have been identified which have attempted this combination, but have not completely established it.

### Keywords

Performance management measures; simulation; system dynamics; statistics.

## 1 Introduction

Measuring performance is a relevant matter of widespread use among researchers and practitioners. Otto and Kotzab (2003) present a review of suitable metrics to measure the effectiveness of supply chain management from six perspectives: system dynamics, operations research/information technology, logistics, marketing, organization and strategy. Tung et al. (2011) analyze the suitability of the multidimensional control and classification of these measures. Other works, like Burgess (1998), Kleijnen and Smits (2003), Barnabè (2011) and Bianchi (2012), have gone one step forward and designed measures defined by system dynamics, which is the modeling approach used in this paper. Cai et al. (2009), among others, propose a framework that uses a systematic approach to improve the accomplishment of key performance indicators (KPIs) in a supply chain context.

This proposal is about handling an initial set of measures whose record suffices to ensure statistical representativeness, with which it is possible to identify correlative performances. In the final set of measures, those measures that are particularly interesting for managers must be identified, which are classified as such. Strategic measures must be ex-

plained according to the remaining set of measures classified as basic or input measures. A multiple linear regression analysis is used to interpret the relations between input measures and their effect on each strategic measure. To the strategic measures, it is also possible to add a third group of measures, known as derivative measures, which are not obtained through linear regression equations, but as formulae predefined by the decision maker (DM), and can involve both basic and other strategic measures. Lastly, a fourth set of metrics, known as ratios, is established to measure the ratios of change among the strategic measures in terms of time or any input measure. Modeling these groups of measures can be done by system dynamics, and in such a way that a sensitivity analysis of the strategic measures can be done with the changes made in the input measures, or by predictive studies on the optimum values of the input measures to accomplish the levels expected in the strategic measure. To illustrate the proposed methodology, a generic analysis of the operations in a supermarket of retail product sales was done using the ratios among the performance measures that resulted from this operation.

The remainder of the paper is organized as follows: Section 2 presents a literature review where the proposed methodology is compared to alternative approaches. Section 3 develops the proposal of a methodology based on statistics and system dynamics for modeling KPIs. Section 4 illustrates this methodology in a supermarket application. Section 5 presents the conclusions drawn and further research.

## 2 Literature review

Nudurupati et al. (2011) thoroughly reviewed the progress made in measuring performance from the management information system concepts viewpoint and development toward performance measurement systems (PMS). Gunasekaran et al. (2004) did a literature review of the different



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metrics that must be used to measure performance in supply chain settings but does not carry out statistical or simulation analyses. Sousa (2004) reviewed various performance measurement techniques in export companies in detail, and analyzed the empirical research conducted. Despite the variety of the statistical analysis employed, it mentioned no study that has combined system dynamics and simulation. Kleijnen and Smits (2003) provided details of applying simulation and system dynamics in performance measurement, and evidenced how system dynamics, and simulation in general, can be used as a means to evaluate performance.

Alfaro-Saiz et al. (2007) developed a PMS for company chains based on three levels: network enterprise, supply chain and individual. Akkermans and van Oorschot (2004) conducted studies on balanced scorecards using system dynamics to evaluate scenarios with conflicting objectives. Angerhofer and Angelides (2006) considered a performance measurement model for supply chains in collaborative settings by analyzing the relations among the metrics with non linear differential equations and ratios of change and developed their model through system dynamics. This study was the most similar one to that considered herein, but the difference lies in our analysis being based on correlative interactions modeled by multiple regression and not being specific for collaborative supply chain environments. Verdecho et al. (2012) also analyzed performance measurement in collaborative settings based on the analytical network process (ANP), where performance measurement was analyzed from the collaborative supply chains perspective in which inter-company relations had to be taken into account as factors to be measured. Boj et al. (2014) also resorted to the ANP methodology, but they used it in this particular case to measure intangible assets and intellectual capital to relate them with the strategic objectives defined in the performance measurement system, which is normally the balanced scorecard.

Cai et al. (2009) presented a study which analyzed interdependences between performance measurement measures and analyzed the iterative cost of achieving them. Mora-Monge et al. (2006) did a multiple regression analysis of performance measures in advanced manufacturing technology based on the sampling results taken from a survey that evaluated North and Central American companies. Finally, Santos et al. (2002) did a performance measurement study based on system dynamics and a multi-criteria analysis. This study is similar to our proposal in that it applied a multi-criteria approach to evaluate tendencies among measures that could come into conflict with each other, and it was possible to perform an optimization analysis. The difference lies in the fact that these authors did not analyze the relations among the defined measures, based on statistical correlations and linear regression analyses.

Of all the works that we reviewed which came closer to the proposed methodology, we found that by Jusoh et al. (2008),

who conducted a study about measuring performance. This work was based on statistically analyzing the correlation of a set of multiple measures. Although this study is similar to our proposal, the main difference lies in our work using linear regression, based on a record of the measure itself. System dynamics-based simulation was also done with possible sensitivity and optimization analysis approaches. Rodriguez et al. (2009) conducted a study that took measures of a previously established MIS, which were statistically analyzed to identify the relations among them. The methodology consisted in identifying the relations among the measures and then to make forecasts of them. Although this study used a similar methodology to ours, it neither performed a direct linear regression analysis to define relations among measures nor made any type of simulation or establish system dynamics as part of the methodology. Therefore, it did not establish optimum levels or a sensitivity analysis. Finally, Rodriguez et al. (2010) extended the work of Rodriguez et al (2009), based on a PCA to identify the relations between the measures in an already existing PMS. The difference with this study is that it included a scenario analysis, which mainly aimed to make future forecasts of the levels of the measures that could be influenced by previously identified external factors. This methodology approaches our sensitivity analysis proposal, but the difference is that it used a PCA. No measure was seen as an optimization objective, nor was system dynamics used to simulate these measures.

### **3 Methodology for modeling performance management measures**

This methodology attempts to determine the impact that each measure's variations may have on the set of measures by describing their statistical performance and, based on this, establishing a system dynamic analysis that allows organizations to suitably re-adjust decision making in operations management. The first step involved is to delimit the problem or the scope of the simulation. Correct prioritization will enable more rigorous controls to be made of measures that mainly influence overall performance.

With the analysis done of the KPIs, the intention was to establish a system dynamics-based simulation model that interprets the generic performance. Here the specific objectives to pursue with such a model were to: Determine the effects that imply variations in the results of the different measures; that is, statistically describe the relation between several monitored measurements; and provide managers with a rapid swift consultation tool for strategic decision making which allows a sensitivity analysis of the model to be done to set the best levels for the values of the variables that ensure good results in cost terms, and without sacrificing a good level of customer satisfaction.

Of all the so-called strategic measures, those which based

on the DM's experience can be classified as dependent variables; that is, those that give the level of important in control terms which the DM wishes to confer them can be calculated as the result of the interaction with other measures, which will be the independent variables, known as the basic measures in the proposed methodology. Next a multiple linear regression analysis is done (for example, see Draper and Smith (1998) and Cohen et al (2013)) for each one in accordance with the stepwise method in the IBM SPSS Statistics 21 software (Field, 2013). This approach aims to select from the independent variables those that mainly describe the variance of the dependent variable with no redundancy or collinearity among them (Chong and Jun, 2005). After checking the appropriateness and validity of the calculation model for each defined dependent variable, it is also necessary to check a series of necessary premises for the study to be robust in statistical terms. Among the minimum requirements evaluated in this study we find:

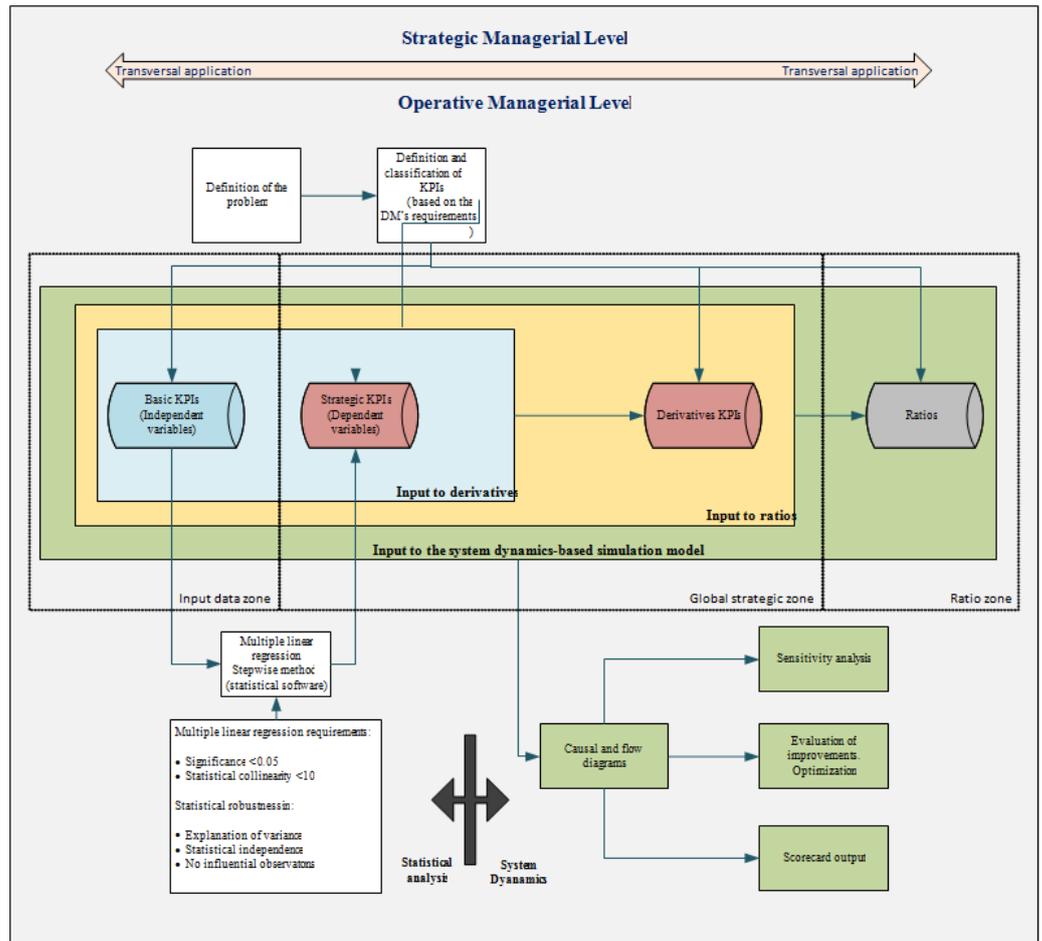
- Explaining the variance of the dependent variable. The R<sup>2</sup> value explains the percentage of variance of the considered measure. As a general criterion, R<sup>2</sup> must come as close to 1 as possible because this scenario will mean that variance will be totally explained. A value of 0.6 or above is considered acceptable.
- Statistical independence of observations. The set of historical data of each measure must show statistical independence. For this purpose, the value by Durbin and Watson (1950) test must be over 0.5 for all the calculation models of the dependent variables.
- Level of significance. It measures the effect of the total set of variables selected for the stepwise method on each dependent variable. This test is done in SPSS with an ANOVA. Records must take a value below 0.05 to be considered acceptable.
- Existence of influential observations. The distance test by Cook (1977) is used and the value of influence is centered (Hazewinkel, 2001). Both test statistics need to take a value below 1.

- Normality in residuals. For the model to be acceptable, these residuals must show a tendency that fits normal tendency. This verification is done by the Kolmogorov-Smirnov test (Hazewinkel, 2001) to fit normal probability distribution. The statistical K-S value must be above 0.05 to accept normality in residuals.
- Homoscedasticity of residuals. It indicates that the error variance of residuals remains constant in measurements and is checked graphically in this proposal. When we graph the predicted dependent variable against its respective residual value in a dispersion graph, the values must be uniformly distributed with no marked tendencies.

Also, we considered the possibility of including variables that can be calculated using the values of the initial measures dubbed as derivative measures. In this way, a derivative measure can be obtained from the calculation made by the formula predefined by the DM. Finally, using a fourth group of metrics, called ratios of change, is considered, whose function consists in relating the ratio of change between the previously defined measures.

The methodology used for the modeling and analyses in this research work was system dynamics (Forrester, 1961; Sterman, 2000). For further information about supply chain system dynamics-based simulation, we refer readers to Campuzano and Mula (2011) and Mula et al. (2013). The sensitivity analysis test aims to explore the performance of the model when submitted to extreme and atypical situations or conditions. The proposed simulation software is Vensim DSS®. For the evaluation of improvements test, the optimization analysis of this simulation software was used. The final part of the developed methodology, preparing a scorecard interface based on the systems dynamics model is proposed. Figure 1 summarizes the methodology proposed in this section.

Figure 1 Methodology for modeling KPIs.



#### 4 The supermarket application

This section provides an example of applying the proposed methodology using the input data of the operations in a supermarket. In order to delimitate the problem, the internal operation is studied because it deals with third parties, e.g. suppliers and transport organizations, which normally adapt quite well to the organization's requirements if we assume that, given the level of demand involved, the supplier is willing to adapt to requirements and conditions. This study centers on the operational plan: a single store. Additionally, some very useful strategical measures exist for top management decision making, which can and must be measured at the operational level to then make an aggregate strategic decision. For instance, the number of staff members that manage a single supermarket is extremely important when it comes to performing aggregation for a supermarket chain, or for forecasting either new supermarkets or a group of supermarkets in the future. For this reason, the quantity of human resources is a purely strategic measure in the proposed methodology. Here everything measured at the operational level can be measured at the strategic level, which is why the name strategic has been given to the high value measures by the DM.

Selecting KPIs implies taking a set of variables and following a priority criterion, and choosing those with a higher interaction between them, and those with the strongest impact on the finally expected store performance. Table 1 provides a list of the measures that are usually controlled in stores of the retail trade. Here we find that the set of measures is divided into the groups that the proposed methodology required. The first group includes the so-called basic measures, which sporadically provide specific information of each activity and/or measure referred to, are static and are used as a basis to calculate other strategic measures. The second group contains the strategic measures defined in this category in accordance with their importance for the DM, along with the strategic and operational decisions that may be made based on them. A derivative measure is also included, whose formula is predefined by the DM. Finally, the ratios to be contemplated in the study are identified. To conduct the present study, we used a set of real store operation data that respond to the basic and strategic measures found in Table 1, measured monthly, and a record with 60 periods. This record is the initial KPI data set.

**Table 1** . List of KPIs. Definition of influence.

| Type        | Code | Measure/indicator                   | Description  | Order | Variable Type |
|-------------|------|-------------------------------------|--|-------|---------------|
| Basic       | IN1  | Average charging rate (items/min)   | Speed of the cashier charging customers              | 2     | Auxiliary     |
|             | IN2  | Average customer count              | Total average of customers served                    | 2     | Auxiliary     |
|             | IN3  | Building area (m2)                  | Total building area                                  | 2     | Auxiliary     |
|             | IN4  | Customer traffic                    | Measuring customers concentration per trade area     | 2     | Auxiliary     |
|             | IN5  | Inventory turnover                  | Monthly rotation of inventory                        | 2     | Auxiliary     |
|             | IN6  | Staff turnover                      | Measure of hiring-firing activity                    | 2     | Auxiliary     |
|             | IN7  | Total items                         | Total items registered in cash registers             | 2     | Auxiliary     |
|             | IN8  | Total sales (€)                     | Total store sales                                    | 2     | Auxiliary     |
|             | IN9  | Trade area (m2)                     | Area where exhibition and sale take place            | 2     | Auxiliary     |
| Strategic   | IN10 | Cash registers (c, r)               | Cash registers installed in the store                | 1     | Auxiliary     |
|             | IN11 | Customer satisfaction               | Customer satisfaction measured with a poll           | 1     | Auxiliary     |
|             | IN12 | Store presentation                  | Store presentation measured with a poll              | 1     | Auxiliary     |
|             | IN13 | Total staff                         | Total people working on the store                    | 1     | Auxiliary     |
|             | IN14 | Total staff hours                   | Total staff paid hours                               | 1     | Auxiliary     |
| Derivatives | IN15 | Cashier staff                       | Total people working specifically at chash registers | 1     | Auxiliary     |
| Ratio       | IN16 | Items per customer (Items/customer) | Average items per customer                           | 2     | Flow          |
|             | IN17 | Items per staff hour (Item/hour)    | Items sold per paid hour of staff                    | 2     | Flow          |
|             | IN18 | Sales per cash register (€/c.r)     | Sales per cash register                              | 2     | Flow          |
|             | IN19 | Sales per staff hour (€/hour)       | Sales per paid working hour                          | 2     | Flow          |
|             | IN20 | Sales per trade area (€/m2)         | Sales per trade area                                 | 2     | Flow          |

Regarding to the statistical analysis of the measures, the strategic measures in Table 1 (from IN10 to IN14) are classified as the dependent variables for the multiple linear regression analysis. In this way, the following dependent variables are defined: Cash registers (c.r.), Store presentation, Total staff, Customer satisfaction and Total staff hours. Table 2 summarizes the results of the multiple linear regression analysis with the stepwise method for all the dependent variables. Column B offers the final coefficients of all the required variables for the equation to calculate the dependent variables. Eq. (1) to (5) show the result of combining the coefficients in Column B. The Significance column in Table 2 provides the significance values of each variable for each dependent variable. Significance must take a value below 0.05 to assume that the considered variable has a significant effect on explaining the variance of the dependent variable. We can see that all the significance values for each considered variable fulfill this condition.

*Cash registers (c.r)*

$$IN10=3.204+0.092 \cdot IN13+0.005 \cdot IN9-5.217 \cdot 10^{-7} \cdot IN8 \quad (1)$$

*Customer satisfaction*

$$IN11=1.757-0.093 \cdot IN10-0.013 \cdot IN1-1.45 \cdot 10^{-7} \cdot IN7+6.23 \cdot 10^{-7} \cdot IN8-1.23 \cdot 10^{-2} \cdot IN2+5.13 \cdot 10^{-2} \cdot IN14 \quad (2)$$

*Store presentation*

$$IN12=3.012-0.016 \cdot IN1-0.002 \cdot IN3-0.011 \cdot IN4+7.78 \cdot 10^{-7} \cdot IN8+7.66 \cdot 10^{-5} \cdot IN14 \quad (3)$$

*Total staff*

$$IN13=15.813-1.47 \cdot 10^{-5} \cdot IN8+3.94 \cdot 10^{-4} \cdot IN2-33.28 \cdot IN6-0.962 \cdot IN5+2.7 \cdot 10^{-6} \cdot IN7 \quad (4)$$

*Total staff hours*

$$IN14=349.41+191.11 \cdot IN13 \quad (5)$$

Finally, the Statistical collinearity-VIF (variance inflation factor) value column presents the inflated variance factor, a statistic that measures collinearity among independent variables which, according to Kutner et al. (2004), must take a value below 10. As we can see, all the independent variables fulfill the condition. Statistical evidence was obtained for the equation's representativeness to calculate each dependent variable, and for lack of collinearities that confers redundant information or can distort the end value. It is noteworthy that eq. (1) to (5) evidence the interaction of the 9 basic measures in Table 1 with all the strategic measures. We can even observe how a dependent variable can play the role of an independent variable in the equation of another variable, provided the collinearity principle is respected. The measures that only appear as independent variables are the data which will have to be supplied as input variables in the system dynamics model in order to obtain the dependent variables values by eq. (1) to (5). In this way, it is possible to run a sensitivity analysis to first evaluate the model's performance when faced with possible brusque changes in any of the basic measures, then to optimize any strategic measure to obtain a given level or value in the objective, and to observe the values required in the basic measures or in the other strategic measures to establish them as performance targets. It will be necessary to follow the same procedure if the measures do not represent a single store, but the performance of a group of them. In this case, the only aspect that might vary are eq. (1) to (5). For this reason, the methodology can be applied cross-sectionally, as seen in Figure 1, at the strategic, managerial and operational levels.

**Table 2** .Results for the multiple regression stepwise method (IBM SPSS Statistics 21).

| Dependent Variable-DV | Independent variables-IV (Calculation model of DV) | B          | Significance (Criteria < 0.05) | Statistical collinearity – VIF value (Criteria < 10) |
|-----------------------|--|------------|--------------------------------|--|
| Cash registers (c.r)  | Constant   | 3.204      | 0                              |  |
|                       | Total staff  | 0.092      | 0                              | 1.77   |
|                       | Trade area   | 0.005      | 3.00E-06                       | 1.02   |
|                       | Total sales  | -5.217E-07 | 8.02E-03                       | 1.76   |
| Customer satisfaction | Constant   | 1.757      | 0                              |  |
|                       | Cash registers (c.r)                               | -0.093     | 7.00E-03                       | 4.24   |
|                       | Average charging rate                              | -0.013     | 3.00E-06                       | 1.64   |
|                       | Total Items  | -1.45E-07  | 3.48E-03                       | 1.83   |
|                       | Total sales  | 6.23E-07   | 1.00E-06                       | 4.43   |
|                       | Average customer count                             | -1.23E-02  | 1.30E-05                       | 3.64   |
|                       | Total staff hours                                  | 5.13E-02   | 9.92E-04                       | 3.15   |
| Store presentation    | Constant   | 3.012      | 1.92E-16                       |  |
|                       | Average charging rate                              | -0.016     | 6.52E-06                       | 1.53   |
|                       | Building area                                      | -0.002     | 5.21E-10                       | 1.43   |
|                       | Customer traffic                                   | -0.011     | 4.26E-10                       | 2.33   |
|                       | Total sales  | 7.78E-07   | 2.48E-08                       | 2.75   |
|                       | Total staff hours                                  | 7.66E-05   | 1.67E-04                       | 2.92   |
| Total staff           | Constant   | 15.813     | 3.17E-18                       |  |
|                       | Total sales  | -1.47E-05  | 1.22E-08                       | 1.84   |
|                       | Average customer count                             | 3.94E-04   | 6.95E-10                       | 1.73   |
|                       | Staff turnover                                     | -33.28     | 5.96E-03                       | 1.86   |
|                       | Inventory turnover                                 | -0.962     | 4.83E-03                       | 1.41   |
|                       | Total Items  | 2.70E-06   | 4.86E-02                       | 1.64   |
| Total staff hours     | Constant   | 349.41     | 2.83E-01                       |  |
|                       | Total staff  | 191.11     | 0.00E+00                       | 1.00   |

Table 3 shows the results of the statistical tests that explain dependent variable variance, the statistical independence of the observations, level of significance, existence of any influential observations, normality in residuals and homoscedasticity in residuals for each calculation model that results

from the multiple linear regression done of the dependent variables. As observed, the results indicate that all the models comply with the statistical assumptions required for the multiple linear regression analysis to be suitable.

Table 3 Statistical test results.

| Test                             | Objective   | Criteria       | Cash registers (c.r) | Customer satisfaction | Store presentation | Total staff | Total staff hours |
|----------------------------------|---|----------------|----------------------|-----------------------|--------------------|-------------|-------------------|
| R2                               | Explanation of the model's variance                                 | Near to 1      | 0.897                | 0.895                 | 0.883              | 0.825       | 0.694             |
| Durbin Watson                    | Statistical independence of the observations                        | > 0.5          | 1.061                | 0.842                 | 1.310              | 1.037       | 1.972             |
| Significance level               | Influence level of the independent variables over the dependent one | < 0.05         | 0.000                | 0.000                 | 0.000              | 0.000       | 0.000             |
| Cook distance                    | Existence of influential observations                               | < 1            | 0.292                | 0.217                 | 0.388              | 0.143       | 0.102             |
| Value of influence centered      | Existence of influential observations                               | < 1            | 0.149                | 0.294                 | 0.282              | 0.248       | 0.051             |
| Z de Kolmogorov-Smirnov          | Normal adjust of the residual values                                | > 0.05         | 0.477                | 0.573                 | 1.000              | 0.971       | 0.869             |
| Dispersion plot of the residuals | Homocedasticity of the residual values                              | Dispersed plot | ok                   | ok                    | ok                 | ok          | ok                |

In this case, a single derivative measure is included (see Table 1), called Cashier staff, Eq. (6), which represents the staff members who operate all the Cash registers (c.r) in a supermarket. In this equation, additional measures IN21, IN22 and IN23 are fixed data that the DM must previously define according to the organization's policy about each one. As a general rule, measures IN21 to IN23 can be added to the group of basic measures since they are set input data and are involved in the derivative measure calculation.

$$Cashier\ staff\ (IN15) = \frac{\left[ \frac{IN7}{60 * IN1} + IN2 * IN21 \right]}{IN22 * IN23} \quad (6)$$

Regarding to the system dynamics-based simulation model, Table 1 offers the classification made of the level, flow and auxiliary variables. Figure 2 depicts the causal diagram of the proposed model. To validate the simulation model, the following tests were considered (Sterman, 2000): test to reproduce known performances, sensitivity analysis and evaluation of improvements. The test to reproduce known performances was done by simulating the 60 periods and by taking the 60 real data records we had available as the input data for Total sales (€), Average customers count and Total items. Table 4 shows the summary of the input data used to validate the model. With these data, the validation process consisted in running the model in Vensim DSS® and extracting the values that were forecast during the 60 monthly

periods for the five variables calculated by linear regression. The difference between the forecast data and the record value defines the general error with which the model operates. The general error average was expected to be around 0%, and this error progressively lowered as we advanced in all 60 forecasts. Note that for the DM, an estimation with an error below 5% is quite good for this measurement type in this specific business kind (supermarkets). Table 5 shows the validation results for all five strategic variables calculated by linear regression. We can see how the general tendency of the errors throughout the consecutive executions during each period diminished and gave values close to 0%. We can also see how the general error average came close to 0%.

Table 6 provides the original values of each variable, along with the minimum and maximum values used for the sensitivity analysis. As we can see, a sufficiently wide range is considered for each measure for the atypical and extreme scenarios to be included.

For the sensitivity analysis five hundred simulations are made. In each simulation, the measures found in Table 6 may vary between the minimum value and the maximum value, with a uniform aleatory probability distribution. The results are measured using the dependent and derivative variables, and the obtained results are shown in Figure 3. We can observe how the remaining data constitute the extreme situa-

tions that the model can adopt if parameters vary considerably. For example, the average charging rate is a measure of the speed at which cashiers pass articles over scanners at cash registers. This value depends on each store and the mean at which staff can charge customers. Hence if the original value shown in Table 4 is 20.51 and an 81% customer satisfaction level can be achieved with this value (Table 5), the optimization analysis can obtain an optimum average charging rate value, which can lead to customer satisfaction levels of over 90%, if desired. We now go on to provide an example of the optimization analysis for the case study . Of the input data shown in Table 4, only Average charging rate, Inventory turnover, Staff turnover, Average service time per customer and % Cashier utilization were considered to allow some range of variation in order to set a goal set by the DM. So these five variables were used for the optimization analysis

(Table 7). The objective was to achieve a maximum value for Customer service and Store presentation (values as close to 1 as possible). These results evidence how minor variations can be made to the model’s input data to accomplish higher Customer satisfaction and Store presentation levels. Although it is true that improvements in optimization did not obtain a very good result for Customer satisfaction, where improvement was only 0.8%, it did improve Store presentation to a better extent (2.1%). Moreover, the scorecard output proposal is depicted in Figure 4, where we can see that all the measures that the model needs to be run are customizably and graphically grouped in the input data zone. Only the measures Average customer count, Total sales and Total items are not directly customizable in this panel because their values must be supplied in a spreadsheet. The optimization analysis results are shown in Tables 8 and 9.

**Table 6** Variation ranges for the sensitivity analysis.

| Code | Measure/indicator                 | Original value | Minimum | Maximum |
|------|-----------------------------------|----------------|---------|---------|
| IN1  | Average charging rate (items/min) | 20.51          | 10      | 30      |
| IN3  | Building area (m2)                | 929            | 0       | 1500    |
| IN5  | Inventory turnover                | 2.41           | 0       | 5       |
| IN6  | Staff turnover                    | 0.034          | 0       | 3       |
| IN9  | Trade area (m2)                   | 540            | 0       | 1000    |
| IN21 | Average service time per customer | 0.0464         | 0       | 0.1     |
| IN23 | %Cashier utilization              | 0.5066         | 0       | 1       |

**Table 7** Optimization analysis of the input ranges.

| Code | Measure/indicator                 | Minumum | Maximum |
|------|-----------------------------------|---------|---------|
| IN1  | Average charging rate (items/min) | 20      | 23      |
| IN5  | Inventory turnover                | 2       | 3       |
| IN6  | Staff turnover                    | 0.02    | 0.05    |
| IN21 | Average service time per customer | 0.017   | 0.083   |
| IN23 | %Cashier utilization              | 0.4     | 1       |

**Table 8** Optimization values for the input data.

| Code | Measure/indicator                 | Initial value | Optimal value | % Var  |
|------|-----------------------------------|---------------|---------------|--------|
| IN1  | Average charging rate (items/min) | 20.51         | 20            | -2.5%  |
| IN5  | Inventory turnover                | 2.41          | 2             | -17.0% |
| IN6  | Staff turnover                    | 0.034         | 0.02          | -41.2% |
| IN21 | Average service time per customer | 0.0464        | 0.051         | 9.9%   |
| IN23 | %Cashier utilization              | 0.5066        | 0.5066        | 0.0%   |

**Table 9** Optimization results for the objectives.

|               | Customer satisfaction | Store presentation |
|---------------|-----------------------|--------------------|
| Initial value | 81.3%                 | 82.8%              |
| Optimal value | 82.1%                 | 84.9%              |
| % dif         | 0.8%                  | 2.1%               |

## 5. Conclusions

The main objective of the methodology proposed herein was to identify the relation between the various performance measures monitored in operations decision support systems. Each performance measure is normally monitored separately without being included in the analysis of their effects on other measures, and they can define overall business performance as a whole set. In this study, both types were analyzed: interactions between measures, and their simulation and optimization to establish objectives and goals. This methodology was not based on traditional performance measurement categories for balanced scorecards, rather we sought a comprehensive cross-sectional analysis of the various metrics considered. This methodology is sufficiently generic for it to be applied to any organization or even supply chain, but is completely flexible for it to be adapted to the specific conditions in each case; i.e. strategic or input data can be varied as required.

In this specific case, by way of example we used the operation of a supermarket of retail product sales. This example evidenced how this methodology is able to take the initial set of measures and transform them into an all-round analysis tool for key variables in decision making, such as customer satisfaction, store presentation, total staff and cash registers. These variables are often crucial in such businesses when making decisions about an already open store, such as re-adjusting staff, investing in its infrastructure, extending or reducing customer movements, exhibiting products, and cus-

tomers charging processes. Eventually, these decisions match the main cost measures in such businesses, and evidently match end consumer satisfaction. This methodology is also useful for evaluating expansion plans, which is another relevant purpose of supermarket supply chains, which can be used for other organization types. Finally, further research is oriented to apply the proposed methodology in other real world cases. A forthcoming work is about the proposal of a simulation model and scorecard output, according to the proposed methodology, to support the analysis stage of new facility implementations and global supplier network developments in the context of the internationalisation of operations decision making.

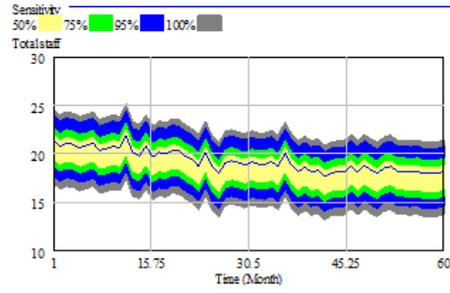
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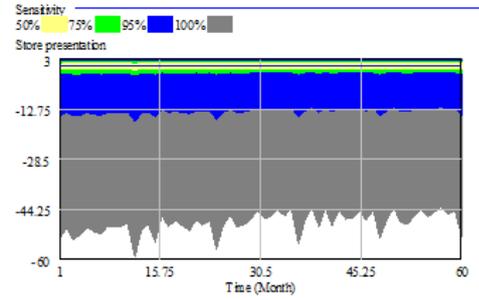
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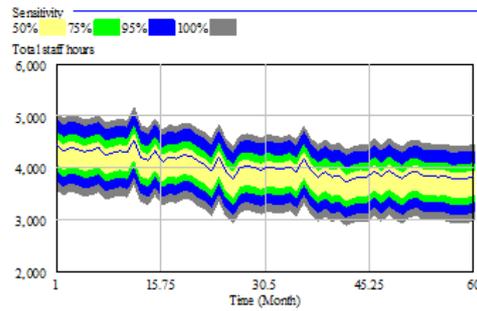
**Figure 3** Causal loop diagram.



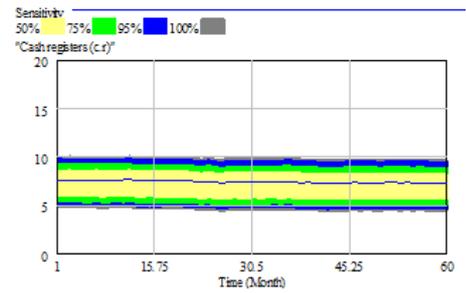
Sensitivity analysis result. Total Staff



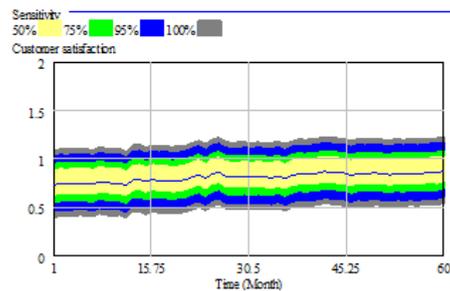
Sensitivity analysis result. Store presentation



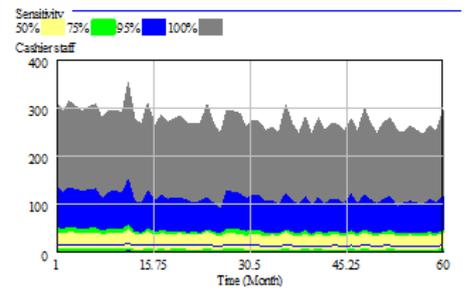
Sensitivity analysis result. Total Staff hours



Sensitivity analysis result. Cash registers

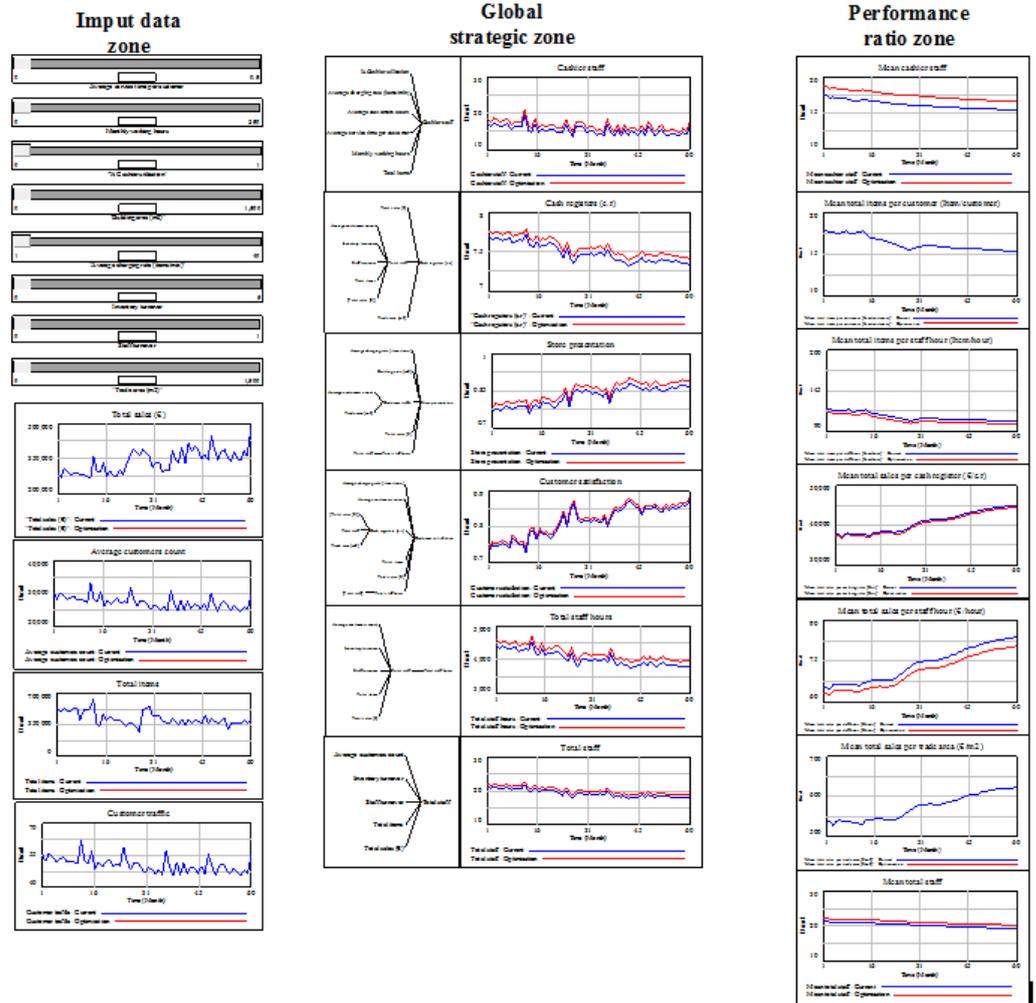


Sensitivity analysis result. Customer satisfaction



Sensitivity analysis result. Cashier staff

Figure 4 Scorecard output



**Table 4** Input data

| Period | Average customers count | Total sales (€) | Total Items | Code | Indicator                         | Validation value |
|--------|-------------------------|-----------------|-------------|------|-----------------------------------|------------------|
| 1      | 29963                   | 290368.6        | 535396      | IN1  | Average charging rate (items/min) | 20.51            |
| 2      | 28191                   | 272769.8        | 487921      | IN3  | Building area (m2)                | 929              |
| 3      | 30295                   | 312431.2        | 531490      | IN5  | Inventory turnover                | 2.41             |
| 4      | 29409                   | 294149.3        | 497898      | IN6  | Staff turnover                    | 0.034            |
| 5      | 28152                   | 282502.9        | 500128      | IN9  | Trade area (m2)                   | 540              |
| 6      | 28812                   | 292993.4        | 535712      | IN21 | Average service time per customer | 0.0464           |
| 7      | 29347                   | 291312.7        | 538969      | IN22 | Monthly working time              | 207              |
| 8      | 27969                   | 279294.6        | 400192      | IN23 | %Cashier utilization              | 0.5066           |
| 9      | 27997                   | 285291.2        | 511976      |      |                                   |                  |
| 10     | 28018                   | 274105.6        | 519854      |      |                                   |                  |
| 11     | 27399                   | 270529.2        | 528086      |      |                                   |                  |
| 12     | 33289                   | 359012.5        | 626895      |      |                                   |                  |
| 13     | 28472                   | 299810.4        | 346572      |      |                                   |                  |
| 14     | 27543                   | 292532.3        | 338579      |      |                                   |                  |
| 15     | 30569                   | 332535.1        | 472351      |      |                                   |                  |
| 16     | 26150                   | 273879.7        | 393661      |      |                                   |                  |
| 17     | 27991                   | 301016.6        | 437954      |      |                                   |                  |
| 18     | 26911                   | 277413.5        | 406026      |      |                                   |                  |
| 19     | 27847                   | 275676.1        | 401306      |      |                                   |                  |
| 20     | 28726                   | 303663.1        | 392907      |      |                                   |                  |
| 21     | 26823                   | 286389.7        | 376539      |      |                                   |                  |
| 22     | 27639                   | 325923.8        | 341386      |      |                                   |                  |
| 23     | 26980                   | 359426.7        | 369730      |      |                                   |                  |
| 24     | 31868                   | 389542.1        | 360635      |      |                                   |                  |
| 25     | 27967                   | 379126.3        | 331724      |      |                                   |                  |
| 26     | 26043                   | 364436.4        | 267830      |      |                                   |                  |
| 27     | 28013                   | 388867.8        | 517942      |      |                                   |                  |
| 28     | 27754                   | 371872.8        | 529835      |      |                                   |                  |
| 29     | 26789                   | 363265.7        | 551395      |      |                                   |                  |
| 30     | 25118                   | 314516.0        | 449960      |      |                                   |                  |
| 31     | 26577                   | 334180.9        | 455216      |      |                                   |                  |
| 32     | 26235                   | 337326.5        | 455084      |      |                                   |                  |
| 33     | 24971                   | 294074.9        | 393103      |      |                                   |                  |
| 34     | 26067                   | 302759.5        | 378152      |      |                                   |                  |
| 35     | 24807                   | 300402.8        | 353115      |      |                                   |                  |
| 36     | 30899                   | 384075.6        | 424138      |      |                                   |                  |
| 37     | 26846                   | 347810.9        | 384012      |      |                                   |                  |
| 38     | 24630                   | 332472.9        | 355971      |      |                                   |                  |
| 39     | 27989                   | 398220.4        | 415942      |      |                                   |                  |
| 40     | 24773                   | 333154.7        | 345918      |      |                                   |                  |
| 41     | 27820                   | 416238.2        | 415348      |      |                                   |                  |
| 42     | 25219                   | 380902.4        | 363285      |      |                                   |                  |
| 43     | 26778                   | 407135.2        | 403976      |      |                                   |                  |
| 44     | 26447                   | 386273.1        | 390972      |      |                                   |                  |
| 45     | 25237                   | 348914.9        | 361430      |      |                                   |                  |
| 46     | 26873                   | 370260.0        | 461150      |      |                                   |                  |
| 47     | 25105                   | 346713.8        | 359727      |      |                                   |                  |
| 48     | 30048                   | 445847.5        | 426542      |      |                                   |                  |
| 49     | 26876                   | 385752.6        | 389852      |      |                                   |                  |
| 50     | 24686                   | 347892.6        | 360021      |      |                                   |                  |
| 51     | 27097                   | 377510.2        | 394819      |      |                                   |                  |
| 52     | 27700                   | 389190.2        | 418179      |      |                                   |                  |
| 53     | 26174                   | 358093.1        | 302654      |      |                                   |                  |
| 54     | 24987                   | 338220.1        | 369830      |      |                                   |                  |
| 55     | 26361                   | 380066.5        | 374306      |      |                                   |                  |
| 56     | 25442                   | 349026.4        | 363065      |      |                                   |                  |
| 57     | 24593                   | 344488.4        | 359228      |      |                                   |                  |
| 58     | 25898                   | 384774.2        | 407147      |      |                                   |                  |
| 59     | 25296                   | 361835.5        | 366164      |      |                                   |                  |
| 60     | 29796                   | 477205.7        | 410579      |      |                                   |                  |

**Table 5** The model validation results

| Period  | Customer satisfaction |       |         | Store presentation |       |         | Cash registers (c.r) |       |         | Total staff |       |         | Total staff hours |         |         |
|---------|-----------------------|-------|---------|--------------------|-------|---------|----------------------|-------|---------|-------------|-------|---------|-------------------|---------|---------|
|         | Real                  | Model | % error | Real               | Model | % error | Real                 | Model | % error | Real        | Model | % error | Real              | Model   | % error |
| 1.0     | 0.73                  | 0.73  | -0.1%   | 0.73               | 0.8   | 4.5%    | 7.75                 | 7.7   | -0.6%   | 21.56       | 21.4  | -0.9%   | 4692.0            | 4431.9  | -5.5%   |
| 2.0     | 0.75                  | 0.75  | 0.0%    | 0.74               | 0.8   | 5.0%    | 7.71                 | 7.7   | -0.7%   | 21.60       | 20.8  | -3.7%   | 4376.8            | 4323.2  | -1.2%   |
| 3.0     | 0.75                  | 0.74  | -0.6%   | 0.75               | 0.8   | 3.4%    | 7.69                 | 7.7   | -0.2%   | 21.21       | 21.2  | -0.2%   | 4398.4            | 4393.1  | -0.1%   |
| 4.0     | 0.74                  | 0.75  | 1.0%    | 0.75               | 0.8   | 3.2%    | 7.69                 | 7.7   | -0.3%   | 21.22       | 21.0  | -1.1%   | 4692.1            | 4360.2  | -7.1%   |
| 5.0     | 0.75                  | 0.75  | 0.8%    | 0.73               | 0.8   | 8.2%    | 7.69                 | 7.6   | -0.6%   | 21.34       | 20.7  | -3.2%   | 4470.5            | 4299.3  | -3.8%   |
| 6.0     | 0.73                  | 0.75  | 2.7%    | 0.73               | 0.8   | 6.7%    | 7.69                 | 7.7   | -0.4%   | 21.33       | 20.9  | -2.2%   | 4335.3            | 4338.1  | 0.1%    |
| 7.0     | 0.72                  | 0.74  | 2.6%    | 0.72               | 0.8   | 7.0%    | 7.68                 | 7.7   | 0.0%    | 21.33       | 21.1  | -1.0%   | 4409.7            | 4384.7  | -0.6%   |
| 8.0     | 0.72                  | 0.77  | 7.0%    | 0.72               | 0.8   | 8.7%    | 7.60                 | 7.6   | 0.2%    | 21.14       | 20.4  | -3.6%   | 4549.3            | 4242.9  | -6.7%   |
| 9.0     | 0.72                  | 0.76  | 5.4%    | 0.72               | 0.8   | 9.1%    | 7.60                 | 7.6   | 0.4%    | 19.79       | 20.6  | 4.1%    | 4174.5            | 4286.0  | 2.7%    |
| 10.0    | 0.72                  | 0.75  | 3.7%    | 0.72               | 0.8   | 9.1%    | 7.60                 | 7.7   | 0.7%    | 20.85       | 20.8  | -0.3%   | 4171.2            | 4323.0  | 3.6%    |
| 11.0    | 0.72                  | 0.75  | 4.9%    | 0.72               | 0.8   | 10.1%   | 7.85                 | 7.6   | -2.7%   | 21.58       | 20.6  | -4.4%   | 4209.7            | 4290.6  | 1.9%    |
| 12.0    | 0.72                  | 0.73  | 0.5%    | 0.72               | 0.8   | 4.3%    | 7.64                 | 7.7   | 1.0%    | 21.08       | 21.9  | 4.0%    | 4257.8            | 4537.4  | 6.6%    |
| 13.0    | 0.73                  | 0.78  | 6.7%    | 0.73               | 0.8   | 7.4%    | 7.64                 | 7.6   | -0.8%   | 20.02       | 20.1  | 0.5%    | 4122.9            | 4195.6  | 1.8%    |
| 14.0    | 0.75                  | 0.79  | 5.6%    | 0.74               | 0.8   | 7.0%    | 7.64                 | 7.6   | -1.1%   | 20.21       | 19.8  | -1.8%   | 3925.1            | 4141.9  | 5.5%    |
| 15.0    | 0.75                  | 0.76  | 1.8%    | 0.75               | 0.8   | 4.0%    | 7.63                 | 7.6   | -0.1%   | 20.03       | 20.8  | 3.9%    | 4354.9            | 4326.9  | -0.6%   |
| 16.0    | 0.74                  | 0.79  | 6.4%    | 0.75               | 0.8   | 7.8%    | 7.63                 | 7.6   | -1.0%   | 19.79       | 19.7  | -0.4%   | 4292.1            | 4117.7  | -4.1%   |
| 17.0    | 0.75                  | 0.78  | 3.8%    | 0.73               | 0.8   | 9.6%    | 7.63                 | 7.6   | -0.6%   | 19.61       | 20.2  | 2.9%    | 4219.0            | 4203.2  | -0.4%   |
| 18.0    | 0.76                  | 0.78  | 2.3%    | 0.74               | 0.8   | 7.3%    | 7.63                 | 7.6   | -0.6%   | 19.57       | 20.0  | 2.2%    | 4048.4            | 4171.5  | 3.0%    |
| 19.0    | 0.77                  | 0.77  | 0.3%    | 0.80               | 0.8   | -2.0%   | 7.63                 | 7.6   | -0.1%   | 19.93       | 20.4  | 2.3%    | 4153.1            | 4244.4  | 2.2%    |
| 20.0    | 0.76                  | 0.78  | 1.7%    | 0.79               | 0.8   | -0.1%   | 7.62                 | 7.6   | -0.3%   | 19.87       | 20.3  | 2.1%    | 4430.7            | 4227.9  | -4.6%   |
| 21.0    | 0.78                  | 0.79  | 1.7%    | 0.78               | 0.8   | 2.6%    | 7.61                 | 7.6   | -0.7%   | 20.00       | 19.8  | -1.2%   | 4143.5            | 4124.5  | -0.5%   |
| 22.0    | 0.78                  | 0.81  | 3.7%    | 0.78               | 0.8   | 3.9%    | 7.58                 | 7.5   | -1.0%   | 20.10       | 19.4  | -3.5%   | 4115.2            | 4057.1  | -1.4%   |
| 23.0    | 0.79                  | 0.84  | 5.8%    | 0.80               | 0.8   | 5.6%    | 7.58                 | 7.4   | -2.1%   | 20.26       | 18.7  | -7.6%   | 4067.0            | 3928.3  | -3.4%   |
| 24.0    | 0.79                  | 0.80  | 1.5%    | 0.68               | 0.8   | 15.9%   | 7.53                 | 7.5   | 0.1%    | 19.99       | 20.2  | 1.0%    | 3967.0            | 4207.4  | 6.1%    |
| 25.0    | 0.86                  | 0.84  | -2.2%   | 0.91               | 0.84  | -7.7%   | 7.53                 | 7.4   | -1.6%   | 19.81       | 18.7  | -5.5%   | 4081.8            | 3927.9  | -3.8%   |
| 26.0    | 0.86                  | 0.87  | 0.3%    | 0.90               | 0.86  | -5.3%   | 7.53                 | 7.4   | -2.4%   | 19.61       | 18.0  | -8.2%   | 3764.0            | 3791.1  | 0.7%    |
| 27.0    | 0.85                  | 0.82  | -3.1%   | 0.90               | 0.85  | -5.6%   | 7.43                 | 7.4   | 0.2%    | 19.83       | 19.1  | -3.7%   | 4165.7            | 4000.3  | -4.0%   |
| 28.0    | 0.84                  | 0.81  | -3.4%   | 0.90               | 0.84  | -6.0%   | 7.43                 | 7.5   | 0.5%    | 19.55       | 19.3  | -1.3%   | 4371.1            | 4034.5  | -7.7%   |
| 29.0    | 0.85                  | 0.82  | -3.6%   | 0.89               | 0.85  | -3.8%   | 7.25                 | 7.5   | 2.8%    | 19.26       | 19.1  | -0.9%   | 3998.8            | 3997.1  | 0.0%    |
| 30.0    | 0.85                  | 0.82  | -3.7%   | 0.88               | 0.85  | -4.0%   | 7.46                 | 7.5   | -0.1%   | 19.26       | 18.9  | -2.1%   | 3840.8            | 3955.3  | 3.0%    |
| 31.0    | 0.85                  | 0.81  | -3.8%   | 0.89               | 0.84  | -5.8%   | 7.46                 | 7.5   | 0.1%    | 19.31       | 19.2  | -0.7%   | 4033.4            | 4012.8  | -0.5%   |
| 32.0    | 0.84                  | 0.82  | -2.4%   | 0.90               | 0.84  | -6.1%   | 7.44                 | 7.5   | 0.2%    | 19.94       | 19.0  | -4.8%   | 4385.2            | 3978.2  | -9.3%   |
| 33.0    | 0.85                  | 0.81  | -3.7%   | 0.90               | 0.84  | -7.1%   | 7.44                 | 7.5   | 0.5%    | 19.36       | 19.0  | -2.1%   | 4177.0            | 3972.1  | -4.9%   |
| 34.0    | 0.86                  | 0.81  | -5.4%   | 0.90               | 0.82  | -8.7%   | 7.44                 | 7.5   | 0.7%    | 19.35       | 19.2  | -0.7%   | 4358.5            | 4022.6  | -7.7%   |
| 35.0    | 0.87                  | 0.83  | -4.5%   | 0.90               | 0.84  | -6.9%   | 7.44                 | 7.4   | 0.1%    | 19.13       | 18.7  | -2.3%   | 3847.0            | 3921.4  | 1.9%    |
| 36.0    | 0.87                  | 0.80  | -7.7%   | 0.91               | 0.80  | -11.9%  | 7.44                 | 7.5   | 1.2%    | 19.24       | 20.1  | 4.3%    | 4216.2            | 4182.5  | -0.8%   |
| 37.0    | 0.87                  | 0.83  | -4.3%   | 0.90               | 0.84  | -7.3%   | 7.44                 | 7.4   | 0.0%    | 18.95       | 18.9  | -0.4%   | 4082.7            | 3958.1  | -3.0%   |
| 38.0    | 0.87                  | 0.85  | -2.2%   | 0.90               | 0.86  | -4.3%   | 7.44                 | 7.4   | -0.8%   | 18.59       | 18.2  | -2.3%   | 3536.3            | 3819.7  | 8.0%    |
| 39.0    | 0.86                  | 0.84  | -2.1%   | 0.90               | 0.85  | -5.5%   | 7.46                 | 7.4   | -0.9%   | 18.47       | 18.7  | 1.2%    | 3852.4            | 3919.6  | 1.7%    |
| 40.0    | 0.86                  | 0.85  | -1.1%   | 0.86               | 0.86  | -0.3%   | 7.46                 | 7.4   | -1.1%   | 18.27       | 18.2  | -0.5%   | 4016.4            | 3823.4  | -4.8%   |
| 41.0    | 0.86                  | 0.86  | 0.1%    | 0.90               | 0.86  | -4.1%   | 7.46                 | 7.4   | -1.4%   | 18.36       | 18.3  | -0.1%   | 3863.6            | 3856.1  | -0.2%   |
| 42.0    | 0.87                  | 0.87  | 0.2%    | 0.89               | 0.88  | -1.2%   | 7.45                 | 7.3   | -1.7%   | 18.35       | 17.7  | -3.5%   | 3654.6            | 3732.3  | 2.1%    |
| 43.0    | 0.88                  | 0.87  | -1.9%   | 0.89               | 0.87  | -1.7%   | 7.43                 | 7.3   | -1.3%   | 18.27       | 18.0  | -1.3%   | 3830.3            | 3797.2  | -0.9%   |
| 44.0    | 0.89                  | 0.86  | -3.1%   | 0.88               | 0.87  | -1.1%   | 7.43                 | 7.4   | -0.9%   | 18.31       | 18.2  | -0.7%   | 4045.0            | 3824.0  | -5.5%   |
| 45.0    | 0.88                  | 0.85  | -2.7%   | 0.87               | 0.86  | -1.4%   | 7.43                 | 7.4   | -0.7%   | 18.69       | 18.2  | -2.8%   | 3764.3            | 3822.2  | 1.5%    |
| 46.0    | 0.87                  | 0.83  | -4.1%   | 0.87               | 0.85  | -1.6%   | 7.38                 | 7.4   | 0.6%    | 17.96       | 18.8  | 4.5%    | 3828.6            | 3937.2  | 2.8%    |
| 47.0    | 0.87                  | 0.85  | -2.2%   | 0.87               | 0.86  | -0.7%   | 7.32                 | 7.4   | 0.7%    | 18.03       | 18.1  | 0.7%    | 3784.8            | 3817.6  | 0.9%    |
| 48.0    | 0.87                  | 0.85  | -2.5%   | 0.86               | 0.85  | -1.8%   | 7.27                 | 7.4   | 1.6%    | 18.18       | 18.8  | 3.5%    | 3902.0            | 3946.7  | 1.1%    |
| 49.0    | 0.87                  | 0.85  | -2.2%   | 0.86               | 0.86  | 0.3%    | 7.27                 | 7.4   | 1.4%    | 17.96       | 18.4  | 2.2%    | 3757.4            | 3857.2  | 2.7%    |
| 50.0    | 0.86                  | 0.86  | -0.3%   | 0.85               | 0.87  | 1.9%    | 7.27                 | 7.4   | 1.2%    | 17.92       | 18.0  | 0.3%    | 3369.2            | 3782.9  | 12.3%   |
| 51.0    | 0.86                  | 0.84  | -1.3%   | 0.87               | 0.85  | -2.1%   | 7.27                 | 7.4   | 1.8%    | 17.84       | 18.6  | 4.1%    | 3824.3            | 3899.5  | 2.0%    |
| 52.0    | 0.84                  | 0.84  | -0.2%   | 0.88               | 0.85  | -3.4%   | 7.27                 | 7.4   | 1.9%    | 17.66       | 18.7  | 5.9%    | 3800.1            | 3924.2  | 3.3%    |
| 53.0    | 0.86                  | 0.86  | -0.5%   | 0.88               | 0.85  | -3.0%   | 7.27                 | 7.4   | 1.5%    | 17.55       | 18.2  | 4.0%    | 3850.5            | 3836.7  | -0.4%   |
| 54.0    | 0.86                  | 0.85  | -1.5%   | 0.88               | 0.86  | -2.0%   | 7.27                 | 7.4   | 1.7%    | 17.53       | 18.3  | 4.1%    | 3691.2            | 3837.7  | 4.0%    |
| 55.0    | 0.85                  | 0.86  | 1.1%    | 0.88               | 0.86  | -1.7%   | 7.27                 | 7.4   | 1.3%    | 17.28       | 18.2  | 5.3%    | 3495.3            | 3826.3  | 9.5%    |
| 56.0    | 0.84                  | 0.85  | 0.6%    | 0.87               | 0.86  | -1.6%   | 7.27                 | 7.4   | 1.6%    | 17.33       | 18.3  | 5.3%    | 3978.9            | 3838.2  | -3.5%   |
| 57.0    | 0.83                  | 0.86  | 3.2%    | 0.87               | 0.87  | -0.1%   | 7.27                 | 7.4   | 1.3%    | 17.01       | 18.0  | 5.7%    | 3524.1            | 3785.0  | 7.4%    |
| 58.0    | 0.83                  | 0.86  | 3.7%    | 0.88               | 0.87  | -0.1%   | 7.27                 | 7.3   | 1.0%    | 17.02       | 18.0  | 5.9%    | 3527.2            | 3795.2  | 7.6%    |
| 59.0    | 0.83                  | 0.86  | 3.2%    | 0.87               | 0.87  | 0.1%    | 7.27                 | 7.4   | 1.2%    | 16.96       | 18.0  | 6.2%    | 3487.6            | 3792.9  | 8.8%    |
| 60.0    | 0.83                  | 0.88  | 5.1%    | 0.87               | 0.87  | -0.3%   | 7.27                 | 7.3   | 0.6%    | 17.13       | 18.2  | 6.3%    | 3736.6            | 3831.7  | 2.5%    |
| Max     | 0.89                  | 0.88  | 7.0%    | 0.91               | 0.88  | 15.9%   | 7.85                 | 7.71  | 2.8%    | 21.60       | 21.91 | 6.3%    | 4692.08           | 4537.44 | 12.3%   |
| Min     | 0.72                  | 0.73  | -7.7%   | 0.68               | 0.76  | -11.9%  | 7.25                 | 7.31  | -2.7%   | 16.96       | 17.70 | -8.2%   | 3369.24           | 3732.27 | -9.3%   |
| Average | 0.81                  | 0.81  | 0.2%    | 0.83               | 0.83  | 0.4%    | 7.48                 | 7.48  | 0.0%    | 19.28       | 19.29 | 0.2%    | 4033.65           | 4036.91 | 0.3%    |