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Additional Information

2 **Improved mixture quality by advanced dual-nozzle, included-**
3 **angle split injection in HSDI engine: Exergetic exploration**

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9 **Abstract**

10 A Ford 1.8 l high speed diesel engine (HSDI) is utilized for a thorough investigation on
11 split dual injection with two included-angle nozzles. The system is equipped with variable-
12 geometry turbocharging (VGT) and high-pressure common-rail (HPCR) technologies
13 which lets multi-injections per cycle. The share of fuel between pulses is divided in three
14 portions of 70-30, 80-20, and 90-10 with included angles of 10, 20, and 30 while the dwell
15 time between pulses are 5CA, 10CA, 15CA, and 20CA. The results demonstrate that the
16 optimum option is 70 (5) 30-30deg with the best homogeneity of mixture ($UI = 0.9742$)
17 and peak temperature ($T_{max} = 2011.58$ K) that yield maximum thermo-mechanical exergy
18 amounting to 439 J. In addition, the highest amount of accumulative irreversibility happens
19 for 90 (10) 10-20deg. It is found that there is a relation between mixture uniformity and
20 accumulative work/heat exergy, whereas high rate of pressure rise (RPR) contribute to
21 irreversibility rate or exergy destruction in diesel engine, i.e. $RPR (80-20) = 904.67$
22 kPa/deg. More, the results are in agreement with literature reporting that higher in-cylinder
23 temperature ($T_{max} (70 (5) 30-30deg) = 2011.58$ K)) can possibly decrease the accumulative
24 irreversibility (147.9 J).

25 **Keywords:** Diverged included spray; Exergy; Irreversibility; Split injection; Uniformity
26 index

27 **1. Introduction**

28 Nowadays human life has closely been entangled with machineries and automotive
29 applications that their emission and consumption is turned into a challenging issue
30 worldwide. Any progress in the field of internal combustion chamber with responsive
31 approach towards reduction of emission and fuel consumption is welcomed in R&D and
32 research centers as long as its performance is elevated. Diesel engines are characterized
33 with rich engine-out NO_x emission that is proved having hazardous effects on human
34 health [1,2]. On the other hand, these types of engine, although having the highest
35 efficiency, waste considerable fuel's chemical energy and fail to capture the majority of
36 the provided energy. One of the cost-effective methods is to use advanced injection system
37 in the form of split injection, multiple injection, and pilot injection, thereby with this
38 flexibility fuel is used at needed time [3-5].

39 It is believed that split injection can enhance the mixture quality thanks to electronically
40 controlled common rail system that computer programs can manage the injection duty
41 precisely and painstakingly [6,7]. It is reported that split injection is beneficial in reducing
42 NO_x content, fuel consumption, and engine noise [8]. Mobasheri [9] performed an
43 investigation of narrow fuel spray and split injection on overall performance of a diesel
44 engine. The main finding of the research showed that start of pilot (SOP) advancement
45 makes more fuel accessible for mixing that explains more heat release rate. As a result of
46 SOP advancing injection, locally fuel-lean mixture is prepared and the NO_x and soot
47 exceed the standard level. How et al. [10] in a relevant study conducted a study on injection

48 timing and split injection on emission and combustion of diesel engine, therein the blend
49 of biodiesel-diesel is considered. The application of B50 fuel in conjunction with multiple
50 injection culminates in lowering NO_x and smoke. Multiple injection was also addressed in
51 recent researches such as the one by Park et al. [11] and also in Ref. [12]. It is pointed out
52 that the start of combustion is affected by multiple injection while the combustion pressure
53 of this type of injection is higher; meanwhile the latter study with focus on multiple
54 injection revealed that it may lean out the mixture, which can considerably decrease soot
55 concentration.

56 The exergy analysis is of concern since it is an index of the quality of energy or availability
57 of energy that can be converted to useful work. In a combustion chamber of the engine,
58 there are three sources of exergy destruction, the heat or energy wasted by the gases exiting
59 from exhaust valve, wall heat flux, and spray fuel droplets that impinges the wall and miss
60 being combusted. Another aspect of this study revolves around exergetic examination of
61 the engine as different divergent split injection implemented. In recent years, couple of
62 works have been performed with incorporation of the second law of thermodynamics in
63 diesel engines [13-16], homogenous charge compression ignition (HCCI) engines [17],
64 spark ignition (SI) engines [18, 19], and some of them are devoted to exergetic analyses of
65 blended fuels in engines [20]. In the field of exergy evaluation, Kul and Kahraman [21]
66 explored a diesel engine fueled with biodiesel-diesel-5% ethanol in terms of energy and
67 exergy. As they concluded, D92B3E5 gave the highest exergy efficiency with 29.38%, and
68 D100 has the better thermal and exergetic efficiency than that of blended fuels.
69 Mahabadipour et al. [22] studied the exergy of exhaust flow in a diesel engine in an attempt
70 to recover the waste energy. The exergetic analyze has taken place in crank-angle resolved

71 base and it was indicated that the specific thermal exergy prevails at the primary period of
72 the exhaust process.

73 The link between the mixture quality and exergy (or irreversibility) is a theme that little
74 has been performed noticing the literature review. Consequently, unravelling the extricate
75 mechanism of combustion-power generation interaction can be of paramount importance
76 since this allows eradication of factors that lead to low efficiency of engines. This study
77 tries to deal with an advanced split injection with two nozzles targeting with diverged
78 included angles to combustion chamber. First, the uniformity of mixture, burned fuel mass
79 fraction, rate of pressure rise is calculated, then the exergy terms are applied to energetic
80 data. This way, an optimum case and the factors leading to gain the most useful work out
81 of the given fixed amount of fuel can be recognized. The final goal is to prevent the heat
82 or energy dissipation from the cylinder and convert the chemical potential of fuel to as
83 much power as possible.

84

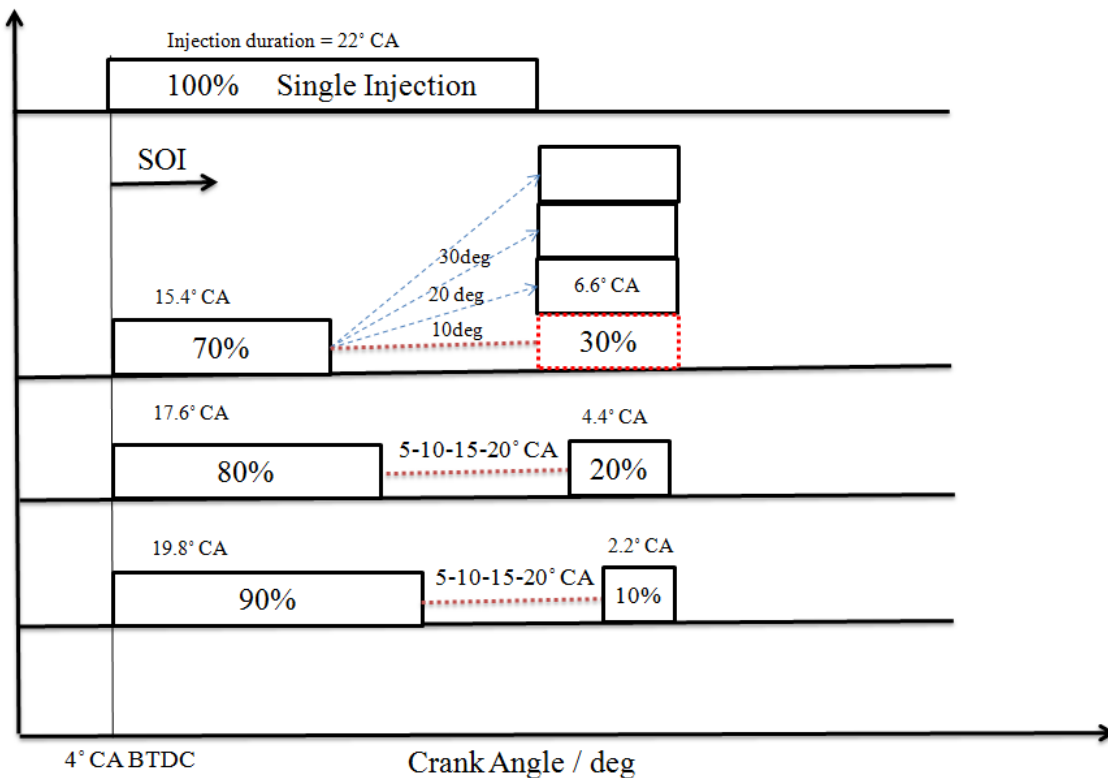
85 **2. Thermodynamic evaluation**

86 *2.1. Injection description*

87 The engine setup used for the numerical simulation [23] is equipped with VGT technology
88 that allows high-pressure, precise, and flexible multiple injection at high engine speed. The
89 injectors issue the fuel asynchronously with two pulses to the bowl and crevice
90 consecutively. The amount of injected fuel mass is constant and considered fixed for the
91 entire test for split and single injection in experimental work that is 37.43 mg/cycle at 2500
92 rpm. The lower nozzle angle is fixed at 140° with respect to $-x$ axis and the upper nozzle
93 for different cases make diffraction angle of the lower nozzle with 10° , 20° , 30° so making

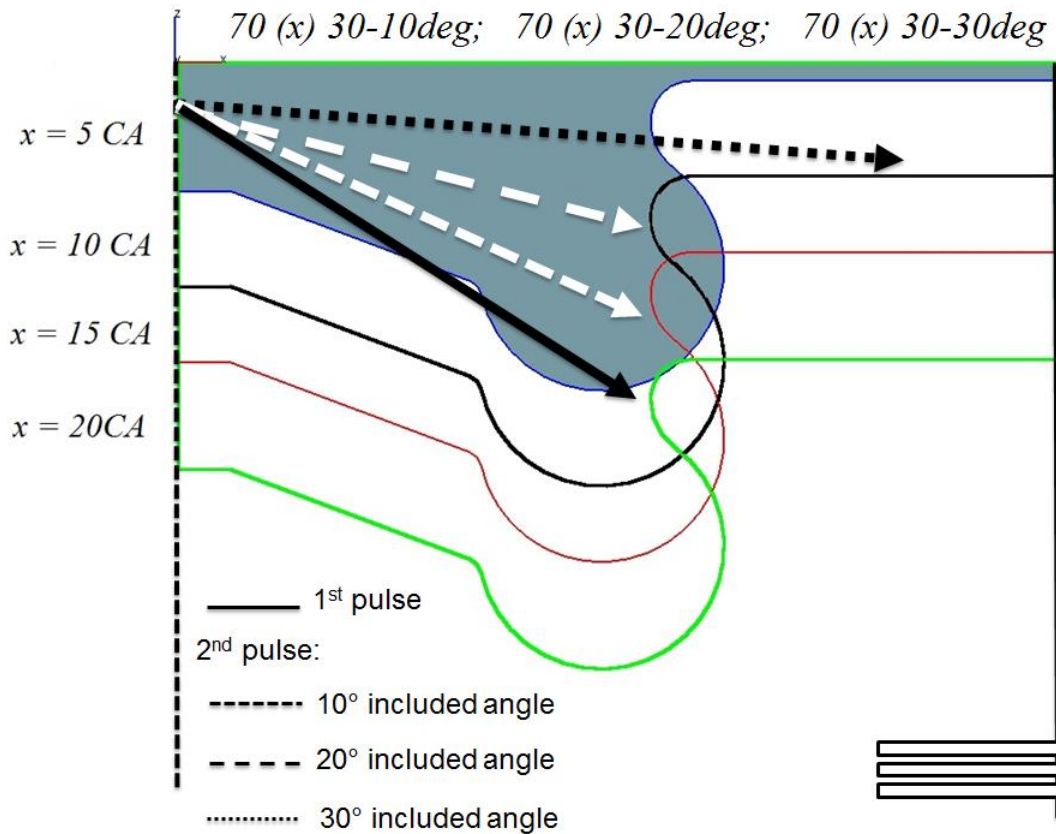
94 150°, 160°, and 170° with -x direction. The fuel mass distribution and the time of injection
 95 is divided on 70%-30%, 80%-20%, and 90%-10% ratios and the span between two pulses
 96 (referred to as dwell time and signified by x in parenthesis) are in four levels of 5 CA, 10
 97 CA, 15 CA, and 20 CA. The first pulse is injected through the lower-angled nozzle at 4
 98 °CA BTDC carrying a share of fuel mass that is pursued by an interval before the second
 99 pulse begins with upper-angled nozzle. For better illustration, a schematic representation
 100 of diverged split injection is shown in Fig. 1. Different cylinder head position with regard
 101 to dwell time as well as the injection orientation of dual spray for typical 70 (x) 30 is
 102 displayed in Fig. 1b. Overall, the study is composed of 36 different cases to cover all
 103 injection modes. The portioning of fuel mass between pulses for diverse injection strategies
 104 in each cycle is mentioned in Table 1.

105 (a)



106

107 (b)



108

109 Fig. 1 (a) schematic representation of split injection, (b) typical 70 (x) 30 split injection

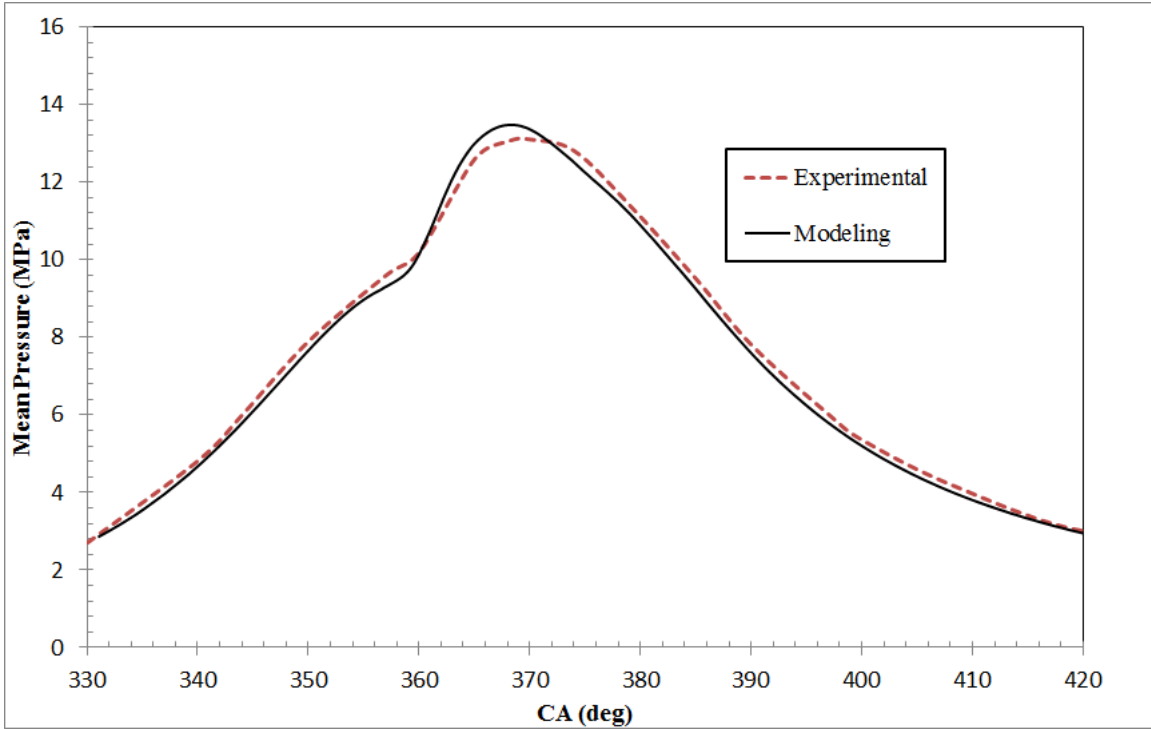
110 2.2. Energy modeling with CFD methodology

111 The finite volume (FV) method is used to solve the conservative set of Navier - Stokes
112 equations in the discretized format of the flow domain. The SIMPLE (semi-implicit method
113 for pressure-linked equations) algorithm is a reasonable choice to deal with the highly
114 unsteady and turbulent flow of combustion phenomena [24]. For spray injection, the DDM
115 (discrete droplet model) method [25] accounts for the evolution of spray in the chamber,
116 therein similar droplets are taken together in parcels. The KH-RT breakup formulates the
117 process of secondary atomization of droplets in spray simulation [26]. The $k-\zeta-f$ model is a
118 successful turbulence closure particularly to meshes with the near wall non-dimensional

119 distance (y^+) [27]. The step-size running procedure portraits the computational cost spent
120 on calculations and the initial stage of calculation is conducted with $\Delta\alpha = 0.1$ CA
121 subdivision. Accordingly for the compression and combustion phases the divisions are $\Delta\alpha$
122 = 1 CA and $\Delta\alpha = 0.2$ CA. The under-relaxation factors are very important for the stability
123 and convergence of numerical solution. These factors are set 0.6, 0.5, and 0.95 for
124 momentum, pressure, and energy. The heat-up and evaporation required for the ignition
125 and combustion is performed via the Dukowicz model with tuning constants of $E1 = E2 =$
126 1 [28]. The turbulent dispersion model and particle interaction model are activated for an
127 accurate flow prediction within the combustion chamber. This is done by a stochastic
128 dispersion model [29]. The detailed multi-zone ECFM-3Z combustion model is selected
129 for the burning of the charge and chemical reaction responsible for production of species
130 [30]. The initial and boundary conditions for an efficient modeling are tabulated in Table
131 2. The engine specifications are listed in Table 3.

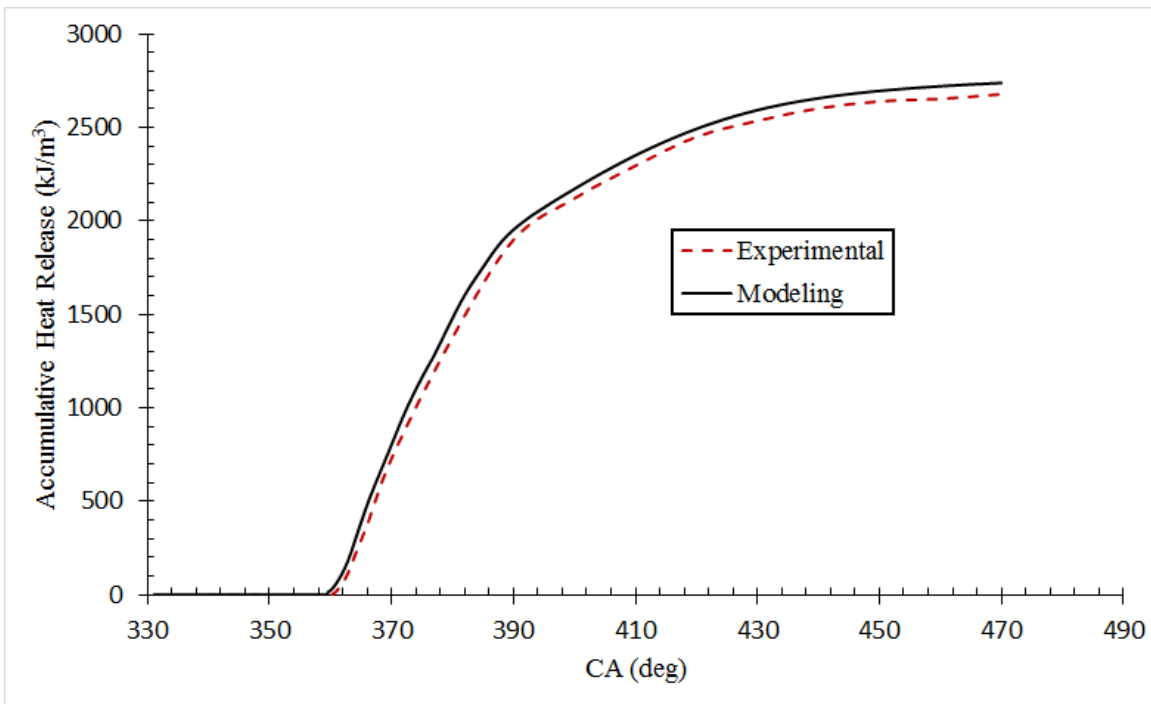
132 In order to prove the reliability of the modeling in terms of accuracy of the achieved results,
133 Fig. 2 is provided wherein mean pressure and accumulative heat release (AHR) of the
134 computed and measured data [23] are compared for the single injection of the engine at
135 2500 rpm engine speed. The max. error is seen at peak pressure (~ 368 °CA) which is still
136 less than 3% and it can be attributable to evaporation rate and breakup simulation models
137 during initial combustion phase as well as experimental setup uncertainties. Other than
138 that, the model is able to predict the engine behavior acceptably.

139 (a)



140

141 (b)



142

143 Fig. 2 Comparison of computed data with experimental results for (a) pressure, (b) AHR

144 2.3. Computation of exergy

145 Cylinder exergy balance can be formulated as follow [31]:

$$\frac{dA_{cyl}}{d\phi} = \frac{\dot{m}_{in} b_{in}^{tm} - \dot{m}_{out} b_{out}^{tm}}{N} - \frac{dA_l}{d\phi} - \frac{dA_w}{d\phi} + \frac{dA_f}{d\phi} - \frac{dI}{d\phi} \quad (1)$$

146 where \dot{m}_{in} is the incoming flow rate from the inlet manifold and consists of air and \dot{m}_{out}

147 is the outlet mass flow to the outlet manifold, b_{in}^{tm} and b_{out}^{tm} refer to the flow thermo-

148 mechanical exergy of incoming and outgoing cylinder mass flow rates [31]:

$$b^{tm} = (h - h_0) - T_0(s - s_0) \quad (2)$$

149 $\frac{dA_l}{d\phi}$ is the heat transfer exergy to the cylinder walls on the basis of crank angle degree. It

150 can be given as follow [31]:

$$\frac{dA_l}{d\phi} = \frac{dQ_l}{d\phi} \left(1 - \frac{T_0}{T_{cyl}} \right) \quad (3)$$

151 $\frac{dQ_l}{d\phi}$ is the heat transfer rate to the cylinder walls on the basis of crank angle degree and

152 T_{cyl} is the instantaneous temperature of the cylinder gasses, which are available from the

153 first law analysis. $\frac{dA_w}{d\phi}$ represents the indicated work transfer. In fact, it can be defined as

154 the value of output exergy from the cylinder associated with the indicated work [31]:

$$\frac{dA_w}{d\phi} = (P_{cyl} - P_0) \frac{dV}{d\phi} \quad (4)$$

155 where $\frac{dV}{d\phi}$ states the rate of cylinder volume change based on crank angle degree and P_{cyl}
 156 is the instantaneous cylinder pressure which both are calculable by the first law analysis in
 157 the engine processes. The burned fuel exergy on the crank angle basis can be calculated as
 158 follow [31]:

$$\frac{dA_f}{d\phi} = \frac{dm_{fb}}{d\phi} a_{fch} \quad (5)$$

159 a_{fch} represents the chemical fuel exergy. The chemical exergy of substances in the
 160 environment (e.g. fuel, sulfur, combustion products such as NO or OH, etc.) can be
 161 evaluated by considering an idealized reaction of the substance with others with the known
 162 chemical exergies [32]. This chemical exergy of the fuel can be expressed on a molar basis
 163 as follow [31, 32]:

$$\bar{a}_{fch} = \bar{g}_f(T_0, P_0) - \left(\sum_p x_p \bar{\mu}_p^0 - \sum_r x_r \bar{\mu}_r^0 \right) \quad (7)$$

164 where index p denotes products (CO₂, H₂O, CO, etc.) and index r is the reactants (fuel and
 165 O₂) of the (stoichiometric) combustion process, T_0 and P_0 are the dead state temperature
 166 and pressure, and the over bar denotes properties on mole basis. For liquid hydrocarbon
 167 fuels with molecular formulation of $C_z H_y$, the chemical exergy of fuel can be expressed as
 168 follows (on a kg basis) [33]:

$$a_{fch} = LHV \left(1.04224 + 0.011925 \frac{y}{z} - \frac{0.042}{z} \right) \quad (8)$$

169 where LHV is the fuel lower heating value.

170 The $dI/d\phi$ term in equation (1) represents the rate of irreversibility production in the
171 cylinder, which includes combustion, viscous loss, turbulence, mixing and etc. According
172 to Dunbar and Lior [34], a combustion reaction has four major sources of internal
173 irreversibility. They are:

- 174 • A chemical diffusion process in which air and fuel molecules are drawn together.
- 175 • Combustion of the fuel-air mixture (thermo-chemical reaction).
- 176 • Internal energy exchange through molecular collisions amongst the products and
177 radiation heat transfer amongst product constituents due to unequal heat
178 distribution.
- 179 • Mixing process whereby reactants mix before combustion, and products mix
180 with reactants during combustion due to proximity.

181 Since the contribution of combustion in irreversibility production is more than 90% [35,
182 36], in the present study, only the combustion irreversibility is taken into evaluate the in-
183 cylinder irreversibilities. The combustion irreversibilities on the crank angle basis can be
184 given as [37]:

$$\frac{dI}{d\phi} = -\frac{T_0}{T_{cyl}} \sum_j \mu_j \frac{dm_j}{d\phi} \quad (9)$$

185 where subscript j includes all reactants and products. For ideal gases, $\mu_j = g_j$ and for the
186 fuel $\mu_f = a_{fch}$.

187 Aforementioned equations can be solved by the numerical methods in order to evaluate the
188 second-law terms in an engine cycle.

189 **3. Results and discussion**

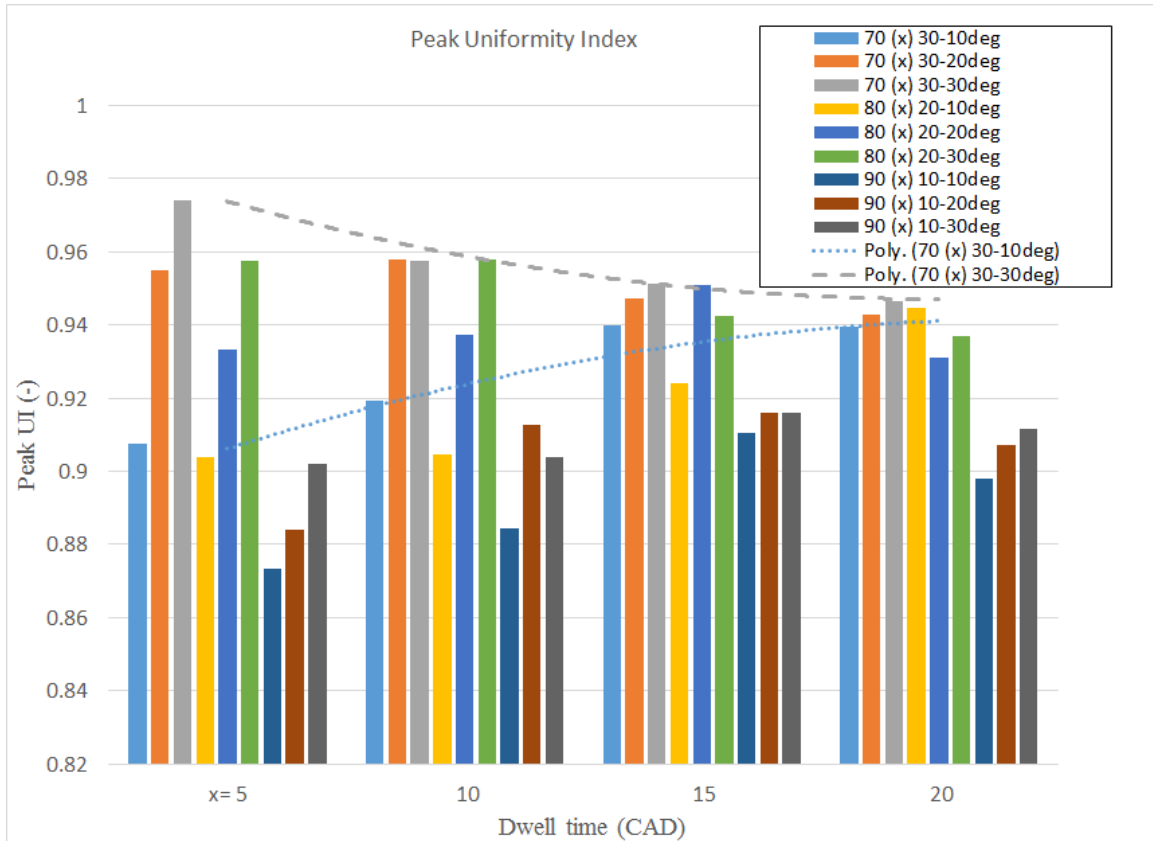
190 *3.1. Energetic evaluation*

191 The mixing process of fuel droplets and air is a crucial mechanism in having an efficient
192 combustion, so the uniformity and homogeneity of mixture is quantified and scaled by “air-
193 fuel uniformity index” as follows:

$$194 \quad UI = 1 - \frac{1}{n} \sum_{i=1}^n \frac{\sqrt{(w_i - w)^2}}{w} \quad (10)$$

195 where w_i is the equivalence ratio in the i -th cell of the meshed domain in the combustion
196 chamber. The scaled quantity of UI varies between 0-1 denoting consummate uniformity
197 when $UI = 1$. The different injection schemes for 36 different injection cases where one of
198 the portions of injection between the first and second pulses, injection angles, or dwell
199 times is meant to let achieving the optimum fuel distribution and hence use the most of fuel
200 energy’s potential.

201 Fig. 3 diagram shows the peak UI variation for different injection strategies of this study.
202 In the first place, it can be observed that the highest UI belongs to 70 (5) 30-30deg and the
203 homogeneity of mixture tends to reduce with dwell time from 5→20 as the polynomial
204 interpolation curve indicates. This is due to well-distributed portions of fuel between the
205 first and second pulses while the divergent injection angle is such timed to target the bowl
206 area after 5 CA dwell time, so that the wall-impingement would be minimized. On the other
207 hand, a reverse trend is spotted with 70 (5) 30-10deg and the more dwell time is spent, the
208 more mixture uniformity is resulted (as the poly. curve interpolation suggests). What is
209 more, it can be stated that in general 70 (x) 30 > 80 (x) 20 > 90 (x) 10 is true in terms of
210 UI wherein this uniformity aides towards better fuel capacity utilization in the form of
211 stoichiometric combustion of the system.



212

213

Fig. 3 Peak UI vs. dwell time for different split injection schemes

214

Subsequently, the flow behavior of the cylinder influences the subsequent combustion

215

phenomena and the peak in-cylinder temperature is plotted for different injection modes in

216

Fig. 4. There is a clear correspondence between uniformity and temperature for different

217

split injection modes. The temperature plot almost follows the UI pattern with the highest

218

temperature happening at 70 (5) 30-30deg (2011.58 K) whereas the lowest one can be noted

219

for the 90 (5) 10-10deg with 1721.65 K. The reason for low mixture uniformity and

220

temperature of 90 (5) 10-10deg is that the distribution of fuel portion is limited and

221

approaches to a single injection. The uniformity of mixture with dwell time is increasing

222

for 70 (x) 30-10deg, this leads to a more complete combustion and oxidation of

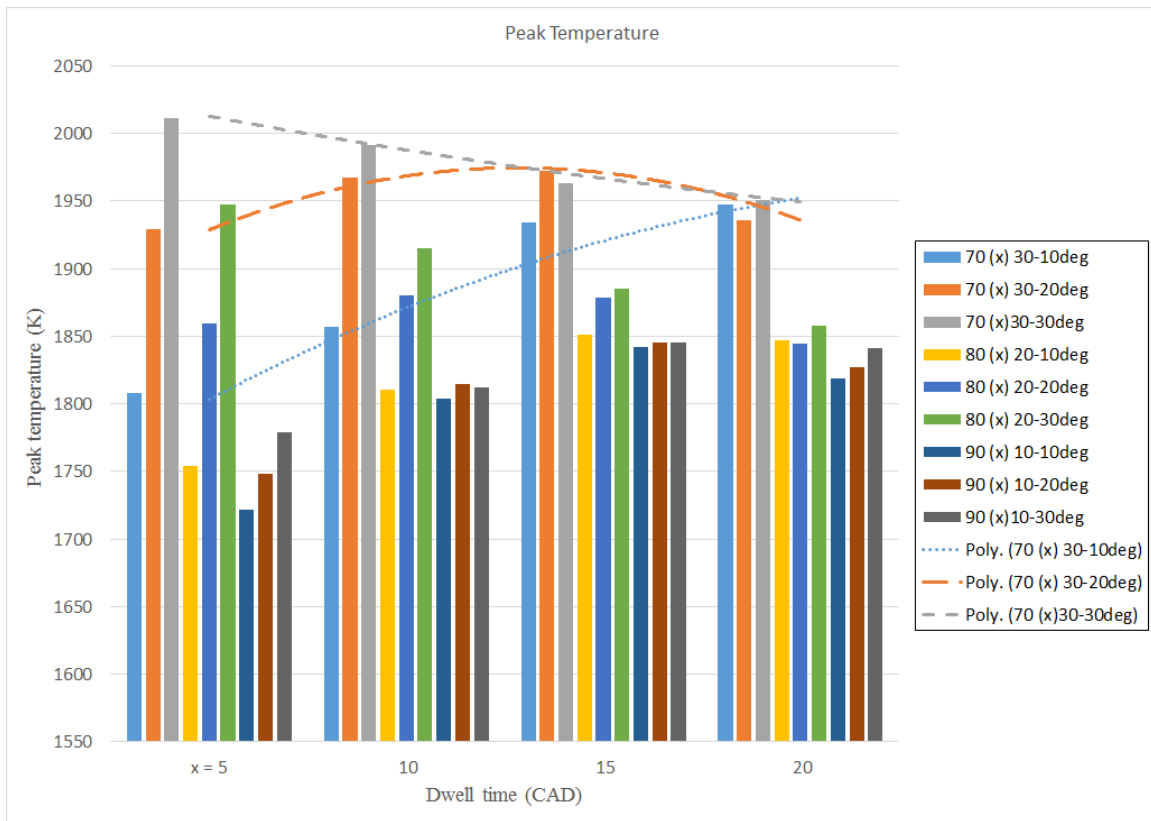
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hydrocarbon fuel, therefore as seen in Fig. 4 the cylinder temperature increases with dwell

224

time. In this case, dwell time acts as an opportunity for droplets to diffuse in air in different

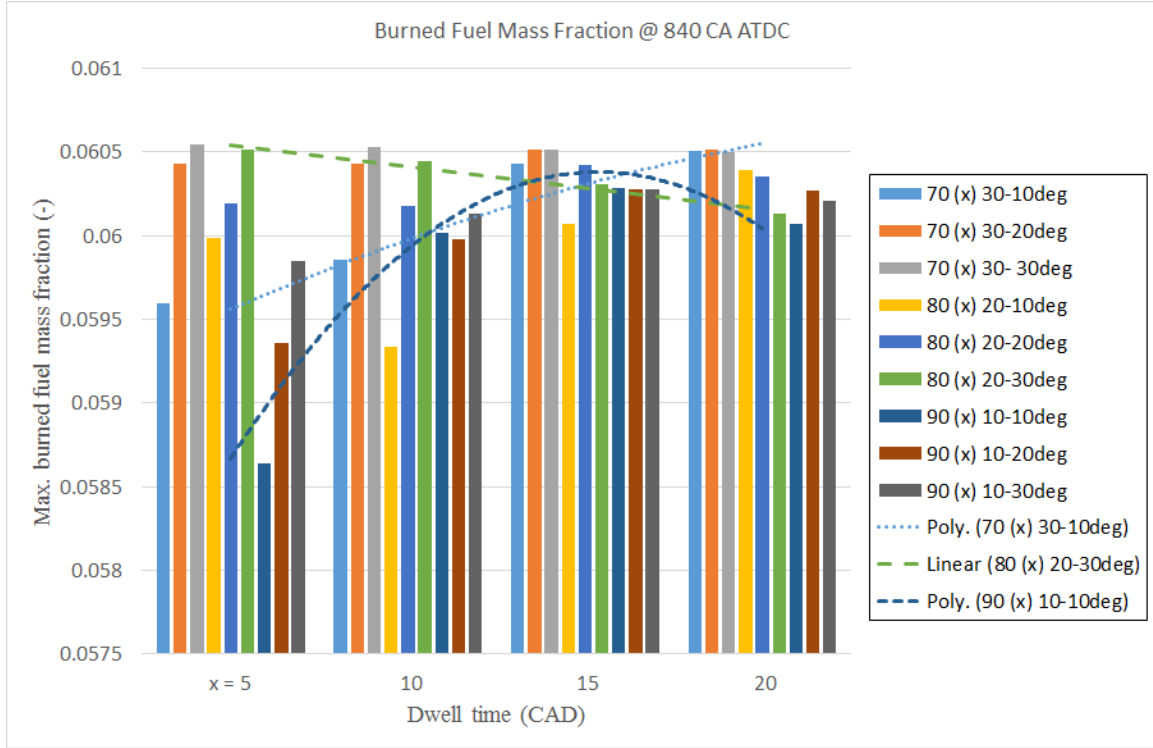
225 chamber areas. Among increasing pattern of 70 (x) 30-10deg and declining pattern of 70
 226 (x) 30-30deg, the maximum temperature for 70 (x) 30-20deg occurs at x= 15 CA.



227

228 Fig. 4 Peak in-cylinder temperature vs. dwell time for different split injection schemes

229 The maximum burned fuel mass fraction at 840 CA ATDC is demonstrated in Fig. 5 for
 230 different split injection modes. Again, for the case of 70 (x) 30, the cylinder contains more
 231 burned fuel than other fuel portioning policies. However, other than 80(x) 20-30deg, other
 232 cases project a growing concentration of burned fuel with dwell time increment. This is
 233 related to a more time given for fuel droplets burning in the greater time span of dwell time
 234 between injection pulses, this issue is evident in the bar chart of x = 20 CA when all burned
 235 fuel fractions of different cases have got closer to each other.



236

237 Fig. 5 Peak burned fuel mass fraction vs. dwell time for different split injection schemes

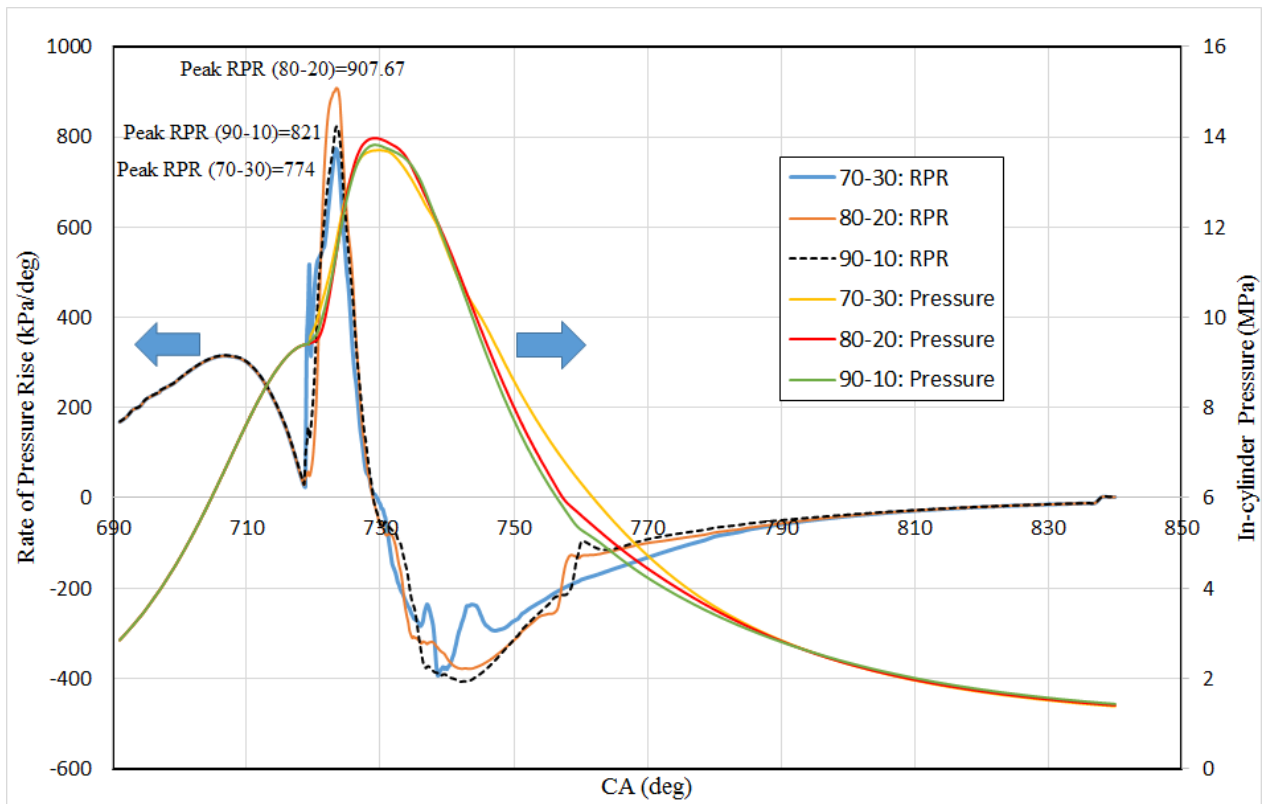
238 The more burned fuel mass fraction indicates that the system is better empowered to utilize
 239 the chemical potential of the hydrocarbon fuel.

240 The cylinder pressure is another parameter of significance in measuring the energetic
 241 performance of the engine that comes with the explosive nature of compression-ignition of
 242 diesel. In this regard, the pressure and rate of pressure rise (RPR) for different injection
 243 plans are displayed in Fig. 6 with respect to CA. The RPR is calculated in 4 intervals step
 244 with central differencing derivatives:

$$245 \quad RPR = \frac{dP_i}{d\theta} = \frac{P_{i+2} - P_{i-2}}{4h} \quad (11)$$

246 P denotes the discrete calculated pressure, h is the change in CA step size between two
 247 consecutive runs, so in our case, $h = \Delta\alpha$.

248 According to Fig. 6, the peak RPR (907.67 kPa/deg) and pressure (13.97 MPa) occurs for
 249 80-20 fuel mass distribution and the lowest is for 70-30. This shows that a good mixing
 250 procedure of fuel and oxidizer for 70-30 injection is a factor for a gradual and qualified
 251 combustion that can enhance the burning rate and chemical kinetics; therein the knock can
 252 be avoided. The higher chamber pressure of 70-30 injection mode during post combustion
 253 phase (i.e. mixing controlled combustion phase) implies the better engine torque and its
 254 overall performance in terms of the first law of thermodynamics.



255
 256 Fig. 6 Pressure and RPR variation with CA for 70-30, 80-20, and 90-10 injection plans

257 *3.1. Exergetic evaluation*

258 The second law of thermodynamics provides a platform for estimation of the energy quality
 259 in a given system. In current research, we are interested to analyze the influence of
 260 advanced split injection on exergy terms, thereby find the best case for extracting the most

261 useful work out of the combustion chamber. The indicated work exergy in the accumulative
262 (time-integrated) form with respect to CA for different advanced injection modes is
263 presented in Fig. 7a. As seen, the work exergy is increasing with CA to deliver the
264 mechanical rotation power at the end period of thermodynamic cycle.

265 With reference to Table 4, the highest and the lowest amount of IMEP as expected goes to
266 70 (5) 30-30deg and 90 (5) 10-10deg with 5.77 bar and 5.334 bar, respectively. This
267 dominant IMEP that stems from better uniformity of mixture and thus better combustion
268 for 70 (5) 30-30deg. Moreover, for the accumulative work exergy (AWE), the following
269 order of $AWE_{(70-30)} > AWE_{(80-20)} \gg AWE_{(90-10)}$ is seen that is acceptable since the
270 distribution of fuel proportion between pulses allows for better utilization of fuel energy.

271 Based on Fig. 7b, which shows variation of peak accumulated work exergy with dwell
272 time, the maximum work exergy is associated with 70 (x) 30-30deg. For that, increasing
273 the dwell time gives the reduction in work exergy that is in close agreement with the trend
274 observed for UI in Fig. 3. That is to say, increasing the dwell time gives away the chance
275 to turn the provided chemical energy to work mainly because the fuel jet to wall
276 impingement with dwell time increment. For the injection cases of 80-20 and 90-10, the
277 dwell time plays a positive role in gaining an efficient fuel droplet diffuse in oxidizer, so
278 the peak accumulated work rises with dwell time.

279

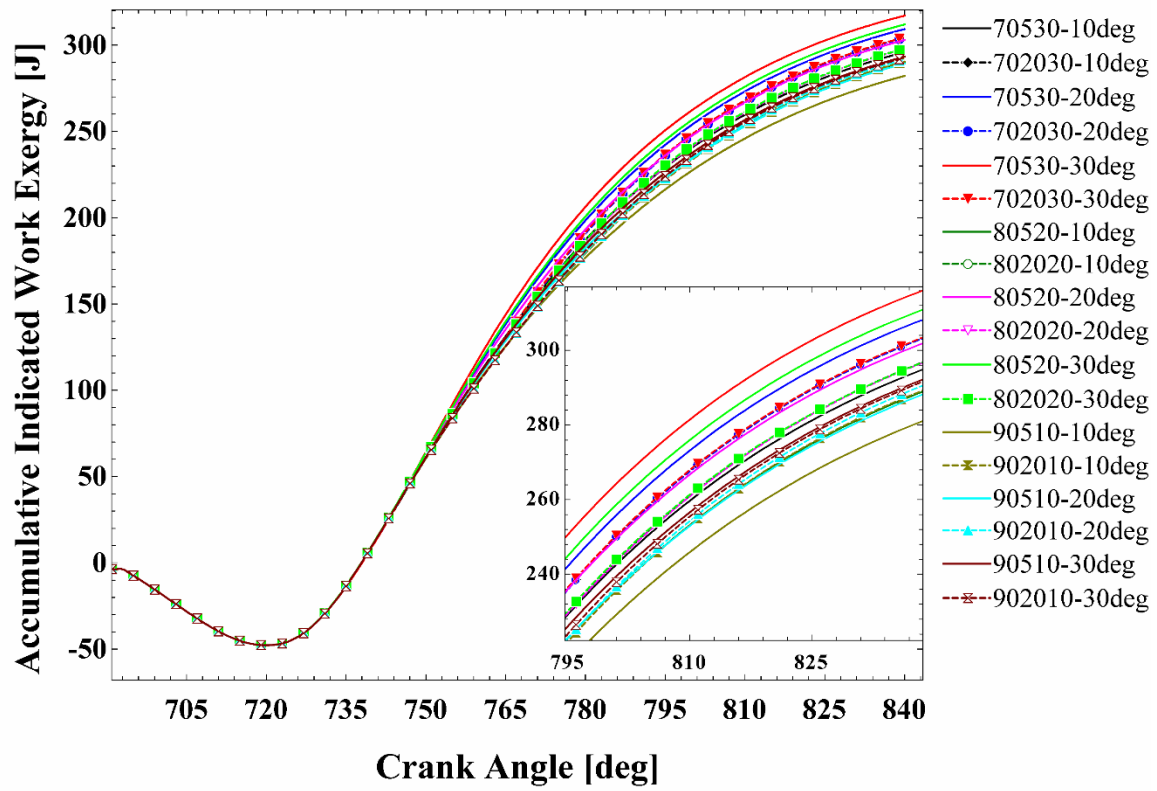
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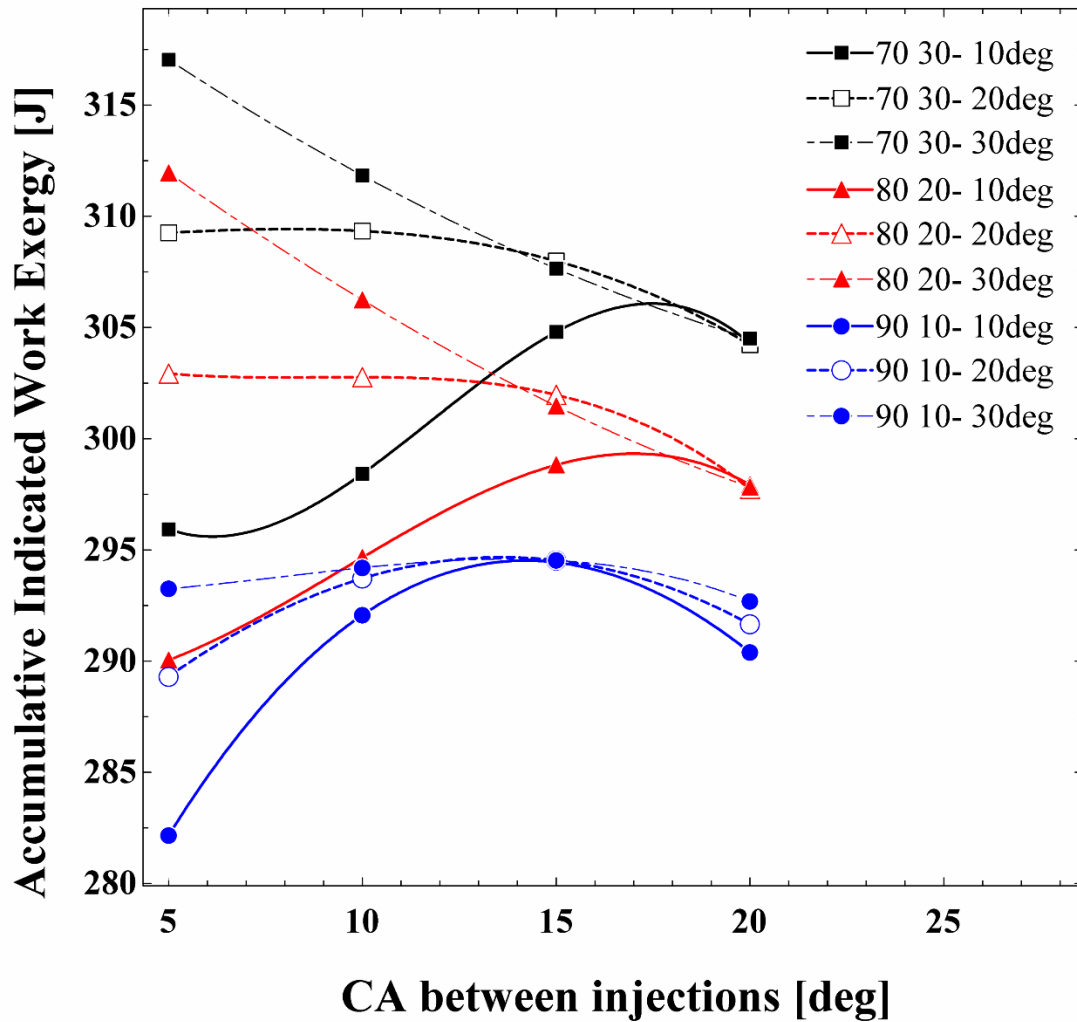
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284 (a)



285

286 (b)



287

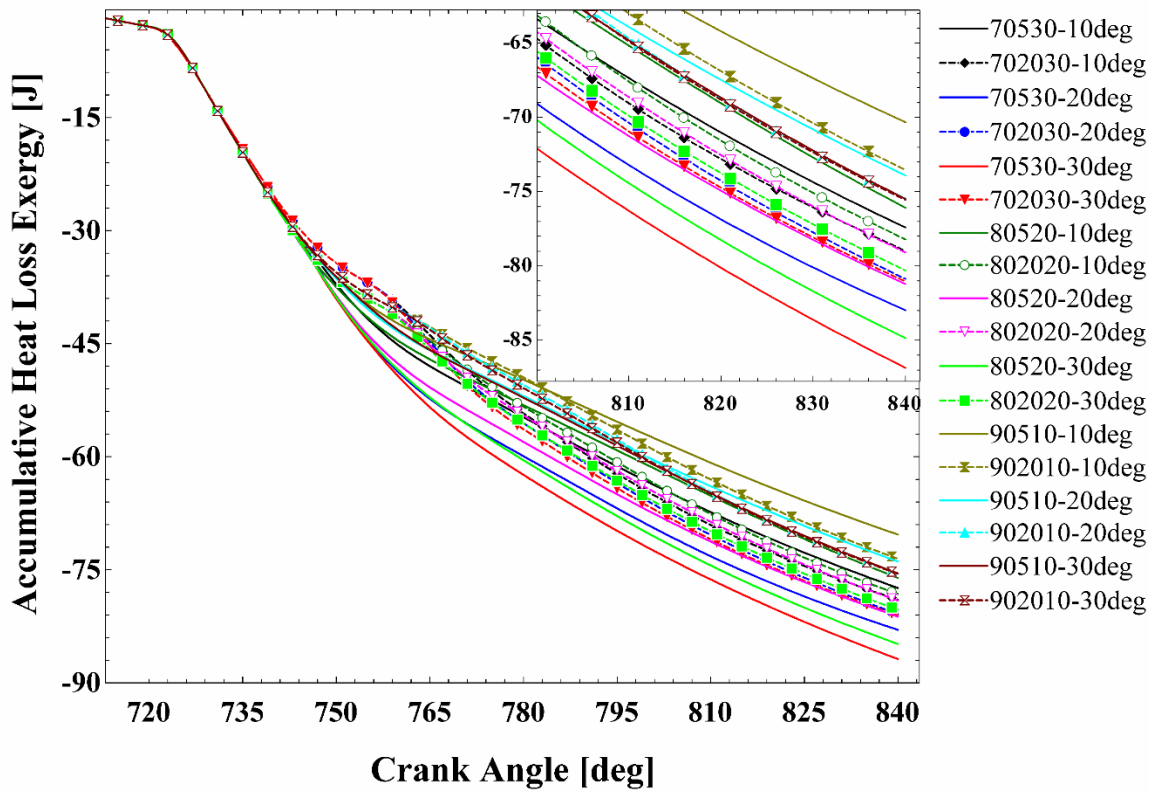
288 Fig. 7(a) variation of accumulative work exergy with CA, (b) peak accumulative work
 289 exergies with dwell time for different injection modes

290 The variation of accumulated heat loss exergy (AHLE) with CA for different split injection
 291 modes is illustrated in Fig. 8a. From Fig. 8a, the most convertible heat comes from 70 (5)
 292 30-30deg and the lowest AHLE corresponds to 90 (5) 10-10deg. The reason lies in the fact
 293 that majority of fuel is burnt at once with little opportunity to change the provided heat.

294 In Fig. 8b, the peak AHLE against dwell time is depicted for various injection plans. It is
 295 clear that the higher heat loss exergy goes for 70-30, then 80-20, and finally the lowest

296 accumulative heat exergy is for 90-10. As mentioned before, 70-30 strategy allocates
 297 suitable amount of fuel between pulses and this action makes an efficient combustion with
 298 higher temperature than in the single injection, which increases thermal waste. For 30deg
 299 divergent split injection, for all 70-30, 80-20, and 90-10 injections, the AHLE are
 300 decreasing with dwell time, although the rate of decrement for 70-30 is more noticeable. It
 301 is mainly originated from more spray cylinder wall interaction and more importantly, the
 302 shift of second pulse injected fuel's combustion towards EVO timing.

303 (a)



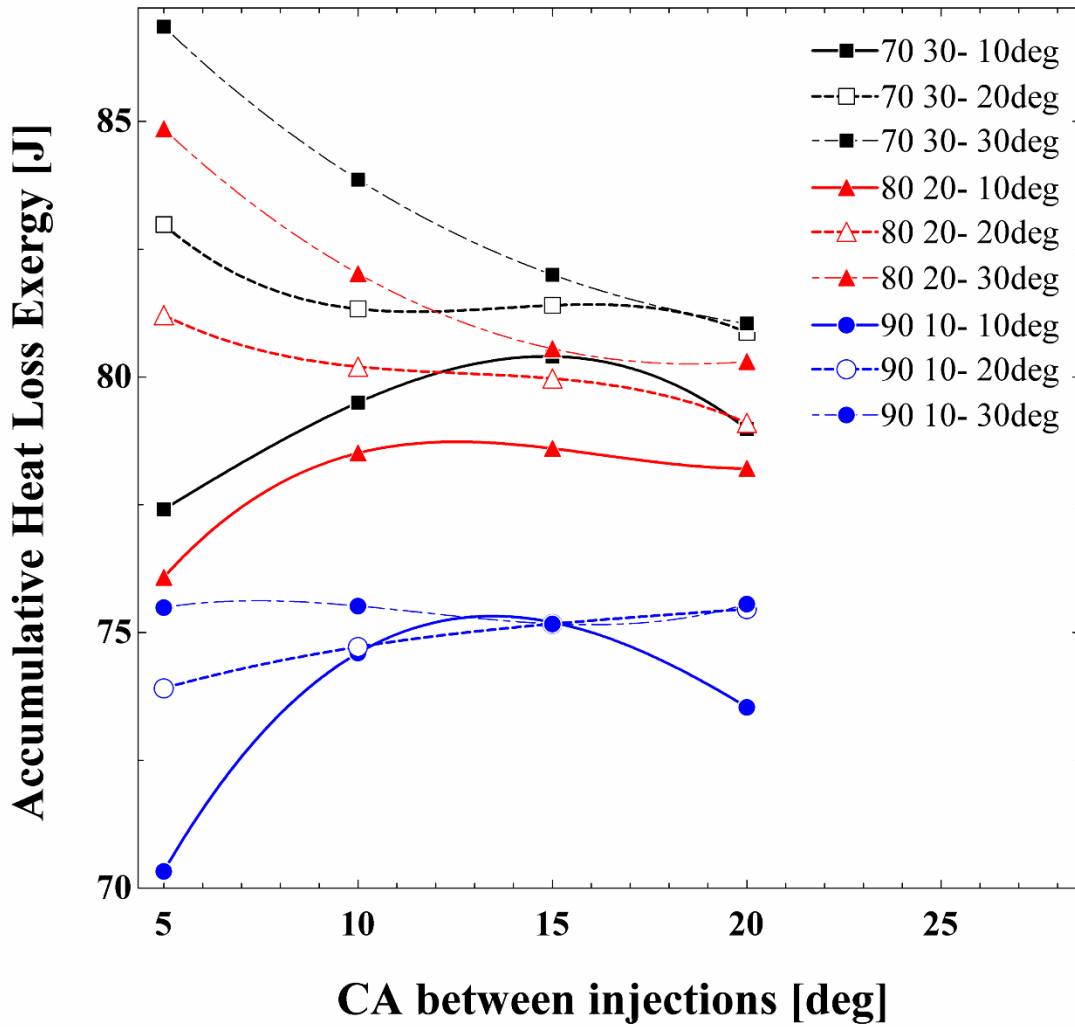
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311 Fig. 8(a) variation of accumulative heat loss exergy with CA, (b) peak accumulative heat
 312 loss exergies with dwell time for different injection modes

313 Thermo-mechanical exergy with CA and exhaust thermo-mechanical exergy with dwell
 314 time is represented in Fig. 9 for different operational split injection modes. The cases that
 315 have a shorter time between two pulses show one peak thermo-mechanical exergy while
 316 longer dwell time exhibit two peak curves and usually their thermo-mechanical exergies
 317 are lower. It is clearly demonstrated that the thermo-mechanical exergy of 70 (5) 30-30deg

318 dominates with 439 J. Three chief reasons can explain this: (a) the fuel mass proportion is
319 properly divided between two pulses, (b) 30deg injection angle between two nozzles
320 provide a proper spatial distribution of fuel spray, (c) the short dwell time ($\sim 5^\circ\text{CA}$)
321 prevents coincidence of the second injection combustion with EVO timing.

322 The missed chance for applying the exhausted gas from chamber to thermo-mechanical
323 exergy for 90-10 is greater and much of the thermal energy is lost from the exhaust valve.

324 The exhaust thermo-mechanical exergy expresses the exergy content that leaves the
325 cylinder from the exhaust valve, which could be used to exert power on piston or converted
326 to work, however this chance is missed. The general observed trend from Fig. 9b is the
327 increase of exhaust thermo-mechanical exergy with dwell time due to shift of combustion
328 towards the expansion (power) stroke. Referring to Fig. 5, one notes the higher burned
329 mass fraction of 70 (5) 30-30deg that is an indication of more reactivity of fuel components
330 with oxidizer. This shows that much more of fuel has burned, thereby more reaction species
331 are released as a result of combustion which gives way to more thermo-mechanical exergy
332 (the opposite trend goes for 90 (5)10-10deg). According to Fig. 9b, the necessity for
333 adopting the proper injection mode can be confirmed since a 9.5% reduction in exhaust
334 thermo-mechanical exergy occurs when 70 (5) 30-30deg is used instead of 90 (20) 10-
335 10deg, thereby a considerable save of fuel chemical potential is created in convertibility to
336 useful work output.

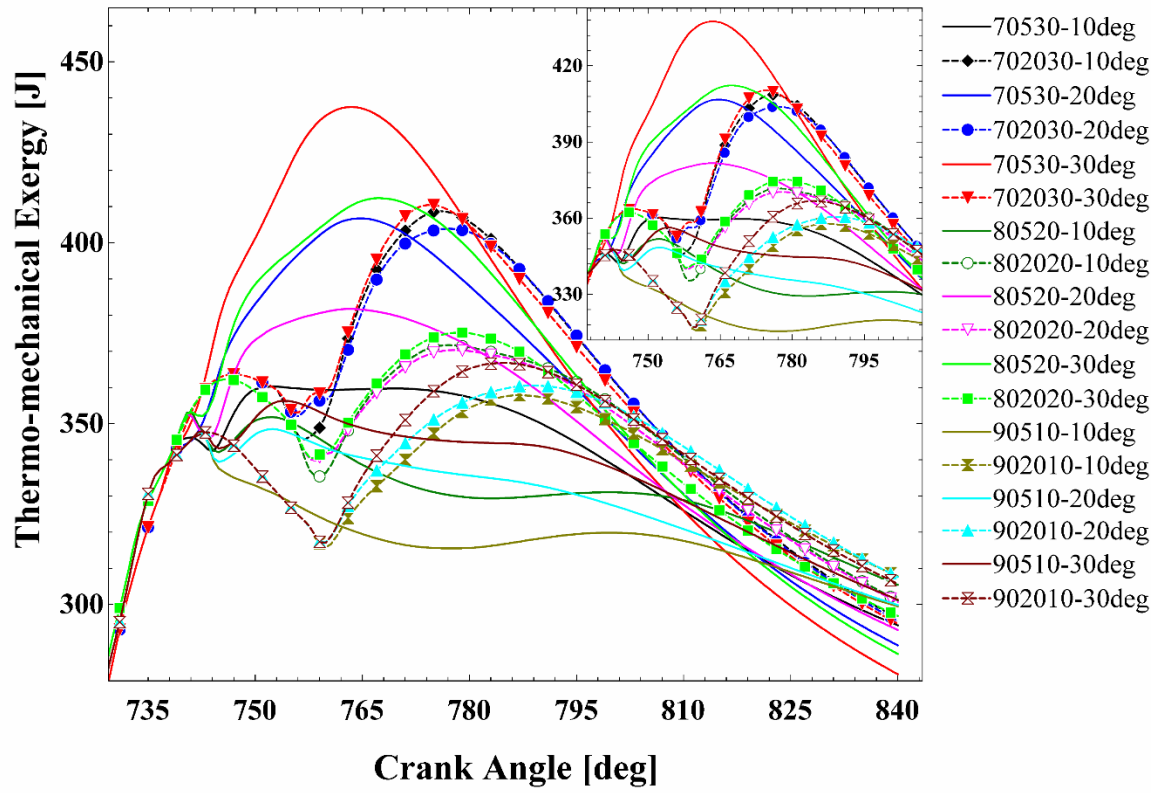
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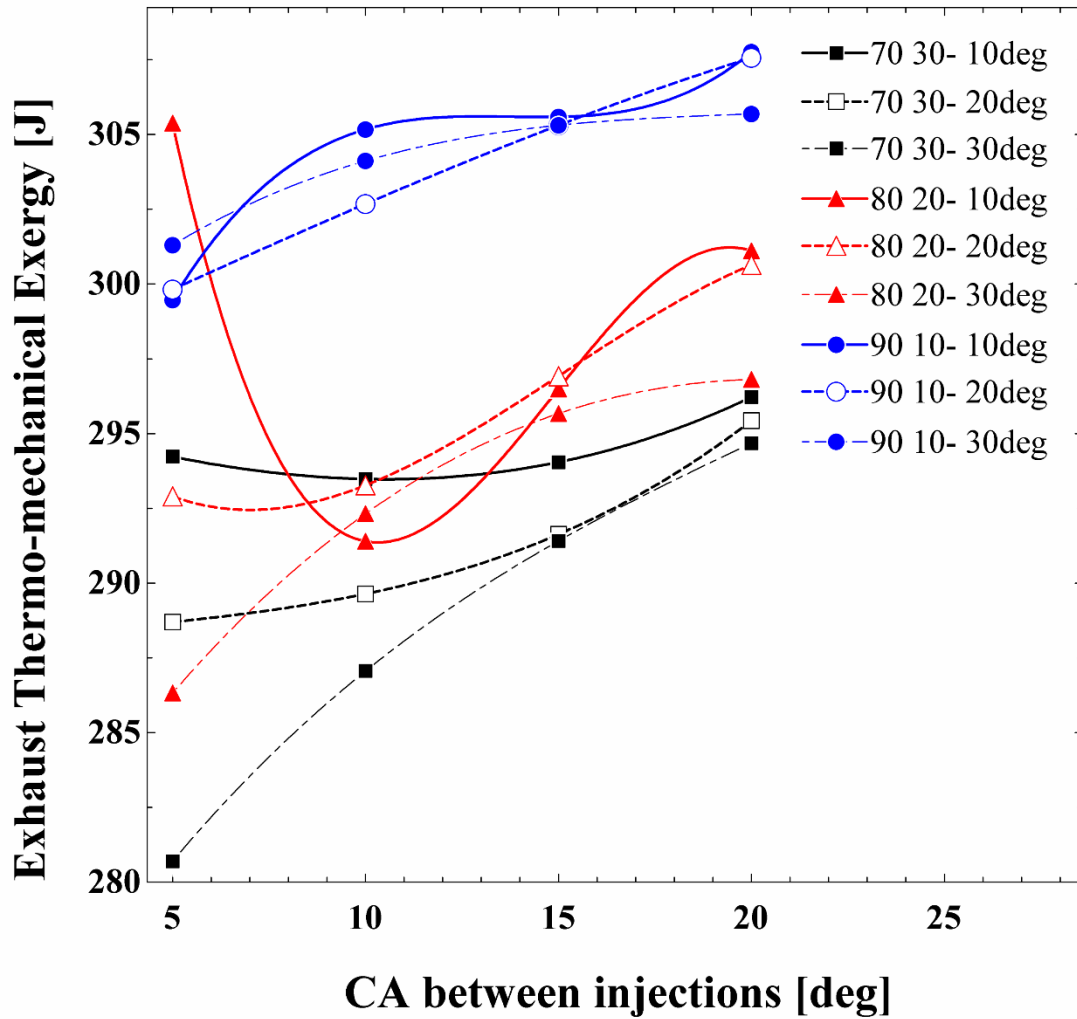
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341 (a)



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343 (b)



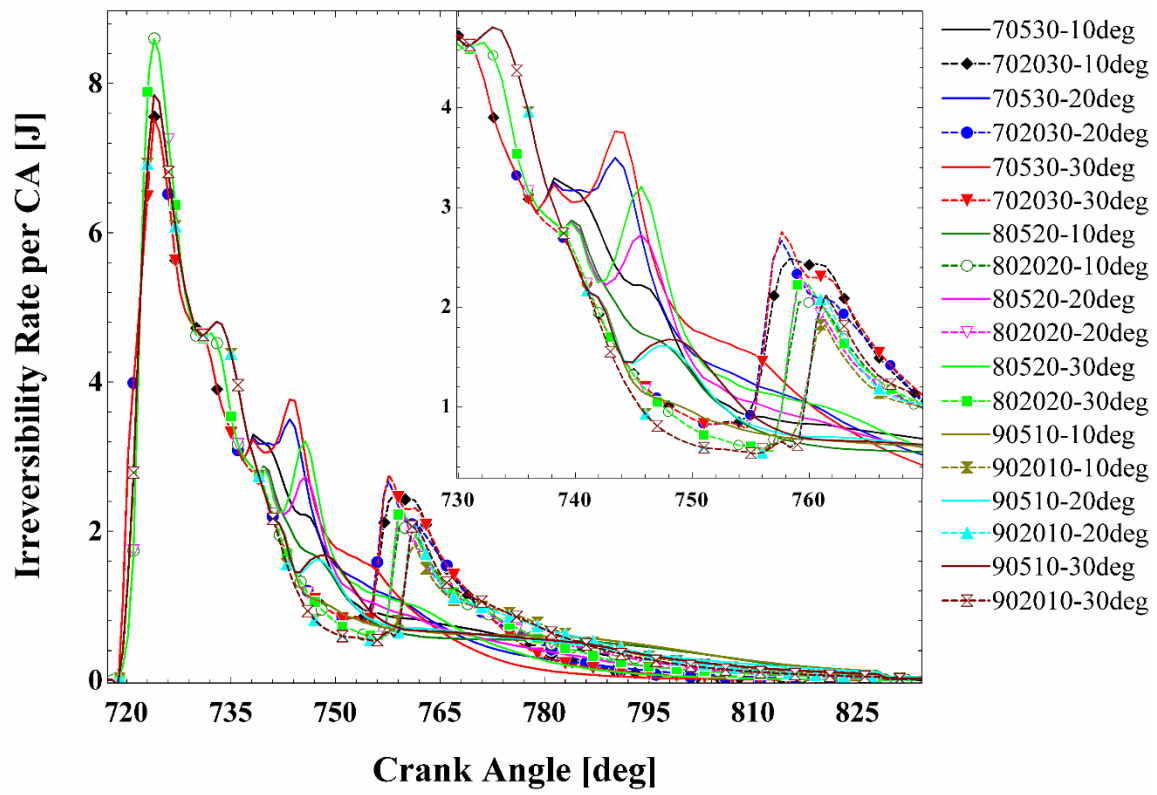
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345 Fig. 9(a) variation of thermo-mechanical exergy with CA, (b) exhaust thermo-mechanical
 346 exergy with dwell time for different injection modes

347 The irreversibility rate variation with CA evolution is shown in Fig. 10a for different
 348 injection modes. Taken Fig. 5 into consideration, the high irreversibility rate for 80 (20)
 349 20-30deg can be explained since greater PRP leads to the rapid burning rate and intense
 350 combustion which accordingly increases the irreversibility of the process. The
 351 accumulative irreversibility with respect to dwell time for different injection modes is
 352 presented in Fig. 10b. It is found that, in contrast to exergy terms, accumulated

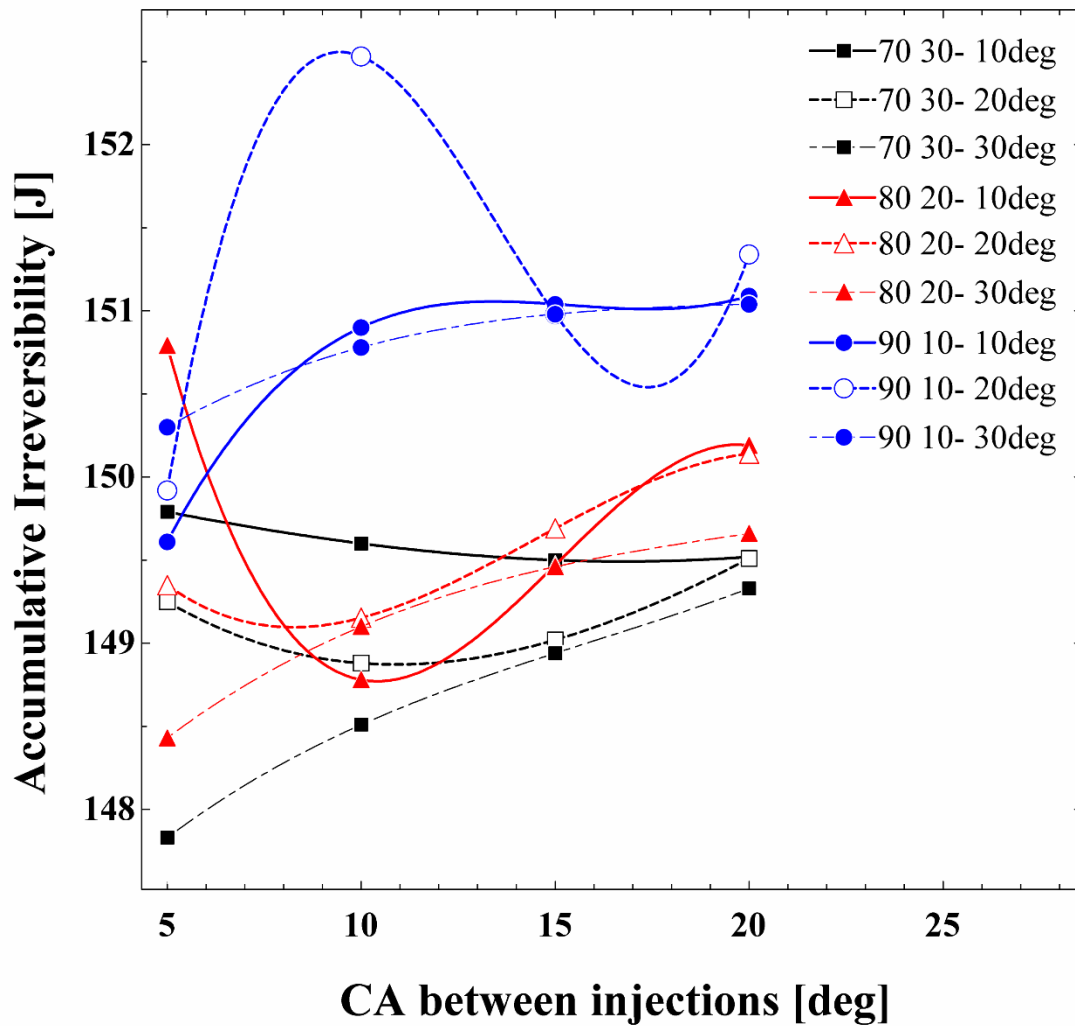
353 irreversibility of 90-10 is prevalent, next comes 80-20, and 70-30 strategies. The maximum
354 accumulative irreversibility occurs at 90 (10) 10-20deg and the lowest amount at 70 (5) 30-
355 30deg, a case that gave the most UI. The similar result more recently reported in [38],
356 where the stoichiometric combustion culminated in the lowest level of exergy destruction
357 fraction. In addition, as it is recorded in Fig. 4, the 70-30 fuel injection scheme generates
358 the greatest in-cylinder temperature and according to Ref. [39], the higher cylinder
359 temperature would decrease the irreversibility. Therefore, based on Fig. 10b, the lowest
360 irreversibility is observed for 70-30 and the most irreversibility can be associated to 90-10
361 due to lower cylinder temperature. The reason is such explained that if the cylinder
362 temperature increases, the heat transfer from hot gases to yet unburned mixture would
363 decrease. In conclusion, it can be summarized that mixture uniformity is a primary
364 parameter to reduce the irreversibility of a combustion system, therefore avoid the waste
365 energy in the form of lost heat.

366 (a)



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368 (b)



369

370 Fig. 10(a) variation of irreversibility rate with CA and (b) accumulative irreversibility

371

with dwell time for different injection modes

372 4. Conclusion

373 In this work, an advanced split injection is undertaken wherein the responsibility of the

374 injection for the first and second pulses is with two discrete nozzles whose angles aim to

375 different zones of combustion chamber and this helps covering wider segments of cylinder.

376 In the modern injection two mechanisms of various dwell time and nozzle included angles

377 are predicted to homogenize the air-fuel mixture. The objective of the research was to

378 determine if there is any correlation between the uniformity of mixture (obtained by split
379 injection) and exergy concept. The results from the CFD code of AVL-FIRE is
380 incorporated with the in-house developed FORTRAN code for exergy analysis, whereupon
381 it is revealed that the case (70 (5) 30 -30deg) could give the highest uniformity and burned
382 fuel mass fraction leading to maximum accumulative work/heat exergy and thermo-
383 mechanical exergy. On the opposite side, the 90 (5) 10-10deg strategy shows the weakest
384 performance due to its closeness to a single injection scheme.

385 According to findings of this research, the single injection (mostly done in conventional
386 diesel engines) has a very big exhaust thermo-mechanical exergy, which means a great deal
387 of the potential energy is wasted without being tapped or utilized as to propel a device.
388 Other than that, it is proved that the irreversibility rate is correlated with RPR such that
389 RPR of 80-20 mode has the highest peak of 907.67 kPa/deg leading to the highest
390 irreversibility rate of 8.6 J/deg, while accumulated irreversibility is reversely proportionate
391 with in-cylinder temperature. It is also concluded that taken a recommended split injection
392 ratio (70 (5) 30-30deg) cause prevention of waste in thermo-mechanical exergy by 9.5%.

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514 Table 1

515 Partitioning of fuel mass between injection pulses

Injection mode	1 st pulse mass (kg/cycle)	2 nd pulse mass (kg/cycle)
70-30	2.6201×10^{-5}	1.1229×10^{-5}
80-20	2.9944×10^{-5}	0.7486×10^{-5}
90-10	3.3687×10^{-5}	0.3743×10^{-5}

516 Single injection mass = 3.743×10^{-5} kg/cycle

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520 Table 2

521 Boundary and initial conditions

Head temperature	550.15 K
Piston temperature	575.15 K
Cylinder temperature	475.15 K
Intake valve closed	52°CA ATDC
Exhaust valve opening	110°CA ATDC
Initialized swirl	1500 1/min
Initial TKE	10 m ² /s ²
Initial TDR	5196.15 m ² /s ³

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532 Table 3

533 Engine specifications

Bore× stroke	82.5× 82 mm
Displacement	438 cm ³ /cylinder
Compression ratio	19.5:1
Swirl ratio @ IVC	3
Rail pressure	540-1255 bar (based on engine speed)
Nozzle geometry	5×0.15 mm
Number of nozzles	4
Clearance	0.86mm
Connecting rod length	104mm
Injection start timing	4°CA BTDC
Residual gas ratio	0.5

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538 Table 4

539 IMEP values (unit: bar) for different injection modes

Injection mode	10deg	20deg	30deg
70-5-30	5.49	5.64	5.77
70-10-30	5.42	5.452	5.475
70-15-30	5.45	5.448	5.45
70-20-30	5.443	5.43	5.448
80-5-20	5.49	5.58	5.64
80-10-20	5.544	5.519	5.526
80-15-20	5.538	5.539	5.537
80-20-20	5.531	5.531	5.531
90-5-10	5.334	5.36	5.38
90-10-10	5.345	5.3459	5.3467
90-15-10	5.35	5.35	5.3464
90-20-10	5.35	5.3464	5.3464

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