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3 Gabor frames for classification of paroxysmal and
4 persistent atrial fibrillation episodes

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15 **Abstract**

16 In this paper, we propose a new classification method for early differen-
17 tiation of paroxysmal and persistent atrial fibrillation episodes, i.e. those
18 which spontaneously or with external intervention will return to sinus rhythm
19 within 7 days of onset from the ones where the arrhythmia is sustained for
20 more than 7 days. Today, clinicians provide patients classification once the
21 course of the arrhythmia has been disclosed. In this work we deal with this
22 problem studying a sparse representation of surface electrocardiogram sig-
23 nals by means of Gabor frames and applying a linear discriminant analysis
24 afterwards. Thus, we provide an early discrimination, obtaining promising
25 performances on a heterogeneous cohort of patients in terms of pharmacolog-
26 ical treatment and state of progression of the arrhythmia: 95% sensitivity,
27 82% specificity, 89% accuracy. In this manner, the proposed method can

28 help clinicians to choose the most appropriate treatment using the electro-
29 cardiogram, which is a widely available and non-invasive technique. This
30 early differentiation is clinically highly significant in order to choose optimal
31 patients who may undergo catheter ablation with higher success rates.

32 *Keywords:* Gabor frames, Atrial Fibrillation, Electrocardiogram

33 **1. Introduction**

34 Atrial fibrillation (AF) is the most common cardiac arrhythmia in clinical
35 practice, and affects up to 4.5 million people in Europe and 2.3 million adults
36 in USA. Its prevalence increases with age, being less than 1% among adults
37 younger than 60 years but about 9% for people older than 80. Indeed, it is
38 likely to increase 2.5-fold by the year 2050 [1].

39 AF is a supraventricular arrhythmia characterized by uncoordinated atrial
40 activation and ineffective atrial contraction, which is reflected on the ECG
41 by irregular heart beat intervals and absence of P-wave [2]. Clinical practice
42 guidelines to manage patients with AF classify them by the duration of the
43 AF episodes as paroxysmal (episodes which spontaneously or with external
44 intervention return to sinus rhythm within seven days after their onset), per-
45 sistent (patients in whom AF is sustained more than seven days and require
46 pharmacological or electrical cardioversion to restore sinus rhythm), and per-
47 manent (both the patient and clinician accept to stop further attempts to
48 control rhythm) [3, 4, 5].

49 Many references of the state-of-the-art have performed an analysis and

50 classification of AF episodes, most of which have used the public AF termina-
51 tion database of Physionet [6], that consists of one-minute ECGs of sustained
52 or self-terminating AF after one second, one minute, or at least one hour of
53 the end of the record.

54 Thus, classification of AF episodes and their spontaneous termination by
55 means of the surface ECG has been addressed in several works, mainly by
56 means of the analysis of the dominant frequency of the atrial activity (AA)
57 signal: by observing more likelihood to terminate AF when the dominant
58 frequency decreases [7] and also to characterize the circadian rhythms of
59 persistent atrial fibrillation [8]. Other references have used the modulus and
60 phase information of several time-frequency transforms [9, 10] to perform the
61 AF paroxysmal and persistent classification, or hidden Markov models to
62 track the frequency changes along ECG signals to early detect AF episodes
63 nearly to terminate [11]. Other authors also study other features, apart
64 from the dominant atrial frequency, such as the amplitude and the waveform
65 shape of the AA [12] or the average heart rate and the index of ventricular
66 activity [13] as optimal discriminators between self-terminating and sustained
67 episodes along 24 hours.

68 Non-linear measures, such as sample entropy, have also been used to ob-
69 serve differences between the AF episodes analyzing the main atrial wave [14],
70 and using long-term ECG recordings [15, 16], or even intracardiac recordings
71 [17].

72 Regrettably, although manifold tools have been developed to aid clini-

73 cal decision recently, the validation across the broad range of AF patients is
74 still incomplete [18]. In this paper we deal with the early discrimination of
75 paroxysmal and persistent AF episodes classified according to current clin-
76 ical guidelines [3, 4, 5]. We perform this clinical classification addressed in
77 previous papers [9, 10] from a different point of view. We have extracted
78 the coefficients of a sparse representation with respect to a Gabor frame,
79 which have been calculated from the frequency spectrum information of the
80 ECG signal, once ventricular activity has been canceled. Then, we use linear
81 discriminant analysis for classification.

82 Sparse representation of signals has been recently introduced for biomed-
83 ical signal analysis. In particular, for ECG processing, it has been mainly
84 used for signal compression [19, 20, 21] and beat classification [22]. Particu-
85 larly, sparse dictionaries have been applied for ventricular and atrial activity
86 estimation in patients suffering from AF in the works presented in [23, 24]. In
87 this paper, we have applied sparse representation by means of Gabor frames
88 on a cohort of signals acquired from real patients, providing good classifi-
89 cation results. Moreover, one value-add of the current work is the diversity
90 of patients included in the cohort under study, in terms of antiarrhythmic
91 treatments and state of progression of the arrhythmia.

92 The rest of the paper is organized as follows. The study population and
93 its clinical characteristics are described in Section 2. Signal pre-processing
94 and the feature extraction methods by means of the sparse representation are
95 described in Sections 3.1-3.4. Next, experimental results and performances

96 are depicted in Section 4. Finally, discussion of results is presented in Section
97 5 and conclusions are drawn in Section 6.

98 **2. Materials**

99 The population of this retrospective study consists of 186 consecutive
100 unselected patients who were suffering from paroxysmal or persistent atrial
101 fibrillation. They were attended in a specific arrhythmia clinic of a tertiary
102 center (La Fe Hospital, Valencia), where the bipolar lead II was registered for
103 five seconds and stored in PDF format by using the Philips PageWriter TC50
104 electrocardiograph. Corresponding original raw data was extracted from the
105 PDF file by using the application presented in [25]. Lead II was analysed
106 since it is the rhythm strip regularly registered by default in this tertiary
107 centre, due to the easy visualization of the presence/absence of P-waves.

108 There were 41 paroxysmal and 145 persistent patients, whose AF cat-
109 egorization was defined according to the current guidelines [3, 4, 5]. This
110 cohort results in a study different from the several references which have
111 studied the AF termination and differentiation based on the Physionet AF
112 Termination Database [6] and Long-Term AF Database [7], which consider
113 paroxysmal patients (as those with self-terminating short episodes) and sus-
114 tained AF when it lasts for more than 24 hours, most of which correspond
115 to permanent AF.

116 Furthermore, as the number of subjects included in each group is clearly
117 unbalanced (since the number of paroxysmal patients is about a quarter of

118 the total number of persistent subjects), we have divided the patients into
119 two different data sets: 40 patients (20 paroxysmal and 20 persistent) to train
120 the classifier, and 146 patients (21 paroxysmal and 125 persistent) to be used
121 as the test dataset. This dataset includes a huge variety of patients who are
122 under different antiarrhythmic drugs, some who have undergone catheter
123 ablation, some who present other comorbidities, and with different state
124 of progression of the arrhythmia (including first AF episodes and recurrent
125 ones). Thus, this dataset diversity is similar to the patients heterogeneity
126 that clinicians must deal with in their daily activity. Clinical characteristics
127 of the subjects included in the present study are shown in Table 1.

128 **3. Methods**

129 *3.1. Signal preprocessing*

130 The first step when processing the ECG signal was to remove the baseline
131 and powerline noise. Then, we upsampled the signal to 1000Hz so as to
132 the R peak detection [26] and their alignment were more accurate for the
133 subsequent QRST complex subtraction [27]. Next, we took advantage of the
134 uncoupling of atrial and ventricular activities during AF, and we extracted
135 atrial activity by suppressing the QRST complexes of the ECG signal using
136 the method presented in [28], since the average beat subtraction is the most
137 widely used method when single-lead information is available.

138 Thus, we canceled the ventricular activity of the ECG signal prior to
139 processing the Fast Fourier Transform (FFT) [29]. Afterwards, the respective

140 coefficients of sparse representations with respect to a Gabor frame calculated
141 for FFT modulus and phase values are obtained, as it is detailed in the
142 subsequent sections. Henceforth, for the sake of simplicity, we will refer to
143 them as sparse coefficients.

Table 1: Statistical summaries of the database (n,%). Hypertension was defined as a systolic blood pressure $\geq 140mmHg$, a diastolic blood pressure $\geq 90mmHg$, or if the patient was prescribed antihypertensive medication(s). Diabetes mellitus was defined as serum fasting glucose $\geq 7.0mmol/L$ or on medications. Hypercholesterolemia was defined as cholesterol $\geq 6.4mmol/L$ or treatment with lipid-lowering drugs. Structural heart disease is defined as LV hypertrophy $> 15mm$, $LVEF < 50\%$, moderate or greater degrees of valvulopathy, prior myocardial infarction, significant coronary artery disease or the presence of primary myocardial diseases. AF: Atrial fibrillation. LV: left ventricle. Parox: paroxysmal, Pers: persistent, according to current clinical guidelines.

	Parox. AF (n=41)	Pers. AF (n=145)	Overall (n=186)	p-value
Age (mean, range)	59 (30-92)	65 (39-84)	63 (30-92)	0.043
Male (n,%)	22 (54%)	90 (62%)	112 (60%)	0.429
Hypertension	23 (56%)	91 (63%)	114 (61%)	0.554
Diabetes	5 (12%)	46 (32%)	51 (27%)	0.023
Hypercholesterolemia	12 (29%)	55 (38%)	67 (36%)	0.403
Any structural heart disease	12 (29%)	84 (58%)	96 (52%)	0.002
Valvular heart disease	7 (17%)	53 (37%)	59 (32%)	0.030
Impaired LV function	5 (12%)	34 (23%)	39 (21%)	0.174
Previous electric cardioversion	2 (5%)	16 (11%)	18 (10%)	0.380
Previous AF ablation	0 (0%)	11 (8%)	11 (6%)	0.149
Left Atrium dilatation	6 (15%)	48 (33%)	54 (29%)	0.035
Antiarrhythmic drugs	15 (37%)	51 (35%)	66 (35%)	1
Betablockers	14 (34%)	73 (50%)	87 (47%)	0.097
Digoxin	2 (5%)	22 (15%)	24 (13%)	0.141
Calcium channel antagonists	1 (2%)	10 (7%)	11 (6%)	0.488

144 3.2. Frames

145 We index the components of a signal vector f in \mathbb{C}^L by $\{0, 1, \dots, L-1\}$
 146 and we write $f(k)$ for the k -th component of f , so that $f = [f(0), f(1), \dots, f(L-$
 147 $1)]$. Moreover, we identify each vector f in \mathbb{C}^L with an L -periodic sequence
 148 indexed in \mathbb{Z} . In what follows $\langle \cdot, \cdot \rangle$ denotes the usual inner product in \mathbb{C}^L
 149 and $\|\cdot\|$ is the euclidean norm.

A family of vectors $(\varphi_j)_{j=0}^{J-1}$ in \mathbb{C}^L is called a *frame* for \mathbb{C}^L if there exist constants $0 < K_1 \leq K_2$ such that

$$K_1 \|f\|^2 \leq \sum_{j=0}^{J-1} |\langle f, \varphi_j \rangle|^2 \leq K_2 \|f\|^2 \text{ for all } f \in \mathbb{C}^L.$$

The numbers $\langle f, \varphi_j \rangle$, $0 \leq j \leq J-1$, are called the *frame coefficients* of f . Associated to any family of vectors $(\varphi_j)_{j=0}^{J-1}$ in \mathbb{C}^L one has *the analysis operator*

$$A : \mathbb{C}^L \rightarrow \mathbb{C}^J \text{ defined as } A(f) = (\langle f, \varphi_j \rangle)_{j=0}^{J-1}$$

and its adjoint *the synthesis operator*

$$A^* : \mathbb{C}^J \rightarrow \mathbb{C}^L, \quad A^*(\gamma) = \sum_{j=0}^{J-1} \gamma(j) \varphi_j, \quad \text{where } \gamma = [\gamma(0), \gamma(1), \dots, \gamma(J-1)].$$

150 Hence, the family $(\varphi_j)_{j=0}^{J-1}$ is a frame for \mathbb{C}^L if and only if A is injective or
 151 equivalently, if and only if A^* is surjective. Thus, $(\varphi_j)_{j=0}^{J-1}$ is a frame for \mathbb{C}^L if
 152 and only if each signal vector f in \mathbb{C}^L can be expressed as a linear combination
 153 of vectors $\{\varphi_0, \varphi_1, \dots, \varphi_{J-1}\}$. Frames in \mathbb{C}^L consisting of L elements are in

154 fact bases. Frames with $J > L$ elements are called redundant. In the case
 155 that the family $(\varphi_j)_{j=0}^{J-1}$ is a frame for \mathbb{C}^L the operator A^*A is called the frame
 156 operator. It is a self-adjoint, positive and invertible operator. This means
 157 that each vector f can be reconstructed from its frame coefficients.

158 For a discrete non-zero window $g \in \mathbb{C}^L$ and $0 \leq k, \ell \leq L - 1$ we write
 159 $(\pi_{k,\ell}g)(n) = g(n - k)e^{-2\pi i \ell n/L}$. Then, $\pi_{k,\ell}g$ represents a translation and
 160 modulation of the window g . The *Gabor transform* $V_g : \mathbb{C}^L \rightarrow \mathbb{C}^{L \times L}$ with
 161 respect to the window g is the injective and linear map defined by

$$V_g f(k, \ell) = \langle f, \pi_{k,\ell} g \rangle = \sum_{n=0}^{L-1} f(n) \overline{g(n - k)} e^{2\pi i \ell n/L}.$$

162 The Gabor system generated by the window g and $\Lambda \subset \{0, 1, \dots, L -$
 163 $1\} \times \{0, 1, \dots, L - 1\}$ is the set of vectors $\{\pi_{k,\ell} g : (k, \ell) \in \Lambda\}$. If the Gabor
 164 system is a frame, we call it a Gabor frame.

A typical choice of Λ is as follows: for $a, b \in \mathbb{N}$ and N, M with $Na =$
 $Mb = L$ we let

$$\Lambda := \{(na, mb) : n = 0, \dots, N - 1, m = 0, \dots, M - 1\}.$$

165 The parameters a and b represent time and frequency sampling intervals. In
 166 order to have a frame, $ab \leq L$. The case $ab = L$ is referred as the critically
 167 sampled Gabor transform and the case $ab < L$ yields an oversampled Gabor
 168 transform. For detailed information about finite frames see the book [30] and
 169 the references therein.

170 In previous work, we analyzed and classified AF episodes by means of
 171 the discrete Stockwell transform. Now our approach is different, we rather
 172 concentrate on the synthesis operator associated to a Gabor frame. Since
 173 the frames we use are redundant, each signal f admits many different repre-
 174 sentations

$$f = \sum_{m,n} \gamma(n, m) \pi_{na,mb} g$$

with the degree of freedom identified with the dimension of the null-space of A^* . We seek for the sparsest representation of a signal as a linear combination of the atoms of a Gabor frame. More precisely, for a signal $f \in \mathbb{C}^L$ and a Gabor frame $\{\pi_{na,mb} g, n = 0, \dots, N-1, m = 0, \dots, M-1\}$ where $MN \gg L$ we look for the coefficient vector $\gamma \in \mathbb{C}^{M \times N}$ solving the convex optimization problem

$$\text{Minimize } \sum_{n,m} |\gamma(n, m)|, \quad \text{subject to } f = \sum_{m,n} \gamma(n, m) \pi_{na,mb} g.$$

175 The implementation to obtain the sparse coefficients has been made by using
 176 the LTFAT toolbox. For detailed information about the methods see [31].

177 3.3. Principal Component Analysis

178 Principal Component Analysis (PCA) provides a new coordinate system
 179 such that the new axes point into the directions of highest variance of the
 180 data [32]. Each new variable (called *principal component*) is obtained as a

181 linear combination of the original variables, so that each principal component
182 is orthogonal to the rest. In this manner, redundant information can be
183 suppressed and the number of features that feed the classifier can also be
184 reduced.

185 To that end, each axis is chosen consecutively in the direction where the
186 variance of the original data is maximum. These are the eigenvectors of the
187 covariance matrix of the data, which correspond to the respective eigenval-
188 ues once they have been decreasingly ordered. Then, the new variables are
189 obtained by projecting the original ones on the new axis.

190 We have performed PCA on the sparse coefficients in order to reduce the
191 number of significant features by keeping most of its relevant information.

192 3.4. Feature extraction

193 Once the modulus and phase of the FFT input are processed to obtain the
194 sparse coefficients, we apply PCA analysis to each subset after their linear
195 normalization to the range [0,1]. This way, PCA helps to reduce the number
196 of features to be considered. In addition, we also calculate the logarithm of
197 the energy entropy for each group of the sparse coefficients, which is defined
198 as:

$$E(s) = \sum_i \log(s_i^2) \quad (1)$$

199 with the convention $\log(0) = 0$, where s_i refers to each element of the repre-
200 sentation of the sparse coefficients in the principal component space. These
201 features will measure the degree of complexity of the sparse coefficients of

202 the frame.

203 Below, the flowchart shown in Figure 1 depicts the steps of the proposed
204 method, where the classifier is feeded with:

- 205 • Entropy of the sparse coefficients of the modulus of the FFT in the
206 principal component space, E_m .
- 207 • Entropy of the sparse coefficients of the phase of the FFT in the prin-
208 cipal component space, E_p .
- 209 • The first four principal components of the sparse coefficients of the
210 modulus of the FFT input $S_{m_k}, k = 1, \dots, 4$.
- 211 • The first two principal components of the sparse coefficients of the
212 phase of the FFT input $S_{p_k}, k = 1, 2$.
- 213 • Average of distance between R peaks in the ECG signal RR_{mean} .

214 Classifier details are described in Section 3.5.

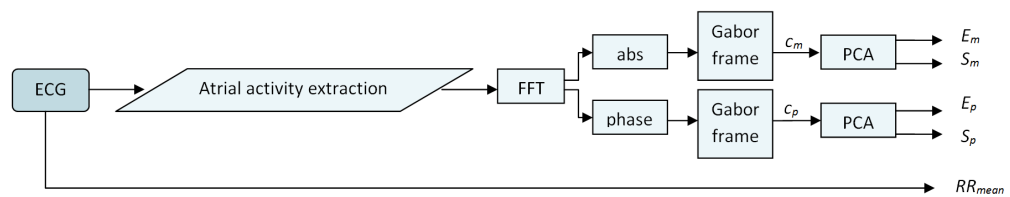


Figure 1: Flowchart of proposed features extraction method.

215 3.5. Classification

216 We have used linear discriminant analysis (LDA) for classifying patients,
217 which is an efficient and low computational cost method [33]. LDA's objective
218 is to reduce the dimensionality of the data and also to preserve most of the
219 class discriminatory information by means of a model which assumes that
220 both classes are linearly separable. Thus, if we assume that patients are
221 classified into two classes, Fisher's linear discriminant [34] pursues to obtain
222 the optimal hyperplane that maximises the separability of the feature vectors
223 x . In order to find it, it is necessary to define a measure of separation between
224 the projections, which should maximise the differences between the means
225 projected on the hyperplane while also minimise the scatter (or variance)
226 within classes.

227 In this study the LDA classifier was trained with 20 paroxysmal and 20
228 persistent AF episode signals, which were chosen by clinicians as those cor-
229 responding to patients who behave as 'clinical models' for each class (parox-
230 ysmal and persistent), in which AF patients are sorted according to current
231 clinical guidelines. Given the unbalanced number of paroxysmal and persis-
232 tent AF subjects that form the population under study, the use of jackknifing
233 or leaving-one-out techniques was not a suitable option, since they produced
234 biased results. We have carried out bootstrap analysis [35] with different
235 number of training samples in order to choose their optimal size. It was
236 observed that performances progressively increased as long as the number of
237 samples used to train the classifier grew up to 40 training samples, meanwhile

238 thereafter there was little or no-significant average increment in performance
 239 figures. Thus, we chose to train our classifier with 20 paroxysmal and 20
 240 persistent subjects.

241 4. Results

242 4.1. Performance measures

243 Sensitivity and specificity are defined as the ratio of paroxysmal or per-
 244 sistent AF patients correctly classified to the total number of paroxysmal or
 245 persistent patients, respectively:

$$Sensitivity = \frac{TP_{paroxysmal}}{TP_{paroxysmal} + FP_{persistent}} \quad (2)$$

$$Specificity = \frac{TP_{persistent}}{TP_{persistent} + FP_{paroxysmal}} \quad (3)$$

246 where TP (true positives) refers to the number of patients correctly classi-
 247 fied according to its AF subtype, and FP (false positives) is the number of
 248 paroxysmal or persistent patients misclassified.

249 In addition, global accuracy is measured by means of average accuracy
 250 (4), in order to eliminate the influence of the unbalanced test dataset with
 251 the number of persistent patients being about 4 times larger than the number
 252 of paroxysmal subjects:

$$Average\ accuracy = \frac{Sensitivity + Specificity}{2} \quad (4)$$

253 Classification performance has also been measured by means of the re-
254 ceiver operating characteristic (ROC) curve, which plots sensitivity against
255 (1-specificity), and by the area under the ROC curve.

256 *4.2. Experimental results*

257 This section contains the classification performances obtained for the pro-
258 posed method (first row of Table 2), and a comparison with several recent
259 references of the state-of-the-art that address the analysis of spontaneous
260 self-termination AF, or sustained and permanent AF.

261 In the proposed method, both sparse representations of modulus and
262 phase information were with respect to Gabor frames, whose parameters have
263 been iteratively adjusted, in order to maximise the average accuracy when
264 classifying the training dataset. Length of each analysed signal was 4096
265 samples, whereas the number of shifts N and the number of modulations M
266 were experimentally set in both frames to 64 and 256, respectively.

267 Table 2 shows that the proposed method outperforms other recent refer-
268 ences (addressed to study self-terminating and sustained AF) when classify-
269 ing the patients included in our database, obtaining about 89% of average
270 accuracy, and sensitivity and specificity performances about 95% and 82%,
271 respectively. These values represent an improvement of global accuracy about
272 5-10% with respect to the other two works that perform best [10]-[13]. These
273 results can also be observed in Figure 2, which displays the Receiver Oper-
274 ating Characteristic (ROC) curve for the proposed classification method, as

275 well as the respective ROC curves for other relevant references. The values
 276 of the areas under convergence (AUC) for each ROC curve are also detailed,
 277 which additionally support results indicated in Table 2.

278 Nevertheless, this comparison should be carefully evaluated, since the
 279 clinical AF classification problem is not equivalent, and clinical databases are
 280 different indeed. Discussion about this remark will be enlarged in Section 5.

Table 2: Classification results for the test dataset (146 patients: 21 paroxysmal and 125 persistent). LDA classifier has been trained with 20 paroxysmal and 20 persistent AF patients. Results for the proposed method are also compared on the same test dataset with relevant references of the state-of-the-art which analyse AF.

Features	Sensitivity	Specificity	Average accuracy
Proposed	0.9524	0.8240	0.8882
Dominant frequency of AA [7]	0.2857	0.7440	0.5149
Dominant frequency of AA, heart rate distance between R peaks [13]	1	0.672	0.836
Sample entropy [15]	0.3810	0.6480	0.5145
Phase variations of GFT [10]	0.8095	0.7840	0.7877

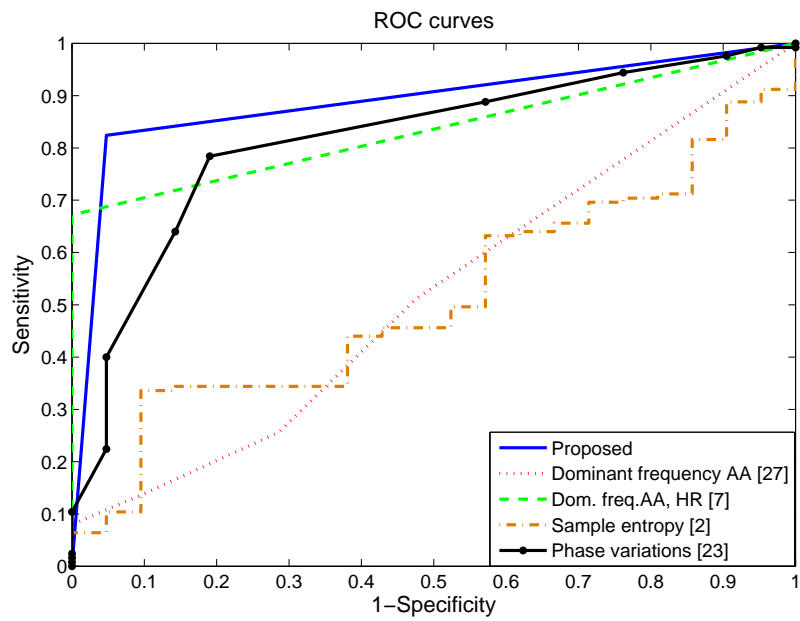


Figure 2: Receiver operating characteristic curves for the proposed method and several recent references. ROC curves have been obtained for the test dataset (146 patients: 21 paroxysmal, 125 persistent). Corresponding areas under ROC curves are: 0.8953 for the proposed method, 0.5168 for [7], 0.8360 for [13], 0.5109 for [15], and 0.8154 for [10].

281 5. Discussion

282 In this paper, classification of paroxysmal and persistent AF episodes
283 according to current clinical guidelines has been studied by means of frame
284 analysis. Good performances have been obtained, which may be of great
285 utility in order to provide clinical assessment to help clinicians to choose the
286 most suitable and effective treatment for patients under AF.

287 The lack of access to Holter recordings of patients included in the ret-
288 rospective study was a major drawback, as the common duration of ECG
289 recordings stored at the tertiary centre where the research was conducted
290 was 5 seconds of length. Therefore, this study aimed for classification of AF
291 episodes by processing very short ECG segments. Although this difficulty
292 was overcome and good results were obtained (details on Table 2 and Figure
293 2), even including patients with multiple pathologies and different state of
294 progression of the arrhythmia (Table 1), the comparison with other methods
295 which have studied AF termination should be carefully evaluated by two main
296 reasons. First, because the clinical problem presented in this paper is not
297 exactly the same as the one proposed in other references, such as [13, 15, 14]:
298 most of them study spontaneous self-termination of AF versus sustained AF
299 for 24 hours based on Physionet AF Termination and Long-Term databases
300 [6, 7] whereas we have proposed the classification between paroxysmal and
301 persistent AF episodes according to current guidelines [3, 4, 5]. Second, some
302 references in Table 2 may not perform optimally and offer poorer results due
303 to the short length of the recordings used in this retrospective study. Doubt-

304 less, they would have performed more properly if we had had long recordings
305 on the same dataset, which unfortunately is not possible currently.

306 Another limitation of the cohort of consecutive unselected patients was
307 that AF subtypes were unbalanced in number: there were about four times
308 more persistent than paroxysmal AF patients. Moreover, it is important
309 to remark that the clinical cost of misclassification is higher for paroxysmal
310 patients than for those persistent. This is due to the fact that an early parox-
311 ysmal atrial fibrillation detection allows a preventive AF treatment against
312 recurrence, such as pulmonary vein isolation, which has been proved to be one
313 of the best options to stop AF progression. Despite the unbalanced dataset,
314 the proposed method obtains not only unbiased results (89% of average ac-
315 curacy), but also about 95% of paroxysmal subjects properly classified.

316 Regarding feature extraction, along the study we tried to characterize
317 the AF subtypes features by using several types of frame, but Gabor frames
318 were the ones which provided the best classification results. For AF analy-
319 sis and spontaneous self-termination prediction, most of the state-of-the-art
320 references have hitherto included Fourier analysis, time-frequency analysis
321 or even non-linear measures of the atrial activity. As previous works have
322 pointed out [10], patients suffering from a paroxysmal AF episode present
323 lower phase variations when studying both the time and frequency domains
324 of the ECG signal. From a physiological point of view, this is explained by the
325 fact that paroxysmal atrial fibrillation patients have lower levels of atrial fi-
326 brosis when compared with persistent atrial fibrillation patients. These lower

327 levels of fibrosis are translated into a faster and more homogeneous electrical
328 conduction in the atrium of patients with paroxysmal atrial fibrillation which
329 may be expressed by lower phase variations.

330 This idea is also related with the results presented in this work. The
331 representation of a signal obtained by the different time-frequency transforms
332 is related with the concrete representation that can be obtained by means
333 of the frame coefficients of the signal with respect to a particular frame.
334 However, if the frame is highly redundant (as it is proposed in this paper),
335 we can obtain many representations of the signal as linear combinations of
336 the frame atoms. Thus, the choice of the sparsest representation fulfilled in
337 this paper has allowed us to improve classification performances by choosing
338 the most suitable representation in that frame. In this manner, presented
339 results reveal that Gabor frames are an efficient and excellent alternative to
340 the aforementioned tools for signal analysis. This different point of view has
341 been successfully applied to ECG compression [20, 21] and atrial activity
342 extraction [24] but, to our knowledge, this is the first attempt to use it
343 for early differentiation of AF episodes, with a significant improvement with
344 respect to previous references that have addressed this classification problem.

345 With regard to clinical implications, it is highly significant to notice the
346 importance of an early differentiation of the nature of the AF episode to
347 which clinicians have to face with. The standard therapy for paroxysmal AF
348 patients who present recurrences despite the antiarrhythmic drug treatment
349 is the catheter ablation procedure implying pulmonary vein isolation. In this

350 context, ablation offers success rates at one year of 70-80%. On the con-
351 trary, success rates of pulmonary vein isolation in persistent AF patients are
352 much worse, around 45-60% at best. The efficacy of ablation in persistent
353 AF patients can be improved by performing additional ablation lines (in the
354 left atrial roof, mitral isthmus or posterior wall), or by ablation of complex
355 fractional atrial electrograms (CFAEs) besides the pulmonary vein isolation.
356 This is why the early knowledge of the type of the arrhythmia of each pa-
357 tient may have vital therapeutic implications, such as the modification and
358 individualization of the therapy to be administered to each patient. Fur-
359 thermore, the proposed method achieves this goal using a widely available
360 resource in daily clinical practice (the ECG), and with no need of any further
361 exploration to the ones which are routinely carried out in these patients.

362 **6. Conclusions**

363 A new classification method of paroxysmal and persistent AF episodes
364 has been presented. It is based on extracting the coefficients of a sparse
365 representation with respect to a Gabor frame, which have been obtained from
366 the frequency spectrum of the atrial activity of short ECG segments. Then,
367 extracted features pass through an LDA classifier, which has been trained
368 to maximise both sensitivity and specificity measures. Good results on real
369 ECG recordings are achieved, which is important to remark as a value-add
370 of the study, specially taking into account that they are obtained on a cohort
371 of patients who present different states of AF progression, are under different

372 antiarrhythmic treatments, and some of which present multiple pathologies.
373 Future work will focus on enlarging the dataset and analyse results on a
374 prospective study with long recordings.

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379 **Competing interests**

380 None declared

381 **Ethical approval**

382 Ethical approval was obtained by the participating centres: Hospital Uni-
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384 Patients also signed an agreement allowing to use their data for clinical stud-
385 ies.

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