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Additional Information

# Enhanced design methodology of a low power stall regulated wind turbine. BEMT and MRF-RANS combination and comparison with existing designs

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## Abstract

Wind energy importance has increased over the past decades. Energy generation by small turbines installed near urban locations has experienced noticeable growth. This work is focused on the development of a design methodology for a low power blade well suited for all the wind operation conditions.

First, a complete Design of Experiments will be presented using the low computational cost tool Blade Element Momentum Theory (BEMT) in order to discard those designs which are clearly not suited to the requirements of the system. Later, the remaining were analyzed using a Computational Fluid Dynamics (CFD) methodology in order to account for three dimensional effects. The value of the left slope of the non-dimensional power curve has been found to be a key parameter for the design.

This methodology has been validated with experimental results available from NREL Phase VI wind turbine, allowing to conclude that BEMT is capable to provide with pre-design accurate results which, nevertheless, should be corrected by CFD.

The results of the proposed design are analyzed and compared to the CFD predictions of a commercial existing blade designed to comply with similar working. For the proposed design, predictions indicate better behavior in terms of maximum power and controllability.

*Keywords:* wind turbine, aerodynamics, BEMT, CFD, RANS, fluid dynamics, blade design, design of experiments, MRF, Moving Reference Frame

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## 1. Introduction

Due to the possible severe climate changes resulting from global warming, there exists a new active interest on the development of renewable energy. In particular, over the past two decades, the percentage of the energy generated by wind turbines has constantly been increased [1], with an annual average increase of 28% since the 1990s. By the 2020s, it is expected that the wind power will generate around 1200 GW, a 12% of the total energy production. In this context, approximately a 3% of the total capacity is expected to be introduced in the domestic market [2].

One of the most critical features to be concerned about during the development of a wind turbine is the blade. After that, the next step is the development of a control system for the generator and the gear box. Thus, the optimization of both the blade shape and the location of the turbine-farms is of primal interest during the development of new designs [3].

This considerable percentage makes that small wind turbines (SWT) with low maximum power generation (up to 50 kW, in accordance with IEC 61400-2 [4]) are becoming especially interesting. Generally, small wind turbines do not have pitch adjustment to optimize angles of attack at different working conditions being thus necessary to perform a passive optimization for a wide range of wind and rotation velocities.

Due to the characteristics of this kind of wind turbines, which are essentially serial-produced, improvement of the wind turbine blade geometry becomes important even from early stages of the design process. Even though some

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17 interesting optimization solutions have been proposed in the literature (see Roshan et al. [5]) their application is rather  
18 costly, and thus simpler ways of enhancement are worth to be investigated.

19 During the design phase, predictions of the wind turbine performance are of interest from cost reduction point of  
20 view. In this context, tools requiring low computational cost are normally used. Among these tools, the Blade Element  
21 Momentum Theory (BEMT) has been extensively used for studying blade geometries both at design conditions or at  
22 off-design (see, for instance Lee et al. [6] or Benini and Toffolo [7]).

23 The main assumption of BEMT is that the flow can be assumed to be nearly 2D at each airfoil section of the wind  
24 turbine. The 2D assumption does not allow to predict the stall-delay phenomenon and could lead to an underestimation  
25 of the power generated at near post-stall working points [8]. While some models have been developed to account for  
26 this effect [9], here any 3D issues will be considered at a later stage.

27 BEMT allows to define geometries which maximize the power produced at the design point of the wind turbine  
28 [10]. Nevertheless, as the wind turbine needs to behave correctly during some off-design stages, the simple criteria  
29 of maximizing the design power is not valid anymore. In this paper, BEMT methodologies are explored and used  
30 in order to select a configuration which complies with power and control requirements for a wide range of operating  
31 conditions.

32 When a design is obtained by using BEMT methodologies, the resulting predicted performance needs to be cor-  
33 rected in order to account for possibly important 3D effects [11]. Computational Fluid Dynamics (CFD) is generally  
34 used with this aim with different complexity levels. For instance, Tran and Kim [12] performed URANS computations  
35 of a complete wind turbine under surge motion and found how the effects of the inclusion of the tower were relatively  
36 small in comparison with the mean generated power. Similar conclusions can be extracted from Mo et al. [13], who  
37 used Large Eddy Simulation (LES) to study the complete NREL Phase VI wind turbine. Thus, the using of a station-  
38 ary calculation formulated at a Moving Reference Frame could lead to an important reduction on the computational  
39 time.

40 Note that the previous assumption is only partially valid when dealing with the prediction of the behavior of arrays  
41 of wind turbines, as can be deduced from the works of Kang et al. [14] or Santoni et al. [15]. However, it also should  
42 be noted that, when dealing with low power wind turbines, they are normally installed in isolated configuration and,  
43 furthermore, as their characteristic length is lower, the distance at which wakes are also of important influence will  
44 also be lower.

45 Some studies can also be found in the literature where the elastic deformations of the blades are taken into account.  
46 For example, Pourrajabian et al. [16] calculated the flexure solicitations over the blades and they were found to be  
47 small compared with the wind turbine dimensions. Similar results can be found in Ponta et al. [17].

48 About the experimental validation of this kind of flows, the National Renewable Energy Laboratory (NREL)  
49 provides with an important amount of information. An important amount of the published literature is based on the  
50 validation and comparison of computations with such measured data ([18], [19]). For instance, Esfahanian et al.  
51 [20] performed a CFD and BEMT computations over the NREL Phase II wind turbine showing applicability of both  
52 methods. Similar conclusions were obtained by Yelmule and EswaraRao [21] for the NREL Phase VI.

53 This paper presents a proposal of an enhanced blade design methodology which allows definition of designs  
54 which are complying not only with the objective of maximizing the produced power under optimum conditions but  
55 also introduces additional requirements to consider controllability issues. The design methodology consists on an  
56 initial wide discard of possible blade geometries using BEMT, followed by a RANS study, to discard unsuited cases  
57 from a reduced number of designs, as will be explained later.

58 During this work, a classic BEMT methodology was used in order to obtain an enhanced design of a low radius  
59 wind turbine. However, BEMT models take into account hypothesis that could lead to inaccurate results, mainly in  
60 situations with significant flow separation and when 3D effects become important. As a consequence the final designs  
61 must be studied using computational tools which allow to account for these effects, as CFD. Therefore, the main aim  
62 of this process is to (a) perform a Design of Experiments (DOE) in order to generate a geometry which is optimum not  
63 only from the point of view of maximum possible generation of energy, but also exhibits an acceptable behavior under  
64 working conditions out of the design (mainly, blade capability of standing under high winds velocities by means of  
65 an improved controllability). For this target BEMT is used for obtaining the features of all the geometries generated  
66 during the DOE and to discard those whose behavior is found to be unacceptable. Due to the already commented  
67 limitations of this theory, the resulting blade families which were not discarded must be later studied using a three

68 dimensional methodology (like RANS) in order to ensure they are still complying with requirements and discard those  
69 which do not.

70 The second aim of the work is (b) compare the resulting design with other commercial wind turbine of similar  
71 characteristics both in terms of maximum power generation and controllability.

72 About the necessity of performing a design that is able to stand under high wind velocity environment, it is known  
73 that, for a stall regulated horizontal axis wind turbine (HAWT), it is crucial to have into account the potential risk of  
74 circuit burnout or structural failure for wind velocities over a critical value ([21], [22]). In this context, in this article,  
75 it will be shown how the left slope of the blade non dimensional power curve is found to be a key design parameter,  
76 not fully explored in the literature, in order to obtain a design able to produce power in a wide range of wind velocities  
77 avoiding this risk.

78 In order to assess with this target, the work flow must be structured as sketched by Figure 1. Three main blocks  
79 can be identified on the structure of this article: First, it is necessary to develop and validate both a CFD and a BEMT  
80 methodology. This will be found during sections 2 and 3, where this validation is performed against the available  
81 experimental data about NREL Phase VI.

82 Once the methodology has been proven to provide with good results, a set of experiments will be designed and  
83 calculated by using BEMT, which, due to its affordable computational expense, allows a good first approximation  
84 for the behavior of a complete set of candidate geometries. The second step at this stage will be the selection of  
85 a reduced family of candidate geometries, which will be analyzed using CFD in order to correct the BEMT results  
86 having into account three dimensional effects and discarding those which become unsuited once these computations  
87 are performed. This work stage can be found at section 3.1, illustrating only the selection of the final blade and its  
88 comparison with CFD. About the use of RANS to discard other blades proposed in this section, reader can refer to the  
89 end of the section 4.2.

90 Finally, once the final design is proposed, it is necessary to compare it with other existent solutions in order to  
91 check its commercial applicability. In this document, the proposed design was compared against one of the leading  
92 low power wind turbines, the commercial blade *Skystream*. As this design is characterized by a curved blade, three  
93 dimensional effects will highly affect its behavior, so this will only analyzed via the CFD methodology. The addition  
94 of other aerodynamic components, like a Vortex Generator (VG) will be also analyzed and discussed. This stage  
95 is developed during the section 4.2, where reader will also find a detailed discussion of the controllability of the  
96 commercial blade, the proposed design and an alternative geometry, which was valid in accordance with BEMT  
97 methodology but, when RANS corrections were performed, it was found to not provide with an acceptable behavior  
98 in terms of control and, in consequence, was discarded.

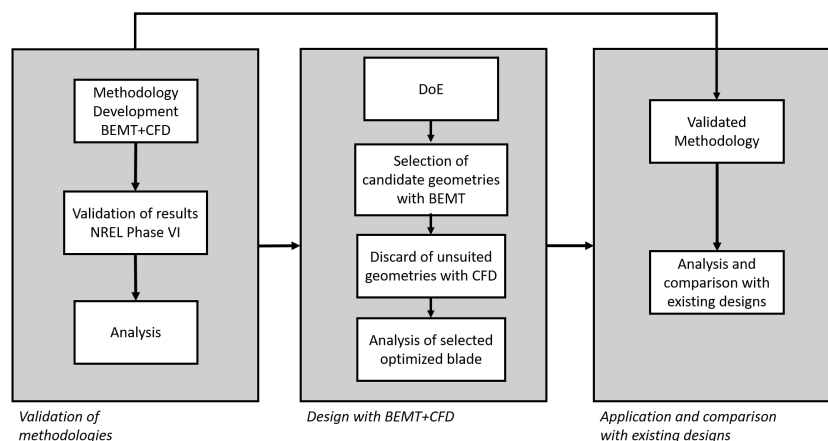


Figure 1: Work flow sketch



## 99 2. Theoretical Background

### 100 2.1. Blade Element Momentum Theory

101 In this paper, the Blade Element Momentum Theory is used in order to predict the steady-state characteristics  
 102 of a set of possible blade designs due to its low computational cost. BEMT models have been extensively used and  
 103 validated in the literature to perform relatively fast/accurate predictions [23].

104 When the flow is assumed to be nearly 2D, a velocity diagram can be stated for an airfoil of the blade located at a  
 105 distance  $r$  with a pitch angle  $\theta$  and a chord  $c$  [24], as shown in Figure 2:

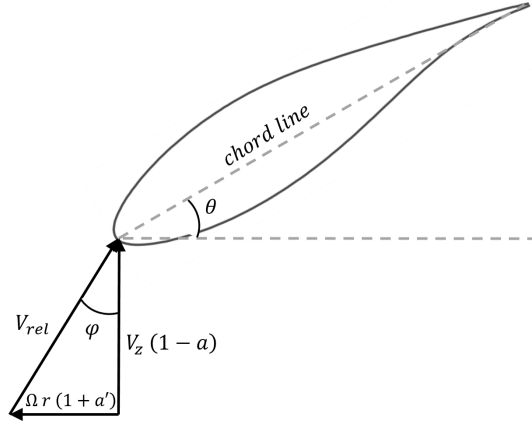


Figure 2: Velocity diagram used for the BEMT explanation at an airfoil section located at radius  $r$

106 Here,  $V_z$  is the wind velocity and  $\Omega$  is the wind turbine rotational velocity, while  $a = v_i/V_z$  and  $a' = \omega'/\Omega$  are  
 107 the axial and tangential induced velocities, respectively.  $V_{rel}$  is the relative wind velocity magnitude, which shows a  
 108 relative angle,  $\varphi$ . These values allow to calculate the angle of attack and the airfoil contribution to the normal force,  
 109  $F_N$ , and power,  $P$ , as follows [10]:

$$\begin{aligned} \tan \varphi &= \frac{V_z}{\Omega r} \frac{1-a}{1+a'} \\ \alpha &= \varphi - \theta \end{aligned} \quad (1)$$

$$dF_N = \frac{B}{2} \rho V_{rel}^2 (C_l \cos \varphi + C_d \sin \varphi) c dr$$

$$dP = \frac{B\Omega}{2} V_{rel}^2 (C_l \sin \varphi - C_d \cos \varphi) c r dr$$

110 where  $B$  is the number of blades conforming the rotor of the wind turbine and  $C_l$  and  $C_d$  are the lift and drag coefficients  
 111 of the airfoil. These are a function of the angle of attack and can be obtained by means of measurements [25] or  
 112 computational studies [20].

113 Once the value of the induced terms  $a$  and  $a'$  is known, the total force and power can be immediately derived as:

$$F_N = \int_0^R dF_N ; \quad P = \int_0^R dP \quad (2)$$

114 The induced factors can be obtained by means of iterative methods. One of the most popular ones starts with  
 115 the formulation of the momentum equation for a differential circumference of width  $dr$ . Then, introducing the non-  
 116 dimensional tip speed ratio  $\lambda = (\Omega R)/V_z$  one may write [10]:

$$dC_T = \begin{cases} 8Fa(1-a)xdx & \text{if } a \leq 2/5 \\ -(4/9)x[-4+a(20-18F)-a^2(25-18F)]dx & \text{if } a > 2/5 \end{cases} ; dC_P = 8Fx^3\lambda^2a'(1-a) \quad (3)$$

117 Here,  $C_T = 2F_N/(\rho\pi R^2V_z^2)$ ,  $C_P = 2P/(\rho\pi R^2V_z^3)$  and  $x = r/R$  are the non-dimensional normal force, power and  
 118 position, respectively. The coefficient  $F$  accounts for the losses at the tip, and one of the most used approximations  
 119 for its determination is based on Prandtl's method (see de Vries [26]):

$$F = \frac{2}{\pi} \cos^{-1} \left[ \exp \left( -\frac{B(1-x)}{2x \sin \varphi} \right) \right] \quad (4)$$

120 Once the induction terms are obtained for each section of the blade and equation (2) is integrated, the power and  
 121 force coefficients of the wind turbine are obtained. An important advantage of the dimensionless form of the equations  
 122 used is that, for a given pitch and turbine geometry, they are a function only of  $\lambda$  and the Reynolds number [27].

## 123 2.2. Reynolds Averaged Navies-Stokes equations

124 In this paper, the fluid flow around an optimum blade shape is modeled by means of the Reynolds Averaged  
 125 Navier-Stokes (RANS) equations formulated on a rotating reference frame. These can be derived from the complete  
 126 set of mass, momentum and energy conservation equations and are shown next for an incompressible flow [28].

$$\begin{cases} \frac{\partial U_i}{\partial x_i} = 0 \\ \frac{\partial U_i}{\partial t} + U_j \frac{\partial U_i}{\partial x_j} = \nu \frac{\partial^2 U_i}{\partial x_j \partial x_j} - \frac{\partial \langle u_i u_j \rangle}{\partial x_j} - \frac{1}{\rho} \frac{\partial p}{\partial x_i} + f_i \end{cases} \quad (5)$$

127 where  $U_i$  represents the component in the  $i^{th}$  direction of the mean velocity field,  $\vec{U}$ ;  $\rho$  and  $\nu$  are the density and the  
 128 kinematic viscosity of the fluid, respectively;  $p$  represents the average pressure field and  $f_i$  is the component on the  
 129  $i^{th}$  direction of the inertial and body forces acting on the fluid. These terms can be evaluated, when the equations are  
 130 formulated in a rotating frame, as follows [29]:

$$\vec{f} = \begin{pmatrix} f_x \\ f_y \\ f_z \end{pmatrix} = -\frac{d\vec{\omega}}{dt} \times \vec{r} + \vec{\omega} \times \vec{\omega} \times \vec{r} \quad (6)$$

131 where  $\vec{\omega}$  represents the rotational velocity of the reference frame, and  $\vec{r}$  is the position vector of a point of the fluid.

132 Closure of equations (5) can only be achieved by modeling the terms  $\langle u_i u_j \rangle$ , which are commonly referred to as  
 133 the Reynolds stresses. The selection of an appropriate turbulence model is of primal importance for the evaluation of  
 134 the flow characteristics. In this paper the  $k-\omega$  model with shear stress transport (SST) will be used with this purpose.  
 135 This turbulence model has been extensively used in the literature for this kind of flows, demonstrating an acceptable  
 136 behavior. As an example, Moshfegui et al. [30] used this model to perform calculations of the NREL Phase VI wind  
 137 turbine with different near wall grid resolutions, obtaining reasonably good results compared with experimental data  
 138 [18]-[19]. Similar results were obtained by Yelmule and EswaraRao [21] with the same turbulence model.

139 The  $k-\omega$  SST model was proposed by Menter [31] and is a transitional model in which the formulation considered  
 140 varies from the  $k-\omega$  turbulence model proposed by Wilcox [32] close to the walls and the  $k-\varepsilon$  model away from  
 141 walls, thus solving the main inconveniences of both models. In addition to a transport equation for the turbulent  
 142 kinetic energy,  $k$ , the  $k-\varepsilon$  and the  $k-\omega$  turbulent models solve a transport equation for the turbulent dissipation  
 143 rate,  $\varepsilon$ , and the specific turbulent dissipation rate,  $\omega$ , respectively. These variables are related by  $\omega \propto \varepsilon/k$  and allow  
 144 obtaining the turbulent viscosity  $\nu_t = C_\mu k^2/\varepsilon$  (being  $C_\mu = 0.09$  a modeling constant). This turbulent viscosity is used  
 145 to model the value of the Reynolds stress tensor as:

$$\langle u_i u_j \rangle = \frac{2}{3} \cdot k \cdot \delta_{ij} - \nu_T \left( \frac{\partial \langle U_i \rangle}{\partial x_j} + \frac{\partial \langle U_j \rangle}{\partial x_i} \right) \quad (7)$$

### 146 3. Methodology

#### 147 3.1. Design of experiments

148 In this section, a geometrical distribution of chord and torsion is proposed and analyzed by using BEMT. An  
 149 important amount of research has been focused on obtaining an optimum maximum power coefficient for a given  
 150 working condition. For instance, Burdett and VanTeuren [33] found an optimized solution for a given tip speed ratio  
 151 assuming that the Reynolds number can affect the 2D airfoil characteristics. It was shown that this influence was  
 152 practically inappreciable.

153 For given design values  $\alpha_d$  and  $\lambda_d$ , Spera [34] demonstrated that optimizing the power coefficient for a blade  
 154 element is equivalent to find the maximum of the function  $f(a, a')$  defined by:

$$f(a, a') = a' (1 - a) \quad (8)$$

155 subject to the condition:

$$(\lambda_d x)^2 a' (1 + a') = a(1 - a) \quad (9)$$

156 Once equations (8) and (9) are solved, for a known airfoil section where  $C_l(\alpha_d) \gg C_d(\alpha_d)$ , its geometrical param-  
 157 eters can be calculated as follows:

$$\begin{aligned} \sigma(x) &= \frac{4a' \sin^2 \varphi}{1 + a' \cos \varphi} \frac{x}{C_l(\alpha_d)} \\ \theta(x) &= \varphi - \alpha_d \end{aligned} \quad (10)$$

158 where  $\sigma(x) = Bc(x)/(2\pi R)$  is defined as the local solidity of an airfoil located at a non-dimensional distance  $x$  from  
 159 the hub.

160 Usually, the value of  $\alpha_d$  is chosen so as to provide the maximum aerodynamic efficiency,  $C_l/C_d$ , at each airfoil  
 161 section for the design tip speed ratio,  $\lambda_d$ . This approximation also allows to obtain a maximum local value for the  
 162 power coefficient, but, however, it can lead to unacceptable performance for out-design points.

163 Due to the cost-performance requirements of low-power wind turbines, it is necessary to minimize the automatic  
 164 control necessities. Thus, to ensure that the automatic control does not have to apply an unacceptable brake torque at  
 165 high wind velocities, the turbine must be effectively stall-regulated. As the generated power scales as  $P \propto C_P V_z^3$  the  
 166 necessity of a stall-regulated turbine leads to the condition  $dP/dV_z < 0$  for the maximum expected wind velocity. This  
 167 can be rewritten in terms of only the tip speed ratio and the power coefficient as:

$$\frac{dC_P}{d\lambda} > \frac{3C_P}{\lambda} \quad (11)$$

168 Equation (11) indicates that, to ensure controllability at maximum wind speed, the  $C_P - \lambda$  curve must have a high  
 169 slope from the left.

170 To guarantee that both the wind turbine is easily controllable and that its maximum power coefficient is also high,  
 171 the simple criterion of taking  $\alpha_d$  for the maximum  $C_l/C_d$  is not sufficiently accurate. Therefore, a design of experi-  
 172 ments (DOE) was defined by varying both  $\lambda_d$  and  $\alpha_d$  and applying Equation (10). Then, the non-dimensional power  
 173 curve was obtained for each possible design. An optimum blade was selected ensuring compliance with Equation (11)  
 174 and considering that the blade should be constructively feasible. The range and step of the parameters considered in  
 175 the DOE were:

$$\begin{aligned} \lambda_d &\in [4.5 - 10.5] & ; & \Delta\lambda = 1 \\ \alpha_d &\in [3 - 12] \text{ deg} & ; & \Delta\alpha = 1 \text{ deg} \end{aligned} \quad (12)$$

176 The NREL S809 airfoil was selected, as it has been extensively studied and has shown to provide good perfor-  
 177 mance [35]. Also, an important amount of information for a wide range of angles of attack is available [25]. This  
 178 airfoil will kept for the whole radius of the wind turbine. Using of a single airfoil is a common practice on the design  
 179 of small wind turbines ([36], [37]). Due to the low size of this kind of wind turbines, all their sections can be consid-  
 180 ered to work under the range of low Reynolds number and, thus, using different airfoils at root and tips should only  
 181 marginally increase the performance of the wind turbine.

182 Once the DOE methodology has been presented, a complete set of candidate geometries will be generated. A  
 183 decision process must be then assessed, as sketched by Figure 3. After a selection of a  $\lambda_{design}$  and  $\alpha_{design}$ , a possible  
 184 geometry will be generated, which will be analyzed using BEMT. If the BEMT calculated design complies with certain  
 185 requirements, which will be explained later, this will be considered as a preliminar candidate and will be analyzed  
 186 using CFD. If similar restrictions are still complied with, the geometry will be considered as a final candidate. If any  
 187 of the requirements is not satisfied at any stage, the blade geometry is discarded.

188 Traditionally, the selection is made mainly by constructive and maximum power criteria. However, for the design  
 189 of a stall regulated wind turbine it is necessary to have into account that the blade should be easily controllable  
 190 in accordance with the left slope condition, Equation 11. Note that, with the current methodology, and depending  
 191 on how the parametric swept is performed, it could be possible that more than one design could arrive to the final  
 192 candidate phase. If this is the case, all the resulting candidates would be valid design and extra conditions could  
 193 be imposed to them (for instance, the design with higher maximum power coefficient could be selected). With the  
 194 conditions of the current work only one geometry complied with the requirements after the CFD decision phase.

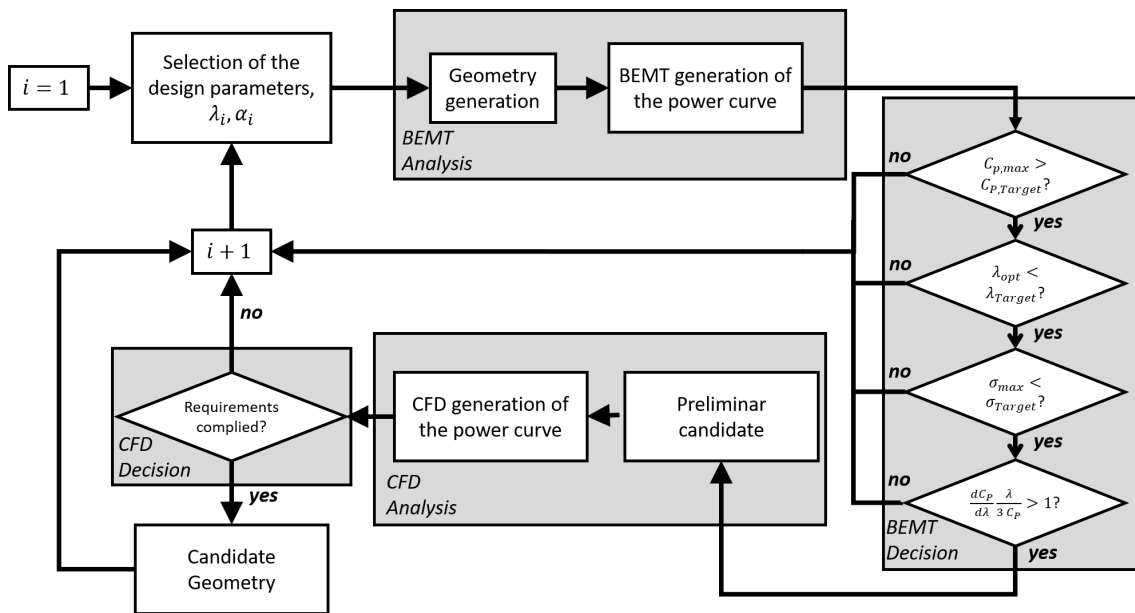


Figure 3: Work flow of the proposed Design of Experiments

195 Once the Design of Experiments has been qualitatively described, it is necessary to establish which value of the  
 196 different parameters will be considered. These are summarized next:

- 197 • The **maximum power coefficient** of the new blade design must be high. In this sense it will be considered that  
 198 the resulting blade should provide a maximum power coefficient at optimum conditions of  $(C_P)_{optim} > 0.37$ ,  
 199 which would correspond with a power generation of approximately  $P = 1500$  W for a blade with radius  $R =$   
 200  $2.50$  m at a wind velocity of  $V_z = 7$  m s<sup>-1</sup>.
- 201 • The optimum **rotational velocity** should be as low as possible in order to minimize radiated noise operating  
 202 under design conditions. In this sense it will be supposed that an acceptable design should present its maximum  
 203 power coefficient at  $\lambda_{optim} < 6.5$ , which would correspond with an optimum rotational velocity of approximately  
 204  $\Omega = 170$  rpm at the conditions of the previous point. It will be shown that RANS predictions will be expected  
 205 to provide a higher estimation of this parameter. In consequence, this constraint will be slightly relaxed during  
 206 the CFD evaluation as the controllability restrictions will be of higher importance. Note how, even with the  
 207 mentioned relaxation of this parameter, the operating rotational speed of the RANS predictions will still be kept  
 208 bounded.

- 209 • As it was previously stated, in order to achieve a geometry which is **easily controllable** for a stall-regulated  
210 blade turbine wind turbine, the left slope of the power curve should be as high as possible. For the purpose of the  
211 current design it will be stated that the new wind turbine should comply with  $\frac{dC_p}{d\lambda} \frac{\lambda}{3 C_p} > 1$  when  $\lambda = 0.85 \cdot \lambda_{optim}$
- 212 • The behavior of the wind turbine for very low values of the tip speed ratio should be acceptable in order to  
213 ensure a correct starting. Note that this is a qualitative statement. As it is expected that for low values of  $\lambda$   
214 the validity of BEMT assumptions are only partially valid, it will also be possible to observe how some BEMT  
215 predicted designs exhibit power coefficients which become negative under certain conditions. This obviously  
216 will not be the case, but it can be assumed that, even with the taken simplifications, the behavior of this design  
217 under low rotational speeds will not be acceptable.
- 218 • The **manufacturing** of the resulting blade turbine should be as simple as possible. In this sense, the maximum  
219 local solidity,  $\sigma$ , (which, as will be seen, will be near to the hub) should never exceed from certain value. If this  
220 solidity is too high it will be difficult to construct the transition between it and the hub. Thus, for the current  
221 work it will be supposed that the design should comply with  $\sigma_{max} < 0.10$ .

222 All the blade geometries complying with the previous constraints will be considered as possible candidates (five  
223 candidates, for the constraints already mentioned). These, will be studied via CFD in order to have into account  
224 3D effects and ensure the so studied design complies with the stated requirements, discarding those which do not.  
225 Although this was performed for all the *BEMT-suited* blades, only the final choice will be shown in section 4.1, for  
226 reasons of brevity. Note also how the second requirement will be slightly relaxed.

### 227 3.2. CFD modeling

228 In order to account for the 3D effects of the flow, the set of Equations (5) are numerically solved in a Moving  
229 Reference Frame (MRF) by means of the Finite Volume Method, using the general purpose commercial package,  
230 *STAR CCM+*, and using a second order upwind discretization. In order to set up the CFD calculation, the rotor NREL  
231 Phase VI was first analyzed and validated against available experimental measurements (see section 3.3). This wind  
232 turbine is formed by 2 blades with radius  $R = 5.11\text{m}$ . The chord and torsion distributions of this wind turbine can be  
233 found in the bibliography ([18]).

234 As, for any operating condition,  $M \ll 0.3$ , the flow can be considered as incompressible. Also, the conservation  
235 equations are formulated in a MRF which moves with the angular velocity of the blade,  $\Omega$ . Formulating equations  
236 in such a reference frame allows to neglect transient effects and resolve only for a stationary mean flow. This last  
237 assumption is well suited as can be observed in the bibliography. For instance, Li et al. [38] performed dynamic  
238 simulations using *Detached Eddy Simulation* (DES) for the NREL phase VI. In this reference it can be found how, for  
239 an optimization purpose, the assumption of a stationary solution is well suited.

240 Other simplification which is to be made is the assumption of periodicity. Thus, a unique blade is being modeled,  
241 allowing to use a reduced domain with an angle  $\Delta\theta = 2\pi/B$ . This assumption has been successfully applied in the  
242 literature [39].

243 Thus the fluid domain is conformed by a truncated cone. The upwind distance is of  $4R$  while the downwind length  
244 is set to be  $8R$ . The inlet radius is of  $4R$  and the outlet radius is  $8R$ , where  $R$  is the blade radius. These dimensions  
245 were set to ensure negligible influence of the position of the boundary conditions.

246 In order to ensure that the result is not dependent on the chosen discretization, the non-dimensional power and  
247 axial force curves are calculated for four different meshes. Figure 4 shows the power (left) and axial force (right)  
248 coefficients as they evolve with the increment of mesh elements,  $N$ . Note how both the power and axial curves  
249 achieve mesh independence with a relatively low number of elements at low values of  $\lambda$  while, for  $\lambda > 5$ , as the flow  
250 is attached to the blade, the necessary number of elements is higher.

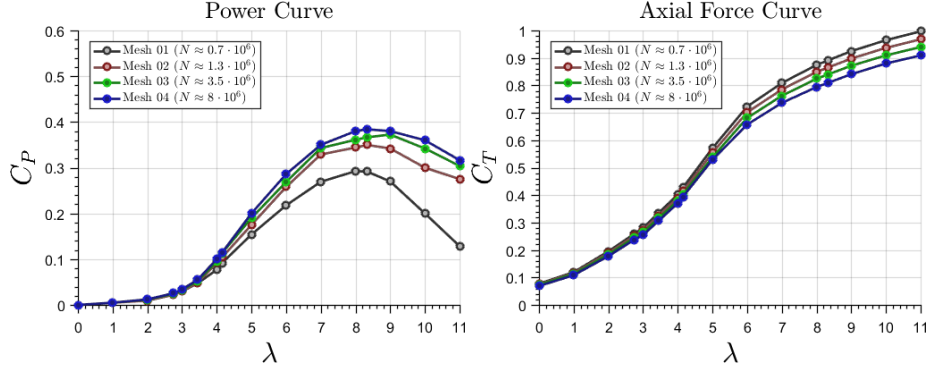


Figure 4: Power (left) and force (right) curves calculated for the blade *NREL Phase VI* using different grid refinements

251 Figure 4 allows to infer that, for fourth studied mesh, mesh independence can be considered to be achieved. In  
 252 order to ensure reproducibility of results, note that this configuratoin corresponds to mean mesh size over the blade of  
 253 approximately  $0.005 R$  and a maximum size far from the blade of  $0.25 R$ . A correct flow resolution just upwind and  
 254 at the wake is of great importance when computing forces and moments over the blade [40]. Thus, a mesh refinement  
 255 zone is set in the wake, with a size of  $0.02 R$ , resulting in a **polyhedral** mesh with  $N = 8120000$  elements.

256 To obtain the non-dimensional power curve of the wind turbine a constant velocity inlet  $V_z = 8 \text{ m s}^{-1}$  is set and the  
 257 rotational velocity is parametrically varied. Under these circumstances the Reynolds number based on the relative tip  
 258 velocity,  $\text{Re} = \rho R \sqrt{V_z^2 + (\Omega R)^2} / \mu$ , varies in the interval  $[2 \cdot 10^6 - 6 \cdot 10^6]$  which is high enough to allow neglecting  
 259 the effects of the Reynolds number on the friction coefficient.

260 The wall  $y^+ = yu_\tau / \nu$  was ensure to be greater than 30 for the major part of the studied geometry, so logarithmic  
 261 wall functions can be used [41]. This can be ensured from the observation of the Figure 5, where the relative cells  
 262 distribution of the wall  $y^+$  are shown for the cases of  $\lambda = 3$  (left) and  $\lambda = 6$  (right). Here, it can be calculated that,  
 263 even for  $\lambda = 3$ , more than the 70% of the wall cells show an  $y^+$  between 30 and 100.

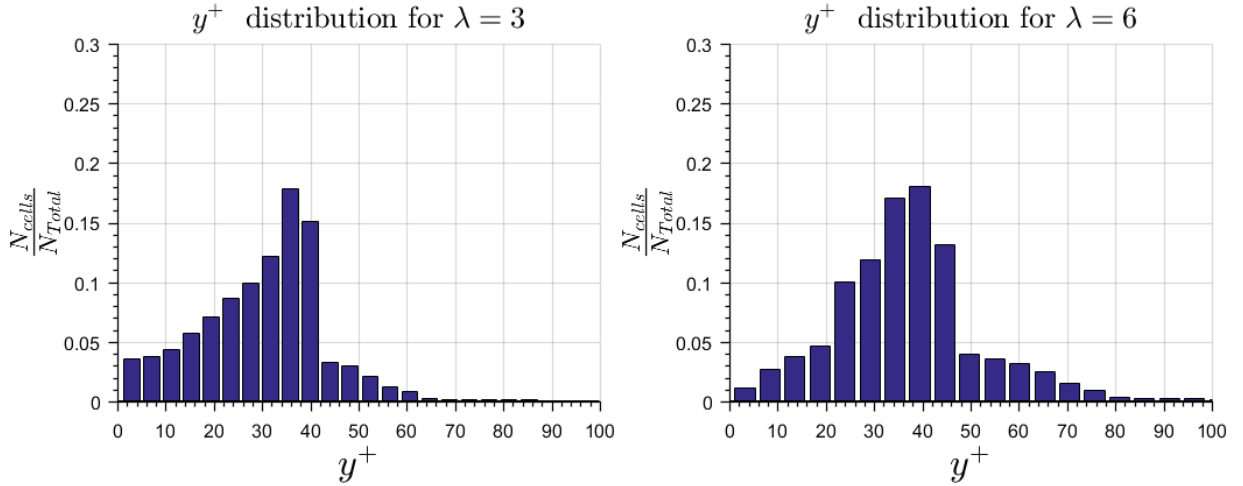


Figure 5: Wall  $y^+$  distribution for  $\lambda = 3$  (left) and  $\lambda = 6$  (right). Calculations performed with the *NREL Phase VI* blade with  $N \approx 8 \cdot 10^6$

264 Once the current numerical methodology was validated against the results of the *NREL Phase VI* bi-blade wind  
 265 turbine (see section 3.3), the same specifications were applied to the optimum three-bladed low power wind turbine  
 266 which will be the main target of the current article. As a result, a sketch of the mesh for this case can be found at  
 267 Figure 6 where all the mentioned refinement levels can be observed at the same time that the angle of the truncated  
 268 cone is found to be  $\Delta\theta = 120 \text{ deg}$ , corresponding to  $B = 3$ .

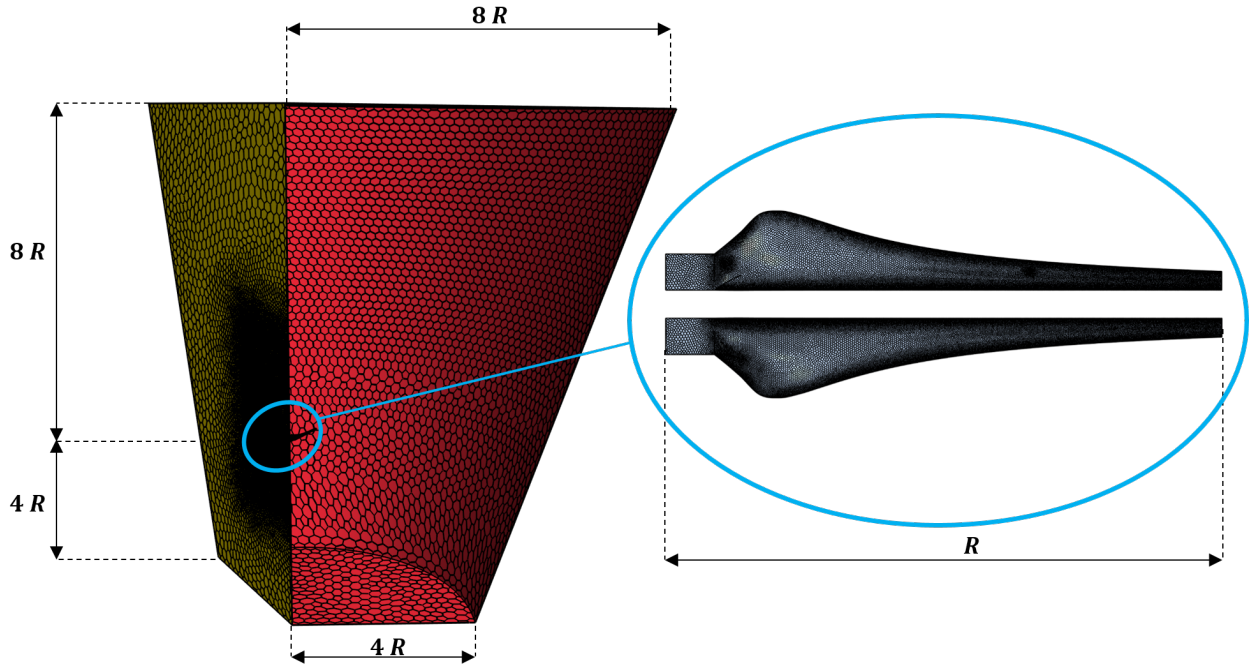


Figure 6: Mesh sketch for a case of a three-bladed wind turbine calculation

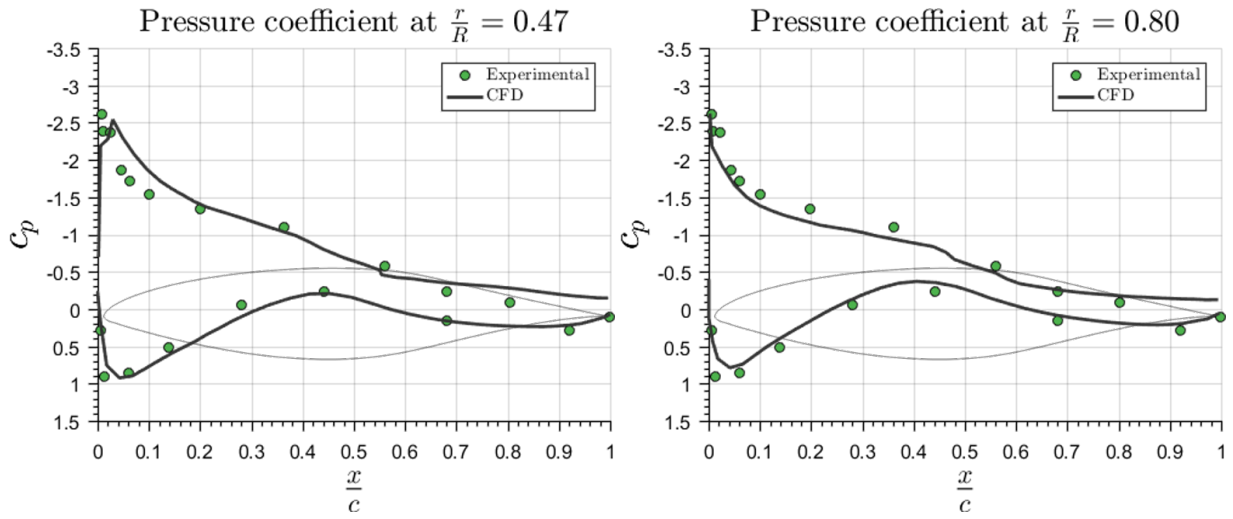
269 *3.3. Model validation*

270 Both the BEMT and the CFD need to be validated against experimental data, for which the NREL Phase VI wind  
 271 turbine was modeled in accordance with the conditions stated in the previous section. The selection of this two-bladed  
 272 wind turbine was made due to the amount of work performed on it found in the literature ([42], [43]) and the available  
 273 experimental data ([18], [19]).

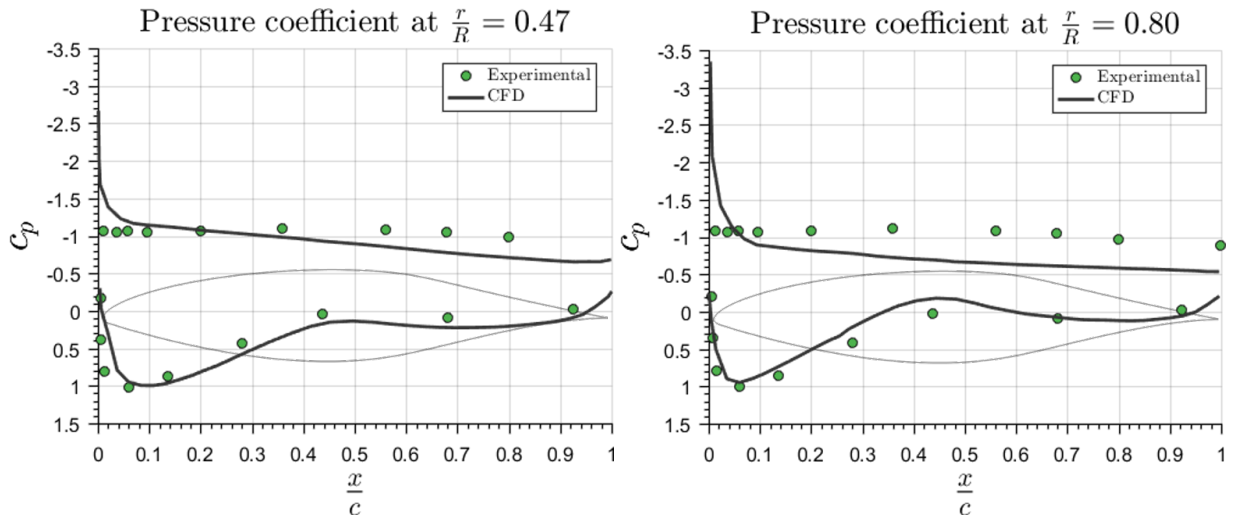
274 Figure 7 shows the evolution of the pressure coefficient,  $C_p$ , along the blade chord for two different radial locations.  
 275 The pressure is non-dimensionalized using the relative wind velocity at each section, as follows:

$$C_p = \frac{p - p_\infty}{\frac{1}{2} \rho (V_z^2 + (\Omega r)^2)} \quad (13)$$

276 It can be observed that the current CFD calculations agree fairly well with the measurements. The agreement is  
 277 slightly worse for low values of  $\lambda$ , for which the local angles of attack are larger [10]. Nevertheless, the results show  
 278 good agreement even under these circumstances.



(a) Pressure coefficient for NREL Phase VI at  $r/R = 0.47$  (left) and  $r/R = 0.80$  (right) for  $\lambda = 6$

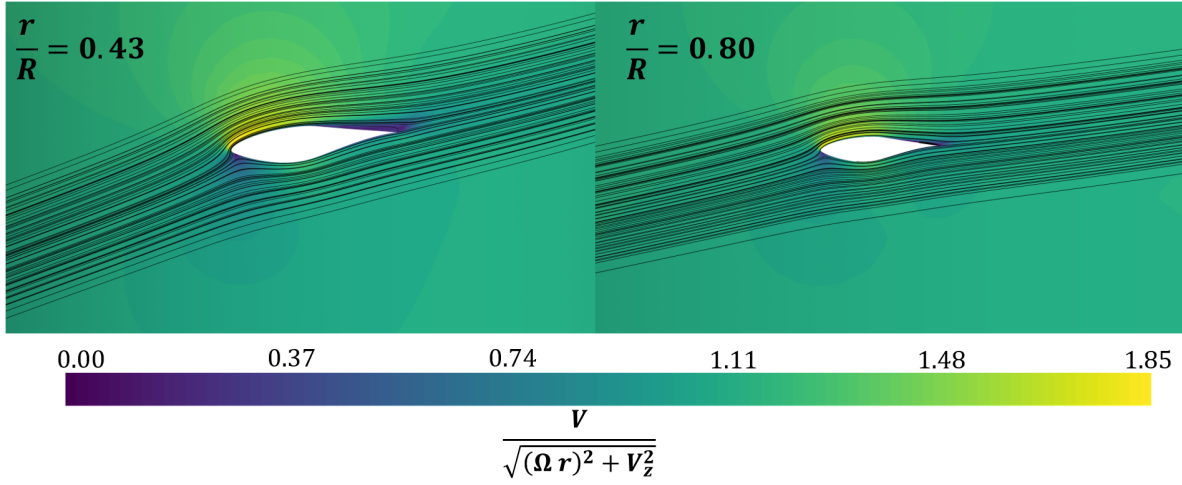


(b) Pressure coefficient for NREL Phase VI at  $r/R = 0.47$  (left) and  $r/R = 0.80$  (right) for  $\lambda = 2.78$

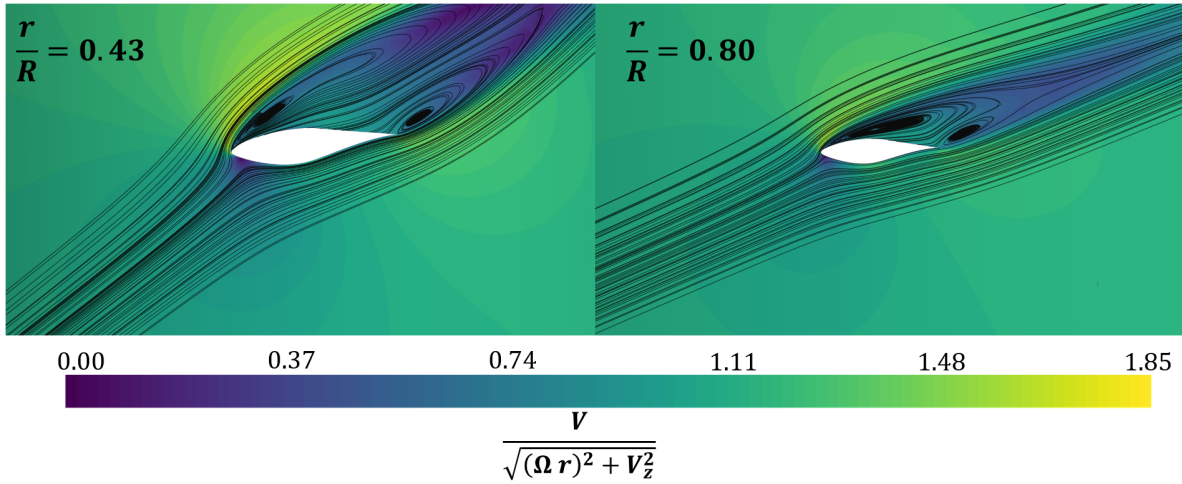
Figure 7: Pressure coefficient. Comparison between experiments and CFD

279 The evolution of the pressure coefficients that were shown in Figure 7 can be easily explained from the observation  
 280 of the Figure 8, where the magnitude non-dimensional velocity  $V^* = \frac{V}{\sqrt{(\Omega r)^2 + V_\infty^2}}$  is shown in the rotating reference  
 281 frame, in conjunction with the field streamlines, for the same characteristic airfoils which were use in the previous  
 282 Figure. Note how, for the case with  $\lambda = 6$  the flow is attached for the blade, leading to a pressure distribution with a  
 283 high pressure drop between pressure side and suction side. For  $\lambda = 3$  the flow is detached at these sections, leading to  
 284 the almost constant pressure coefficient which can be observed at the suction side at Figure 7(b).





(a) Contours of non dimensional velocity field around two different sections for  $\lambda = 6$



(b) Contours of non dimensional velocity field around two different sections for  $\lambda = 2.78$

Figure 8: Velocity fields around the NREL Phase VI geometry

285 Additionally, Figure 9 shows the value of the power coefficient as a function of  $\lambda$ . It can be observed that the  
 286 current CFD-MRF simulations agree fairly with the experiments. As expected, and due to the limitations of the  
 287 model, the BEMT tends to over-predict the power value for low values of  $\lambda$ . Nevertheless, this model is able to  
 288 provide an acceptable preliminary prediction for the whole working range with a significantly reduced computation  
 289 time. Thus, this model was used in order to perform a previous analysis of possible enhancement actions. However,  
 290 it should be had into account that, if the new design's features lead to the appereance of important 3D effects, the  
 291 BEMT-predicted power curve should be analyzed accounting for them. Thus, the BEMT-optimized wind turbine  
 292 families were later studied using CFD in order to obtain a more realistic power curve. The comparison of the curves  
 293 shows a difference of approximately a 3% on the prediction of the maximum power coefficient, and approximately a  
 294 12% on the location of the optimum tip speed ratio, which is in agreement with the already reported differences found  
 295 by other researches [44] when comparing these methods.

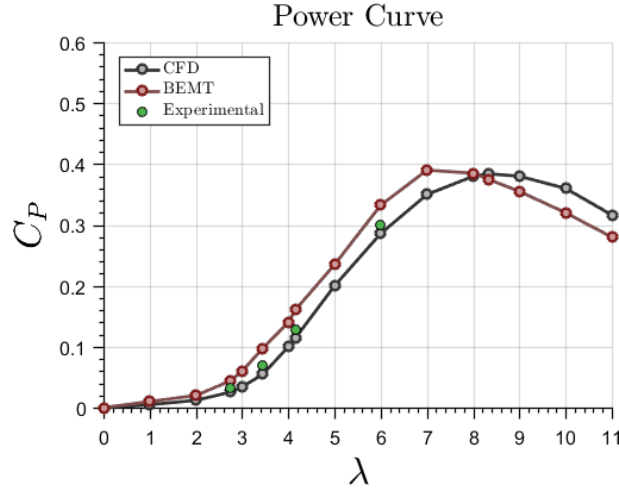


Figure 9: Power coefficient curve. Comparison between current methodologies and experiments

296 In order to check the validity of neglecting the influence of the Reynolds number the NREL Phase VI behavior  
 297 curves have been calculated for three different sets of the velocity inlet, covering the whole expected working range.  
 298 Figure 10 shows the power curve (left) and axial force (right) at  $V_z = 4\text{ms}^{-1}$ ,  $V_z = 8\text{ms}^{-1}$ ,  $V_z = 12\text{ms}^{-1}$ . It can be  
 299 concluded that, although some differences can be found at high values of  $\lambda$  they are below a 5% and therefore, the  
 300 assumption of Reynolds number independence can be considered to be accurate enough.

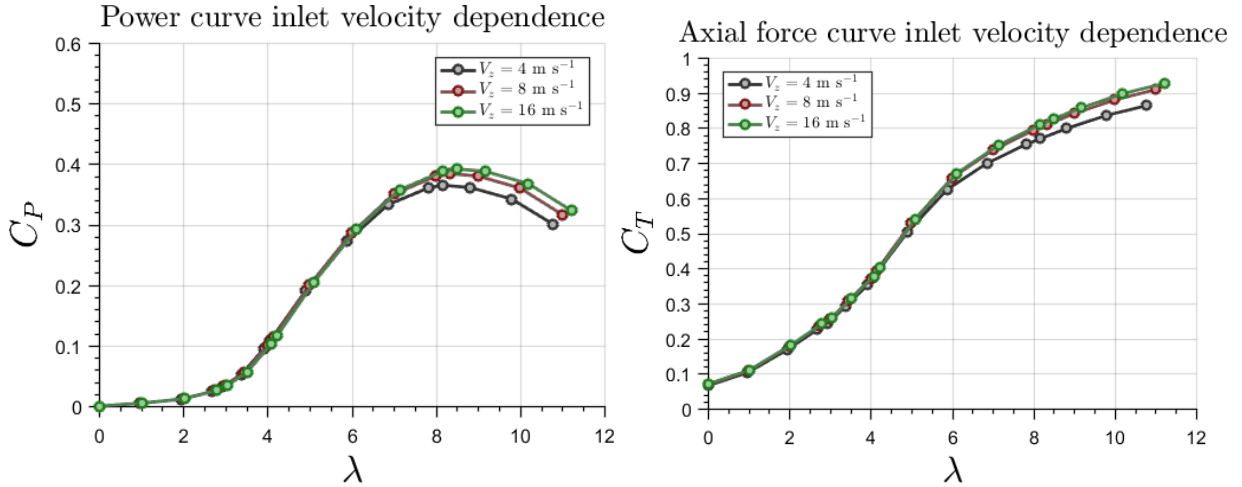


Figure 10: Power (left) and axial force (right) coefficient curves computed for the blade NREL Phase VI. CFD calculations at different inlet velocities

## 301 4. Results

### 302 4.1. DOE results

303 After the DOE was performed, a family of power curves was obtained. Figure 11 shows a typical selection of  
 304 the different power optimization possibilities. As it can be observed, as  $\lambda_d$  increases, the left slope of the curve  
 305 is decreased. Also, it can be seen that when  $\alpha_d$  is increased, the inverse trend is observed. During the design of  
 306 experiments the number of blades was supposed to be  $B = 3$  and the radius was fixed to  $R = 2.50\text{m}$ .

307 For high values of  $\alpha_d$  the power curve tends to values of  $C_p \ll 1$  for low values of  $\lambda$ . From the point of view  
 308 of maximum power coefficient and controllability (see Equation (11)), the designs shown for  $(\lambda_d = 4.5, \alpha_d = 7 \text{ deg})$

309 and ( $\lambda_d = 7.5, \alpha_d = 7 \text{ deg}$ ) could both be valid. Nevertheless, the manufacturing criterion is not complied with for  
 310 the first combination of values, due to the high value of solidity that should be used. This can be seen at Figure 12,  
 311 where these values are shown as a function of the non-dimensional distance to the hub. As a result, it was considered  
 312 to select the case generated by ( $\lambda_d = 7.5, \alpha_d = 7 \text{ deg}$ ) from this set of blades.

313 The former explanation serves as an example in order to provide with a picture of how an automatic selection  
 314 procedure allows a reduction of the blade designs, using a low number of starting blades with illustrative purposes.  
 315 This very same procedure, applied to the whole 70 possible designs generated during the design of experiments  
 316 explained in section 3.1 allowed a high reduction of the designs to be evaluated by means of CFD (a total of 5 blades  
 317 were obtained in this case, although the number could be affected by the selection of the restrictions sketched in  
 318 section 3.1).

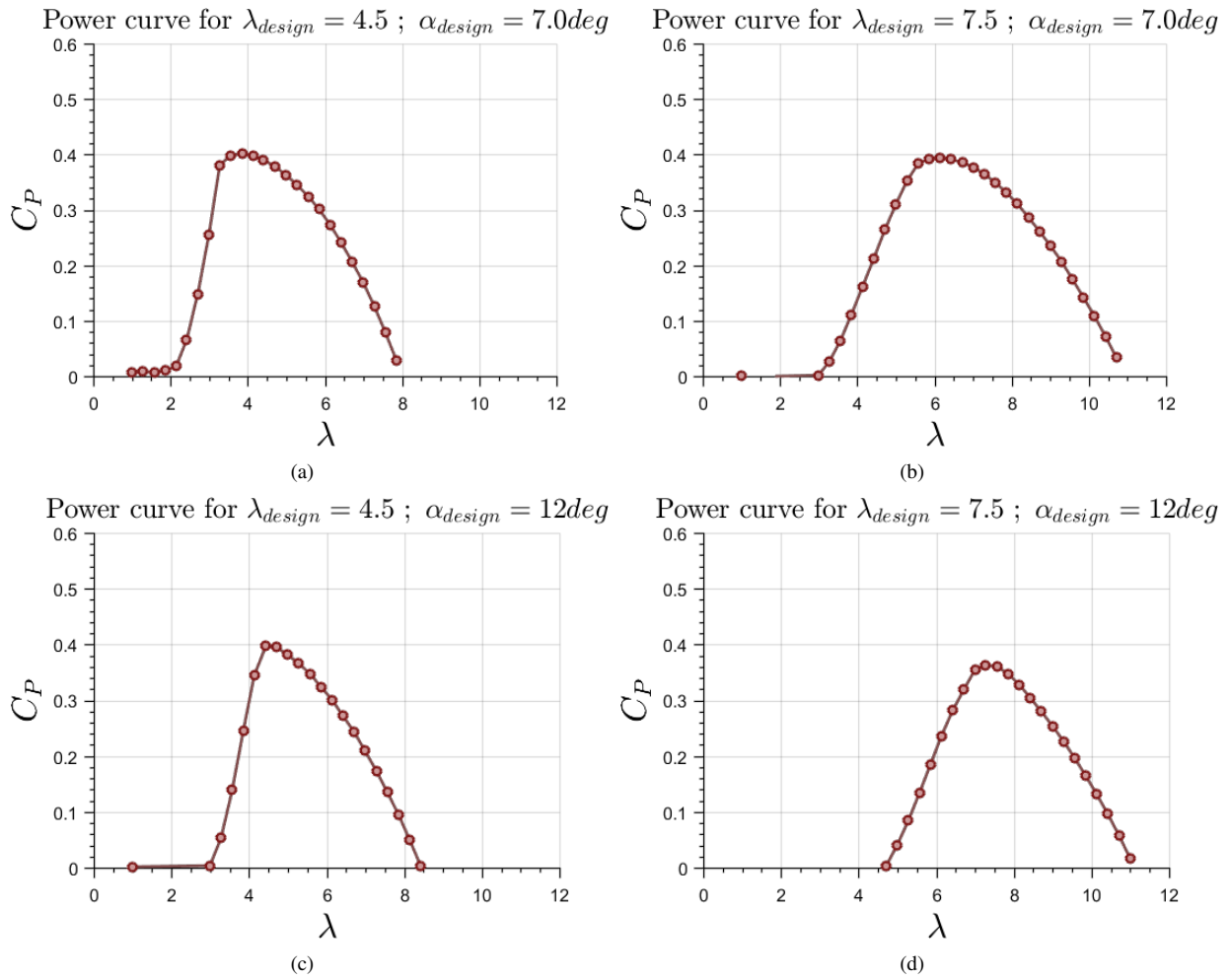


Figure 11: Power curves for different optimization parameters

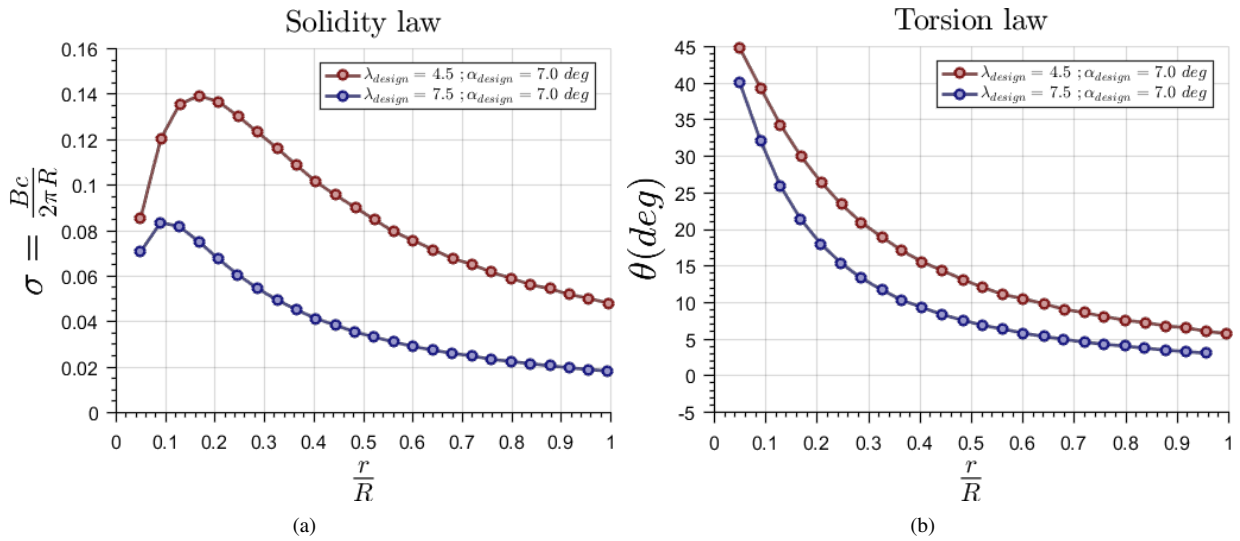


Figure 12: Local solidity (left) and torsion (right) distributions for two different resulting geometries from the DOE

319 The proposed blade design strategy was analyzed using the CFD model presented in subsection 3.2. The results  
 320 on the power coefficient were compared by using both methodologies. Figure 13 (left) shows the comparison between  
 321 the predictions which were made during the design process using BEMT and the 3D CFD steady calculations. It can  
 322 be observed that the major discrepancies appear in the prediction of the location of the tip speed ratio of maximum  
 323 power coefficient, where a difference of the order of 11% is obtained. The value of the maximum  $C_P$  is well predicted,  
 324 with a difference of approximately a 4%. Similar differences between CFD and BEMT have already been reported by  
 325 other researches applied to the MEXICO rotor aerodynamics [44].

326 A visual inspection of the power curve shown in Figure 13 (left) allows to observe how the qualitative differences  
 327 at low values of  $\lambda$  could look to be more accentuated than those observed during the validation study of Figure 9. This  
 328 is mainly due to the narrow shape of the power curve for the case of the current proposed blade design. Although  
 329 the differences on the location of the maximum power coefficient and the maximum coefficient itself are on a similar  
 330 order of those which were shown in Section 3.3, the high left slope of the curve makes them more visible.

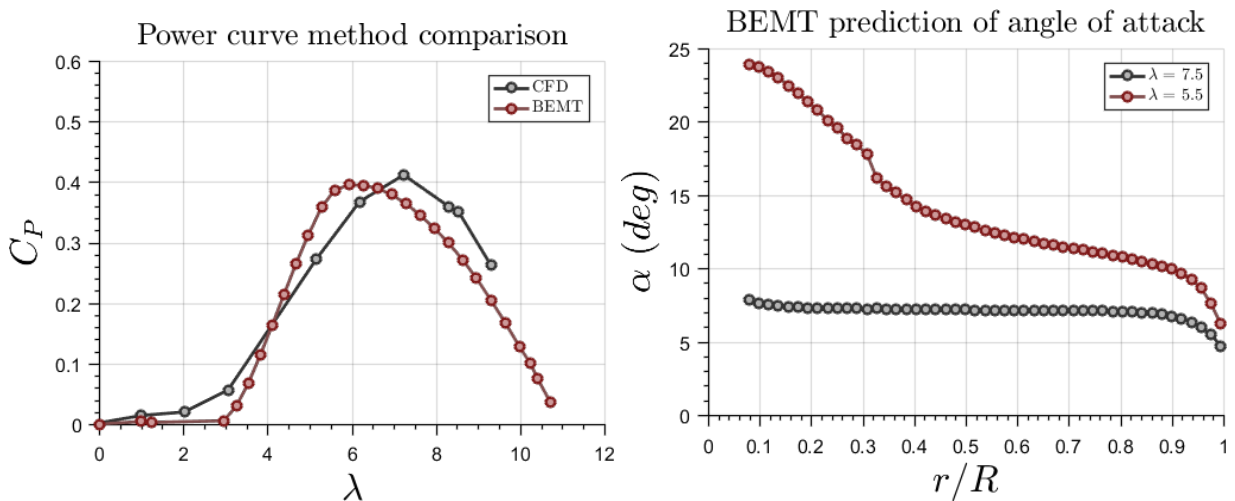


Figure 13: Comparison between the CFD and BEMT predicted power curves for the current proposed geometry (left) and BEMT prediction of the angle of attack for two different tip speed ratio (right)

331 Also, it can be observed that, for low values of the tip speed ratio ( $\lambda \in [4 - 5]$ ), the BEMT tends to over-predict  
332 the power coefficient, which is mainly due to the non-inclusion of the 3D stall delay phenomenon in the model.

333 Additionally, it can be seen that the left side slope of the power coefficient curve is over-predicted by the BEMT.  
334 However, this discrepancy is compensated by the increase of  $\lambda$ , from the controllability point of view, in accordance  
335 with Equation (11). Thus, the BEMT can be considered to be sufficiently good for the DOE performed, as will be  
336 later shown.

337 The differences on the prediction of the power coefficient for low values of  $\lambda$  (and, as a consequence, on the  
338 prediction of the power curve slope) can be interpreted referring to Figure 13 (right). In this Figure, the BEMT  
339 predicted angle of attack is compared for two different values of the tip speed ratio: For a value of  $\lambda = 7.5 = \lambda_{design}$   
340 and  $\lambda = 5.5 < \lambda_{design}$ . Note how, for the former, an almost constant value of the angle of attack  $\alpha \approx 7.0 \text{ deg} = \alpha_{design}$   
341 is found for the most part of the blade. When the value of  $\lambda$  decreases, as expected, the predicted angle of attack tends  
342 to increase. Due to the high difference on torsion angle between the root and the tip, compared with NREL Phase VI,  
343 this increment on angle of attack is more abrupt at the root. This, generates an important gradient of angle of attack  
344 under these conditions which, in conjunction with being working at stall conditions, will lead to the appearance of  
345 very important 3D effects which are not taken into account with the current BEMT.

346 It can also be noted how, for these geometries, if no additional three dimensional corrections are applied to the  
347 BEMT, the predictions at very low values of the tip speed ratio ( $\lambda \leq 3$ ) can not be considered to be sufficiently  
348 accurate, and therefore, CFD or experimental measurements should be used in order to obtain valuable results at these  
349 conditions.

#### 350 4.2. Comparison against other designs

351 As it was previously mentioned, once a design is generated and selected via the Design of Experiments, its be-  
352 havior must be studied and analyzed against a functioning known design. The blade of the low power wind turbine  
353 *Skystream* was selected in order to do so, as this model is one of the current leaders in the market of low wind power  
354 generation. The geometry of the commercial blade was digitalized, so CFD calculations can be performed. Note also  
355 that, as stated before, due to the horizontal curvature of the blade, the current BEMT methodology should no directly  
356 be applied for this problem. Figure 14 shows a geometrical comparison between the proposed current design (left) and  
357 the *Skystream* geometry (middle). Figure 14 (right) shows a zoom of the *Skystream* geometry, where a geometrical  
358 protuberance can be observed for most of the radial coordinates of the blade.

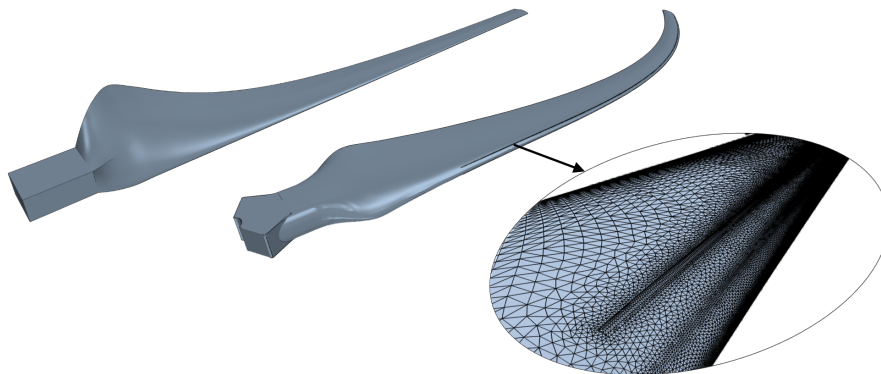


Figure 14: Comparison between current design (left) and a commercial geometry (right)

359 The mentioned geometrical feature will act as a Vortex Generator (VG) and its aim would be influencing on the  
360 boundary layer behavior. Due to the usual turbulence intensities and three dimensional flows this kind of products  
361 are subjected to, it is expected that setting the transition between a laminar and a turbulent boundary layer will not be

362 primal. Then it is necessary to study how the VG will affect to the energy production, and the *Skystream* geometry  
 363 with the VG removed was also be studied.

364 With this aim, Figure 15 shows the CFD-calculated power curve for the mentioned geometries. As it can be  
 365 seen, the current design shows higher values of the power coefficient for a wide range near the working zone (from  
 366  $\lambda = 6.2$  to  $\lambda = 8.5$ . For  $\lambda < 6.2$  the current design shows a pronounced slope and lower  $C_P$  values, contributing to a  
 367 better stability for high values of  $V_z$ . Additionally, the peak value of  $C_P$  is improved up to a 14 % compared with the  
 368 commercial design.

369 It is also of interest the comparison between the commercial design with and without the VG. The design with  
 370 VG shows a lower value of  $C_P$  for the whole working range of the wind turbine. This allows to state that seems that  
 371 this VG does not improve the wind turbine performance from the point of view of energy generation. However, the  
 372 reduction of power coefficient on the whole range could lead to a better stability performance.

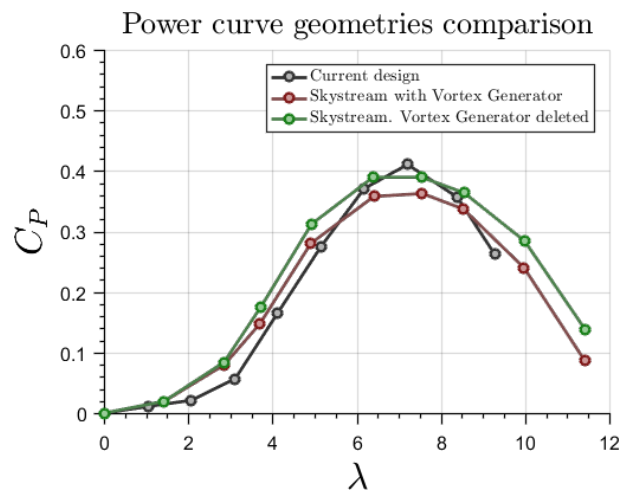


Figure 15: Comparison of the power curve for the different analyzed blades

373 The differences in the pressure coefficient between the different geometries are closely related to the pressure  
 374 distribution over the suction side and the pressure side of the different blades at different operating conditions. Figure  
 375 16 shows the pressure coefficient distribution, defined in accordance with Equation (13). For each blade the suction  
 376 side and the pressure side are shown above and below, respectively. Notice that the pressure coefficient presents  
 377 higher values over the pressure side in all the cases. For values of  $\lambda \approx \lambda_{opt}$  the pressure coefficient over the suction  
 378 side exhibits a distinct minimum close to the blade leading edge.

379 In Figure 16 lines which are tangent to the wall shear stress at each blade point are represented. The locations  
 380 where these lines present abrupt changes represent the zones where the flow is suddenly separated. As a general  
 381 trend for all the designs it can be observed that, for low values of  $\lambda$ , the area where the flow is separated tends to be  
 382 increased. This is due to the higher local angles of attack that appear at these low rotational velocities (see Equation  
 383 (1)).

384 Regarding the comparison between the different design solutions it can be observed that, for the current enhanced  
 385 design (Figure 16(a) and 16(b)), the blade surface covered by the separation area is smaller than in the case of the  
 386 commercial blade (Figure 16(c) and 16(d)). The removal of the VG in the commercial blade (Figures 16(d) and 16(e))  
 387 significantly reduces the separation area, specially for high values of the tip speed ratio. This phenomenon is strongly  
 388 related to the fact that the blade without VG tends to produce a higher power, specially for high values of  $\lambda$ .



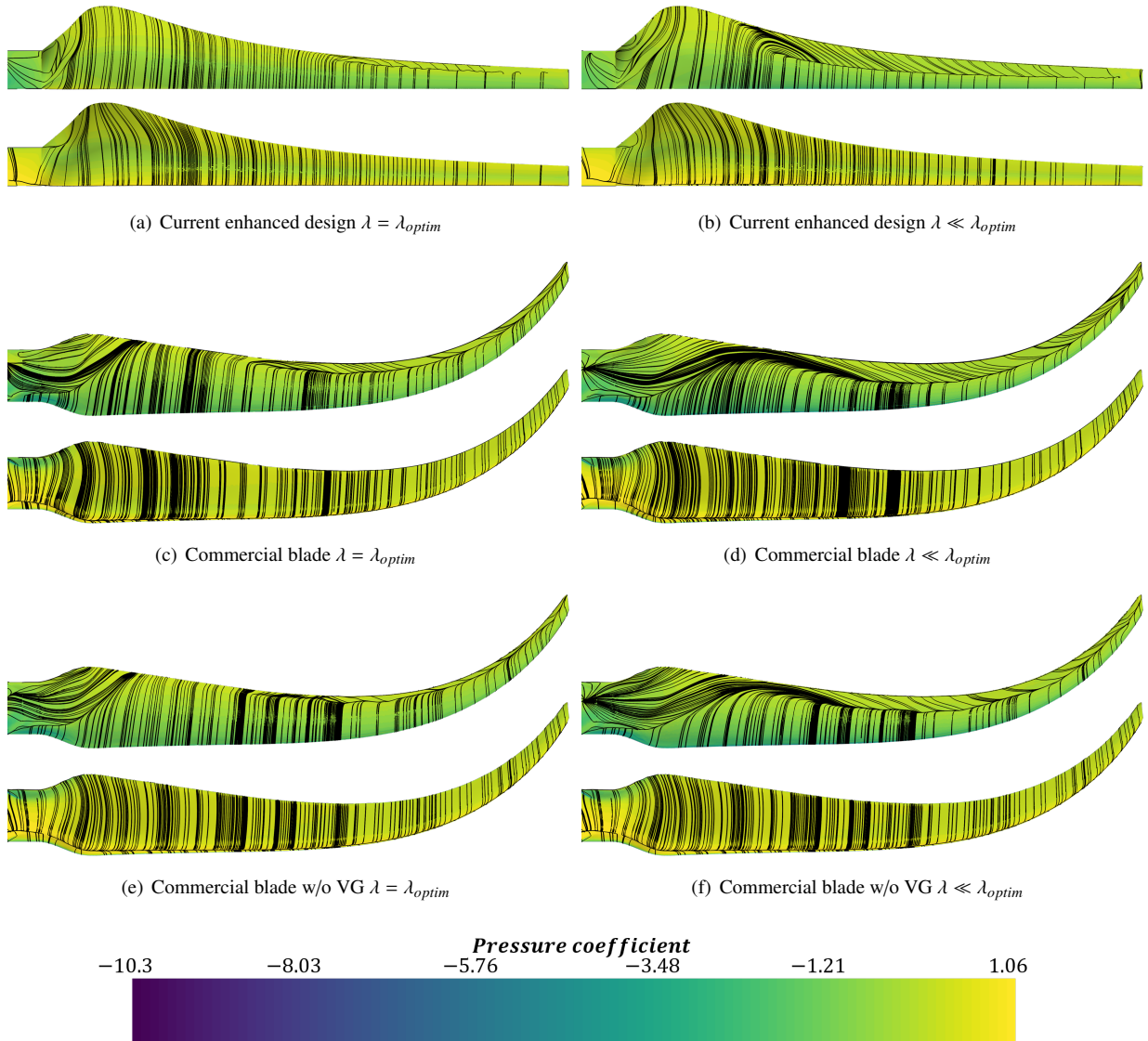


Figure 16: Contours of the pressure coefficient for the current design (up); the *Skystream* commercial blade (middle) and the *Skystream* commercial blade with the VG removed at the value of tip speed ratio of maximum power (left) and a low tip speed ratio (right) and stream lines of wall shear stress.

389 Once the non dimensional behavior of the proposed current design and the commercial blade has been analyzed, it  
 390 is necessary to perform a validation on the controllability parameter expressed by the left-slope condition of Equation  
 391 11. Additionally, it will be shown the necessity of performing a CFD analysis to correct BEMT predictions of other  
 392 candidate geometries in order to discard those which are expected to present difficult controllability issues.

393 As it was previously mentioned, during the development of the Design of Experiments multiple candidate ge-  
 394 ometries were obtained. In particular, additionally to the already mentioned proposed design (which it should be  
 395 remembered was generated by using the parameters  $\lambda_d = 7.5$  and  $\alpha_d = 7$  deg), other geometries were considered. One  
 396 example could be the design which can be reconstructed by an application of the parameters  $\lambda_d = 6.5$  and  $\alpha_d = 6$  deg.

397 The non dimensional power curve (left) and non dimensional torque curve ( $C_Q = C_P/\lambda$ ) (right) of this alternative  
 398 design are shown in comparison with the corresponding curves of the current design and the commercial blade at  
 399 Figure 17. Observe how this alternative design shows a power coefficient slightly higher than the shown by the

400 proposed blade. Furthermore, note how the left slope of the power coefficient is significantly lower. Intuitively, one  
 401 could assign low slopes of the power coefficient to easier control but, due to the cubic dependence of the dimensional  
 402 power with incoming fluid velocity (see the derivation of Equation 11) this is not the case and, therefore, it should be  
 403 ensured that, when applying a mechanical brake under high wind conditions, the power coefficient (and, therefore, the  
 404 torque coefficient) should quickly decrease to compensate the increment of velocity.

405 This fact can be easily understood by a numerical application. Once the non dimensional power and torque  
 406 coefficients are obtained in terms of the tip speed ratio, and given that its dependence with Reynolds number is of  
 407 second order (see Figure 10), it is straightforward to obtain the dimensional power, given a wind turbine radius, for  
 408 any combination of rotational speed  $\Omega$  and wind velocity,  $V_z$ .

409 One typical law of control which is often followed by stall regulated wind turbines is to work on conditions of  
 410 maximum power coefficient,  $\lambda = \lambda_{opt}$ , for low values of wind speed and with constant rotational speed  $\Omega = \Omega_{max}$   
 411 when wind velocity exceeds certain value [45], [46], [47]. When the wind velocity becomes even higher, a brake  
 412 torque must be employed in order to stop the wind turbine. In order to ensure that this is possible it is mandatory that  
 413 both the generated power and torque do not increase with wind velocity in an uncontrolled manner.

414 Therefore, Figure 18 shows the prediction of the dimensional power and torque, calculated for the blades of Figure  
 415 17, supposing that they are working under a normal ambient with  $\rho_{\infty} = 1.225 \text{ kg m}^{-3}$ . They will be supposed to be  
 416 of the same size, with  $R = 2.50 \text{ m}$  and they will work on conditions of maximum power coefficient,  $\lambda_{optim}$  until  
 417 the rotational speed exceeds a value of  $\Omega_{max} = 170 \text{ rpm}$ . For higher values of the velocity the rotational speed is  
 418 maintained and, as a consequence, the value of  $\lambda$  will be decreasing.

419 It can be observed how, for values of the wind velocity below  $V_z = 8 \text{ m s}^{-1}$  the three blades behave in a very similar  
 420 manner in terms of power and torque. However, when the wind speed increases the power of the discarded design  
 421 increases in an uncontrollable manner. This can be attributed to the low value of the left-slope, which relates with a  
 422 high value of the torque coefficient. Similar tend can be observed at the commercial blade, which shows the same  
 423 behavior, although slower. The proposed design shows how, when wind speed exceeds from  $V_z = 12 \text{ m s}^{-1}$  both the  
 424 power and torque stay bounded and, therefore, it will be possible to stop the wind turbine.

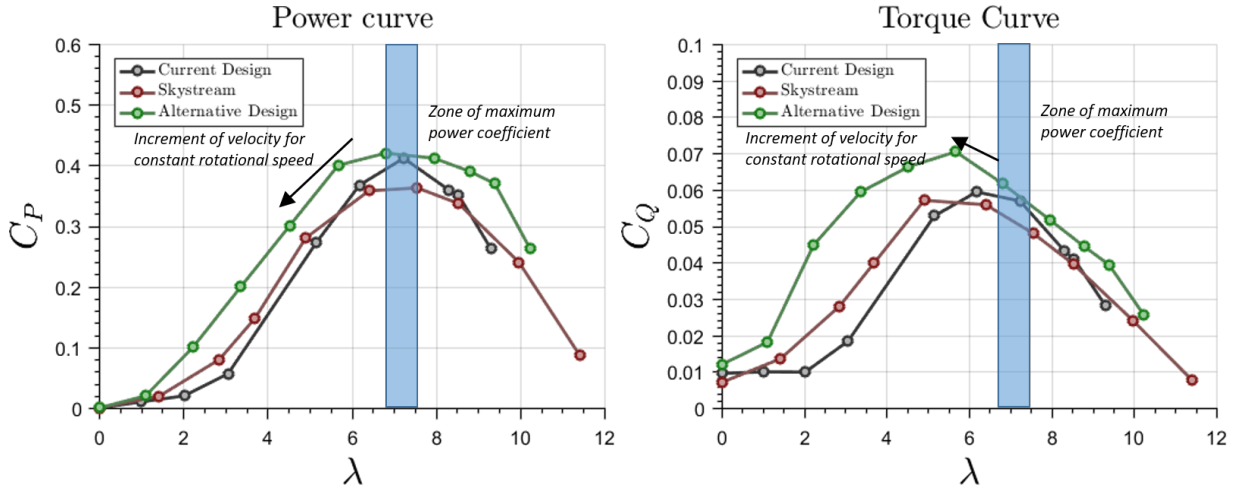


Figure 17: Evolution of both non dimensional power and torque for the current design (gray), the commercial blade (red) and an alternative discarded design (green). Predictions made with RANS



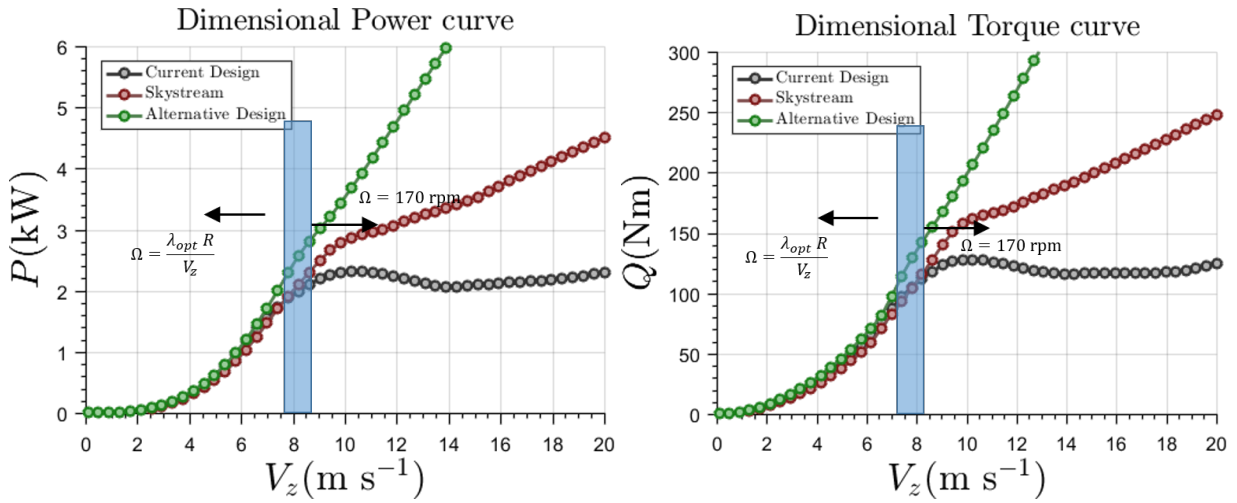


Figure 18: Evolution of both dimensional power and torque for the current design (gray), the commercial blade (red) and an alternative discarded design (green) with wind velocity. Numerical application supposing wind turbines of similar radius  $R = 2.50$  m working under normal conditions with  $\rho_\infty = 1.225$  kg  $m^{-3}$

425 Previous statements refer just to a direct application with the data obtained in this work. Nevertheless, conclusions  
 426 may be extended to other control laws. Figure 19 shows the performance of a wind-turbine equipped with the alterna-  
 427 tive design by using different control laws at different maximum rotational velocity (50 rpm, 100 rpm and 200 rpm).  
 428 It could be stated that a completely controllable torque of the wind turbine is obtained at a lower rotational velocity  
 429 values (50 rpm) despite both the torque and power curves are monotonically increasing. However, this is achieved by  
 430 drastically decreasing the generated power, since the wind turbine is always working far from the optimum value of  
 431  $\lambda$ . If the rotational speed is increased to 100 rpm, admissible power around 2.5kW could only be achieved just with  
 432 wind velocities above 20  $m s^{-1}$ .

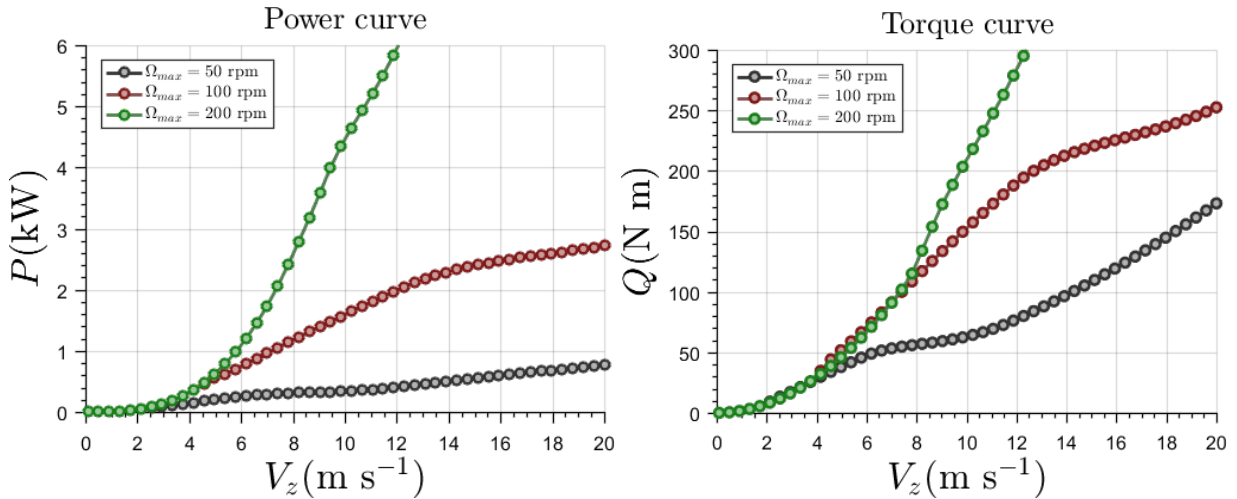


Figure 19: Evolution of the power (left) and torque (right) of the discarded design as a function of maximum control rotational velocity for a given radius of  $R = 2.50$  m

## 433 5. Conclusions

434 The current work provides with a wind turbine blade design methodology which can be considered as a flexible  
 435 accurate tool. The method can be used as the base for the development of designs of increased complexity, given

436 that the work has been presented with a complete validation and discussion of the differences between the used tools.  
437 For instance, the methodology can be used in order to explore the sensitivity of the restrictions, adding or removing  
438 them as a function of the design objectives or even to propose an optimization tool based on the minimization of an  
439 objective function based on the current proposed restrictions. Particularly, it has been applied to the design of a low  
440 power stall regulated wind turbine.

441 The methodology combines a complete set of design of experiments using a low computational cost tool as BEMT  
442 in order to select blade geometries for optimal performance and control. Furthermore, CFD methodology has been  
443 presented to accurately take into account three dimensional flow effects and, therefore, allow to discard those geome-  
444 tries which were initially valid in accordance with BEMT but are not easily controllable once these three dimensional  
445 effects are taken into account.

446 This combined methodology has been validated with experimental results available from NREL Phase VI wind  
447 turbine public data catalog. Results have been successfully compared in terms of wind turbine power but also in terms  
448 of pressure coefficients along the complete blade at different radial sections.

449 The proposed BEMT design procedure includes additional restrictions to the power curve form, in order to obtain  
450 a blade geometry which, not only maximizes the power coefficient, but allows having into account controllable issues  
451 for the design of stall regulated HAWT. As a result, a reduced set of feasible blade designs has been obtained, allowing  
452 to perform CFD calculations over them and finally select a blade which allows both an increment in maximum power  
453 coefficient (compared with a commercial design) and an almost flat dimensional power curve for a simple control law.

454 The predicted behavior of the proposed design has been analyzed in terms of power generation and controllability  
455 and compared to the predictions over a commercial existing wind turbine under similar working conditions. This  
456 comparison showed how the new design allows obtaining higher values of power while improving the velocity range  
457 at which the turbine could safely operate.

458 Additionally, the influence of Vortex Generators, installed near the blade leading edge, on the performance and  
459 control ability has been also studied. It was found that VG solution proposed seems to negatively affects maximum  
460 power generation. Furthermore, VGs affects flow separation phenomena and therefore the capability of the blade to  
461 control the rotation velocity of the wind turbine.

462 It has been shown how a combination of the Blade Element Momentum Theory and Reynolds Averaged Navier  
463 Stokes can be used in order to take advantage of the capabilities which are related with each model:

- 464 • BEMT allowed to obtain a significant amount of candidate designs at low CPU cost, and discard those candi-  
465 dates that clearly do not comply with the performance requirements. Nevertheless, it does not take in to account  
466 3D effects which could be important for the correct prediction of performance at low TSR values.
- 467 • RANS has been used in this work to accurately obtain behavior of a reduced number of pre-selected designs  
468 and to discard those not fulfilling the performance and control requirements.

469 Finally, the left-slope of the non-dimensional power curve has been shown to be a key parameter for the successful  
470 design of a stall regulated wind turbine. In fact, taking into consideration this parameter as a relatively simple design  
471 constraint allows one to generate a blade geometry which is able to provide higher power than similar designs and can  
472 safely operate in a wide range of wind velocities.

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## 554 Nomenclature

$r$	Distance to the hub
$\theta$	Blade pitch angle
$c$	Section chord
$V_z$	Wind velocity
$\Omega$	Wind turbine rotational speed
$v_i$	Axial induced velocity
$a$	Axial induced velocity factor
$\omega'$	Tangential induced velocity
$a'$	Tangential induced velocity factor
$\varphi$	Relative velocity angle
$V_{rel}$	Relative velocity
$F_N$	Normal force
$P$	Power
$Q$	Torque
$C_l$	Airfoil lift coefficient
$C_d$	Airfoil drag coefficient
$\alpha$	Angle of attack
$\lambda$	Tip speed ratio
$F$	Tip losses factor
$x$	Non-dimensional distance
$C_T$	Normal force coefficient
555 $C_P$	Power coefficient
$C_Q$	Torque coefficient
$c_p$	Pressure coefficient
$\rho$	Free stream density
$R$	Blade radius
$B$	Number of blades
$U_i$	Mean velocity component on the $i^{th}$ direction
$\nu$	Free stream kinematic viscosity
$\mu$	Free stream dynamic viscosity
$\vec{f}$	Inertial forces vector
$\vec{r}$	Position vector
$\vec{\omega}$	Moving Reference Frame rotational velocity
$\langle u_i u_j \rangle$	Reynolds stresses
$\nu_T$	Turbulent viscosity
$\delta_{ij}$	Dirac delta
$\sigma$	Local solidity
$u_{tau}$	Shear velocity
$y^+$	Non-dimensional wall distance
Re	Reynolds number
$C_p$	Pressure coefficient
$p$	Absolute static pressure
$p_\infty$	Free stream absolute static pressure

557 **List of Figures**

558	Figure 1	Work flow sketch . . . . .	3
559	Figure 2	Velocity diagram used for the BEMT explanation at an airfoil section located at radius $r$ . . . . .	4
560	Figure 3	Work flow of the proposed Design of Experiments . . . . .	7
561	Figure 4	Power (left) and force (right) curves calculated for the blade <i>NREL Phase VI</i> using different	
562		grid refinements . . . . .	9
563	Figure 5	Wall $y^+$ distribution for $\lambda = 3$ (left) and $\lambda = 6$ (right). Calculations performed with the NREL	
564		Phase VI blade with $N \approx 8 \cdot 10^6$ . . . . .	9
565	Figure 6	Mesh sketch for a case of a three bladed wind turbine calculation . . . . .	10
566	Figure 7	Pressure coefficient. Comparison between experiments and CFD . . . . .	11
567	Figure 8	Velocity fields around the NREL Phase VI geometry . . . . .	12
568	Figure 9	Power coefficient curve. Comparison between current methodologies and experiments . . . . .	13
569	Figure 10	Power (left) and axial force (right) coefficient curves computed for the blade NREL Phase VI.	
570		CFD calculations at different inlet velocities . . . . .	13
571	Figure 11	Power curves for different optimization parameters . . . . .	14
572	Figure 12	Local solidity (left) and torsion (right) distributions for two different resulting geometries from	
573		the DOE . . . . .	15
574	Figure 13	Comparison between the CFD and BEMT predicted power curves for the current proposed	
575		geometry (left) and BEMT prediction of the angle of attack for two different tip speed ratio (right) . . . . .	15
576	Figure 14	Comparison between current design (left) and a commercial geometry (right) . . . . .	16
577	Figure 15	Comparison of the power curve for the different analyzed blades . . . . .	17
578	Figure 16	Contours of the pressure coefficient for the current design (up); the <i>Skystream</i> commercial	
579		blade (middle) and the <i>Skystream</i> commercial blade with the VG removed at the value of tip speed	
580		ratio of maximum power (left) and a low tip speed ratio (right) and stream lines of wall shear stress. . . . .	18
581	Figure 17	Evolution of both non dimensional power and torque for the current design (gray), the com-	
582		mercial blade (red) and an alternative discarded design (green). Predictions made with RANS . . . . .	19
583	Figure 18	Evolution of both dimensional power and torque for the current design (gray), the commercial	
584		blade (red) and an alternative discarded design (green) with wind velocity. Numerical application	
585		supposing wind turbines of similar radius $R = 2.50$ m working under normal conditions with $\rho_\infty =$	
586		$1.225 \text{ kg m}^{-3}$ . . . . .	20
587	Figure 19	Evolution of the power (left) and torque (right) of the discarded design as a function of maxi-	
588		mum control rotational velocity for a given radius of $R = 2.50$ m . . . . .	20