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Payri, R.; Salvador, FJ.; Carreres, M.; Belmar-Gil, M. (2020). Thermal effects on the diesel injector performance through adiabatic 1D modelling. Part II: Model validation, results of the simulations and discussion. *Fuel*. 260:1-17. <https://doi.org/10.1016/j.fuel.2019.115663>



The final publication is available at

<https://doi.org/10.1016/j.fuel.2019.115663>

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Additional Information

1 **THERMAL EFFECTS ON THE DIESEL INJECTOR PERFORMANCE THROUGH ADIABATIC 1D**  
2 **MODELLING. PART II: MODEL VALIDATION, RESULTS OF THE SIMULATIONS AND DISCUSSION**

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13

14 **ABSTRACT**

15 In this paper, a one-dimensional computational model of the flow in a common-rail injector is used to compute local  
16 variations of fuel temperature (including the temperature change produced upon expansion across the nozzle) and analyse  
17 their effect on injector dynamics. These variations are accounted through the adiabatic flow hypothesis, assessed in a first  
18 part of the paper where the model features are also described. They imply variations in the fuel properties and the flow  
19 regime established across the injector internal restrictions driving the solenoid valve. An extensive validation of the model  
20 against experimental results is presented for a wide range of conditions. Multiple injection strategies are also explored,  
21 analysing the influence of the inlet fuel temperature and its variations on the mass injected by successive injections and  
22 the critical dwell time below which they cannot be separated. Results show significant changes in fuel temperature across  
23 some injector restrictions. These changes are greater the highest the rail pressure and lowest the fuel temperature at the  
24 injector inlet. In the case of the flow across nozzle orifices, the fuel can be either heated or subcooled depending on the  
25 operating conditions, the heating being especially relevant for cold-start-like fuel temperatures at the inlet. Thermal effects  
26 also influence the injection rate and duration. This influence on injector dynamics is particularly accused in the injector  
27 of study due to its ballistic nature. In this regard, the time needed to effectively separate two successive injections is  
28 greater the higher the fuel temperature and the injection pressure.

29 **KEYWORDS**

30 diesel, injection, computational, 1D modelling, fuel temperature, adiabatic flow

31 **LIST OF NOTATION**

32  $A_o$  outlet area

33  $Ad$  adiabatic number

34  $C_a$  area coefficient

35  $C_d$  discharge coefficient

36  $CN$  cavitation number

37  $D$  diameter

38  $D_{cl}$  clearance on diameter

39  $D_{pist}$  piston diameter

40  $D_o$  orifice outlet diameter

41  $F_{fric}$  force due to friction

42  $F_{needle}$  force acting on the needle

43  $F_{\Delta p}$  force due to pressure differences

44  $h$  specific enthalpy

45  $L$  length

46  $L_{cl}$  clearance length

47  $l$  needle lift

48  $m_i$  total mass injected per cycle

49  $\dot{m}_f$  fuel mass flow

50  $Nu$  Nusselt number

51  $Pr$  Prandtl number

52  $p$  pressure

53  $p_{cv}$  pressure in the control volume

54  $p_{dw}$  downstream pressure

55  $p_i$  injection pressure

56  $p_{up}$  upstream pressure

57  $p_v$  vapour saturation pressure

58	$Re$	Reynolds number
59	$T$	temperature
60	$T_{dw}$	downstream temperature
61	$T_i$	fuel temperature at the injector inlet
62	$T_{up}$	upstream temperature
63	$T_w$	wall temperature
64	$t$	time
65	$t_{aSOE}$	time after the injector Start of Energizing
66	$U_n$	needle velocity
67	$u$	flow velocity
68	<b>GREEK SYMBOLS</b>	
69	$\rho_f$	fuel density
70	$\mu_f$	fuel dynamic viscosity
71	<b>ABBREVIATIONS</b>	
72	DT	Dwell Time
73	ET	Energizing Time
74	NFL	nozzle feeding line
75	OA	control volume outlet orifice
76	OZ	control volume inlet orifice
77	ROI	Rate of Injection
78		

## 79 **1. INTRODUCTION**

80 Great effort has traditionally been placed on the research and development of the fuel injection system, due to its role on  
81 the air-fuel mixture, combustion and formation of emissions [1–3]. The current scenario involving an ever growing  
82 population and an increase in their transportation needs, together with the limited availability of fossil fuels [4,5], lead to  
83 raised concerns and environmental awareness culminating in strict regulations in the matter such as the Euro 6 in Europe  
84 and those yet to come. Technological responses to comply with these regulations, such as the gradual increase in injection  
85 pressure [6,7] or the use of split injection strategies [8–11], have resulted in a greater complexity of the injection system.  
86 This fact highlights the need for computational tools that allow to predict and understand its behaviour for a wide range

87 of realizable conditions.

88 In this sense, 1D modelling appears to be an appropriate solution, since it may provide a deep insight on the complete  
89 injection process at a low computational cost compared to computationally expensive 3D CFD simulations usually  
90 restricted to a specific part of the injector [12–14] or to spray development [15]. In fact, the 1D modelling approach has  
91 been used by the authors in the past in order to study the injection system behaviour [16–18].

92 Temperature and pressure significantly modify the fuel properties that are relevant in the injection process (namely density,  
93 viscosity and speed of sound) [19]. Several researchers have experimentally studied the influence of the fuel temperature  
94 and the associated fuel properties on the spray formation [20,21], but generally left injector dynamics out of their scope.  
95 Wang et al. [22] did study the effect of the fuel temperature on the performance of split injection strategies, finding that  
96 cold conditions reduced the interaction among split injection events. With the aid of 1D modelling, the authors of the  
97 present investigation tried to start the study upstream of the nozzle in order to further understand the mechanisms behind  
98 the experimental findings, despite treating the flow as isothermal [17]. We found the flow regime induced by the operating  
99 conditions (including the fuel temperature at the injector inlet) on the nozzle and the control volume orifices could  
100 importantly drive needle dynamics. However, the model capabilities did not allow the study of the effect of split injections.

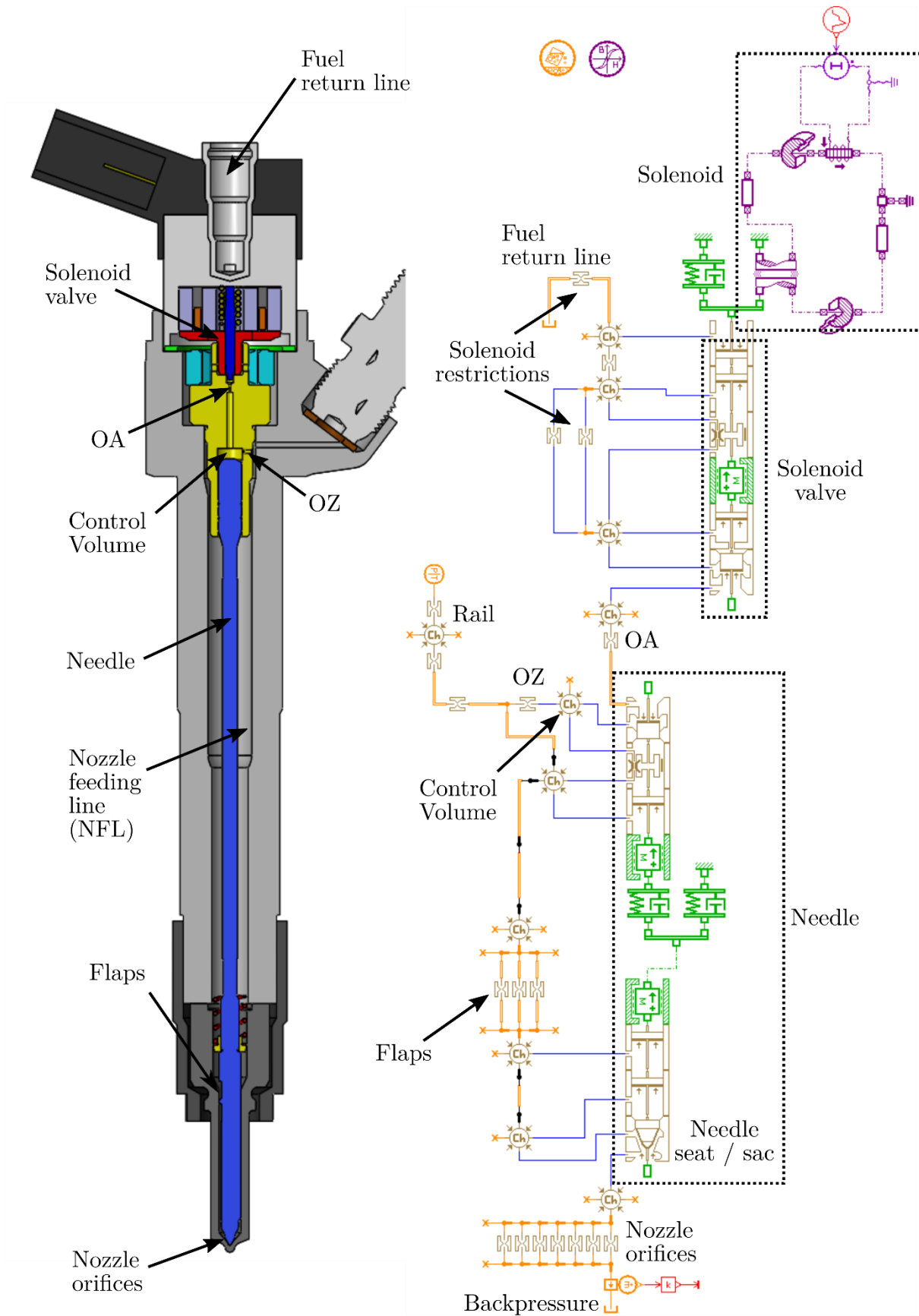
101 The purpose of this work is to gain further understanding on the topic thanks to the use of a 1D model improved by the  
102 implementation of the adiabatic flow assumption. Details on the implementation of this hypothesis and the assessment of  
103 its validity for realistic conditions are addressed in the first part of the paper [23]. In the current paper, the model is  
104 extensively validated against experimental results and then used to quantitatively estimate the fuel temperature variations  
105 along a solenoid-driven common-rail injector. This prediction allows to study the influence of the fuel temperature and  
106 its changes on injector dynamics and the injection rate shape thanks to the analysis of the flow regime that these variations  
107 establish on the internal orifices driving the solenoid valve. On the other hand, the estimation of the fuel temperature at  
108 the injector outlet will be relevant for experimentalists in the field and CFD modellers in need of suitable boundary  
109 conditions. Additionally, since the propagation of the pressure wave along the injector will have been validated, split  
110 injection strategies are also explored. In this regard, the time needed to split successive injections is determined as a  
111 function of the inlet fuel temperature and the rail pressure. An assessment on the influence of these operating conditions  
112 on the mass injected by separated injections is also carried out.

113

## 114 **2. VALIDATION OF THE 1D ADIABATIC MODEL OF THE INJECTOR**

115 In the first part of the paper, the validity of the adiabatic flow hypothesis has been evaluated and it has been established

116 that, prior to a given injection, it may be necessary to consider a certain fuel temperature change at the injector inlet with  
117 respect to the fuel temperature in the rail [23]. Keeping this fact in mind, the model of the Bosch CRI 2.20 implemented  
118 in AMESim (here reproduced as Figure 1 for illustrating purposes) can now be validated as a whole for a wide range of  
119 operating conditions. This validation is carried out in two steps. First, the ability of the model to estimate the mass flow  
120 rate and the temperature change across a single hydraulic restriction is tested under continuous flow. Once the proper  
121 behaviour is ensured for each orifice, the model capabilities in terms of predicting the way the pressure waves are  
122 transmitted along the injector (mandatory for a proper description of the multiple injection strategies) and the delivered  
123 ROI are ensured for regular pulsed injections.



124

125 Figure 1. Bosch CRI 2.20 injector diagram and AMESim model sketch.

Payri, R., Salvador, F.J., Carreres, M., Belmar-Gil, M., "Thermal effects on the diesel injector performance through adiabatic 1D modelling. Part II: Model validation, results of the simulations and discussion", Fuel 260:115663 (author version).

doi: 10.1016/j.fuel.2019.115663

126 **2.1. Mass flow rate prediction through a single injector orifice**

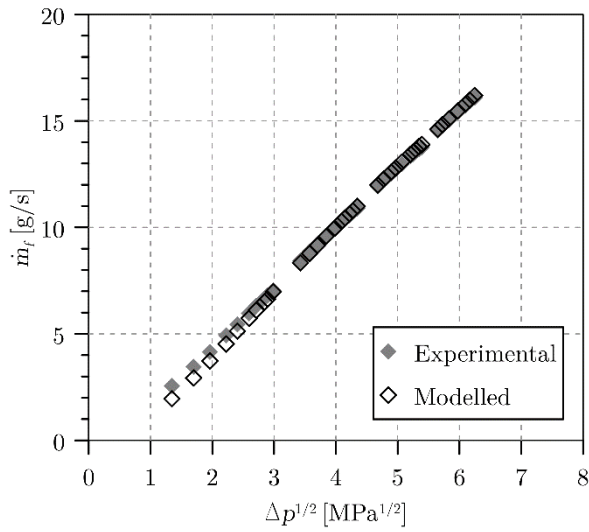
127 Prior to the validation of the injector as a whole, the behaviour of the most significant hydraulic restrictions of the injector  
128 (namely the OZ, OA and nozzle orifices; seen in **Figure 1**) was independently validated against experimental  
129 measurements of mass flow rate under continuous flow carried out by the authors in a previous work [24]. As stated in  
130 the first part of the paper [23], these measurements were taken by isolating the orifice to be tested within a purpose-built  
131 test rig and submitting it to a controlled pressure drop. Specifically, this was achieved by setting a value of upstream  
132 pressure ( $p_{up}$ ) and independently modifying the downstream pressure ( $p_{dw}$ ). This procedure was repeated for several values  
133 of upstream pressure. Conditions tested to reproduce all the possible flow regimes induced during the regular operation  
134 of the injector are compiled in Table 1. In the particular case of the multi-hole nozzle, the large effective area of the 7  
135 orifices prevented the two largest values of  $p_{up}$  from being tested, due to flow rate limitations in the high pressure pump.

$p_{up}$ [MPa]	$p_{dw}$ [MPa]
5	0.5, 1, 1.5, 2, 2.5, 3, 3.5, 4, 4.2, 4.4, 4.6, 4.8
10	0.5, 1, 1.5, 2, 2.5, 3, 4, 5, 6, 7, 8, 9
20, 30, 40, 50, 60	0.5, 1, 1.5, 2, 2.5, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12

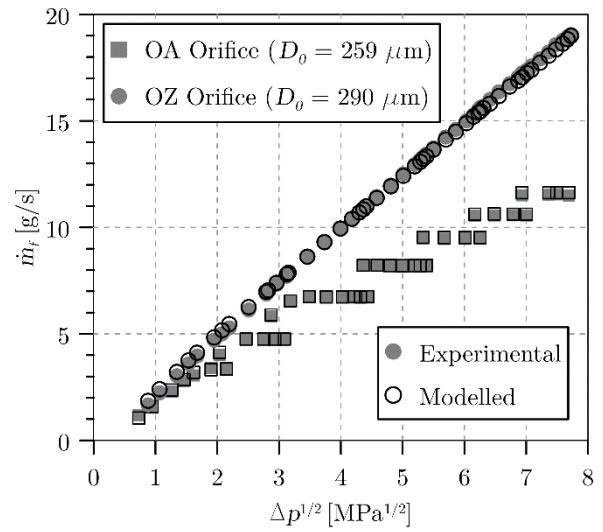
136 Table 1. Conditions considered in the independent validation of the flow through the injector internal orifices.

137 The experimental facility was reproduced in AMESim with the same model of the orifice used for the complete injector  
138 model. Results of this validation are shown in **Figure 2**. Focusing on the nozzle orifices, **Figure 2(a)** shows that the mass  
139 flow rate is linear with respect to the square root of the pressure drop. This implies that the nozzle does not cavitate for  
140 any of the operating conditions tested [25,26]. Results show a good agreement for most of the pressure conditions tested.  
141 The highest deviations in the predictions take place for the lowest values of the pressure drop, resulting in an  
142 underestimation of the mass flow rate. The explanation for these deviations resides in the low values of  $Re$  established  
143 for these conditions, which induce a laminar flow regime or the laminar-turbulent transitional regime. In these flow  
144 regimes, the nozzle orifices discharge coefficient has not reached its asymptotic behaviour yet [27]. The model computes  
145 the discharge coefficient at each time step through a certain function of the local  $Re$ , as described in the previous work by  
146 the authors on the isothermal variant of the model [17]. This modelled trend could lead to larger deviations in the regime  
147 transition. Anyway, the deviations are bounded for values of  $\Delta p^{1/2} > 3$  (i.e. pressure drops around 9 MPa), reached in the  
148 injector nozzle for the typical engine operating conditions).





(a) Nozzle orifices (7 orifices with  $D_0 = 117 \pm 1 \mu\text{m}$ ).



(b) Control volume orifices.

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Figure 2. Modelled mass flow rate through the injector internal orifices compared against experimental data.

The comparison for the control volume orifices is shown in **Figure 2(b)**. In the case of the OZ orifice, cavitation is not found either and the mass flow rate predictions show a good agreement with the experimental measurements. Focusing on the OA orifice, a mass flow collapse is detected for each value of upstream pressure from a certain value of downstream pressure. The deviations among the predictions and the experiments are negligible, also demonstrating the ability of the model to predict the appearance of cavitation.

## 2.2. Temperature change prediction through a single injector orifice

As stated in the first part of the paper [23], the temperature changes across an injector restriction are computed considering the adiabatic flow assumption through Eq. (1):

$$h(T_{dw}, p_{dw}) = h(T_{up}, p_{up}) - \frac{1}{2} \Delta u^2 \quad (1)$$

159

160

161

162

For the restrictions where the velocity change is not relevant (such as the nozzle feeding line), Eq. (1) leads to the conservation of specific enthalpy in order to calculate the temperature changes through them. In the particular orifices submitted to large pressure drops (such as the nozzle orifices and the OA orifice), Eq. (1) could be approximated by Eq.

(2):

$$h(T_{dw}, p_{dw}) \approx h(T_{up}, p_{up}) - \left(\frac{C_d}{C_a}\right)^2 \frac{(p_{up} - p_{dw})}{\rho_f} \quad (2)$$

163

164

It is important to note here that cavitation leads to a local cooling associated with the enthalpy of phase change. This phenomenon is not taken into account by the model, considering its relatively low importance as found by Franc [28] for

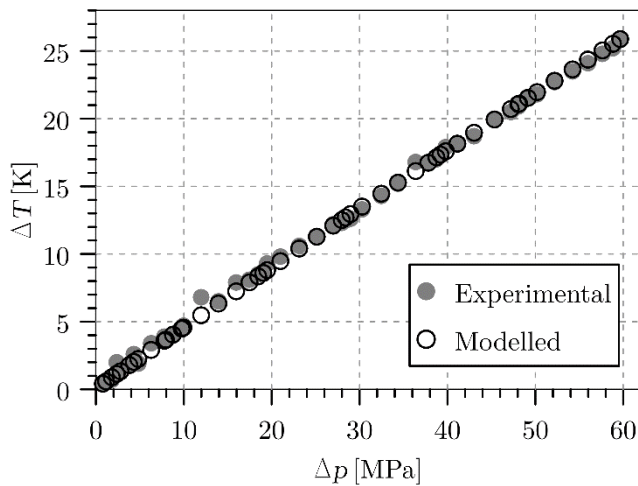
165 other fluids and checked by the authors in the case of diesel fuel (in the order of  $10^{-3}$  K). In addition, as highlighted in  
166 **Section 2.1**, cavitation was only found in the OA orifice. Therefore, the omission of the enthalpy phase change due to  
167 cavitation is not expected to influence the validity of the model estimations.

168 In this Section, the temperature changes predicted by the model across the OZ orifice (for which  $C_a = 1$  due to the absence  
169 of cavitation [29]) are compared to experimental results. In the experiments used as a basis for the validation of Section  
170 2.1, the temperature variation across the injector internal orifices was also measured for the set of upstream and  
171 downstream conditions depicted in Table 1 [24], controlling the upstream temperature at all times so that  $T_{up} = 293$  K.  
172 Figure 3 shows the results of the comparison of the temperature drop predicted by the model against the experimental  
173 results for the OZ orifice. As expected according to the *specific enthalpy map* of the winter diesel fuel presented in the  
174 first part of the paper [23], the temperature change upon expansion tends to increase linearly with the pressure drop. The  
175 computational results offer a good prediction of the experimental data, with the higher deviations being present for the  
176 lowest values of pressure drop. This fact is aligned with the findings of the previous work by the authors [24], in which  
177 the dimensionless parameter defined in Eq. (3) was derived to establish the variables that influenced the proneness of the  
178 flow through an orifice to exchange heat with the surroundings.

$$Ad = \frac{1}{4} \frac{D}{L} St^{-1} = \frac{1}{4} \frac{D}{L} \frac{Pr Re}{Nu} \quad (3)$$

179 The different diameter of the internal orifices and the different conditions (i.e. pressure drops) experimentally tested were  
180 associated to several values of  $Ad$ . It was found that low values of  $Ad$  ( $Ad < 4$ ) could lead to a significant heat exchange  
181 during the process, whereas high values of  $Ad$  ( $Ad > 6$ ) led to heat transfer being practically negligible. Thus, the lowest  
182 pressure drops in Figure 3 lead to low values of  $Ad$  for which heat transfer from the surroundings prevents the adiabatic  
183 flow assumption from being accurate. Nevertheless, such low values of pressure drop only take place during short  
184 transients at the injector opening (when the pressure at the control volume is still close to the rail pressure) or closing, but  
185 they do not take place across this orifice during the steady operation of the injector. Please note that the heating produced  
186 inside the OZ orifice for a pressure drop of 60 MPa (representative of the steady pressure drops established through this  
187 orifice for usual engine operating conditions) is close to 30 K. This increase can affect the fuel properties at the orifice  
188 outlet, influencing injector dynamics, as explored in the present investigation.

189



190

191 Figure 3. Modelled temperature change through the injector OZ orifice compared against experimental data.

192 **2.3. Pressure waves transmission**

193 Once the injector computational model has been partially validated by ensuring its ability to predict the individual  
 194 behaviour of the internal orifices, the accuracy of the predictions of the complete injector model must be tested for a wide  
 195 range of operating conditions. As the first step to this end, the modelled evolution of the pressure at the injector inlet is  
 196 compared to the experimental evolution found at this location for the ROI measurements performed in a previous work  
 197 [30]. This comparison allows to assess the capability of the model to describe the propagation of the pressure wave along  
 198 the injector. This capability is key to ensure a proper prediction of the injector behaviour under split injection strategies,  
 199 considering that once an injection finishes, the induced pressure wave influences the next injection event depending on  
 200 the timing among injections.

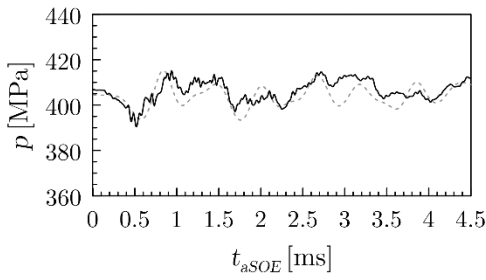
201 The operating conditions for which the ROI measurements were taken are summarized in Table 2. A wide range of values  
 202 of the fuel temperature at the injector inlet (from those ones representative of cold-start to those others representative of  
 203 long engine runs), injection pressures and energizing times (from short injections to injections long enough to ensure that  
 204 the steady conditions are accurately described) are considered. It is important to note that these experimental  
 205 measurements were taken in a laboratory environment in which  $T_i$  was controlled and the hardware was thermally  
 206 insulated so that  $T_i = T_w$ . This implies that the heat transfer process in the time lapse among injections is not relevant.  
 207 Heat transfer could only take place during the injection itself if the  $Ad$  values induced across the injector hydraulic  
 208 restrictions were low. It was already stated in Section 2.2 that this might be the case during the transient stages (injector  
 209 opening and closing), whereas in steady-state conditions it can be ensured that  $Ad$  is high enough to prevent heat transfer  
 210 from being relevant. In short, heat transfer in the experiments could only be relevant to some extent during the transient  
 211 stages of the injection, being negligible when steady-state conditions are reached. In these conditions, the flow can be

212 safely regarded to as adiabatic.

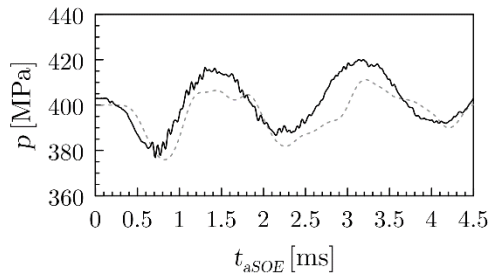
Property	Values tested
$T_i$ [K]	253 – 273 – 303 – 353 – 373
$p_i$ [MPa]	40 – 70 – 120 – 180
$p_b$ [MPa]	4
ET [ms]	0.25 – 0.5 – 1

213 Table 2. Operating conditions tested in the experimental ROI measurements used to validate the injector model.

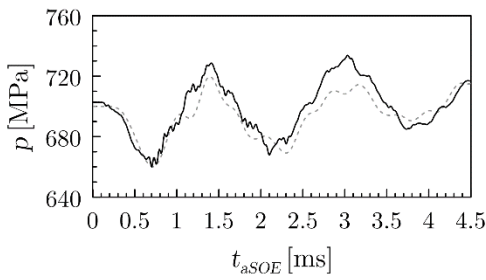
214 Sample comparisons among the modelled and the experimental pressure evolution at the high-pressure line connecting  
215 the *common-rail* to the injector are shown in Figure 4, covering the conditions corresponding to the most extreme values  
216 of speed of sound in the ROI measurements (low pressures and high temperatures on the one hand, with high pressures  
217 and low temperatures on the other). Different energizing times are also shown. As can be seen, the model accurately  
218 represents the pressure evolution for most of the tested points. The first drop in pressure, which coincides with the injector  
219 opening, always takes place slightly later for the injector model. As highlighted by the points corresponding to ET = 0.5  
220 ms, both the period and the amplitude of the oscillations are properly predicted. The amplitude of the second pressure  
221 peak is underestimated, although the differences seem to be reduced for the next peak. Results for the extreme energizing  
222 times are less accurate, especially in terms of amplitude, even though the period of the oscillations seems to be captured.  
223 The proper matching of this last parameter is essential for the model behaviour, since it defines the trends followed by  
224 the mass injected by post-injections depending on the dwell time among injections, as explored in Section 4.



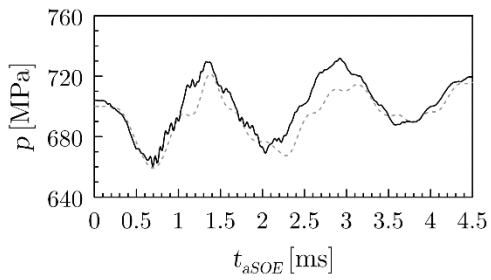
(a)  $p_i = 40$  MPa,  $T_i = 373$  K, ET = 0.25 ms



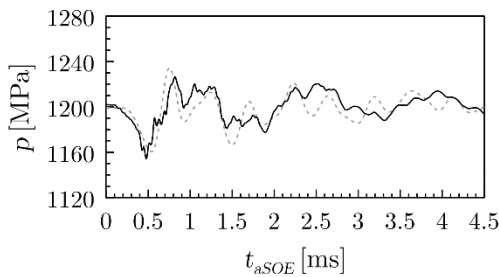
(b)  $p_i = 40$  MPa,  $T_i = 373$  K, ET = 0.5 ms



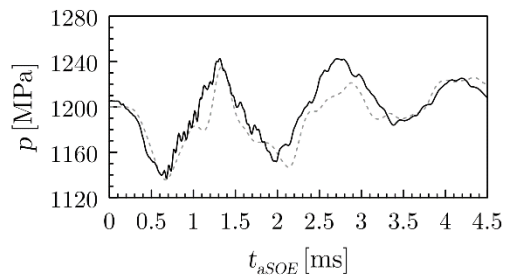
(c)  $p_i = 70$  MPa,  $T_i = 353$  K, ET = 0.5 ms



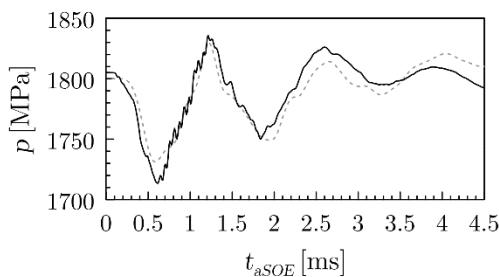
(d)  $p_i = 70$  MPa,  $T_i = 303$  K, ET = 0.5 ms



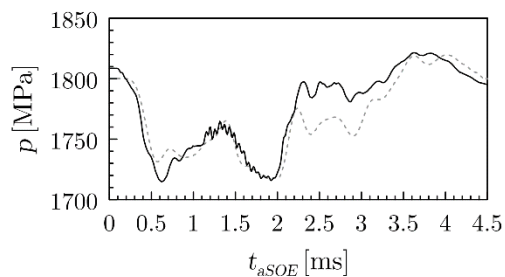
(e)  $p_i = 120$  MPa,  $T_i = 303$  K, ET = 0.25 ms



(f)  $p_i = 120$  MPa,  $T_i = 303$  K, ET = 0.5 ms



225 (g)  $p_i = 180$  MPa,  $T_i = 253$  K, ET = 0.5 ms



(h)  $p_i = 180$  MPa,  $T_i = 253$  K, ET = 1 ms

226 Figure 4. Modelled pressure signal (dashed) at the common-rail high pressure line compared against experimental data  
 227 (continuous).

#### 228 2.4. Prediction of the mass flow rate at the injector outlet

229 The analysis of the behaviour in terms of fuel delivery by the injector is the last step to validate the computational model.

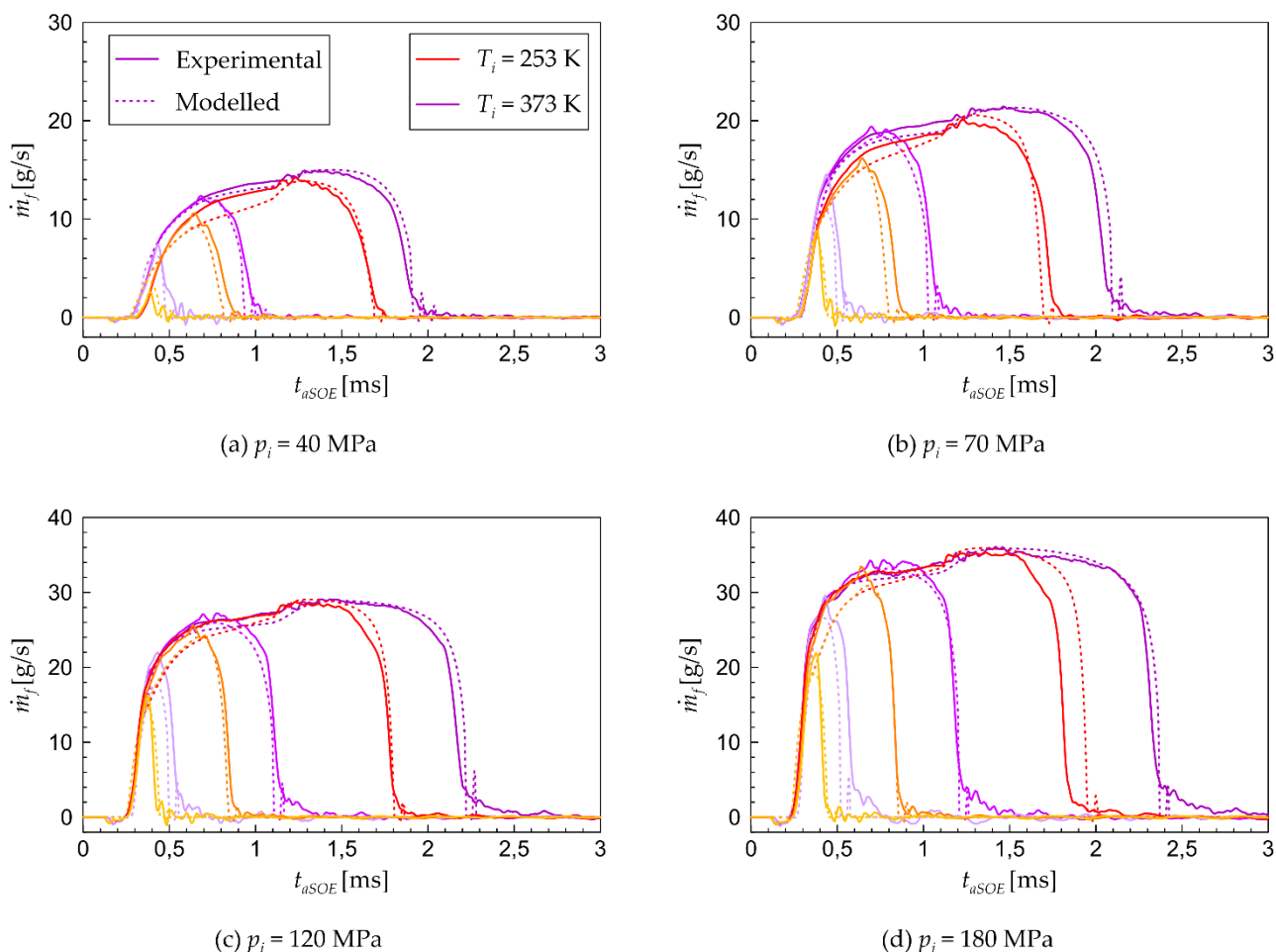
230 Figure 5 shows the comparison of the modelled ROI with the experimental data for the extreme values of fuel temperature

231 at the injector inlet for the different energizing times tested. These experimental data are available in a previous work by  
232 the authors [30], where details on the experimental campaign and the methodology employed to control the fuel  
233 temperature at the injector inlet were reported. Further details on the processing, filtering and correction of the measured  
234 signal in order to obtain ROI curves with the Bosch long tube method can also be found in a previous work by the authors  
235 [31]. The authors quantified the uncertainty of this methodology in providing the injected mass flow rate to be lower than  
236 2%.

237 On the one hand, Figure 5 reproduces the main findings previously reported in [30] concerning injector dynamics and the  
238 steady-state stage of the injection: the injector opening is slower for low values of  $T_i$ , due to the high fuel viscosities  
239 associated to low temperatures. This fact delays needle dynamics due to an enhancement of viscous friction and a change  
240 in the flow regime in the control volume orifices, as will be quantified in Section 4. This effect is more accused for low  
241 injection pressures. In addition, the injection duration is appreciably reduced the lower the value of fuel temperature. This  
242 can be explained due to the ballistic nature of the injector, considering that the increase in viscosity at low temperatures  
243 results in a lower position of the needle being achieved during the injector energizing. Therefore, the distance the needle  
244 needs to travel to close back against its seat is shorter, travelling it in reduced times. As far as the steady-state stage of the  
245 injection is concerned, the experimental results depicted in Figure 5 were analysed in the previous work, showing that for  
246 low injection pressures the steady-state ROI increases when the fuel temperature increases (despite the reduction in fuel  
247 density), whereas for high injection pressures the steady-state ROI decreases when the fuel temperature increases. This  
248 was explained considering the opposed effects of the fuel temperature on the mass flow rate through the fuel density itself  
249 and through the discharge coefficient (in turn influenced by the fuel density and viscosity). In any case, the relative  
250 differences among cases are found to be low, and they could already be satisfactorily explained without the aid of the  
251 model. They are thus not analysed in the present work since the local variations of fuel temperature do not give a deeper  
252 insight into the topic.

253 On the other hand, Figure 5 proves the ability of the adiabatic model to predict the actual behaviour of the injector, both  
254 during the transient and steady stages of the injection event. The predictions are reasonable for most operating conditions,  
255 with a certain underprediction of the mass flow rate during the opening for the extreme case of low pressure and low  
256 temperature. Precisely, these are the conditions for which the adiabatic flow assumption is less valid, due to the low values  
257 of  $Re$  induced to the flow through the orifices, resulting in turn in a low  $Ad$  even during the steady-state stage of the  
258 injection. Nevertheless, it must be noted that the previous version of the model presented by the authors (using the  
259 assumption of isothermal flow) could not be validated for  $T_i < 273$  K [17]. It can then be stated that the introduction of

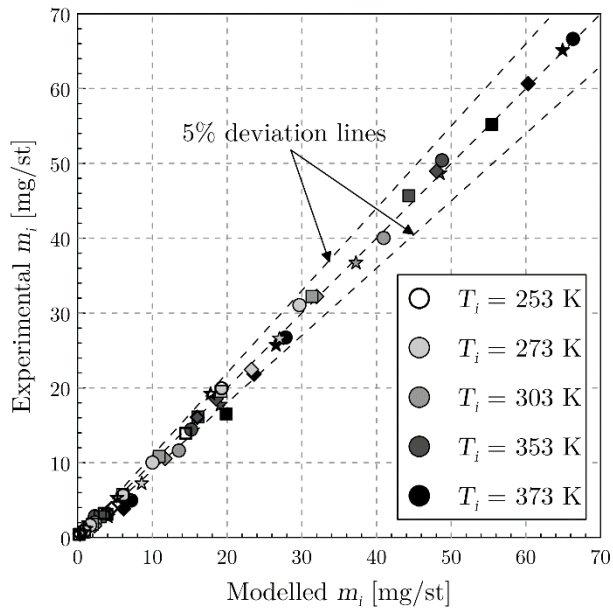
260 the assumption of adiabatic flow allows widening the range of injector operating conditions for which a 1D model is valid,  
 261 including the extreme temperature conditions found for the cold-start operation of the injector.



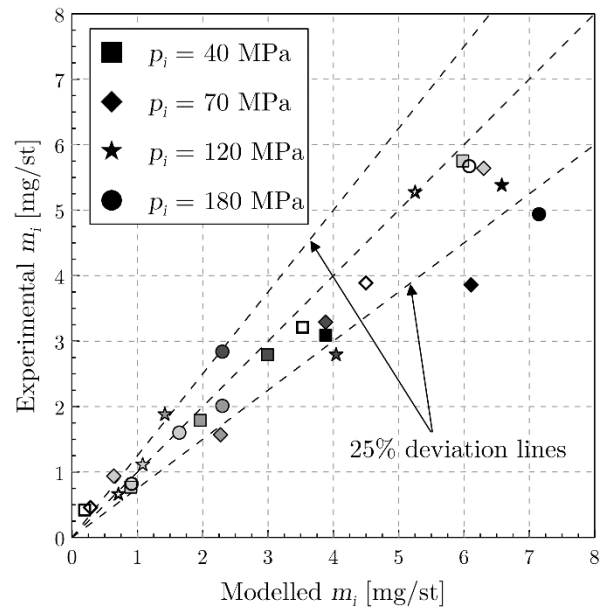
262 (a)  $p_i = 40$  MPa (b)  $p_i = 70$  MPa  
 263 (c)  $p_i = 120$  MPa (d)  $p_i = 180$  MPa

263 Figure 5. Modelled ROI compared against experimental data from [30]. Each plot shows results for ET = 0.25 ms (light  
 264 color), ET = 0.5 ms (medium color) and ET = 1 ms (dark color).

265 As a summary of the validation results, including all the operating conditions compiled in Table 2, **Figure 6** shows the  
 266 comparison between the modelled and experimental results of total mass injected per injection event. The lines  
 267 representing the perfect matching and 5% of deviation are also depicted. Results show a fair prediction for most of the  
 268 operating conditions studied, as a consequence of the findings from Figure 2 to Figure 5. More than 90% of the conditions  
 269 leading to  $m_i > 10$  mg/st show deviations lower than 5%. The conditions resulting in the poorest predictions generally  
 270 correspond to the extreme cases of injection pressure and temperature. The injections corresponding to  $m_i < 8$  mg/st are  
 271 shown in Figure 6(b). For those conditions, more than 70% of the tested points have been predicted with a deviation lower  
 272 than 25%. It should be noted that, for these small quantities, short absolute deviations lead to a high percentage of  
 273 deviation even if the ROI curve is accurately modelled.



(a) All operating conditions tested.



(b) Detail of the short injections.

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Figure 6. Modelled mass injected per stroke compared against experimental data.

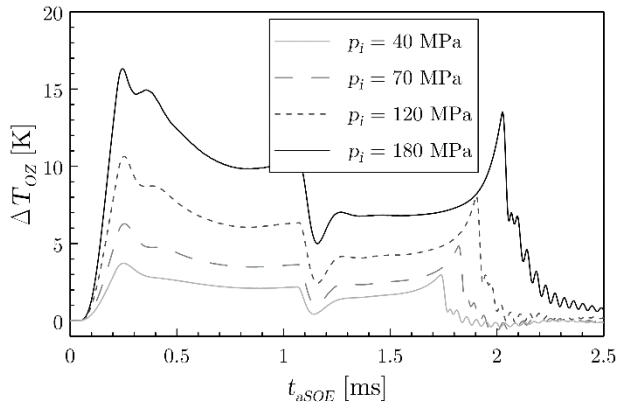
### 3. MODEL PREDICTION OF THE FUEL TEMPERATURE VARIATIONS ALONG THE INJECTOR

The temperature variations computed by the model through the most important injector restrictions during a pulsed injection are analysed in this Section. These temperature changes result in variations in the fuel properties that, in turn, establish the flow regime across the restrictions controlling injector dynamics. Hence, the resulting flow regime in the orifices is identified for each injector operating condition, allowing to determine the conditions for which the pressure in the control volume drops in a quicker way. This evolution of the pressure in the control volume, together with the viscous forces opposing the needle motion, will help analysing injector dynamics in Section 4.

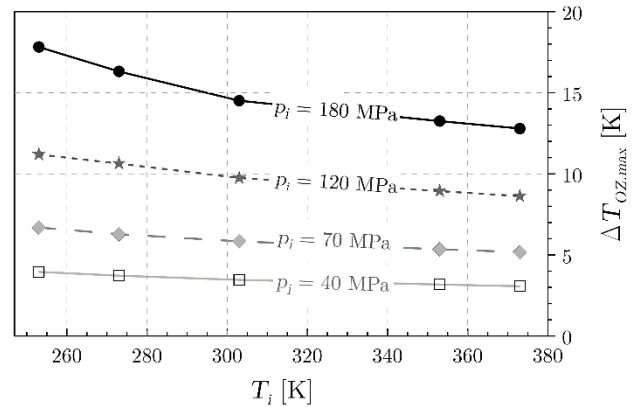
#### 3.1. Analysis for the control volume orifices and hydraulic lines

Figure 7 shows the predicted temperature changes across the control volume orifices and the nozzle feeding hydraulic line NFL (line among the OZ orifice and the nozzle sac, recall Figure 1), deemed to be the most important ones in the possible paths of the fuel along the injector. For each restriction, the temporal evolution of the temperature variation is presented for the different values of  $p_i$  tested and a sample value of  $T_i$  (ET = 1 ms). As a synthesis, the maximum temperature change registered for each operating condition is also shown for each restriction.

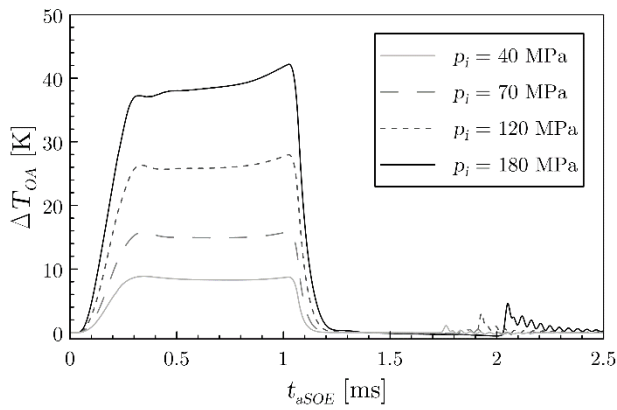




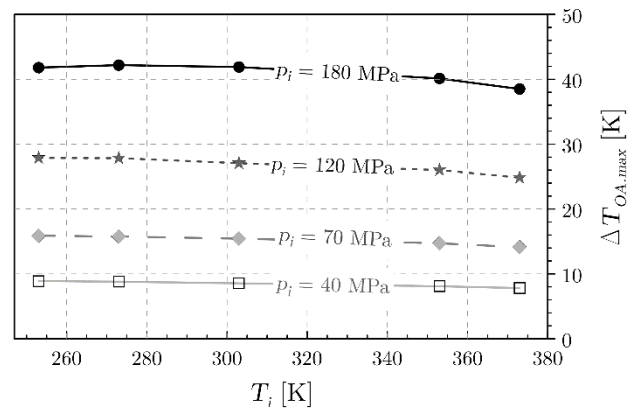
(a) Temporal evolution of  $\Delta T$  across OZ ( $T_i = 273$  K).



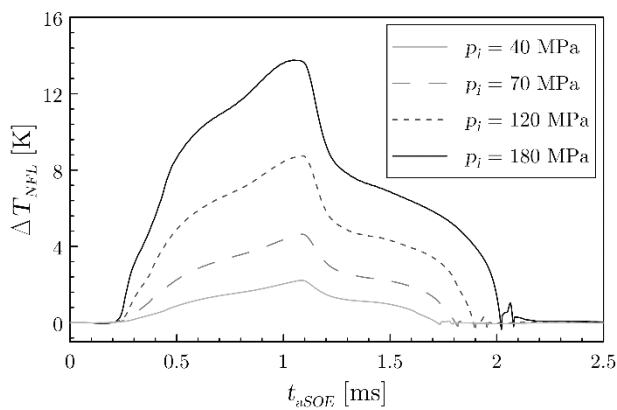
(b) Maximum  $\Delta T$  across OZ (all operating conditions).



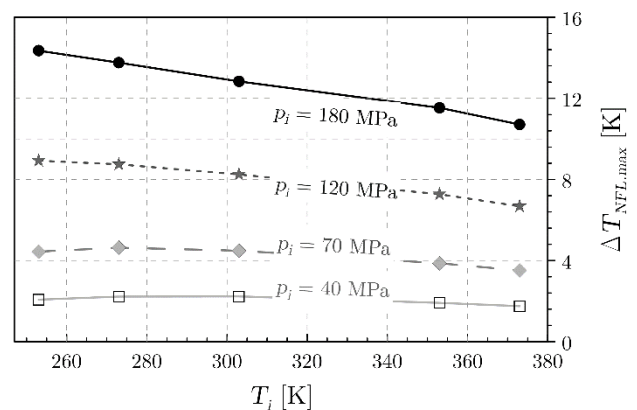
(c) Temporal evolution of  $\Delta T$  across OA ( $T_i = 253$  K).



(d) Maximum  $\Delta T$  across OA (all operating conditions).



(e) Temporal evolution of  $\Delta T$  along NFL ( $T_i = 303$  K).



(f) Maximum  $\Delta T$  along NFL (all operating conditions).

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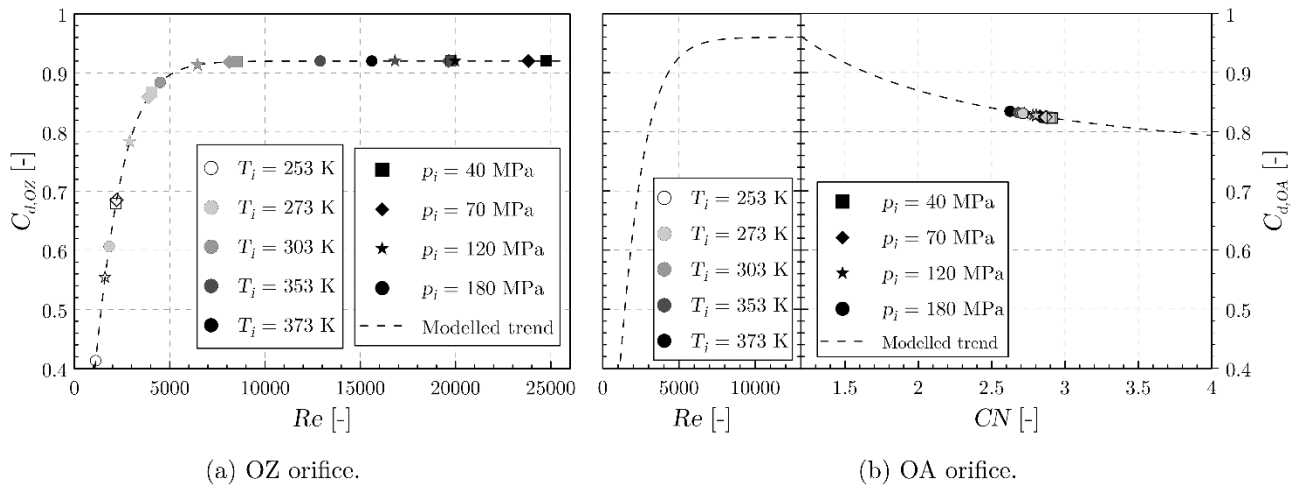
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Figure 7. Temperature changes across the control volume orifices and the nozzle feeding line.

Starting with the OZ orifice, Figure 7(a) shows that the fuel temperature increases through the orifice during the whole injection. Considering that this restriction generates a pressure drop in the control volume, this fact is consistent with the reasoning made in the first part of the paper [23] (in the view of Eq. (1) and considering a negligible velocity change

294 across the orifice) about the fuel temperature increasing upon this adiabatic expansion. Therefore, the temperature rise is  
295 greater the higher the injection pressure, since the absolute pressure drop across the orifice also gets larger. The computed  
296 temperature change is not constant during the injection: after a first peak matching the injector opening stage ( $t_{aSOE} \approx$   
297 0.3 ms),  $\Delta T$  gets less important during the injection. This fact can be explained because the pressure upstream of the  
298 orifice decreases when a higher amount of fuel bypasses the OZ orifice inlet and leaves the injector through the nozzle  
299 feeding line and the nozzle orifices, resulting in a less important pressure drop through OZ. When the injector stops being  
300 energized and the pressure in the control volume is restored, the pressure drop across OZ is even lower, generating the  
301 valley in the curve ( $t_{aSOE} \approx 1.2$  ms). At this moment, the needle starts falling, leaving more room above it (i.e. in the  
302 control volume) for the fuel, which keeps being introduced through OZ. The orifice still generates a pressure drop that  
303 leads to the temperature rise observed until the injector completely closes.

304 Figure 7(a) and Figure 7(b) show that the maximum temperature change is greater the higher the injection pressure, as it  
305 has been justified. Moreover, for each injection pressure, the temperature increase is more accused the lower  $T_i$ . This fact  
306 can be attributed to the orifice working under a different flow regime at low temperatures. In this sense, Figure 8(a) shows  
307 the modelled evolution of the discharge coefficient of the inlet orifice as a function of  $Re$ . As it may be seen, there is a  
308 certain temperature value from which no influence of  $T_i$  on the discharge coefficient is reported. Namely, for  $T_i > 303$  K,  
309 the maximum discharge coefficient is already reached regardless of the injection pressure. On the contrary, for lower  
310 values of  $T_i$ , the higher fuel viscosity induces a laminar flow regime that leads to a lower discharge coefficient, implying  
311 higher losses through the orifice. As a consequence, the pressure drop established in the control volume is relatively larger  
312 than the one found for higher values of  $T_i$ , leading to a greater temperature rise across OZ as seen in Figure 7(b). This  
313 reasoning also explains why the trend of  $\Delta T_{OZ,max}$  with  $T_i$  is not completely linear for the highest injection pressure, since  
314 the associated  $C_d$  importantly varies in this region.



315

(a) OZ orifice.

(b) OA orifice.

316 Figure 8. Discharge coefficient predicted for the control volume orifices according to the flow regime set during the  
 317 opening stage at the tested operating conditions.

318 In the case of the OA orifice, the analogous results of temperature change across the restriction are shown in Figure 7(c)  
 319 and Figure 7(d). The temperature upstream of this orifice matches the one downstream of OZ (as per Figure 7(a) and  
 320 Figure 7(b)). Therefore, the complete temperature variation from the injector inlet to the fuel return line is the addition  
 321 of both values of  $\Delta T$ . In this case, the fuel only crosses the orifice while the electromagnetic valve is open (recall Figure  
 322 1). During this period, the temperature change is almost constant with time. The magnitude of the temperature rise along  
 323 this orifice is greater than the one reported for OZ. This is due to the larger pressure drop expected across this orifice for  
 324 the injector operating conditions, since the fuel is discharged from the control volume to the return side of the injector (at  
 325 atmospheric pressure) through this orifice and some minor hydraulic restrictions in the solenoid valve (depicted in the  
 326 model sketch from Figure 1). The absolute pressure drop along this orifice is higher the larger the injection pressure,  
 327 justifying the findings from Figure 7(c) and Figure 7(d) for which the temperature variation grows higher with the  
 328 injection pressure. For this orifice, the values of  $\Delta T_{OA,max}$  shown in Figure 7(d) are representative of both the opening  
 329 and closing stages of the injection event. The temperature rise across this orifice is mostly governed by the injection  
 330 pressure, with only a marginal influence of the fuel temperature at the injector inlet. This low influence of  $T_i$  can be  
 331 attributed to the fact that the flow through OZ is prone to cavitate, as depicted in Figure 2(b). Figure 8(b) shows the  
 332 discharge coefficient predicted for OZ at the injector opening stage. The modelled trends for  $C_d$  as a function of  $Re$  (for  
 333 non-cavitating conditions) and the so-called cavitation number  $CN$  (for the cavitating ones) are shown, together with the  
 334 points corresponding to the variables induced for each injector operating condition.  $CN$  is defined by Eq. (4) (for more  
 335 details on the significance of this variable, please refer to some works where it was introduced [26] and applied [17]):

$$CN = \frac{p_{up} - p_{dw}}{p_{dw} - p_v} \quad (4)$$

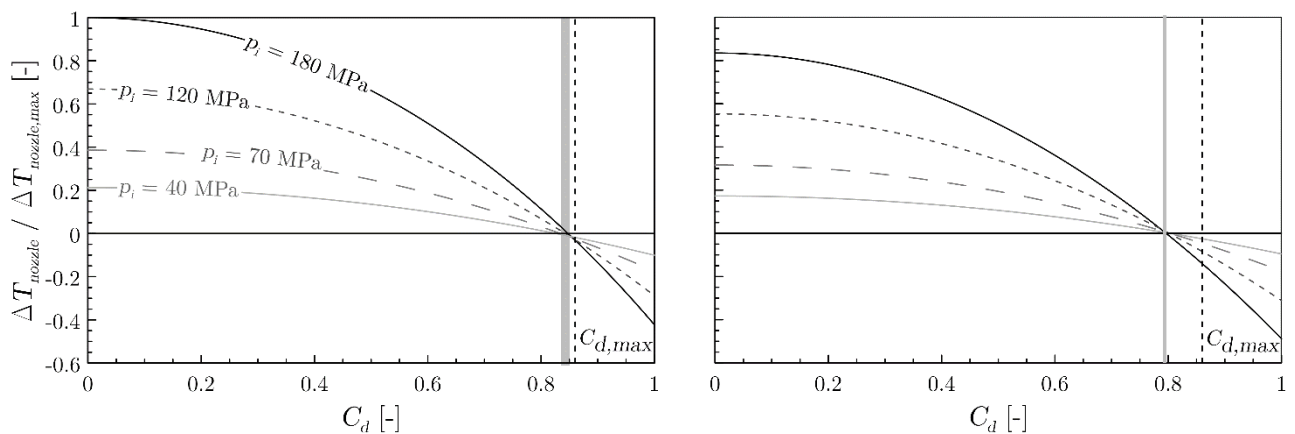
336 **Figure 8(b)** then shows that cavitation appears for all the injector operating conditions tested due to the large pressure  
 337 drops established across OZ. This implies that  $C_d$  is not dependent on  $Re$  (which varies with the fuel properties induced  
 338 by each condition of temperature and pressure) but rather on  $CN$  (which exclusively depends on the pressure ratio among  
 339 upstream and downstream pressure). As it can be seen in the figure,  $CN$  takes similar values regardless the injection  
 340 pressure tested (since the pressure drop from the control volume to the atmospheric pressure is proportionally splitted  
 341 among the OA orifice and the minor restrictions in the solenoid valve shown in **Figure 1**), not significantly modifying  
 342  $C_d$ . The low differences among temperature rise observed for the different values of  $T_i$  could be attributed to these marginal  
 343 differences. In addition, the temperature upstream of OA has already been submitted to the temperature change through  
 344 OZ, meaning that the different temperature rises induced in OZ depending on the injection pressure and temperature also  
 345 influence the starting temperature for the expansion across OA.

346 As far as the nozzle feeding line (NFL) is concerned, this line contains the flaps (see **Figure 1**) as a significant constraint  
 347 to the flow. These restrictions impose the pressure losses responsible for the temperature variations shown in **Figure 7(e)**  
 348 and **Figure 7(f)**, which need to be taken into account to determine the conditions right upstream of the nozzle orifices. In  
 349 this case, the maximum temperature variations take place when the solenoid valve stops being energized. The magnitude  
 350 of the temperature changes is not relevant at low injection pressures, but it is not negligible from medium values of  
 351 injection pressure. No significant influence of the fuel temperature at the injector inlet is noticed for the low pressure  
 352 cases, although differences among temperatures are reported for higher values of injection pressure. The reasons for this  
 353 behaviour are analogous to the ones given for OZ.

### 354 **3.2. Analysis for the nozzle orifices**

355 The adiabatic flow through the nozzle implies that the stagnation enthalpy is preserved, with an important change in  
 356 kinetic energy along the orifices. As established by Eq. (2), the temperature downstream of the orifices depends not only  
 357 on the specific enthalpy of the fuel, but also explicitly on the pressure drop across the orifices, their discharge coefficient  
 358 and the fuel density, assuming  $C_a \approx 1$  since cavitation was not found in the nozzle orifices of the Bosch CRI 2.20 injector  
 359 (**Figure 2(a)**). It is important to remind that Eq. (2) was derived under the assumption that no net work was done on the  
 360 system or by the system. As stated in the first part of the study, this assumption may not hold during the transient stages  
 361 of the injection, when the low needle lift may lead to an exchange of mechanical work with the flow established through  
 362 the nozzle [23]. In a previous investigation, the authors reported that the interaction among needle and nozzle flow only

363 seems to be relevant for needle lift values lower than  $75 \mu\text{m}$  [16]. This situation is restricted to about 0.1 ms during both  
 364 the opening and closing stages of the injection. In this section, quantitative results are only reported for steady conditions,  
 365 once the rate of injection is nearly constant with time. This will ensure that any deviation introduced by this assumption  
 366 on the fuel temperature calculations is already damped by the time steady-state conditions are reached.  
 367 In any case, it is interesting to analyse the steady-state temperature change ( $t_{aSOE} = 1 \text{ ms}$  for the cases of  $ET = 1 \text{ ms}$ )  
 368 modelled by Eq. (2) along the nozzle orifices as a function of their  $C_d$  for the different operating conditions tested (the  
 369 steady values of upstream temperature and pressure passed by the nozzle feeding line discussed in Section 3.1 are thus  
 370 accounted for), as shown in Figure 9. This analysis illustrates the possible range of values of  $\Delta T$  across the nozzle orifices,  
 371 also serving a qualitative estimation on the expected behaviour in the transient stages of the injection: in these stages, the  
 372 needle motion when discovering or covering the orifices establishes low values of  $Re$  that in turn lead to low values of  
 373 discharge coefficient. The figure shows that, in steady-state conditions, the fuel temperature increases across the nozzle  
 374 for low values of  $C_d$ , due to the important losses associated. Indeed, there is a value of  $C_d$  for which the low losses and  
 375 high flow velocities result in the fuel being subcooled rather than heated. It is important to note that, given the 1D approach  
 376 followed in this work, the values of  $\Delta T$  presented correspond to the fuel bulk temperature. A similar result has been  
 377 reported in the literature through 3D CFD approaches by Theodorakakos et al. [32], Strotos et al. [33] and the authors  
 378 [34], showing that the fuel temperature is expected to vary in the radial direction, being heated in the wall vicinities where  
 379 the friction losses are located (boundary layer) and being subcooled near the orifices axes.



380 (a)  $T_i = 253 \text{ K}$ .

(b)  $T_i = 373 \text{ K}$ .

381 Figure 9. Steady-state temperature change across the nozzle as a function of the discharge coefficient ( $t_{aSOE} = 1 \text{ ms}$ ,  $ET = 1 \text{ ms}$ ). Values normalized with  $\Delta T_{nozzle,max} = 71.4 \text{ K}$  (found for  $T_i = 253 \text{ K}$  and  $p_i = 180 \text{ MPa}$ ).  $C_{d,max}$  is also represented.  
 382  
 383 The shaded bands highlight the transitional  $C_d$  for which the flow stops being heated and is subcooled.

384 The transitional  $C_d$  among heating and cooling in steady-state conditions is slightly lower than the maximum discharge  
 385 coefficient of the nozzle orifices. Hence, situations for which the fuel cools upon expansion through the nozzle may be

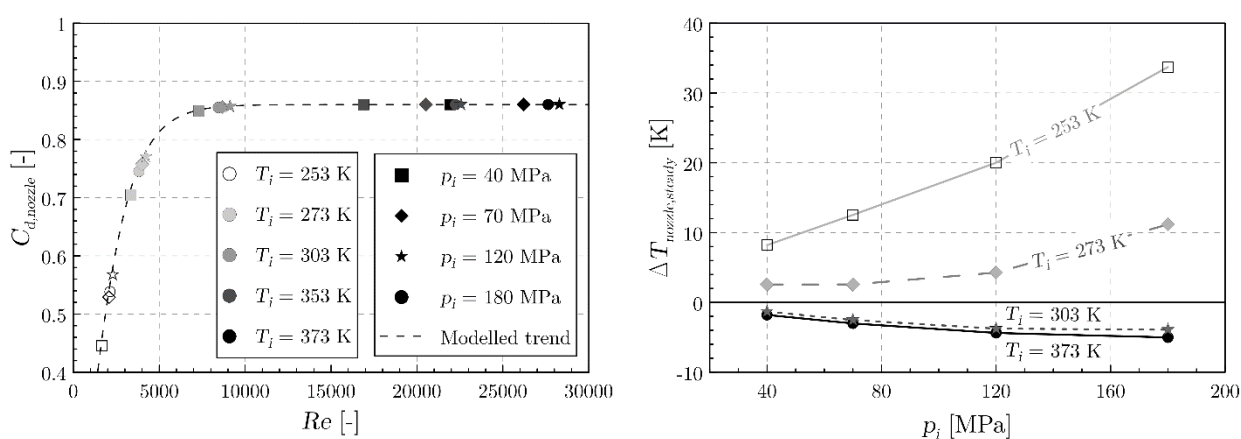
386 present. As can be seen in **Figure 9**, the fuel is expected to heat more importantly the lower  $T_i$  for low values of  $C_d$ . As it  
387 happened for the OA orifice, this can also be related to the different values of pressure and temperature set upstream of  
388 the nozzle after the losses through the NFL restriction. The effect of  $T_i$  on the temperature change through the nozzle also  
389 leads to the transitional discharge coefficient among heating and cooling being lower the higher the value of  $T_i$ . Hence,  
390 the difference among this transitional  $C_d$  and  $C_{d,max}$  gets higher, leaving room for a more important cooling effect the  
391 higher  $T_i$ .

392 In the view of these observations, the fuel temperature is expected to increase across the nozzle during the injector opening  
393 and closing transient stages. The low needle lifts impose a restriction to the flow that results in a lower effective cross-  
394 sectional area (i.e. lower effective diameter) of the orifices, implying a lower  $Re$  and higher losses that in turn lead to low  
395 values of discharge coefficient. Once steady conditions are achieved,  $C_d$  is expected to become higher and the pressure  
396 drop across the nozzle reaches the conditions for which the temperature changes were displayed in **Figure 9**. The  
397 magnitude of these temperature changes then depends on the flow regime established by each operating condition. In  
398 order to analyse them, **Figure 10(a)** shows the flow regime established through the nozzle orifices in steady conditions  
399 for each operating condition tested.

- 400 • As it can be seen on the one hand, values of temperature at the injector inlet above a certain threshold (found to  
401 be  $T_i \approx 283$  K) lead to the nozzle working in the turbulent regime regardless of the injection pressure, implying  
402  $C_{d,max}$  is reached. In these cases, the losses through the orifices are small, minimizing the viscous friction near  
403 the orifice walls and thus leading to the fuel being subcooled (mainly in the centre of the orifice) during the  
404 steady-state stage. The values of this cooling are reported in **Figure 10(b)**, where the justified low influence of  
405 the injection pressure is observed. The fact that a slightly greater cooling is observed for  $T_i = 373$  K can be  
406 explained since the value of  $C_d$  showing the transition among the cooling and heating effects departs more  
407 importantly from  $C_{d,max}$  the higher the fuel temperature, as stated in the view of **Figure 9**. In any case, the  
408 magnitude of this cooling is not high: considering the addition of the heating effect observed along the nozzle  
409 feeding line, it is possible to state that the fuel does not significantly change its temperature from the injector  
410 inlet to the nozzle outlet in steady-state conditions. Next, there will be a transitional time during the injection  
411 event (corresponding to a certain needle lift) from which the fuel stops being subcooled in order to be heated  
412 again during the closing stage.
- 413 • On the other hand, the nozzle orifices work in the laminar-turbulent transition for temperatures below a certain  
414 threshold ( $T_i \approx 283$  K), even during the steady-state stage, due to the exponential increase of the fuel viscosity

415 when both high pressures and low temperatures are combined. The variations in injection pressure strongly  
 416 modify the injector discharge coefficient through the Reynolds number, both by means of the effective velocity  
 417 and the fuel viscosity again. In these cases (even though to a lower extent than during the transient stages) the  
 418 fuel keeps being heated during the whole injection event. The values of  $\Delta T$  achieved during the steady-state  
 419 stage are shown in **Figure 10(b)**. This heating is more important the higher the injection pressure, displaying a  
 420 non-linear trend. This can be justified in the view of Eq. (2) by the combination of pressure drop and discharge  
 421 coefficient. The magnitude of this heating effect, added to the heating observed along the nozzle feeding line,  
 422 may importantly influence the flow conditions downstream of the nozzle and the spray development, especially  
 423 considering the high sensitivity of the fuel viscosity to changes in fuel temperature for cold conditions.

424 It is important to note that, if  $C_{d,max}$  had been higher for the injector nozzle, a lower heating effect would have been  
 425 observed for low values of  $T_i$  and a greater cooling effect would have been observed for high values of  $T_i$ . On the contrary,  
 426 higher temperatures at the nozzle outlet would have been observed if  $C_{d,max}$  had been lower, even leading to a net heating  
 427 for high values of  $T_i$ . Also, if  $C_{d,max}$  had been higher (keeping the same value of critical  $Re$  for transition among laminar  
 428 and turbulent regime), those operating conditions now leading to the laminar-turbulent transition in **Figure 10** would still  
 429 lead to this transitional regime. However, the slope of the curve in this transitional region would be greater, leading to a  
 430 lower heating effect (or even a cooling) being observed for low values of  $T_i$ . Hence, higher values of  $C_{d,max}$  imply a  
 431 reduction in the threshold value for  $T_i$  below which the fuel is heated along the nozzle instead of being cooled down.  
 432 Additionally, operating conditions for which steady conditions are not achieved (i.e. low ET) may result in the fuel being  
 433 importantly heated at all times.



434 (a) Established flow regime. (b) Temperature change.

435 Figure 10. Predicted discharge coefficient and temperature change along the nozzle orifices according to the flow regime  
 436 set during the steady-state stage at the tested operating conditions ( $t_{aSOE} = 1$  ms for injections with  $ET = 1$  ms).

437 Additionally, it may be seen that the fuel temperature changes along the nozzle tend to reduce the initial differences  
438 among extreme conditions (the fuel initially colder is heated along the nozzle, whereas the fuel initially warmer is cooled  
439 along the nozzle). This acts in the sense of reducing the differences in fuel density and fuel viscosity among cases, thus  
440 contributing to the small difference in steady-state stage ROI identified in Section 2.4 in the view of the experimental  
441 results of Figure 5.

442 Last, it is interesting to analyse at this point the influence of the deviations among the predicted and the measured ROI  
443 pointed out by the validation (Figure 5) on the estimated temperature changes across the nozzle. In this sense, the  
444 operating conditions for which the greatest differences in the ROI curves were found (low injection pressures for  $T_i = 253$   
445 K) lead to under-predictions in the specific enthalpy change along the orifices. This in turn leads to under-predictions in  
446 the fuel temperature changes, quantified as 5 K and 3 K, respectively. The lower deviations in ROI found in the rest of  
447 the cases would lead to negligible uncertainties in these predictions (in the order of 1 K).

448

#### 449 4. ANALYSIS OF THE INJECTOR DYNAMICS

450 As the experimental ROI curves demonstrated (see Figure 5), the operation of the Bosch CRI 2.20 injector leads to a  
451 different dynamic behaviour (namely delay among the start of energizing and start of injection, injector opening slope  
452 and injector duration) for a single injection depending on the fuel injection pressure and temperature at the injector inlet.  
453 The differences in injection duration have been attributed to the ballistic nature of the injector, since the varied operating  
454 conditions lead to different top values of needle lift from which the needle has to fall in order to close against its seat. The  
455 present section aims at the observation of the injector internal features by means of the implemented adiabatic model in  
456 order to fully understand these differences. Later on, the hydraulic performance of the injector under split injection  
457 strategies is also examined thanks to the model.

##### 458 4.1. Analysis of the forces driving the needle motion

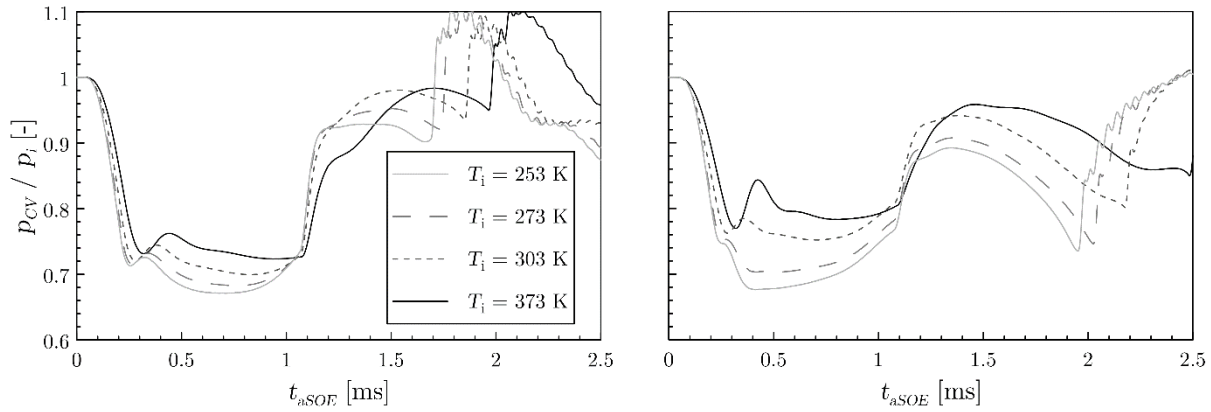
459 Injector dynamics is mainly driven by the forces acting on the needle, which are mainly due to two contributions:

$$F_{needle} = F_{\Delta p} - F_{fric} \quad (5)$$

460 where  $F_{\Delta p}$  is the force due to the pressure difference among the upper part of the needle (control volume in Figure 1) and  
461 its lower part, acting in the sense of the needle motion; whereas  $F_{fric}$  is the force generated by viscous friction in the  
462 clearance between the needle and the injector wall (especially relevant when this clearance is small), opposing the needle  
463 motion.



464 The term  $F_{\Delta p}$  in Eq. (5) is governed by the performance of the control volume orifices analysed in Section 3.1, since the  
465 flow rate through them determines the ability to generate the pressure drop at the control volume when the solenoid valve  
466 is energized (making the needle rise, discovering the nozzle orifices) or to restore it when the injector stops being  
467 energized (making the needle close against its seat). Figure 11 shows the evolution of the pressure in the control volume  
468 (normalized with the injection pressure) responsible for this force for some of the operating conditions tested, focusing  
469 on the cases of  $ET = 1$  ms. The figure shows that, for any injection pressure condition, the depression generated in the  
470 control volume during the opening stage occurs earlier and achieves a greater magnitude the lower the fuel temperature.  
471 This result can be explained due to the different flow regime established at both control orifices depending on the injector  
472 operating conditions. As shown in Figure 8, the range of values taken by the discharge coefficient of the OA orifice is not  
473 wide. In the case of OZ, however, important differences were seen depending on the injection operating conditions: for a  
474 given injection pressure, the discharge coefficient was lesser the lower the fuel temperature. This implies higher pressure  
475 losses through the orifice that result in an earlier and larger pressure drop, explaining the trends observed in Figure 11.  
476 On the other hand, Figure 11 shows that it takes longer for the control volume to restore its pressure the higher the value  
477 of  $T_i$  once the injector stops being energized. At this instant, the OA orifice is locked and OZ is responsible for re-  
478 establishing the pressure in the volume. This behaviour may be justified by the mass flow rate through the orifice: even  
479 though  $C_d$  is higher for high values of  $T_i$ , the pressure drop that it induces across the orifice is lower, resulting in a lesser  
480 theoretical flow velocity. In addition, the fuel density is considerably lower when compared to the one at cold conditions.  
481 These two factors are able to overcome the effect of the discharge coefficient and lead to small mass flow rates through  
482 the orifice. As a consequence, longer times are needed for the control volume to restore the rail pressure, as observed. No  
483 significant influence of the injection pressure is noticed on the normalized pressure drops in the control volume, although  
484 a greater influence among temperatures is seen the higher the injection pressure.



485

(a)  $p_i = 40$  MPa.

(b)  $p_i = 180$  MPa.

486 Figure 11. Temporal evolution of the pressure in the control volume (normalized with the injection pressure) for some  
 487 operating conditions tested (ET = 1 ms).

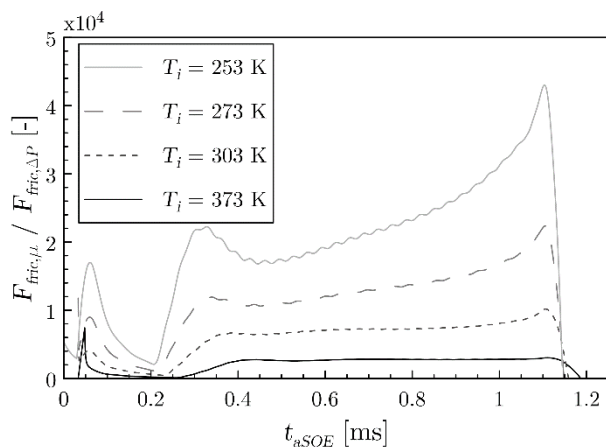
488 It is important to note that the sole effect of the discussed hydraulic parameters of the control volume orifices would lead  
 489 to a faster response of the injector at low temperatures, since the more accused pressure drop at the control volume would  
 490 generate a higher unbalance at both sides of the needle.

491 The second term of Eq. (5),  $F_{fric}$ , is modelled according to Eq. (6) [35]:

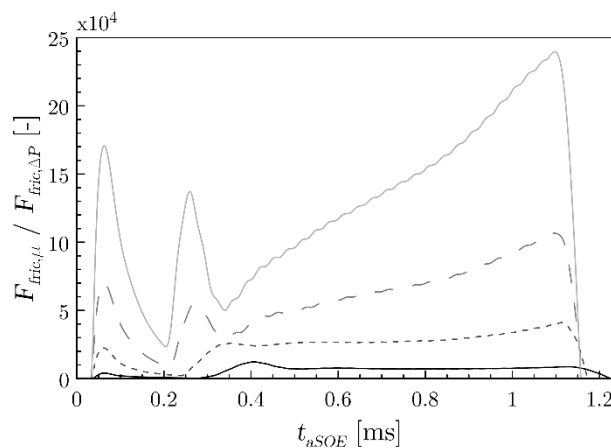
$$F_{fric} = F_{fric,\mu} - F_{fric,\Delta p} = 4\pi\mu_f U_n L_{cl} \left( \frac{D_{pist}}{D_{cl}} - 1 \right) - \pi \frac{D_{cl}}{2} \frac{D_{pist} - D_{cl}}{2} \Delta p_{cl} \quad (6)$$

492 As it may be seen, the friction force appearing on the needle depends both on the fuel viscosity (which in turn depends  
 493 on fuel temperature and pressure) and the pressure losses along the part of the needle where the clearance is small ( $\Delta p_{cl}$ ,  
 494 concentrated in the upper part of the needle –right below the control volume- as seen in Figure 1), with opposed effects.

495 It is then interesting to determine which of the two terms in Eq. (6) plays a more significant role in the needle motion of  
 496 the diesel injector. Figure 12 shows the value of the ratio among  $F_{fric,\mu}$  and  $F_{fric,\Delta p}$  along part of an injection event for  
 497 some of the tested conditions. The figure only shows the time range corresponding to the stage in which the needle is  
 498 rising. As it may be seen, the term related to fuel viscosity is several orders of magnitude higher than the one related to  
 499 the pressure drop. In addition, its influence is even more important the lower the fuel temperature at the injector inlet and  
 500 the higher the injection pressure, due to the high viscosities associated. Hence, it is possible to state that the net effect of  
 501 increasing the fuel temperature is a reduction in the friction force, which would in turn act in the sense of a faster needle  
 502 opening.



(a)  $p_i = 40$  MPa.

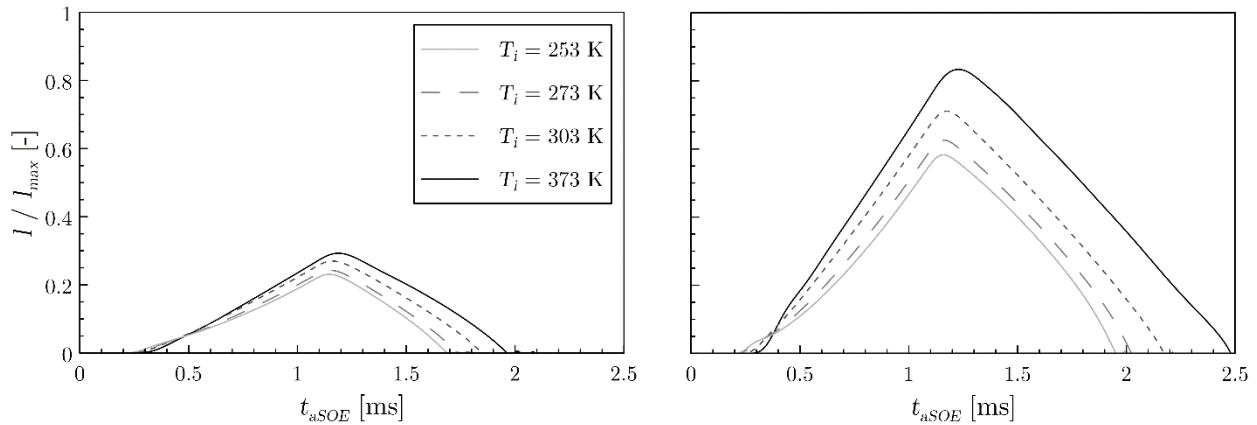


(b)  $p_i = 180$  MPa.

503

504 Figure 12. Temporal evolution of the ratio among the viscous force on the needle generated by fuel viscosity and the one  
 505 induced by the pressure losses along the part of the needle with a small clearance (ET = 1 ms).

506 From the previous considerations, it follows that there are two opposed effects of the fuel temperature on injector  
 507 dynamics: a lower fuel temperature would lead to a faster injector opening if only the pressure forces were considered,  
 508 whereas it would lead to a slower opening by the sole effect of viscous friction. These opposed effects of the fuel  
 509 temperature on injector dynamics have already been found in previous works by the authors [36,37] and reported in the  
 510 literature [21]. In order to observe how they are translated into needle motion, Figure 13 shows the evolution of the needle  
 511 lift computed by the model. The figure shows that the time at which the injector closes depends on the fuel temperature  
 512 at the injector inlet, as was observed experimentally (Figure 5). For each injection pressure, it is observed that the needle  
 513 starts to rise earlier the lower the fuel temperature. In the absence of needle motion (thus, in the absence of friction forces  
 514 acting on the needle), this fact is in agreement with the findings from Figure 11 about the pressure in the control volume  
 515 dropping faster and to a larger extent the lower the fuel temperature. Nevertheless, the slopes of the curves reveal that the  
 516 injector opening is slower the lower the fuel temperature. This result is also aligned with the previous findings: once the  
 517 needle moves, friction forces proportional to the fuel viscosity appear, opposing this motion. Given the significant increase  
 518 in fuel viscosity at low temperatures (and especially at high injection pressures, for which Figure 13 shows the higher  
 519 differences in opening slope), this soon results in the needle moving slower for cold conditions. Indeed, it can be seen  
 520 that once the needle reaches among 5 to 10% of its maximum lift ( $t_{aSOE} \approx 0.4$  ms), it has already reached upper positions  
 521 the higher the fuel temperature at the injector inlet. On the other hand, as expected, the effect of the injection pressure on  
 522 the opening stage is to achieve faster rates. This is explained considering the larger absolute pressure drops achieved in  
 523 the control volume (Figure 11), which generate a higher pressure unbalance among the lower and the upper side of the  
 524 needle.



(a)  $p_i = 40$  MPa.

(b)  $p_i = 180$  MPa.

525

526 Figure 13. Temporal evolution of the needle lift (normalized with the mechanical limit of the injector  $l_{max} = 850 \mu\text{m}$ ) for  
 527 some operating conditions tested (ET = 1 ms).

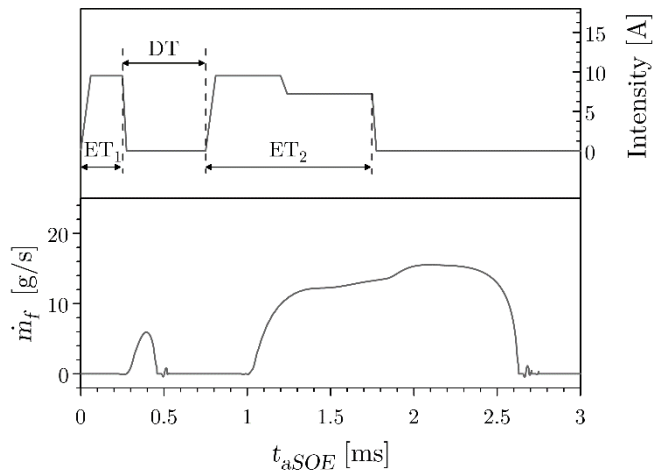
528 It is also confirmed that a slower needle opening results in lower top positions reached by the needle during an injection  
 529 event. Hence, during the closing stage, the needle falls from lower positions the lower  $T_i$ , resulting in shorter times needed  
 530 for the needle to close against its seat and cut the injection. This confirms the injection duration trends pointed out in  
 531 Figure 5. Also, the time at which the top position is reached by the needle varies depending on  $T_i$ , being achieved later  
 532 the higher  $T_i$ . This finding may be justified in the view of Figure 11, where it was observed that the pressure in the control  
 533 volume was restored in a slower manner the higher  $T_i$ . This reasoning could also be valid to explain the slightly slower  
 534 closing found for high values of  $T_i$ : once the needle lifts, it reduces the fuel volume at the upper part of the needle. When  
 535 the needle falls back towards its seat, this volume is increased again. Therefore, it needs to be replenished with fuel in  
 536 order to restore the pressure. For high values of  $T_i$ , the taller top positions reached by the needle result in a higher volume  
 537 needing to be replenished during the closing in order to restore the initial pressure. However, these high values of  $T_i$  result  
 538 in lower fuel densities that reduce the mass flow rate employed to that end.

539 In any case, an acceleration in the needle closing is observed at the end of the injection for most conditions. This  
 540 acceleration, especially relevant at cold conditions, has also been reported in the literature. Moon et al. [38] observed this  
 541 increase in needle speed through an X-ray imaging technique, and relate it to the sudden decrease of sac pressure due to  
 542 the flow restriction (throttling) from the needle at low needle lifts. The higher restriction (i.e. lower effective discharge  
 543 coefficient) generates a higher pressure drop through the needle seat. Consequently, the sac pressure decreases, generating  
 544 an even higher unbalance among the pressure forces at the upper and lower sides of the needle, abruptly increasing the  
 545 needle speed. Wang et al. [22] also noticed through ROI measurements that this phenomenon was especially important  
 546 for cold fuel temperature conditions. They reasoned that the major friction induced by high viscosity could curb the fuel

547 flow generating an even higher pressure drop in the sac.

#### 548 4.2. Behaviour under multiple injections

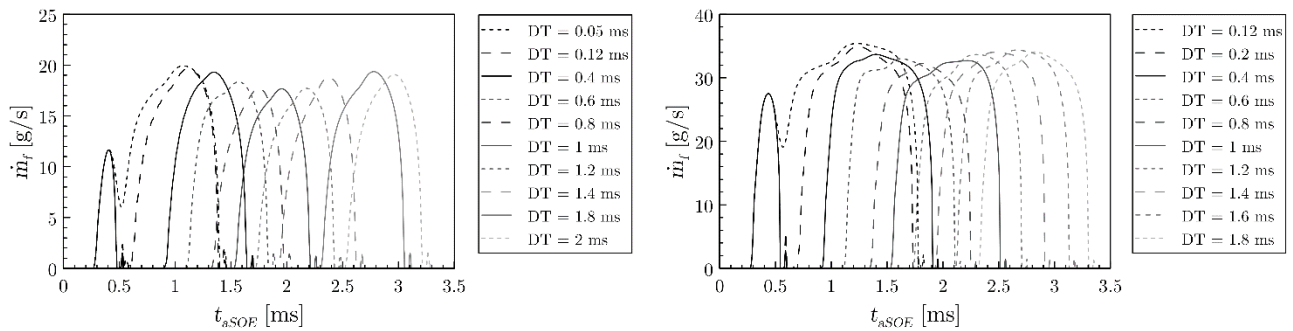
549 The impact of the operating conditions on the hydraulic performance of the Bosch CRI 2.20 injector under split injection  
550 strategies has been examined by means of the implemented computational model. In order to analyse this influence,  
551 several electric dwell times (DT) among injections have been tested. DT is defined in Figure 14 as the temporal separation  
552 among the end of the energizing pulse of an injection and the beginning of the pulse of the subsequent injection.



553

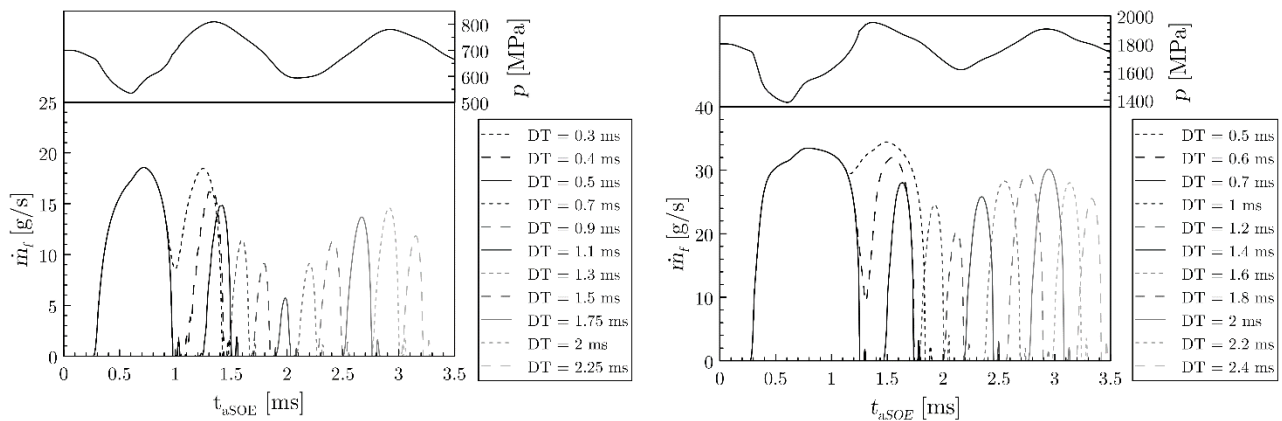
554 Figure 14. Definition of the electric dwell time (DT).

555 The time needed for the injector to stop delivering fuel once the energizing signal has ended cannot be neglected. Hence,  
556 if DT is too small, an overlapping among two subsequent injections may take place, preventing them from being splitted.  
557 A sample of this statement is shown in Figure 15 for several tested conditions including pilot plus main injection strategies  
558 and main plus post injection strategies. An important influence of the dwell time on the amount of fuel delivered by the  
559 second injection (more accused for the main plus post injection case) is observed. The pressure wave induced by the  
560 opening of the injector for the first injection is responsible for this phenomenon. As seen in Figure 4, the pressure at the  
561 injector inlet still oscillates once the injector is effectively closed. Similarly, the pressure upstream of the nozzle orifices  
562 represented in Figure 15(c) and Figure 15(d) takes some time to be stabilized after a given injection. Hence, if the injector  
563 is reenergized during this period, the new injection will introduce a higher or lower amount of fuel mass than its single  
564 injection equivalent depending on the instantaneous value of pressure at the nozzle inlet. Pressure wave propagation is  
565 influenced by the fuel speed of sound and bulk modulus [19], meaning that both the amplitude and period of the pressure  
566 oscillations at the nozzle inlet will depend on fuel temperature and pressure. Thus, the injector operating conditions are  
567 expected to affect the critical dwell time to effectively separate injections and the total mass injected by the second  
568 injection.



(a)  $p_i = 70$  MPa,  $T_i = 303$  K,  $ET_1 = 0.25$  ms,  $ET_2 = 0.5$  ms

(b)  $p_i = 180$  MPa,  $T_i = 353$  K,  $ET_1 = 0.25$  ms,  $ET_2 = 0.5$  ms

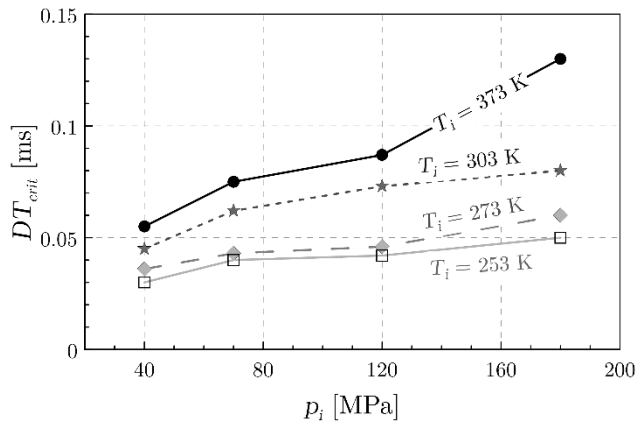


569 (c)  $p_i = 70$  MPa,  $T_i = 303$  K,  $ET_1 = 0.5$  ms,  $ET_2 = 0.25$  ms

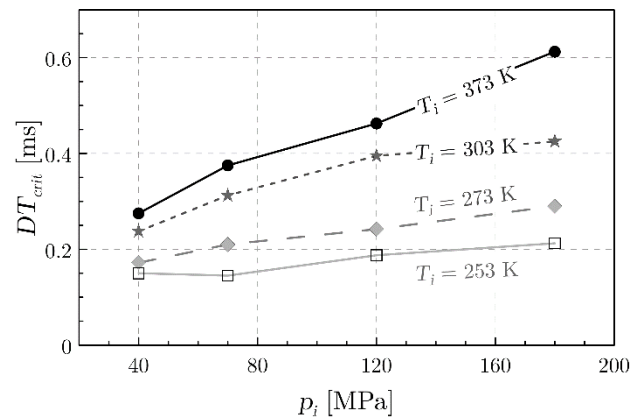
(d)  $p_i = 180$  MPa,  $T_i = 353$  K,  $ET_1 = 0.5$  ms,  $ET_2 = 0.25$  ms

570 Figure 15. Modelled injection rate for pilot plus main injection strategies (a,b) and for main plus post injection strategies  
 571 (c,d) for sample operating conditions. The evolution of the pressure upstream of the nozzle orifices corresponding to the  
 572 single injection case equivalent to the main injection is also represented for the main plus post injection strategies.

573 Figure 16 shows the critical dwell time at which two desired injections stop being overlapped to be effectively separated  
 574 for each of the tested values of fuel temperature at the injector inlet and injection pressure. As it may be seen in Figure  
 575 16(a) for the pilot plus main injection strategy, the injector may be reenergized shortly after the first pulse is finished. In  
 576 general, a larger separation among energizing pulses is required the higher the injection pressure and the higher  $T_i$ . This  
 577 result is consistent with the trends in injection duration found experimentally (Figure 5) and justified in Section 4.1. With  
 578 regard to the main plus post injection strategy depicted in Figure 16(b), the same trends are observed, since the factors  
 579 influencing the process remain the same. Comparatively higher values of  $DT_{crit}$  are exhibited, since the duration of the  
 580 first injection directly establishes the critical dwell time to separate the next one. This reasoning remains true unless the  
 581 mechanical limit of the needle is reached during the main injection, thus influencing the observed trends among operating  
 582 conditions and injection duration.



(a) Pilot plus main injection strategy.

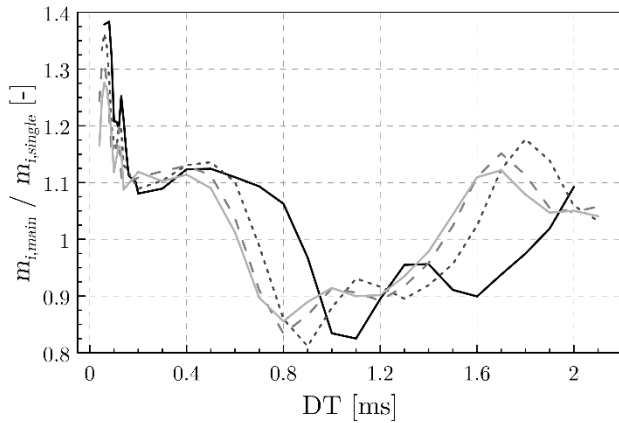


(b) Main plus post injection strategy.

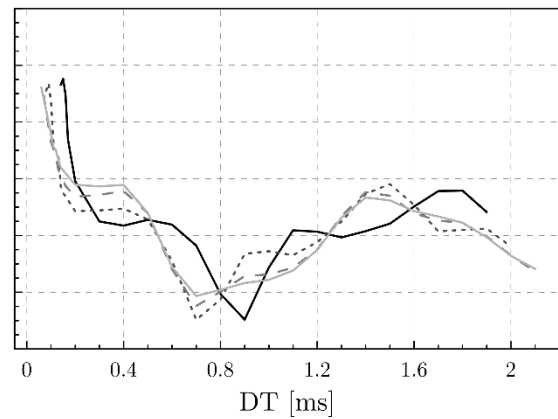
583

584 Figure 16. Critical dwell time to split successive injections depending on the operating conditions ( $ET_{\text{pilot}} = 0.25$  ms,  $ET_{\text{main}} = 0.5$  ms,  $ET_{\text{post}} = 0.25$  ms).  
585

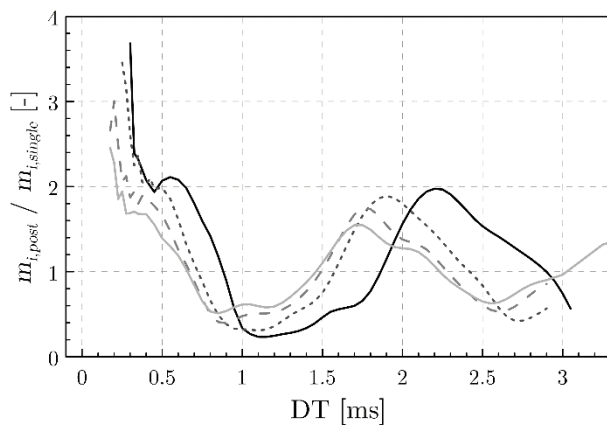
586 The effect of the first injection on the mass injected by the second injection has been quantified for different values of  $DT$   
587 (higher than the critical one) for each tested condition, as shown in Figure 17. A strong influence of the dwell time is  
588 observed in all cases. Focusing on the results found for the pilot plus main injection depicted in Figure 17(a) and Figure  
589 17(b), it may be seen that the mass values are greatly influenced for short dwell times, close to  $DT_{\text{crit}}$ . This leads to  
590 masses of the main injection that can even increase those of the equivalent injection by a 40%. This result, already  
591 observed by the authors [37,39], is attributed to the pressure overshoot that takes place right upstream of the nozzle  
592 orifices as observed in Figure 15(c) and Figure 15(d). After a certain value of  $DT$ , this influence gets lower, obtaining  
593 masses that oscillate from about 80% to 115% of the values corresponding to the single injection. The oscillations  
594 depending on  $DT$  are also induced by the fluctuation of the pressure upstream of the nozzle, as already stated. As far as  
595 the main plus post injection strategy is concerned, as shown in Figure 17(c) and Figure 17(d), the relative influence of  
596 the interaction among injections is higher, since the pressure above the nozzle is disturbed to a larger extent the longer  
597 the first injection. Masses almost 400% higher than the analogous ones for single injections may be delivered by the post  
598 injection, whereas the variability of the mass delivered depending on  $DT$  after this initial peak ranges from 10% to 200%.



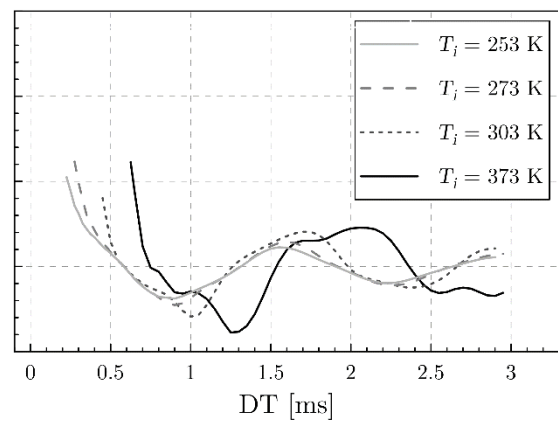
(a) Pilot plus main injection,  $p_i = 40$  MPa.



(b) Pilot plus main injection,  $p_i = 180$  MPa.



(c) Main plus post injection,  $p_i = 40$  MPa.



(d) Main plus post injection,  $p_i = 180$  MPa.

599

600 Figure 17. Fuel mass injected during the second injection for several operating conditions tested ( $ET_{pilot} = 0.25$  ms,  $ET_{main} = 0.5$  ms,  $ET_{post} = 0.25$  ms). In each case, the values are normalized with the mass injected by a single injection  
 601 equivalent to the second injection.  
 602

603 A strong influence of the fuel temperature at the injector inlet is observed on the phasing of the oscillations depending on  
 604 DT. In general, the decrease of the normalised mass with DT takes place at earlier dwell times for the lowest values of  $T_i$ .  
 605 This may be attributed to the higher values of fuel speed of sound and bulk modulus achieved at these temperatures [19],  
 606 which reduce the period of the pressure fluctuations upstream of the nozzle once the injector is closed. The injection  
 607 pressure does not seem to have such an important influence on the results. On the other hand, the variability of the mass  
 608 delivered depending on DT seems to be damped the higher the injection pressure and the lower  $T_i$ . This influence of the  
 609 fuel temperature on the variability of mass injected by a second injection was already reported by Wang et al. [22], who  
 610 attributed it to the addition of the effects of shorter injection duration and longer injection delay induced by low  
 611 temperatures.

612

613



614 **5. CONCLUSIONS**

615 A computational 1D model has been used to evaluate the influence of the fuel temperature and its variations within a  
616 solenoid-driven common-rail ballistic injector on the injector performance. The model makes use of the adiabatic flow  
617 hypothesis, whose validity is assessed in the first part of the study. The model itself has been extensively validated against  
618 experimental results for a wide range of operating conditions, including several injection pressures and values of fuel  
619 temperature at the injector inlet ranging from those representative of cold start to those representative of long engine runs.  
620 The main conclusions of the use of this model are summarized as follows:

- 621 • The introduction of the adiabatic flow hypothesis allowed to extend the range of operating conditions for which  
622 the computational model is reliable, including low fuel temperatures at the injector inlet representative of cold-  
623 start.
- 624 • The fuel warms upon expansion across the control volume orifices (OZ and OA) and the nozzle feeding line  
625 during the whole injection event. These temperature increases are more relevant the higher the injection pressure,  
626 due to the larger absolute pressure drops established. In the case of the OZ orifice and the nozzle feeding line,  
627 the magnitude of the temperature increase is greater for low values of the fuel temperature at the injector inlet,  
628 since the high fuel viscosities associated to these temperatures imply low values of  $Re$  that induce a laminar or  
629 transitional flow regime identified with a greater heating. In the case of the OA orifice, the fuel temperature at  
630 the injector inlet does not importantly affect the temperature rise across the orifice for a given pressure, since all  
631 the operating conditions induce the same cavitating regime in the orifice.
- 632 • As far as the nozzle orifices are concerned, it may be stated that the fuel heats along the nozzle during the  
633 transient stages of the process, whereas it may be heated or subcooled during the steady-state stage depending  
634 on the discharge coefficient achieved (i.e. flow regime) and the maximum discharge coefficient of the nozzle.  
635 The magnitude of this heating or cooling is more accused the larger the injection pressure. For the particular  
636 injector studied, a threshold value of fuel temperature at the injector inlet of 283 K has been found. Above this  
637 value, the fuel is subcooled during the steady-state stage of the injection. Nevertheless, this cooling is not  
638 especially relevant ( $\approx 10$  K) and is compensated with the heating taking place along the nozzle feeding line,  
639 allowing to state that the fuel temperature is virtually unchanged from the injector inlet to the outlet. However,  
640 fuel temperatures at the injector inlet below 283 K induce a laminar or transitional flow regime leading to an  
641 important heating. The magnitude of this heating effect, added to the one along the nozzle feeding line, may  
642 importantly influence the flow conditions downstream of the nozzle and the spray development.

- 643 • Needle dynamics is influenced by the pressure unbalance established among its upper and its lower side once  
644 the injector is energized. For a given injection pressure, the depression generated in the control volume during  
645 the opening stage occurs earlier and achieves a greater magnitude the lower the fuel temperature, since the  
646 laminar or the transitional regime are established across OZ. This generates higher pressure losses across the  
647 orifice, further reducing the pressure in the control volume and influencing the delay among the start of  
648 energizing and the start of injection. Once the needle starts moving, its lifting velocity not only depends on the  
649 pressure unbalance at both sides of the needle, but also on the viscous friction opposing the needle motion. This  
650 effect is more important the lower the fuel temperature, due to the important increase in viscosity. As a result,  
651 once the solenoid stops being energized, the needle will fall from different positions depending on the operating  
652 condition, taking more or less time to close against its seat and influencing the injection duration.
- 653 • In terms of split injection strategies, fuel properties influence the critical dwell time that allows to totally separate  
654 two subsequent injections. In general, this time is higher the higher the fuel temperature and the injection pressure,  
655 since the needle falls from an upper position in these conditions. The timing among injections affects the total  
656 mass injected by the second injection differently depending on the injection pressure and the fuel temperature at  
657 the injector inlet, due to the different induced values of speed of sound and bulk modulus affecting pressure wave  
658 propagation. In addition, the variability in fuel mass injected depending on the dwell time is more accused the  
659 higher the fuel temperature.

660

## 661 **ACKNOWLEDGEMENTS**

662 This work was partly sponsored by FEDER and the Spanish “Ministerio de Economía y Competitividad” in the frame of  
663 the project “Desarrollo de modelos de combustión y emisiones HPC para el análisis de plantas propulsivas de transporte  
664 sostenible (CHEST)”, reference TRA2017-89139-C2-1-R-AR. On the other hand, the support given to Mr Mario Belmar  
665 by “Universitat Politècnica de València” through the “FPI-Subprograma 2” grant within the “Programa de Apoyo para la  
666 Investigación y Desarrollo (PAID-01-18)” is gratefully acknowledged by the authors.

667 The authors would also like to thank Mariano Sánchez for his technical help.

668

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