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Additional Information

# Fatigue Assessment of Steel Riveted Railway Bridges: Full-Scale Tests and Analytical Approach.

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**Keywords:** Fatigue, Structural Health Monitoring, Steel bridges, Truss structures, Full-scale tests.

## Abstract

This paper describes a double experimental and analytical study of the fatigue behaviour of the Quisi and Ferrandet Bridges, twin 170 m long steel railway bridges constructed between 1913 and 1915 with typical Pratt truss structures and riveted connections. These bridges are part of the Spanish national railway network connecting the towns of Alicante and Denia, one of the key networks in the Valencia Region (Spain). The experimental laboratory investigation involved fatigue testing in one of the ICITECH laboratories at the *Universitat Politècnica de València* of: (i) a full-scale bridge span and (ii) an upper cross beam from the Ferrandet bridge. During the tests, Linear Variable Displacement Transducers (LVDTs) and Strain Gauge (SG) sensors were used to capture the possible nucleation and propagation of fatigue cracks. Fatigue test carried out on the cross beam identified: (i) **fatigue life of the critical detail**, (ii) fatigue hot-spots along the cross beam and (iii) strain redistribution along the riveted element during crack growth. The experimental results from the full-scale bridge were adopted to calibrate an elastic numerical model of the whole structure, which was in turn used to estimate the Quisi Bridge's remaining fatigue life. The definition of the class of detail and remaining fatigue life were calculated by the S-N curves method, according to Eurocode 3, considering the available information on the bridges' loading histories.

## 30           **1. Introduction**

31   Most steel bridges designed between the early 19th century and the mid-20th century were  
32   built of structural steel with riveted joints. The fatigue behaviour of riveted joints has become a  
33   topic of interest due to the large number of bridges of this type still in service despite the heavy  
34   traffic volumes they have sustained over the years. A fact that deserves special mention is that  
35   more than 60% of the railway bridges in Europe are over 50 years old and more than 30% are  
36   over 100 years old [1]-[9]. Most of these bridges were built prior to standardization  
37   [10][11][12][13] and the widespread use of design codes, and now are subjected to higher loads  
38   and speeds than those for which they were originally designed. Many therefore require  
39   maintenance and in some cases need to be partially or completely replaced.

40   Due to the large number of riveted steel railway bridges in Europe, replacing all these structures  
41   will be extremely costly and virtually impossible unless phased over several decades [7]. The  
42   riveted connection construction technique has been one of the most durable techniques in the  
43   history of steel bridges and was the preferred system until the 20th century [5][6]. In spite of  
44   this, the damage statistics of various steel structures clearly demonstrate that steel bridges are  
45   38% more likely to fail due to fatigue crack propagation [1]. Several studies [2][4][8] indicate  
46   that old riveted bridges suffer from a combination of multiple aspects, including construction  
47   material characteristics and degradation, while [2] points out that old riveted bridges were  
48   mainly constructed using puddle iron and mid-low carbon steel. The combination of  
49   heterogeneous material and slag with low C and Si contents favour degradation processes and  
50   reduce the steel's chemical and mechanical resistance to microstructural damage and promote  
51   the nucleation of fatigue cracks. These findings also apply to other types of steel bridges  
52   constructed in the same era.

53   Microstructural damage is likely to affect the structural behaviour of steel bridges only at an  
54   advanced state of crack propagation. The observations of studies adopting multiple approaches  
55   highlighted their high structural redundancy as a common feature. This means that the failure of  
56   a component generally does not lead to the gradual collapse of the entire structure, since a crack  
57   in a riveted girder will most likely remain within the cracked component. In this situation the  
58   rivets help the compartmentation of the damage in the cracked girder and prevent it from  
59   spreading to other elements. However, after the failure of one element and the distribution of  
60   the loads to the remaining components, a progressive failure can start or there may even be a  
61   new fatigue failure due to the higher cyclic loads they receive. In-field monitoring of steel  
62   railways bridges [14]-[17] is therefore of paramount importance in understanding the actual  
63   state of steel structures subjected to cyclic loads.

64 The authors of [16] pointed out that fatigue damage is expected to occur in primary elements,  
65 mostly in stringers and cross beams, which directly bear the cyclic loads. Similar findings  
66 emerged in [18]-[20], when the authors analysed the fatigue behaviour of riveted connections.  
67 Advanced numerical studies later confirmed by experimental tests [21] revealed that the angle  
68 fillet and the rivet head-to-shank junction and holes are fatigue-starting hot-spots. The authors  
69 of [18] demonstrated by means of several parametric FE analyses that defects can affect the  
70 fatigue behaviour of riveted connections in the presence of: (i) clearance between the rivet  
71 shank and rivet hole and (ii) the loss of a rivet. The authors in [22] analysed the behaviour of  
72 stringer-to-floor beam connections in old riveted bridges and underlined that primary elements  
73 are the most prone to experience fatigue failures because they are usually short in length and  
74 accumulate large stress fluctuations. The fatigue tests performed by the authors also revealed  
75 that riveted connections performed better than expected, assuming detail class 71, thus,  
76 confirming that it is a safer assumption in the absence of experimental data [22]. They also  
77 found that **the state of stress** is strongly influenced by the connection quality and thus its end-  
78 fixity plays a crucial role.

79 Considering the level of skill required to produce riveted connections and the absence of  
80 standardized quality controls, it is not surprising that the authors detected high uncertainty  
81 related to the determination of rivet fatigue strength. Among the experimental works carried  
82 out on riveted elements, it is worth mentioning the investigations carried out in [23][24]. In  
83 [23] the authors performed a wide experimental and analytical investigation on riveted railway  
84 bridge girders and subjected them to full-scale bending tests. The lab tests confirmed that the  
85 critical point in the bridge was the riveted connections of the shear-diaphragms directly  
86 carrying the loads. Fatigue failure also originated in rivet shanks and resulted in their head loss.  
87 Finally, a detail category of 117 was suggested. In [24] the authors experimentally analysed the  
88 behaviour of a 12.4 m long railway bridge. In agreement with [22] and [23], Pipinato et al.  
89 identified the riveted connections of the shear diaphragms carrying the rails as the bridge's  
90 fatigue hot-spot, mainly in the rivet shanks. The analytical studies confirmed that a detail class  
91 of 100 should be preferred in case of failure triggered by **tangential stresses (shear stresses)**.  
92 This finding is partially in agreement with Eurocode 3 recommendations that suggest detail  
93 classes 80 and 100 should be adopted.

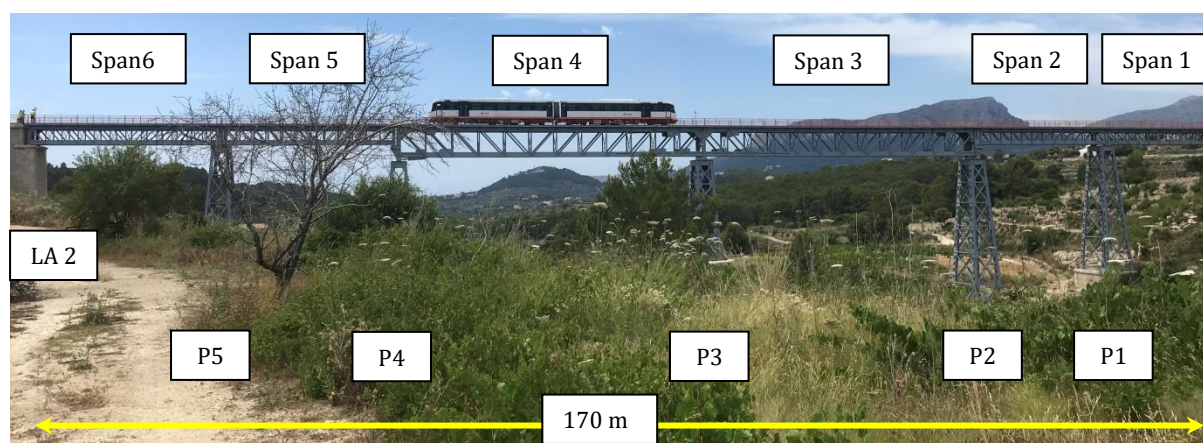
94 From a structural point of view, few studies [25][26] in the literature deal with the experimental  
95 fatigue testing of full-scale riveted bridges or subassemblies due to the huge financial and  
96 operational implications. The aim of the present study was to enrich the broader scenario of  
97 experimental fatigue studies of riveted elements with a double experimental and analytical  
98 study dealing with: (i) a full-scale span of a riveted steel railway bridge after more than 100

99 years of operational service and (ii) a full-scale localized fatigue test of a cross beam. The results  
100 obtained from the two lab tests were coupled with load tests on bridges, Linear-Static Finite-  
101 Element Analysis (LSFEAs) and the current recommendations to define an integrated multi-field  
102 analytical method for predicting the residual fatigue life of steel bridges. The proposed  
103 approach could be extended to other bridges on the basis of: (i) real loading tests and (ii)  
104 numerical simulations, assuming detail categories 71 and 100, according to whether the  
105 expected failure mechanism is normal or tangential. This method was also applied in this work  
106 to the Quisi Bridge, which is still in service.

107 The paper is organized as follows: After this Introduction, Section 2 describes the bridge  
108 geometry, while Section 3 describes the method used in the study. Sections 4 and 5 report the  
109 results obtained from both studies and Section 6 discusses the analytical approach adopted to  
110 estimate the detail class and the bridge's residual fatigue life. Section 7 summarizes the most  
111 important findings obtained and outlines future work.

## 112 2. Geometrical description of the Quisi and Ferrandet Bridges

113 These Pratt truss bridges are part of the Spanish national railway network connecting the towns  
114 of Alicante and Denia and were constructed between 1913 and 1915. As can be seen in **Figure**  
115 **1**, the Quisi Bridge is approximately 170 m long and is composed of 6 spans with lengths  
116 varying between 21 and 42 m resting on two lateral abutments (LA 1 and 2) and five steel truss  
117 columns (P1, P2, P3, P4 and P5) of different heights fixed to ashlar foundations. The two central  
118 spans form a continuous hyperstatic beam (spans 3 & 4), while the lateral spans 1, 2, 5 and 6  
119 were constructed as isostatic elements. The span nomenclature and main geometrical details  
120 are also reported in **Figure 1** and **Figure 2**.

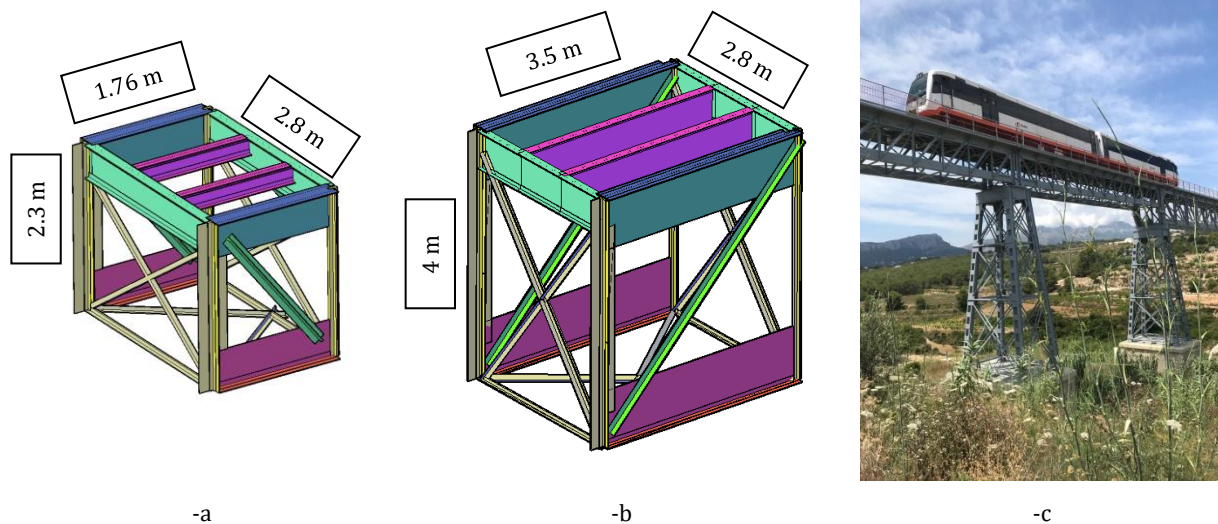


**Figure 1:** Quisi bridge geometry and span nomenclature.

121 After more than 100 years in service and due to the general increase in rail traffic, the railway  
122 company activated different restoration strategies for steel bridges, one of which involved

Revised version, modifications highlighted in color **YELLOW**

123 replacing the Ferrandet Bridge by a completely new structure. This gave us a unique  
124 opportunity to move one of its spans, with the same geometry as spans 2 and 5 of the Quisi  
125 Bridge, to the ICITECH laboratories at the *Universitat Politècnica de València* (Valencia, Spain),  
126 where it was tested under fatigue loads. The results obtained can be extended to other similar  
127 railway bridges (like the Quisi Bridge, **Figure 2**), with the same geometry.



**Figure 2:** Quisi bridge: geometry of the isostatic (-a) and iperstatic (-b) modules and (-c) 3D view of piers 4 and 5.

### 128 3. Experimental investigation

#### 129 3.1 Methodology

130 The study was organized into two parts: a laboratory study and an analytical assessment. The  
131 experimental results were used to validate the current recommendations proposed by  
132 Eurocode 3 and extend our knowledge of fatigue failures in old riveted steel elements. It was  
133 considered of paramount importance to test riveted bridge structures after years of operational  
134 service and environmental degradation. Since fatigue tests on full-scale bridges under  
135 controlled laboratory conditions have obvious technical limitations, it was decided to carry out  
136 a double experimental investigation on two different scales. One of the lab tests was on an  
137 upper cross beam subjected to railway load cycles and thus vulnerable to fatigue damage. The  
138 second, and more ambitious, lab test was applying cyclic loads to a full-scale isostatic bridge  
139 span.

140 The first test identified the following data: (i) maximum number of cycles before fatigue failure,  
141 (ii) identification of fatigue hot-spots inside the element, (iii) the precision, position and utility  
142 of the different SG and LVDT sensors and (iv) crack growth rates. The information from (i)  
143 allowed us to define the detail class by adopting the S-N curves method proposed in  
144 [10][11][13][26] (see below). The data provided by (ii), (iii) and (iv) identified effective fatigue-

145 crack monitoring strategies. The results from the second investigation were used to calibrate a  
 146 Finite Element numerical model for the analytical assessment. The overall findings were: (i) the  
 147 identification of the elements most vulnerable to fatigue failure, and (ii) the expected  
 148 operational life up to fatigue failure.

### 149 **3.2 Preliminary assessment of materials**

150 The following tests were performed on different samples from the bridges: (i) tensile tests  
 151 according to EN ISO 6892-1 [27] (ii) the Charpy impact test according to EN ISO 148-1 [28] and  
 152 (iii) mineralogical and chemical tests. The mechanical and impact test results are summarized in  
 153 **Table 1** and **Table 2**. All the tested samples showed consistent results in terms of both yielding  
 154 and ultimate strengths, while the impact results were widely scattered. The good quality of the  
 155 steel comparable with that of current steel can be seen in the results in Table 1.

**Table 1:** Quisi and Ferrandet bridges: tensile test results.

Sample	Yielding strength	Ultimate strength	Elongation [%]
	[MPa]	[MPa]	
Quisi	271	399	32
Ferrandet	299	325	36

156

**Table 2:** Quisi and Ferrandet bridges: Charpy impact test results (Joule).

Sample	Temperature [°C]	
	0	20
Quisi	32	64
Ferrandet	18	34

157 The chemical results are summarized in **Table 3** for different types of samples (rivet, plate and  
 158 profile). According to [2], the brittle nature of old riveted bridges is associated with the  
 159 presence of impurities and low C and Si content steel (<0.1% and 0.03%, respectively). The  
 160 Ferrandet Bridge clearly shows these features while the Quisi Bridge has higher C and Si  
 161 contents.

**Table 3:** Chemical test results of Quisi and Ferrandet Bridges (%).

Bridge	Sample	C	Si	Mn	P	S	Cr	Ni	Mo
Quisi	Rivet	0.193	0.018	0.492	0.060	>0.130	-	-	-
Ferrandet		0.037	0.036	0.33	0.048	0.063	-	-	-
Quisi	Plate	0.139	0.108	0.520	0.079	0.072	-	-	-
Ferrandet		0.046	<0.017	0.336	0.063	0.089	-	-	-
Quisi	Profile	0.139	0.105	0.510	0.066	0.071	-	-	-
Ferrandet		0.042	<0.017	0.346	0.041	0.050	-	-	-

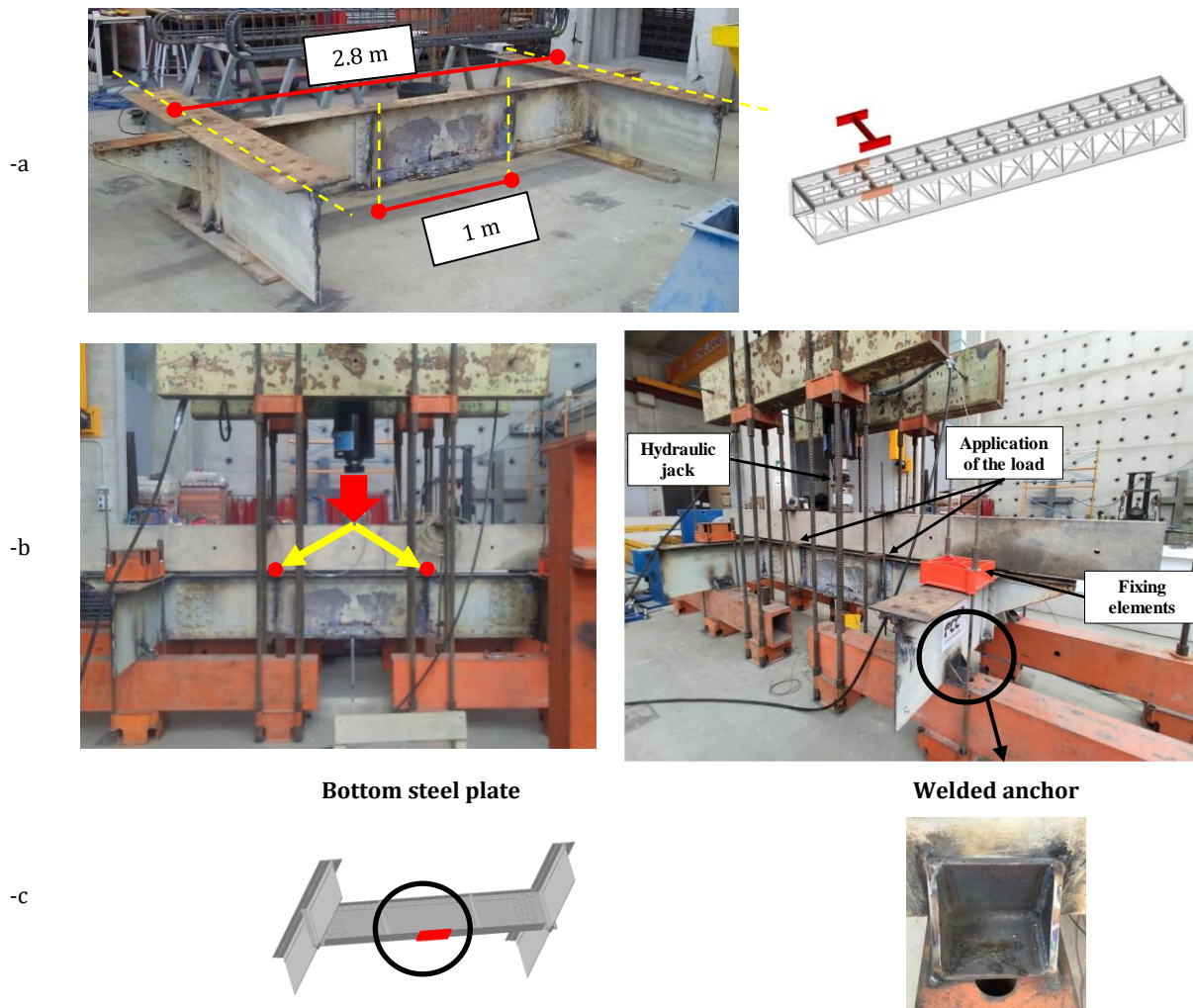
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## 164 4. Riveted cross beam element

### 165 4.1 Fatigue load protocols and experimental set-up

166 The geometry of the tested element is shown in **Figure 3-a**, while **Figure 3-b** depicts the  
167 experimental set-up adopted.



**Figure 3:** Geometry of the riveted truss beam tested (-a), experimental set-up (-b) and details of the beam and welded anchors (-c).

168 The experimental set-up comprised the application of a 0.55 Hz frequency cyclic load  
169 (maximum speed of the hydraulic jack) ranging from 50 to 650 kN, redistributed at two points  
170 by a stiff beam designed to simulate load transfers in real traffic scenarios. The loading points  
171 were in fact under the railway tracks. The load range and frequency were determined in order  
172 to exploit the maximum capability of the hydraulic jack used during the investigation. To this  
173 scope, the experimental design stress range was designed to reasonably minimize the number

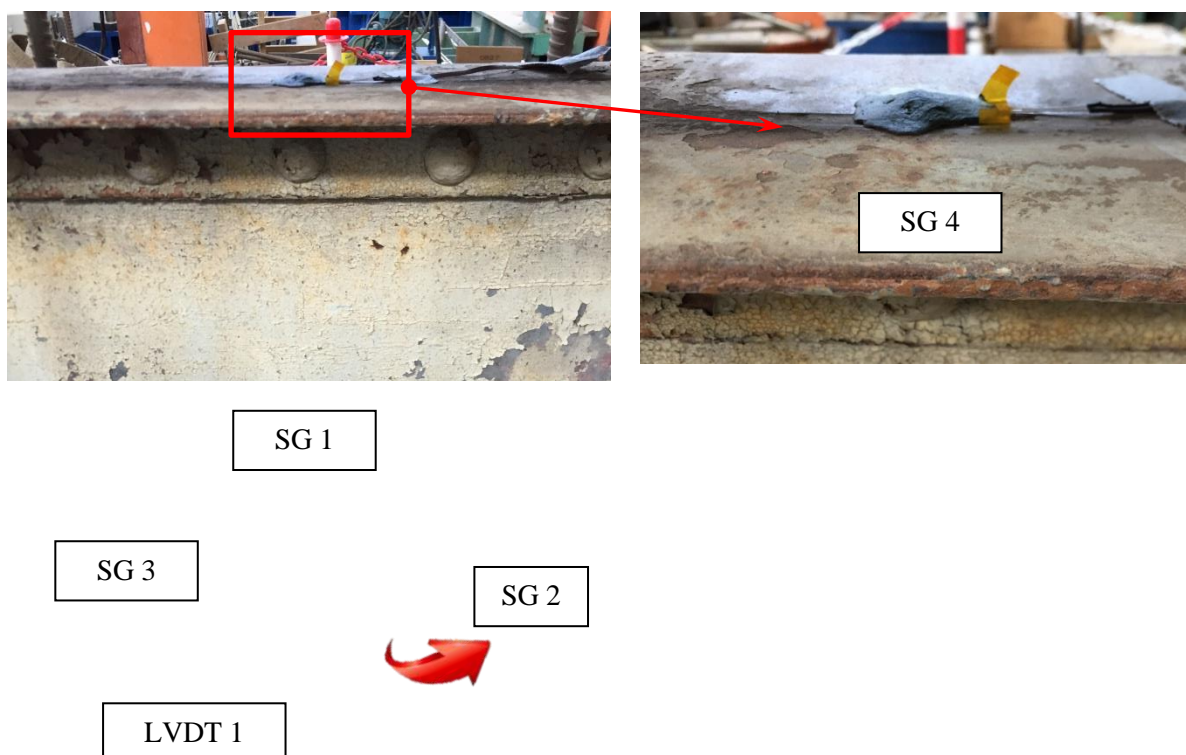


174 of cycles (using S-N curve method) whilst preventing the structures to experience any plastic  
 175 deformation that could trigger (or anticipate) the formation of fatigue cracks. The same strategy  
 176 was used when designing the experimental test on the full-scale span bridge. Lateral restraints  
 177 play a crucial role in the stress state of the riveted beam when subjected to cyclic loads, when  
 178 the riveted beam is mainly subjected to bending transmitted to the lateral chords by the riveted  
 179 connections. The riveted beam was firmly anchored to the reaction floor by four lateral welded  
 180 anchors positioned so that they did not introduce additional stiffness to the lateral restraints. A  
 181 detail of the anchorage can be seen in **Figure 3-b-c**.

**Table 4:** Description of sensor positions

Sensor	Position	Sensor	Position
SG 1	Centre, lateral bottom part of the web	LVDT 1	Mid-span
SG 2	Centre, mid lower flange	LVDT 2	Lateral riveted connection
SG 3	Centre, mid lateral lower flange		
SG 4	Centre, mid upper flange		

182 The fatigue behaviour of the riveted element was monitored by four strain gauges (SG) and two  
 183 Linear Variable Displacement Transducers (LVDT). **Figure 4** shows the sensor network, while  
 184 **Table 4** gives their positions. Fatigue cracks can be initiated by abrupt local changes in the cross  
 185 section, such as by the presence of an additional steel plate anchored to the beam bottom  
 186 flanges (see **Figure 3**). One LVDT was positioned below the tested element to monitor vertical  
 187 deflections and another to evaluate possible relative movements between rivet head and the  
 188 lateral profile indicating a possible weak point of the cross beam.





**Figure 4:** Position of the sensors: strain gauges and Linear variable Displacement Transducers.

## 189        4.2        Experimental Results

190        The riveted cross beam element can be seen in **Figure 3-a**. **Figure 5** gives the experimental  
191        envelopes obtained monitoring strain gauges SG1, SG2, SG3, SG4, and LVDT 1 and LVDT 2.  
192        Similarly, **Figure 6** gives the strain increment history obtained by the four strain gauges at the  
193        beam mid-span subjected to a constant cyclic load range of 600kN. The strain increment  
194        (**Figure 7**) was calculated as the absolute difference between maximum and minimum strains  
195        recorded in each cycle. All the sensors monitored similar strain increment trends in four  
196        different stages (see **Figure 6**). In the first, there was an initial transitory period of  
197        approximately 100 cycles to stabilize the beam's cyclic response, after which the behaviour was  
198        stable until approximately the 10000<sup>th</sup> cycle (stage 2), when a fatigue crack started. At 12k  
199        cycles, the strain increment trends abruptly changed due to the rapid propagation of a fatigue  
200        crack (stages 3 and 4), which involved a gradual loss of cross beam flexural stiffness and stress  
201        redistribution. The strain increments either increased or decreased according to the position of  
202        the sensor and the quality of the riveted connection (**Figure 6**).

203        The cross beam failed at approximately 31k cycles. Between cycles 0.1k and 10k, when the  
204        behaviour of the cross beam was almost elastic, the strain distribution along the mid-section  
205        was not as expected by classic beam theory. According to the literature [2][23][24], the quality  
206        of the connections together with high uncertainty plays a crucial role in redistributing the  
207        strains in the beam elements. Despite this, the sensors were able to deal with the different  
208        stress redistribution as the cracks grew. SG 2 and 3 detected a fatigue crack at an early stage.  
209        These sensors monitored varying rates of strain reduction, while, SG1 detected the expected  
210        rise of the strain increments (see **Figure 5-a**). This behaviour was caused by the strain  
211        redistribution along the element. SG4, on the upper compressed surface, showed a smoother  
212        increase of the strain increments than the others (see **Figure 5 -d**). As expected, the SG sensors  
213        were all able to warn of the changes in the cross beam's behaviour. Those close to the cracks

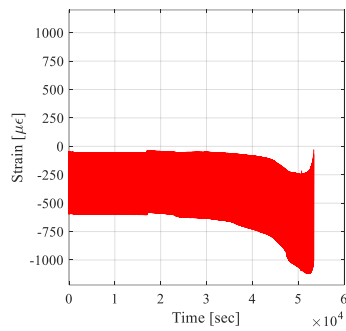
214 (i.e. SG 1, 2 and 3) clearly detected the formation and propagation of cracks at an early stage,  
215 while SG 4 was the worst at replicating the spread of the structural failure **(see Figure 5 -a-b-c**  
216 **and -d).**

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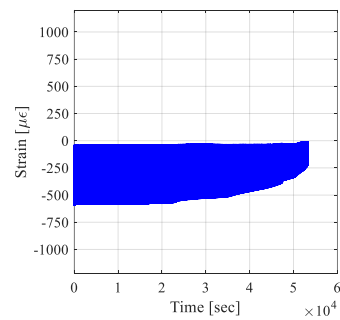
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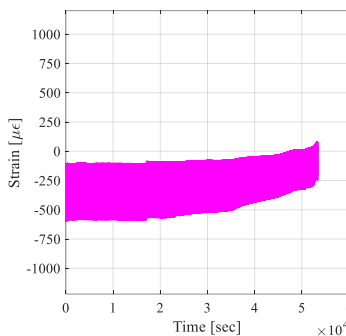
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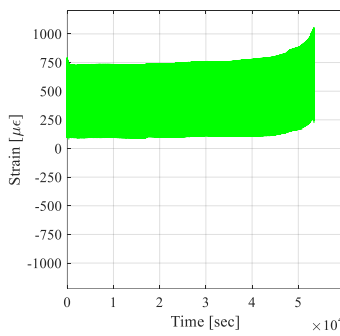
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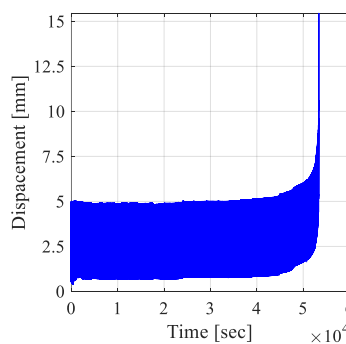
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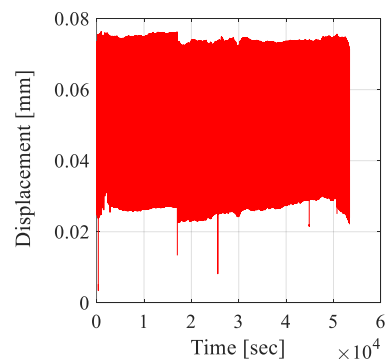
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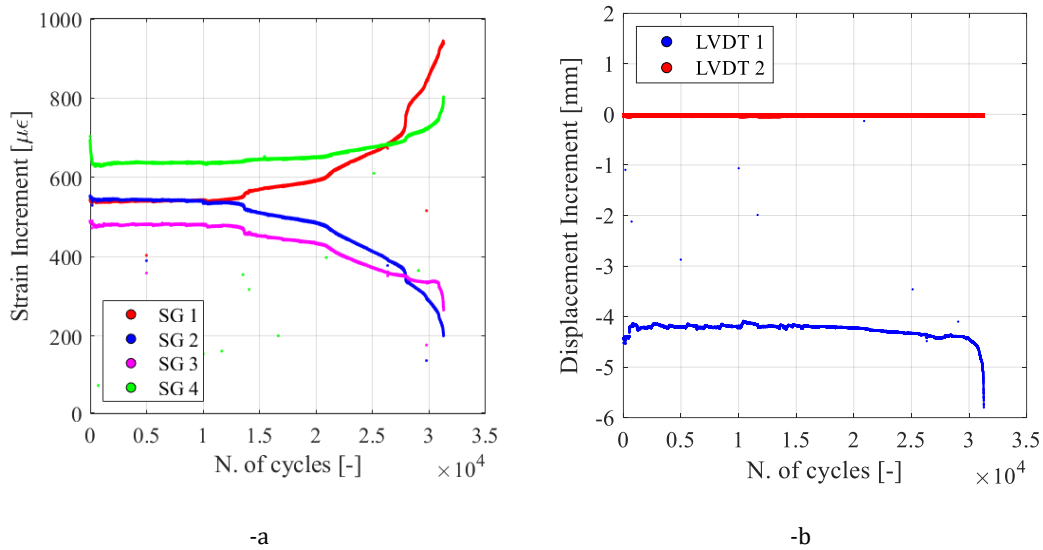
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-f

**Figure 5: Fatigue test result envelopes: strain gauge SG 1 (-a), SG 2 (-b), SG 3 (-c), SG 4 (-d) (negative strains mean traction) and LVDT1 (-e), LVDT2 (-f).**

221



**Figure 6: Strain (-a) and displacement (-b) increment histories.**

222 A quite different trend was observed in the two LVDTs on the cross beam. LVDT 1 recorded the  
 223 vertical displacements in the mid-section and LVDT 2 the possible relative movements at one of  
 224 the lateral riveted connections. As can be seen in **Figure 5-e and -f and Figure 6-b**, there were  
 225 no relative displacements at the lateral joint, showing that the riveted connection maintained its  
 226 integrity. Conversely, LVDT 1 recorded a fairly smooth increase of the mid-span vertical  
 227 displacements until approximately 30k cycles, when the cross beam element was about to fail.  
 228 Deformation sensors (such as SG) are preferable to displacement sensors because they provide  
 229 much more information about the local formation and propagation of fatigue cracks, especially  
 230 in elements subjected to bending such as primary girders.

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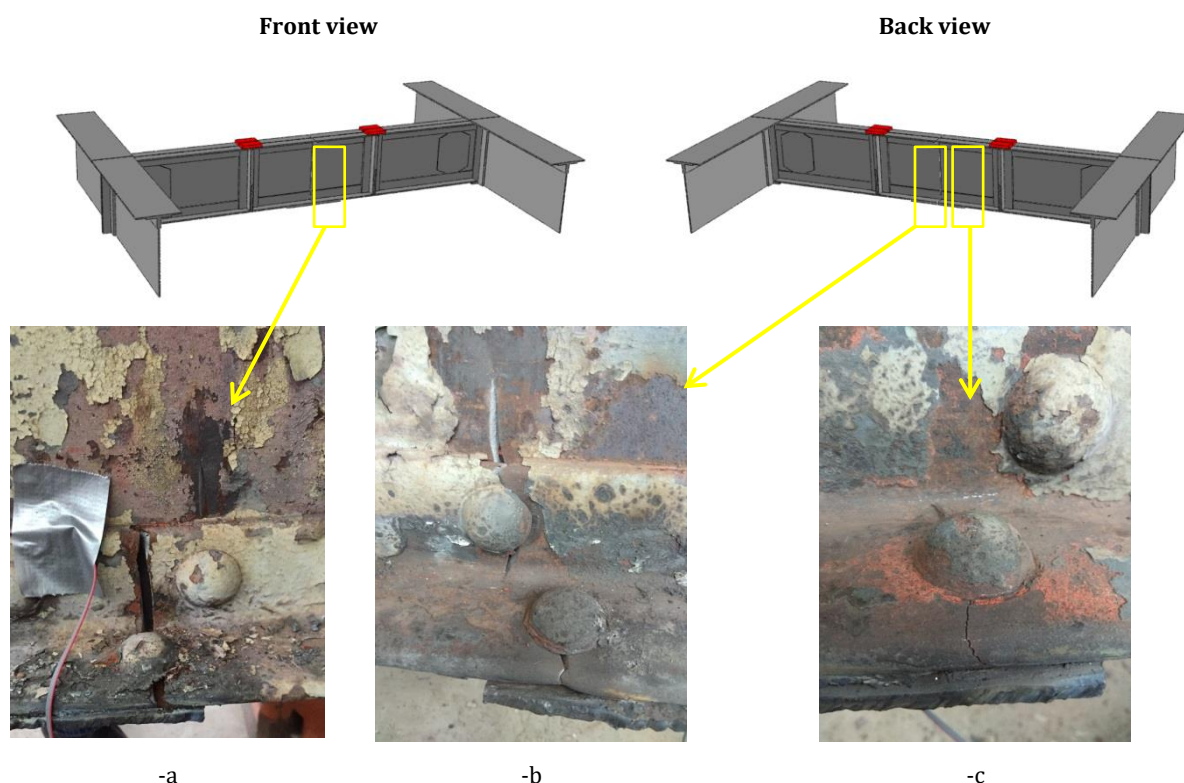
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**Figure 7:** Fatigue cracks observed at the end of the experimental investigation: front (-a) and back (-b) views of first fatigue crack and (-c) back view of the second crack.

240 **Figure 7** shows the crack patterns at the end of the lab test. The cross-beam element has three  
 241 similar fatigue cracks at the edges of the cross beam mid-span plate. The mid-span section  
 242 comprised one steel plate anchored to the bottom flange which was anchored to the vertical  
 243 web. It should be noted that all the joints were riveted. This particular construction technique is  
 244 prone to the following issues: (i) a local change of the cross beam flexural stiffness at the ends of  
 245 the bottom plate and (ii) a reduction of the bottom flange section due to the presence of rivets.  
 246 According to the literature, the most severe cracks begin in the last rivet connecting the bottom  
 247 flange to the steel plate, as can be seen in **Figure 7**. The crack then propagated until  
 248 compromising the bottom flange and reached the vertical web. **In this case, the different**  
 249 **elements composing the girder and connected by rivets were not able to stop the crack**  
 250 **propagation.** Indeed, one fatigue crack severely damaged the vertical web in a symmetrical  
 251 pattern, which was probably due to the flexural behaviour of the cross beam. During the lab test,  
 252 the fatigue crack front propagated from the bottom flanges to the vertical web due to the higher  
 253 stresses caused by the progressive drop in the beam's flexural stiffness caused by the damage  
 254 itself. It is also interesting to note that another two cracks opened on the opposite plate edge  
 255 (see **Figure 7**) but were narrower than the first and did not reach the web.

## 256 5. Full-scale riveted steel bridge

### 257 5.1 Fatigue load protocols and experimental set-up

258 A 21 m long isostatic span from the Ferrandet Bridge was moved to the ICITECH laboratories at  
259 the *Universitat Politècnica de València* (Spain) (see **Figure 8**). In the laboratory, the bridge was  
260 positioned on two hinged and two simple supports (see **Figure 9**). A cyclic load was then  
261 applied ranging from 50 to 1300 kN at a frequency of 0.2 Hz (**maximum load and speed of the**  
262 **hydraulic jack**) by means of a hydraulic jack positioned vertically over the centre of the span,  
263 redistributing the load at four points by means of three stiff beams (green and yellow in **Figure**  
264 **9**).



**Figure 8:** Movement phases: taking from storage area (-a), movement (-b) and laboratory placement (-c).

265 The bridge's structural response was monitored by 40 strain gauges (SG) and 8 Linear Variable  
266 Displacement Transducers (LVDTs) collecting data at a sampling rate of 50Hz.

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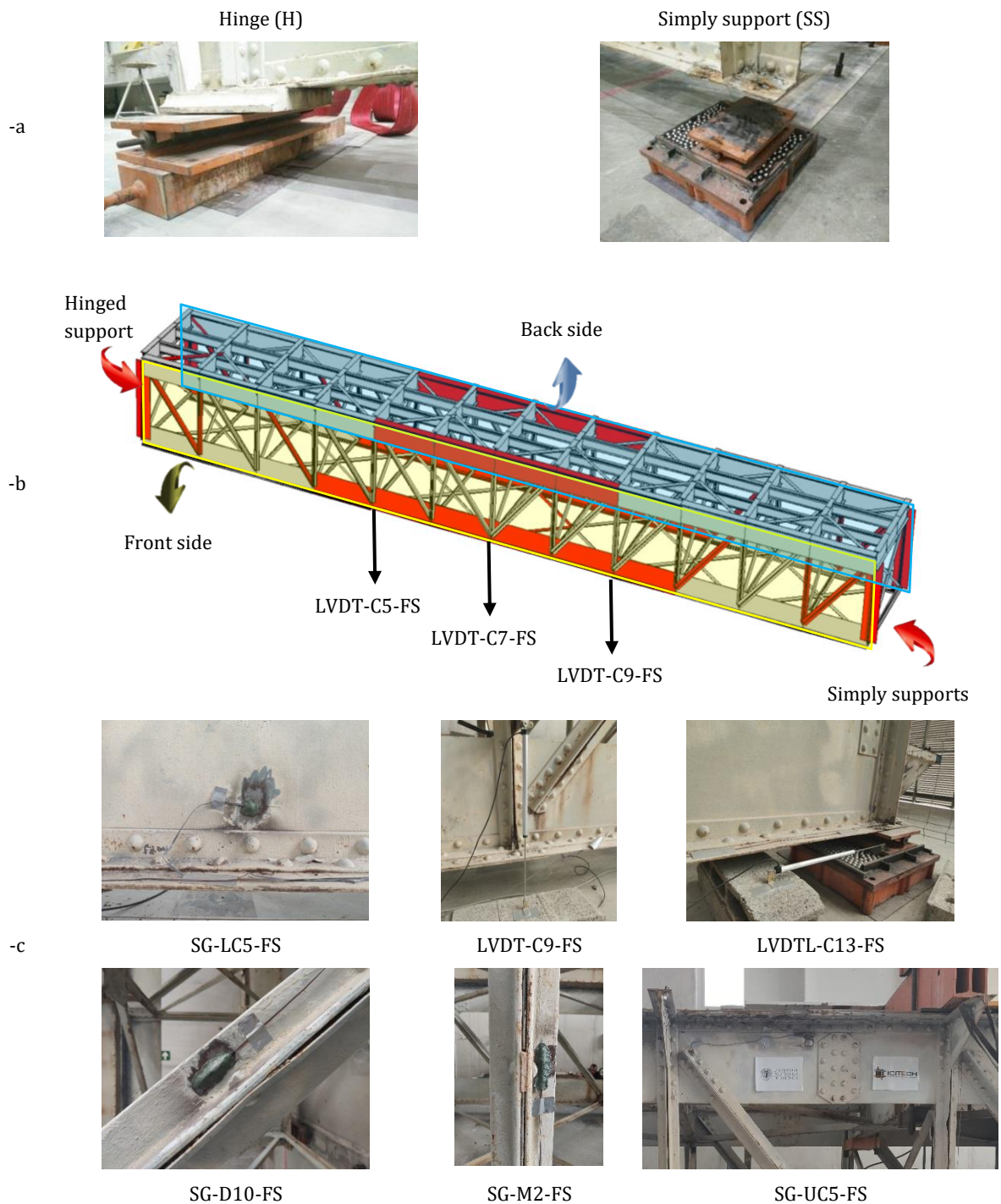
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**Figure 9:** Experimental set-up and sensor network: types of supports (-a), nomenclature details (-b) and types of sensors (-c).

276 The sensor positions are shown in **Figure 9**: (i) position and orientation of the LVDTs (blue  
 277 lines) and (ii) structural elements with SGs (red lines), which comprised: upper and lower  
 278 central chords, lateral diagonals, vertical truss and upper and lower horizontal bracings. The SG  
 279 sensors were placed at the centre of mass of the elements (such as upper and lower chords) and  
 280 at the centre **of each element length**. The LVDTs were placed: (i) on the central vertical columns  
 281 to monitor the maximum vertical displacements, and (ii) close to the lateral supports to study

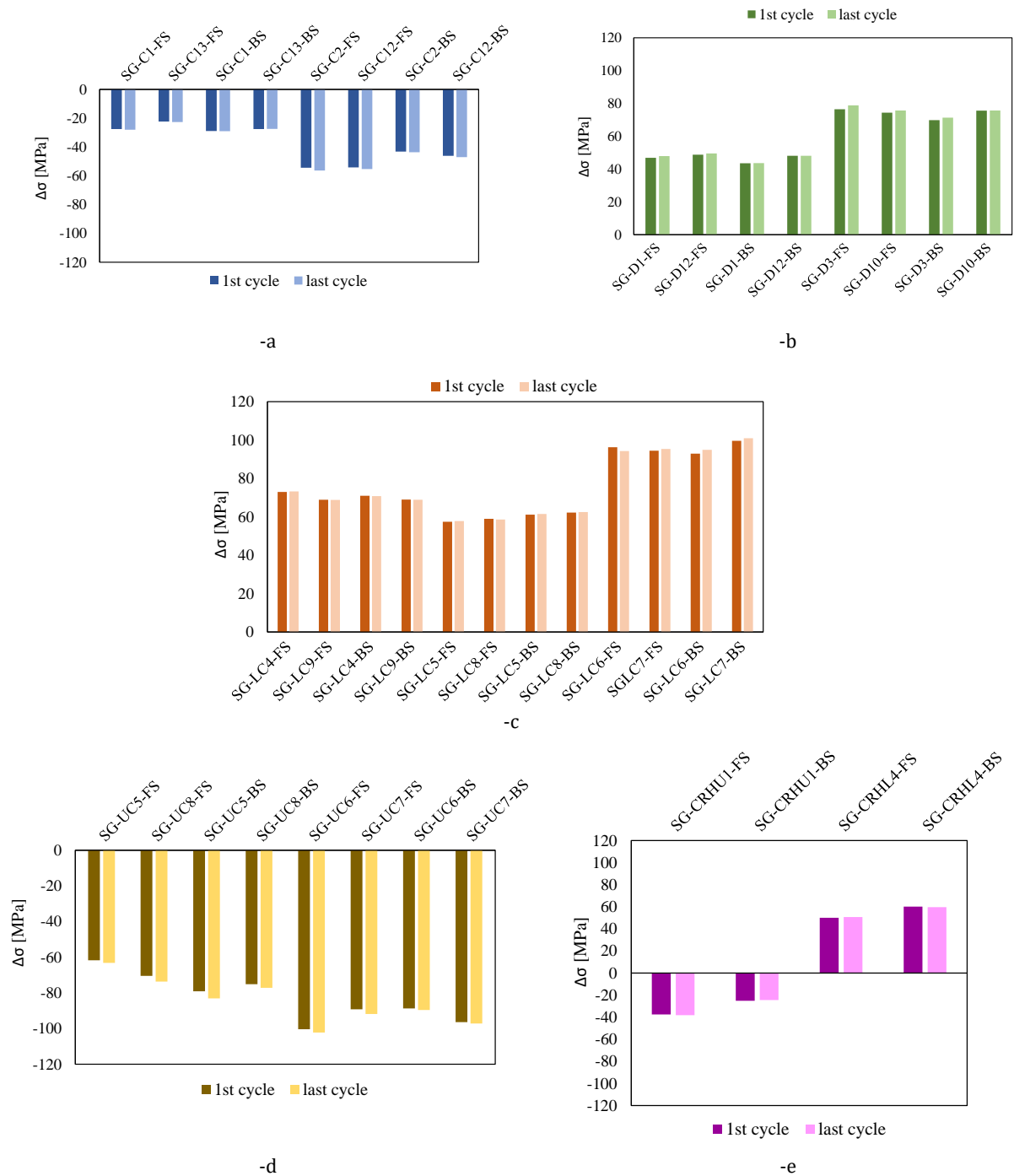
282 the transversal and longitudinal movements of the whole structure. The sensor nomenclature  
283 followed the general rule: X-YN-Z, where X indicates the sensor type (i.e. SG for strain gauges  
284 and LVDT for Linear Variable Displacement Transducers), Y means the element to which the  
285 sensor is applied (i.e. C=vertical columns, UP=upper chord, LC=lower chord, D=diagonal,  
286 CRV=vertical crux, CRHU=upper horizontal crux and CRHL= lower horizontal crux), N indicates  
287 the number of the element starting from the hinged side and Z stands for the position of the  
288 element (i.e. FS=front, BS=rear). The horizontal LVDT nomenclature also indicates the sensor  
289 orientation (i.e. L and T stand for longitudinal and transversal, respectively).

## 290 **5.2 Experimental Results**

291 The strain gauge results are depicted in **Figure 10** and include: vertical struts, diagonal  
292 elements, upper and lower chords and horizontal bracing. For the sake of brevity, since the  
293 fatigue test was over 45k cycles (equivalent to an extra of 27 years more of operational service),  
294 only the first and last cycle stress ranges are compared. The calculation of the equivalent  
295 number of years was performed considering the strain increment monitored during the  
296 laboratory test on the most loaded bottom chord and transforming this value in a stress range  
297 (92 MPa) using the elastic modulus of steel. With this stress range, together with the  
298 consideration of the real detail category of the structure (see Section 6.3 for more details) and  
299 applying the S-N curves methodology, the structure is able to withstand approximately 624k  
300 cycles until reaching the collapse of the structure. Since during the lab test 45k cycles were  
301 applied to the riveted span, the damage accumulated during the laboratory campaign was equal  
302 to approximately 7.2%. Therefore, considering an appropriate behaviour of the structure under  
303 fatigue loading until a level of damage of 7.2%, and also taking into account a series of data for  
304 the future traffic volume and characteristics (e.g. the maximum real stress of the most loaded  
305 bottom chord of the structure is 42.1MPa which is a value monitored in a real field test of the  
306 structure, the train passes over the bridge for the future corresponds to the Type 9, 32  
307 circulations per day; see Section 6.4 for more details) and the S-N curves methodology, a  
308 number of cycles equal to 320k may be withstood by the structure, which could be attained in  
309 27 years. The stress ranges were deduced from the strain increments from the sensors and  
310 multiplied by the steel Elastic Modulus (210 GPa). In **Figure 10-a** it can be seen that there is a  
311 low scatter between the increments in elements C1-FS and C1-BS and on their opposite  
312 counterparts C13-FS and C13-BS. Similar findings could be deduced from the results in **Figure**  
313 **10-b, -c and -d**, showing almost symmetrical bridge behaviour in both directions. As expected,  
314 the stress distribution along the structural elements comprised the central lower chords  
315 subjected to higher stress ranges (LC6-FS/BS and LC7-FS/BS). Similarly, higher compressive  
316 stresses were obtained in the upper counterparts (UP6-FS/BS and UP7-FS/BS). Diagonals D3-



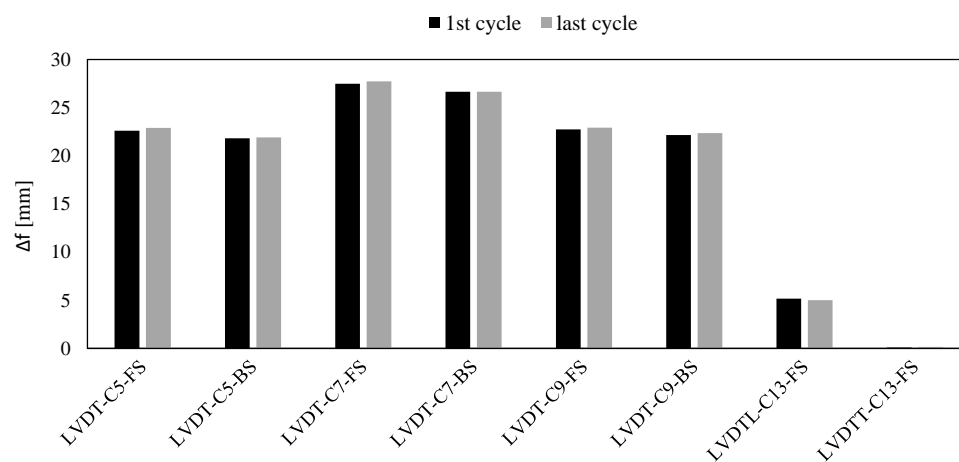
317 FS/BS and D10-FS/BS were the two subjected to the highest stresses. The shear loads were  
 318 higher on the external diagonals and vertical columns, although the stresses were higher in  
 319 other elements due to having smaller cross-sections. Three general observations can be made:  
 320 (i) the stress level in all the elements is far lower than the elastic limit obtained from the lab  
 321 tests reported in Section 3, (ii) none of the elements analysed in the present study obtained  
 322 more than a 5% difference between the first and the last cycles; and (iii) visual inspection did  
 323 not reveal any damage in the structure.



**Figure 10:** Stress range computed at the beginning and at the end of the test in: (-a) columns, (-b) diagonals, (-c) columns, (-d) columns, (-e) diagonals.

upper chords, (-d) lower chords and (-e) bracing cruxes.

324 **Figure 11** gives the displacement increments read by the LVDTs on the central portion of the  
 325 bridge (LVDT-C5-FS/BS, LVDT-C7-FS/BS and LVDT-C9-FS/BS) and those that monitored the  
 326 longitudinal and transversal movements of the structure (LVDTL-C13-FS and LVDTT-C13-  
 327 FS/BS). As expected, the maximum vertical displacements were observed in the centre of the  
 328 bridge. As in **Figure 10**, displacement increments did not vary between the first and last cycle,  
 329 again confirming the absence of damage and the elastic behaviour of the bridge. LVDTT-C13-FS  
 330 monitored the possible presence of transversal displacement of the support. As shown in  
 331 **Figure 11**, there were negligible movements in that direction.

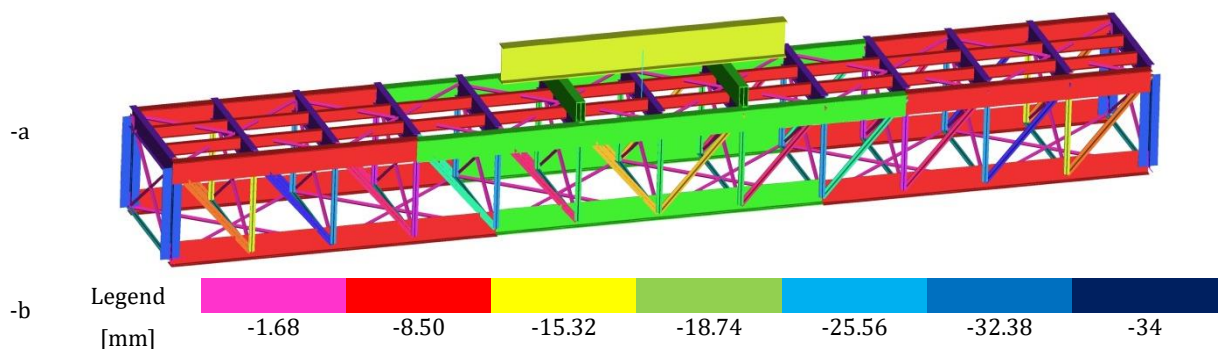


**Figure 11:** Displacement increment computed at the beginning and at the end of the fatigue test.

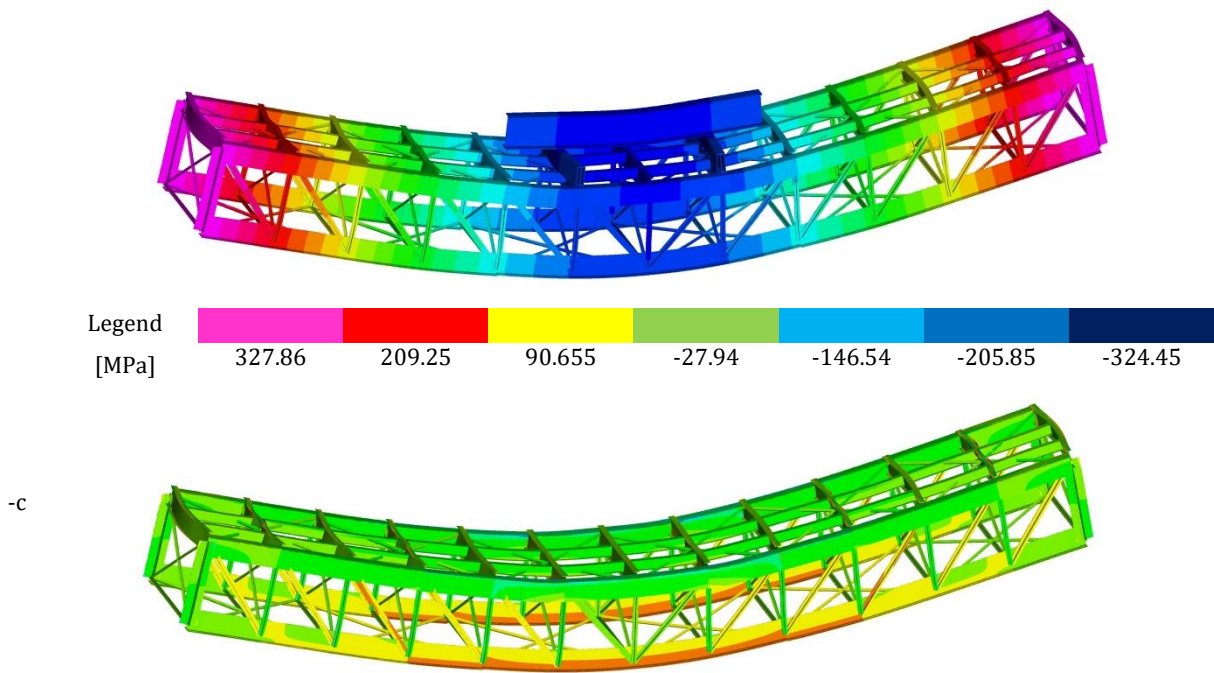
332 The experimental results were also compared to the numerical outputs obtained using a 3D  
 333 Linear-Static Finite-Element model (LSFE). The isostatic span tested during the lab investigation  
 334 was modelled by means of two-noded beam elements, as shown in **Figure 12-a**.

335

336

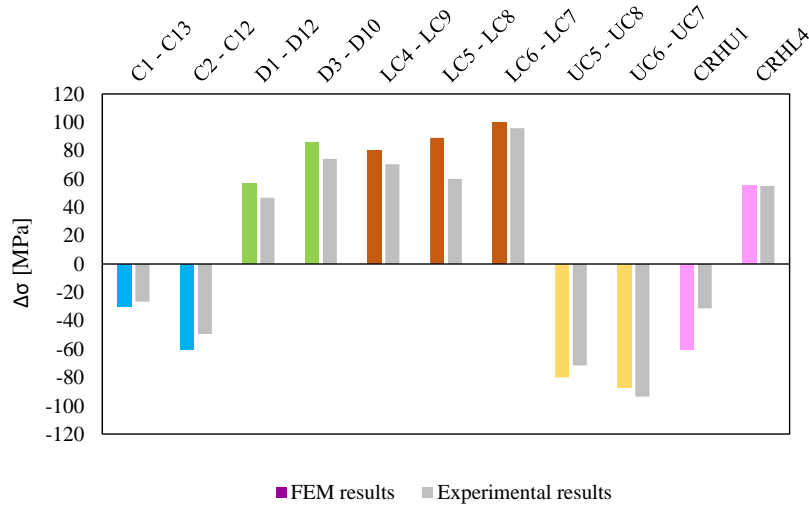


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**Figure 12:** Finite Element model developed to analyse the behaviour of the isostatic span tested during the lab investigation (-a), vertical displacements (negative downwards) (-b) and total stresses along the bridge (-c).

337 **Figure 12-b and -c** gives the vertical displacement and **fibre stresses** produced in the structure  
338 by a static load equal to 1250 kN applied on the top of the longitudinal stiff beam. **It is worth**  
339 **mentioning that the stresses depicted in Figure 12-c consider both axial stresses and bending**  
340 **stresses.** The results slightly overestimated the bridge deformability, with 32 mm of vertical  
341 displacement at the centre of the beam, compared with the 27 mm registered by LVDT-C7-  
342 FS/BS. A comparison between the experimental and numerical results in terms of total stresses  
343 is shown in **Figure 13**. The experimental results given in **Figure 13** were obtained from the  
344 average output obtained from each element and their symmetrical counterparts. The model  
345 accurately predicted the stress state of each element. The reliability of the model led to its being  
346 used for the further analyses described below.

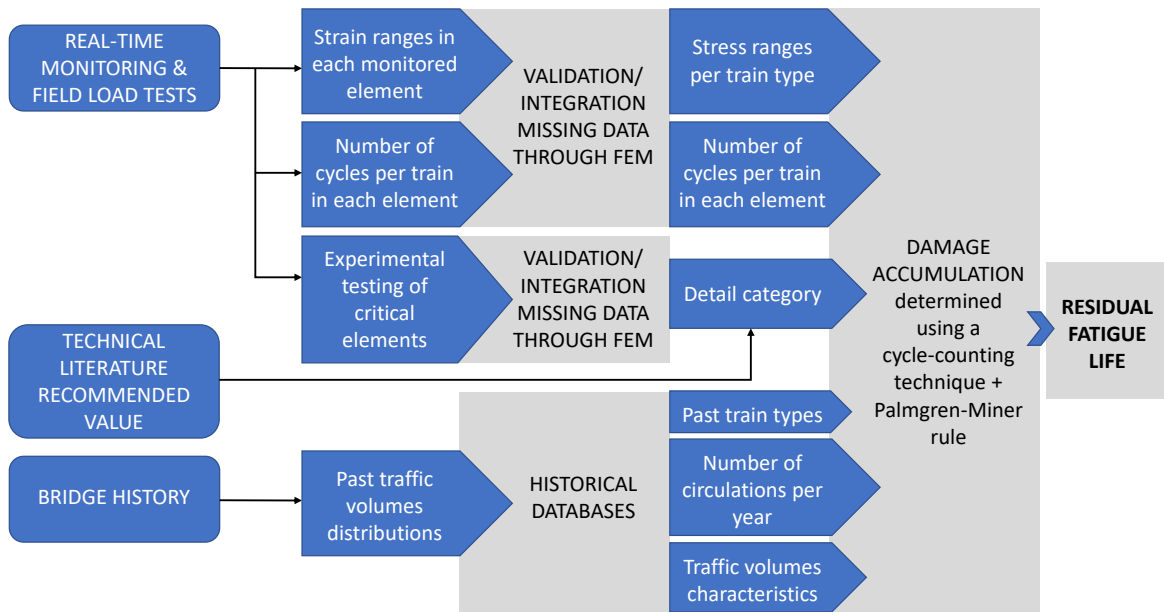


**Figure 13: Comparison between experimental (grey bars) and FE results (coloured bars).**

## 347 6. Analytical evaluation

### 348 6.1 Method

349 This method was defined for a general case and then applied specifically to the Quisi Bridge. The  
 350 analytical assessment following this general method included: (i) load tests on the bridge, (ii)  
 351 experimental results from the double experimental tests described in Sections 4 and 5, (iii) the  
 352 numerical model validated by the full-scale test outputs, and (iv) the recommendations  
 353 proposed by [10]. When all the experimental data is not available, this method also suggests the  
 354 criteria to use.



**Figure 14: Relational flowchart of the proposed approach.**

355

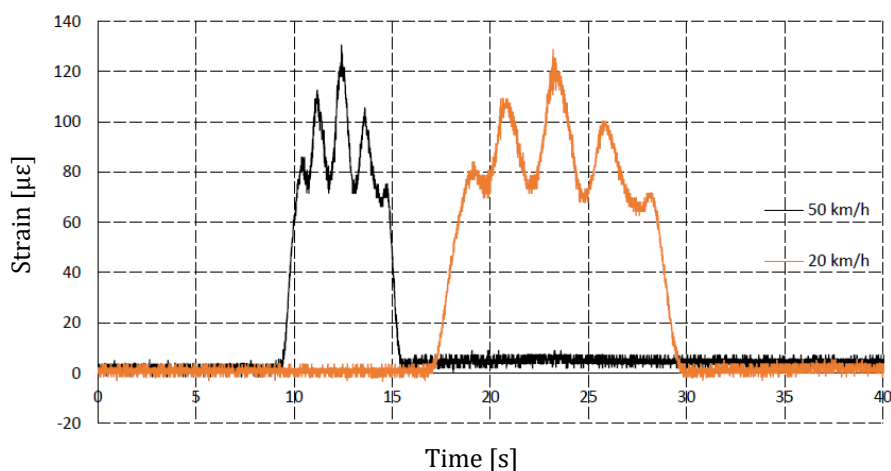
356 The method is organized into five steps **summarized in the relational flowchart depicted in**  
357 **Figure 14:**

- 358 1- Collection of information from past traffic volumes considering different train types (see  
359 Section 6.2).
- 360 2- Definition of (i) the number of cycles suffered by each element for each train type  
361 passing over the bridge and (ii) number of stress-increments in each type of element for  
362 a known type of train by real time monitoring during field load tests (see Section 6.2) if  
363 available or with the help of numerical simulations.
- 364 3- Extrapolation of stress ranges considering other types of trains and elements and  
365 validation throughout numerical simulations (see Sections 6.3 and 6.4).
- 366 4- Definition of detail category, depending on the available data:
- 367 - Adoption of recommended values from [10][11][13], namely: detail category 71 and  
368 100, depending on the expected triggered failure mechanism being normal or  
369 tangential, respectively.
  - 370 - Through fatigue failure tests of isolated elements such as the one described here and  
371 the application of damage accumulation rules such as the Palmgren-Miner rule  
372 recommended by EC3 (see Section 6.3).
- 373 5- Estimation of the remaining life of the bridge components applying damage  
374 accumulation rules, such as Palmgren-Miner (EC3) and the component's load history.  
375 For this, the current accumulated damage of each element is calculated for the  
376 subsequent projection of its remaining service life (see Section 6.4).

## 377 **6.2 Load history and data from field load tests**

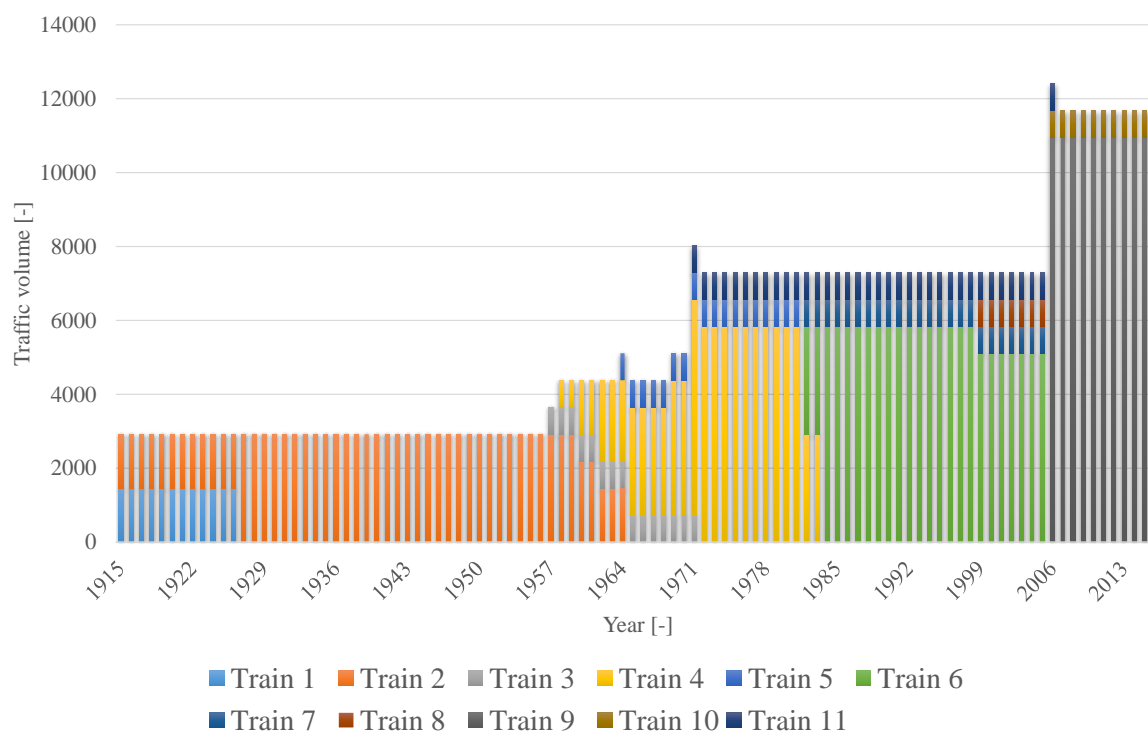
378 Rolling loads on bridges such as those produced by vehicles cause variable amplitude stress  
379 distributions and typically a large number of cycles. In the broad field of fatigue assessment, the  
380 stress distribution can be determined using a cycle-counting technique such as the rainflow  
381 counting method. Current standards like the Eurocode 3 [10] for bridge fatigue assessment is  
382 based on the Palmgren-Miner rule to account for linear damage accumulation. Although  
383 structures with riveted joints are not explicitly referred to in EC3, several experimental  
384 investigations have classified these structures as detail category 71 [13]. In the present study,  
385 the damage accumulation rule was defined by coupling the stress distribution obtained from  
386 field load tests [29] together with the maximum stresses obtained in the elements of a 3D LSFE

387 model of the whole bridge. The field tests on the Quisi Bridge were used to estimate its dynamic  
388 behaviour under the load of a specific train type (Train 9) [29].



**Figure 15:** Strain distribution caused by the circulation of train 2500 in the central lower chord (isostatic span) assuming two different train velocities. Source: Ivorra et al. [29].

389 **Figure 15** gives the strain distribution monitored in the central lower chord of one of the  
390 isostatic spans. The measurements were taken at two different train speeds. **Figure 15** shows  
391 that the speed did not affect the maximum strain or the number of cycles obtained in the lower  
392 chord. The strain distribution of the most representative elements was compared to the  
393 numerical output obtained from a static analysis. The results of the field tests were used to  
394 evaluate: (i) cyclic stress characteristics associated with the different train loads. These results  
395 showed that cross-beams and stringers (longitudinal primary beams) are subjected to one cycle  
396 per axle, while all the other elements are subjected **to** lower cycles (cycles per train); (ii) the  
397 dynamic effect of train loads and the **stress ranges** in all the elements (the latter was deduced  
398 from the LSFE model). Deformation was found to increase by 30% **in the field tests with respect**  
399 **to the FE analysis**, resulting in a dynamic amplification factor of 1.3. The bridge's detail class  
400 was calculated from the information available on its loading history in service expressed by  
401 traffic volumes and their characteristics (**see more details in Section 6.3**). Assuming a period  
402 dating from 1915 to the present, 11 different types of train passed over the bridge, as can be  
403 seen in **Figure 16**.



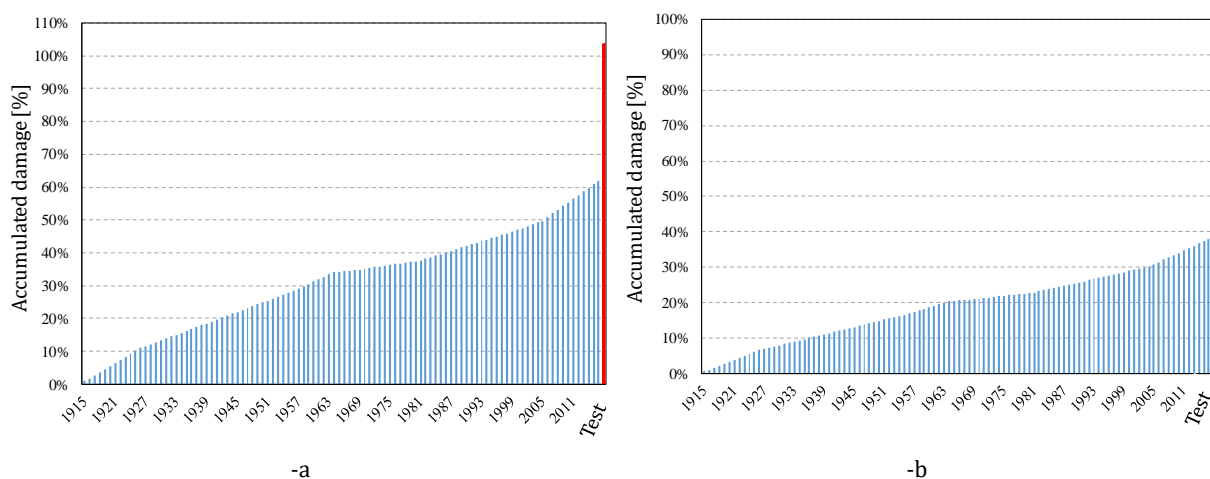
**Figure 16:** Loading history of the bridges during their exploitation expressed by train typology distributions over the years and traffic volumes. Data provided by the railway administration.

### 404      6.3      Definition of detail category based on test results

405 This section describes the calculation of the detail class of the cross beam from the experimental  
 406 results described in Section 4, the information available on traffic volumes and the Eurocode 3  
 407 recommendations. The cross beam detail class was obtained assuming two different  
 408 hypotheses: (i) trains were either completely loaded or (ii) only 80% loaded (this load is  
 409 approximately the self-weight of the different train types). These two assumptions were made  
 410 to take into account the uncertainty of the historical traffic loads. **Past damage accumulation**  
 411 **was deduced from the traffic volumes reported in Figure 16 considering that the cross beam**  
 412 **was 100% damaged during the lab test (i.e. after 31,377 cycles) and following the Palmgren-**  
 413 **Miner rule. In detail, the total damage accumulation was divided into two parts: (i) damage**  
 414 **accumulated during past train circulations and (ii) residual damage needed to reach the failure**  
 415 **of the structure (100% damage as it was damaged during the lab test). In the first part, the**  
 416 **accumulated damage was estimated as a function of the detail category (still unknown) and**  
 417 **based on typical strain distribution patterns obtained in critical cross beams during field load**  
 418 **tests. The information obtained during the real time field load tests allowed the calculation of**  
 419 **the number of cycles per train passage and the strain increment associated with each**  
 420 **circulation. In the second part, the number of cycles and the stress ranges applied to the**  
 421 **element during the laboratory test were used to calculate the total damage of the cross beam as**

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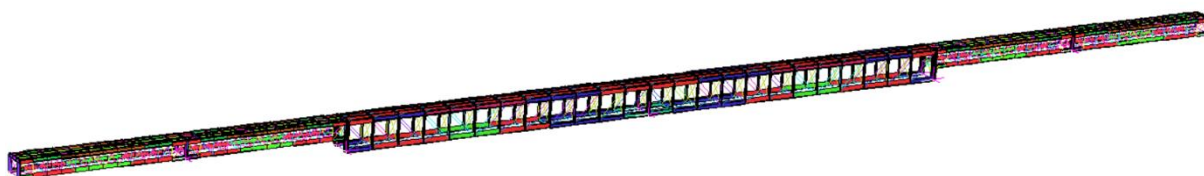
422 a function of the detail category. It is worth mentioning that the procedure adopted included a  
423 first hypothesis of the detail category which was then estimated by verifying that the complete  
424 damage (damage 100%) had been obtained after the laboratory test. In the 100% and 80%  
425 loading scenarios detail classes of 71 and 63 were deduced, respectively. The results, in terms of  
426 accumulated damage during consecutive periods of bridge operation from 1915 (blue bars) and  
427 the lab test (red bar) are given in **Figure 17-a and -b** and confirm that the cross beam would  
428 fail at detail category 71, for fully loaded trains, and at detail category 63 for 80% loaded trains.



**Figure 17:** Accumulated damage distributions over the bridges exploitation, considering: trains loaded at 100% (-a) and at 80% (-b).

#### 429 **6.4 Estimation of the remaining fatigue life**

430 Remaining fatigue life can be analysed using LSFE models for stress amplitudes and the number  
431 of cycles undergone by each element. The Quisi Bridge was analysed adopting the LSFE model  
432 described above (see **Figure 18**). **Table 5** shows the results obtained for future traffic loads  
433 over the bridge (Train Type 9) without considering a dynamic amplification factor. **In detail,**  
434 **strain increment patterns due to train circulation obtained from field load tests were used**  
435 **together with FE outputs to estimate the number of cycles per train circulation and the**  
436 **maximum stress ranges in the most critical elements composing the structure. This information**  
437 **was used to extrapolate the damage accumulated from 1915 till 2016.**

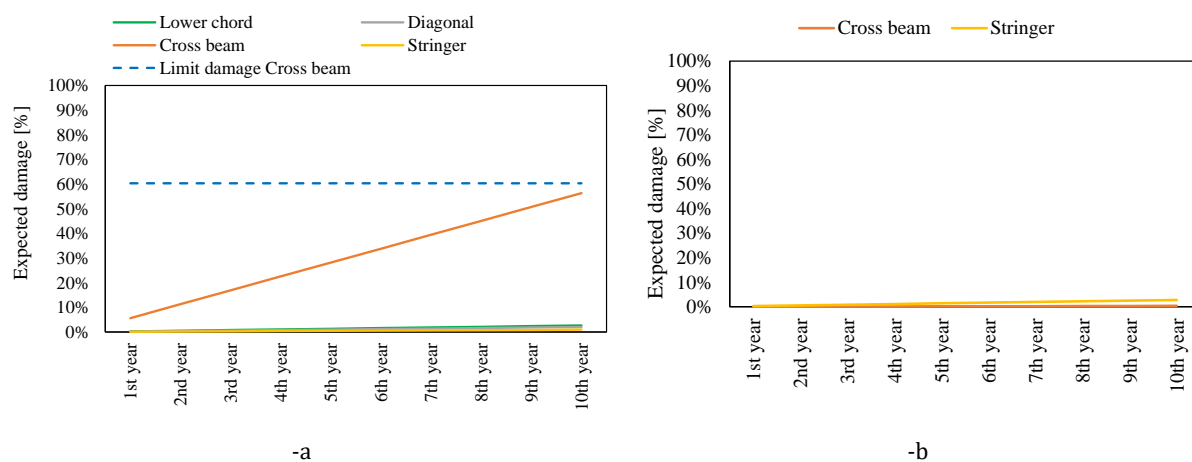


**Figure 18:** Finite Element model of the whole bridge, considering the strengthening and reparations introduced in the structure.



Structural Element		Maximum stress [MPa]
Lower chord		32.4
Diagonal		29.7
Cross beam	Axle 1	32.8
	Axle 2	28.6
Stringer	Axle 1	14.8
	Axle 2	12.9

439 It is important to remember that, in this case, cross beams and stringers are directly subjected  
 440 to the cycles produced by each axle, instead of 3 cycles per train, and therefore to higher  
 441 accumulated damage than other elements. Considering a detail class equal to 71 or 63 for fully  
 442 or 80% loaded trains, respectively (computation was performed in this case with detail class 63  
 443 but results are identical in both situations), assuming that the expected traffic volume in the  
 444 next 10 years will consist of 32 type 9 trains **per day** and using the S-N curves method  
 445 recommended by Eurocode 3, the damage caused in this period can be extrapolated.



**Figure 19:** Expected accumulated damage in different structural elements considering: normal stresses (-a) and tangential stresses (-b).

446 **Figure 19-a** gives the damage percentages (due to normal stresses) expected to be accumulated  
 447 in future train passages. This information must be coupled with the results illustrated in **Figure**  
 448 **17-b** which shows the percentages of past damage accumulated by the bridge during  
 449 operational service using the detail category of 63 and 80% of the loaded trains. From that data  
 450 it is possible to see that, before the laboratory test, the bridge accumulated (from 1915 to 2016)  
 451 about 40% of damage. In the next 10 years, the cross beams will reach the 60% damage limit  
 452 available considering a detail class 63 and 80% loaded train (Section 6.2), according to the  
 453 information in **Figure 19-a**. The same calculation was repeated considering the tangential

454 stresses in the riveted connections taking into account the number of rivets composing the  
455 lateral connections of each element and the cross-section of each rivet. The results are given in  
456 **Figure 19-b** considering only cross beams and stringers and the lower detail class  
457 recommended by Eurocode 3 (80, the lowest in EC3). As can be seen in **Figure 19-b**, the damage  
458 expected in the next 10 years due to tangential stresses is quite low. Results from **Figure 19 -a**  
459 **and -b** confirm that the cross beams are the most vulnerable elements in the bridge (**Figure 19**  
460 **-a**) and that normal stresses will be responsible for future fatigue damage (**Figure 19 -a and -**  
461 **b**).

## 462 7. Conclusions

463 This paper describes a study that aimed to provide meaningful experimental results on the  
464 fatigue behaviour of riveted steel railway bridges subjected to rolling loads in a combination of:  
465 (i) an ambitious experimental study with two full-scale tests to study local and overall bridge  
466 fatigue performance; and (ii) an analytical evaluation to assess the bridge's remaining fatigue  
467 life. The study was carried out on two riveted steel bridges in the Valencia railway network: the  
468 Quisi and Ferrandet Bridges, from which the following conclusions can be drawn:

- 469 - A cross beam element was subjected to a 0.55 Hz frequency cyclic load ranging from 50  
470 to 650 kN to assess the local behaviour of the structure. The results showed that:
  - 471 ○ Fatigue cracks most probably nucleated after 10 k cycles and progressed fairly  
472 quickly until collapse at approximately 31k cycles.
  - 473 ○ The LVDT that monitored maximum vertical displacements was unable to  
474 capture any warning signs of imminent failure before 30k cycles, while strain  
475 gauges on the central section were able to track the redistribution of stresses as  
476 the cracks grew.
  - 477 ○ A fatigue test on a cross beam showed that fatigue cracks are likely to appear  
478 near to the central section. This finding could be explained by the peculiar  
479 geometry of the element and by the presence of an additional lower plate  
480 responsible for a sudden change in flexural stiffness.
  - 481 ○ Estimation of the detail class using the traditional S-N curves method found  
482 cross beam detail classes of between 63 and 71, depending on the uncertainties  
483 related to traffic loads.
- 484 - A full-scale fatigue test of an isostatic span was carried out to assess the structure's  
485 overall behaviour and reached the following conclusions:
  - 486 ○ The test identified the most heavily loaded elements and furnished the  
487 experimental results to calibrate a Finite Element model.

- 488           ○ The fatigue test lasted for 45k cycles with a **load range** equal to 1250kN. During  
489           the lab investigation, the steel span showed elastic behaviour without the  
490           appearance of any fatigue damage. This confirmed that the non-primary  
491           elements of the bridge could be expected to operate safely for 27 more years.
- 492       - An analytical method based on load tests, numerical modelling, recommendations and  
493       codes was **adopted** to evaluate remaining bridge fatigue life. Its application to the bridge  
494       under study reached the following conclusion:
- 495           ○ Fatigue calculations of the Quisi Bridge's remaining fatigue life identified the  
496           cross beams as the most vulnerable elements. Fatigue failures can be expected to  
497           arise in the next 10 years due to normal stresses, but not in the lateral riveted  
498           connections.

499       **This work represents a step toward understanding the overall and local fatigue responses of old**  
500       **riveted steel bridges with a unique double experimental investigation. The results are expected**  
501       **to increase the existing fatigue test database: (i) confirmation of the detail category of steel**  
502       **riveted structures and (ii) the adoption of an analytical method applicable to other cases. A**  
503       **possible future extension of the present research line is represented by the evaluation of a**  
504       **wider number of critical principal elements (i.e. transversal girder and stringers) subjected to**  
505       **variable amplitude stress ranges, such as those produced in highway bridges.**

506

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517

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