

An animal feed distribution company based in Alzira must serve more than twenty clients daily. An example of a typical day can be found in the following table.

| Towns | # Pallets | X | Y |
|--------------------------|-----------|---------|--------|
| ALBORACHE | 17 | -7,5 | 7,5 |
| ALCACER | 2 | -0,25 | 6,75 |
| ALCUDIA DE CARLET | 6 | -1,5 | 1,5 |
| ALGEMESÍ | 2 | 0,00001 | 1 |
| ALMOINES | 12 | 5,5 | -6,5 |
| BENIFAIÓ | 4 | 0,0001 | 4 |
| BENIGANIM | 6 | -0,25 | -6,5 |
| CARCAIXENT | 2 | -0,5 | -1 |
| CARLET | 4 | -2 | 2,5 |
| CHIVA | 6 | -6,25 | 10,25 |
| DENIA | 6 | 12 | -9,75 |
| L'OLLERIA | 12 | -2,5 | -7,5 |
| LLOMBAI | 4 | -3 | 4,25 |
| ONTINYENT | 12 | -3,75 | -10,25 |
| SILLA | 4 | 0,5 | 6,85 |
| SUECA | 12 | 2,75 | 1,65 |
| TAVERNES DE LA VALLDIGNA | 4 | 3,75 | -2,5 |
| VILANOVA DE CASTELLO | 6 | -1,75 | 2,5 |
| XATIVA | 12 | -2 | -5 |

The matrix of distances between the towns is given in the above table. It is assumed that loading a truck takes around 45 minutes and unloading the truck in each customer’s company location takes about 30 minutes on average. No driver must dedicate more than 8 hours a day to driving or working more than a total of 12 hours a day. The average speed of each truck is 60 Kilometers / hour.

The company has 3 types of trucks:

- Trucks which are 7 meters long and 2 meters wide. The cost (€) per kilometer is 0.25.
- Trucks which are 10 meters long and 2.3 meters wide. The cost (€) per kilometer is 0.3.
- Trailers which are 12.5 meters long and 2.5 meters wide. The cost (€) per kilometer is 0.35.

Propose a mathematical programming model in order to:

- Determine the most suitable routes to ensure a daily service.
- Consider that delivery does not have to be made on a daily basis. However, if the delivery made is higher than the daily demand, you have to pay for the excess of stock at the client's location. Each pallet stored implies a cost of 0.1 € / (pallet * day).
- Consider that there are some time-windows for loading/unloading trucks.