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Additional Information

A practical guide for setting up a Fourier lightfield microscope

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Abstract: A practical guide for the easy implementation of a Fourier Lightfield Microscope is reported. The Fourier Lightfield concept applied to microscopy allows the capture in real time of a series of 2D orthographic images of microscopic thick dynamic samples. Such perspective images contain the spatial and the angular information of the lightfield emitted by the sample. A feature of this technology is the tight requirement of a double optical conjugation relationship, and also the requirement of NA matching. For these reasons, being the Fourier Lightfield Microscope a non-complex optical system, a clear protocol on how to set up accurately the optical elements is needed. In this sense, this guide is aimed to simplify the implementation process, which will help the widespread of this recent technology. © 2022 Optica Publishing Group.

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1. Introduction

Optical microscopes are designed for obtaining 2D images of small samples. Although it is commonly believed that the main feature of microscopes is their ability for providing highly magnified images, this is not entirely correct. This statement is more evident in the context of digital images, which can be easily magnified by a simple resizing operation, often performed with two fingers. Thus, high magnification is not a distinct feature, mainly in the digital world. Clearly, the main feature of microscopes is their capacity for producing images with high lateral resolution. Resolution is defined as the capability of an optical system for producing images in which the small details are distinguishable. Resolution is usually evaluated in terms of the Rayleigh criterion, which measures the minimum distance reachable between two equal-intensity point sources so that their images are still distinguishable. An alternative approach, due to Ernst Abbe, is to measure the cut-off spatial frequency. In any case, the two approaches provide similar results, which mainly depend on the numerical aperture (NA) of the microscope objective. Additionally, the influence of the pixel size must be taken also into account, especially when the pixel size is comparable with the Rayleigh resolution limit.

An important drawback of conventional microscopes is their performance when imaging 3D objects. In that case, the sensor captures a 2D image that is the result of collapsing onto the image plane the 3D image of the 3D sample. This includes the blurring associated with object planes out from the system's Depth of Field (DoF). As a result, the angular (or perspective) information of the sample is lost, even in the case that one captures a focal stack and builds a 3D image from it [1].

Aiming to overcome these problems, Lightfield Microscopy (LMic) was reported a few years ago [2–7]. LMic is based on the smart idea, reported by Lippmann [8], that a collection of perspective images of a 3D scene, stores both the spatial and the angular information of the rays emitted by the scene. Specifically, an LMic is built by inserting a microlens array (MLA)

46 at the image plane of a conventional microscope and shifting the sensor up to the microlenses
47 rear focal plane. This capability of capturing in a single shot the spatial-angular information
48 of 3D specimen, allows LMic to be specially adapted to deal with the 3D behavior of dynamic
49 biological processes [6, 9–12].

50 However, the images captured with LMic still show the following drawbacks. (a) The
51 perspective images (also known as elemental images – EI) are not obtained directly but computed
52 from the captured microimages. (b) The lateral resolution of EIs is determined by the microlenses
53 pitch, whereas the number of pixels covered by any microlens determines the density of the
54 angular sampling. As consequence, LMic provides images with a spatial resolution that is about
55 10 times worse than that of the host microscope where the MLA is inserted. (c) The lateral
56 resolution of computed depth sections is inhomogeneous. (d) The system is not linear and
57 shift-invariant, and therefore not easy application of deconvolution tools is possible.

58 Naturally, much work has been reported aiming to overcome these drawbacks by computational
59 means. However, such methods have to tackle two essential difficulties. One is that the images
60 captured by LMic have a low spatial resolution, and therefore much high-frequency information
61 has escaped, which cannot be recovered by digital processing. The other is the complexity of
62 the deconvolution procedures application. This implies that the algorithms need to be highly
63 sophisticated and time-consuming. Nevertheless, the results obtained by such computational
64 methods are inspiring [13, 14].

65 To avoid these problems, Fourier Lightfield Microscopy (FLMic) was proposed [15–19].
66 FLMic is based on a new paradigm since the microlenses, whose pitch is now one order the
67 magnitude bigger than in LMic, are placed no longer at the image plane but at its far field; the
68 Fourier plane. Then the EIs are captured directly and have a spatial resolution that is 3 to 5 times
69 worse than that of the host microscope, but 2 to 3 times better than in LMic. Importantly, here
70 the captured EIs have shift invariance, which allows the direct use of deconvolution tools and the
71 computing of depth sections that have homogeneous resolution through the system DoF. Another
72 advantage of FLMic is that it can be implemented easily by inserting an accessory at the camera
73 port of a conventional microscope, and therefore can make use of the usual facilities of such
74 microscope as for example the dark-field illumination mode [20, 21].

75 Even though the impact aroused in the microscopy community [22–32], the generalization
76 of the use of FLMic is still limited. One of the problems is the selection of the set of optical
77 components, which must to fulfill many crossed relations. This problem was already addressed
78 in our previous paper [33]. As a follow on to that paper, we still consider that it can be very
79 useful to provide a similar tutorial on construction, alignment, and test/validation methods. This
80 conviction has aimed this laboratory note, in which we show, step by step, a comprehensive guide
81 for the accurate implementation of a FLMic.

82 **2. Basic theory**

83 Fourier lightfield microscopy (FLMic) is an optical technique that permits the direct capture
84 of a series of orthographic perspective views of thick microscopic samples. The concept
85 behind FLMic is simple; a microlens array (MLA) is inserted at the aperture stop (AS) of
86 an infinity-corrected microscope objective (MO) and the sensor is set at the lenslets rear FP.
87 This permits the simultaneous capture of orthographic images of the specimen. However, this
88 preliminary scheme lacks flexibility, since the MLA must be fully adapted to the selected MO and
89 also to the requirements in resolution and parallax. Then, if a researcher wanted to implement
90 a FLMic in the laboratory, and aimed to have enough flexibility, it is preferable not to insert
91 the MLA directly at the AS, but at a conjugate plane. This is achieved by using a telecentric
92 relay ($L_{R1} + L_{R2}$) formed by two converging lenses and a circular aperture as shown in Fig. 1(a).
93 Note that, since a FLMic deals with 3D samples, we must define a reference object plane (ROP)
94 within the region of interest, which must be placed at the MO focal plane. As stated above, the

Table 1. List of acronyms used in the paper.

Acronym	Full name
AS	Aperture Stop
DoF	Depth of Field
EI	Elemental Image
FLMic	Fourier Lightfield Microscope
FOV	Field of View
FP	Focal Plane
FS	Field Stop
LED	Light Emitting Diode
LMic	Lightfield Microscope
MLA	Microlens Array
MO	Microscope Objective
NA	Numerical Aperture
ROP	Reference Object Plane
S & M	Shift and Multiply
S & S	Shift and Sum

95 conjugations relations are key. In this sense, the MO together with the first lens of the telecentric
96 relay (L_{R1}) conform a telecentric coupling that conjugates the ROP with the back focal plane
97 (FP) of L_{R1} , where a field stop (FS) is placed. Also, the image of the AS through L_{R1} is at the
98 infinity. On the other hand, the telecentric relay provides the image of the AS at the rear focal
99 plane of second lens of the telecentric relay (L_{R2}), where the MLA is placed. The image of the
100 ROP is now at infinity. Finally, the microlenses provide multiple images (named as elemental
101 images –EI) of the object at the lenslets rear focal plane, where the sensor is set.

102 In Fig. 1(b) we have made explicit the conjugation relation between the AS and the MLA by
103 painting a shaded MLA at the AS. Also, we have represented with different colours the light
104 beams that pass through different microlenses. Clearly, each microlens collects the light passing
105 through a different, non-overlapping, region of the AS. The size of the AS determines the number
106 of microlenses that fit into it, and then the number (N_{EI}) of captured EIs,

$$N_{EI} = \frac{\phi_{AS}}{\hat{p}} = \frac{2f_{ob}f_{R2}NA}{f_{R1}p}, \quad (1)$$

107 where $\hat{p} = pf_{R1}/f_{R2}$ is the lenslets pitch, p , as back-projected onto the AS.

108 Conversely, the lenslets diameter determines the effective numerical aperture (NA) under
109 which the EIs are captured. We can conclude from Fig. 1(a) that the FLMic captures N_{EI} images
110 (along one Cartesian direction), each with different perspective information and under an effective
111 NA given by

$$NA_{ef} = \frac{NA}{N_{EI}}, \quad (2)$$

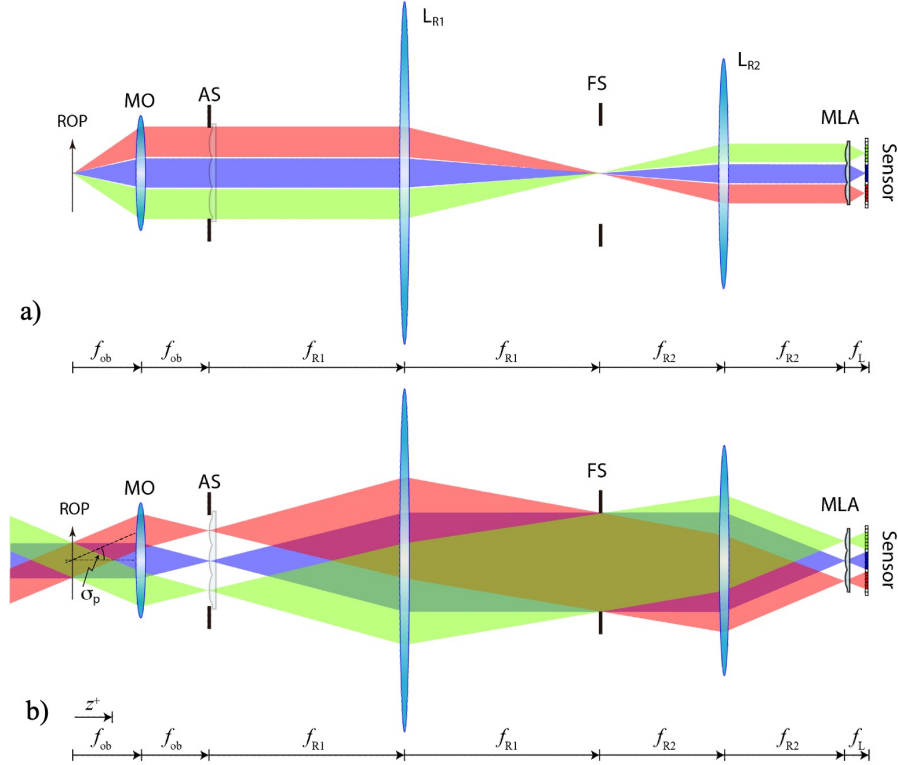


Fig. 1. Layout of the FLMic and ray tracing of light proceeding from the center of the ROP. (a) Aiming to make explicit the virtual insertion of the MLA at the AS, we have plotted a shaded MLA at the AS plane. (b) The lightbeams that pass through the optical centers of the microlenses are plotted. Axial coordinate, z , in the object space takes origin at the ROP.

112 In Fig. 1(b), it is illustrated the importance of the field stop and the orthographic nature of
 113 the EIs. The ROP, the field stop and the sensor are conjugated. The field stop plays the role of
 114 avoiding the overlapping between EIs. Then its diameter should fulfill the relation

$$\phi_{FS} = \frac{f_{R2}}{f_L} p. \quad (3)$$

115 Also interesting in the figure is the ray tracing in the object space. Since the ROP is set at
 116 the MO front FP, other parts of the sample are in front or behind that plane. The EIs of the
 117 ROP are identical, with no disparity. However, parts of the 3D sample in front of the ROP
 118 are captured with positive disparity, and parts behind with negative disparity. Interesting is that
 119 in the object space, the ray beams are collimated. This means that all the sections of the 3D
 120 sample are captured with the same magnification; in other words, all the EIs have an orthographic
 121 perspective. Any perspective is characterized by its parallax angle, which is an integer multiple of

$$\sigma_p = \frac{f_{R1}}{f_{R2} f_{ob}} p. \quad (4)$$

122 The higher the parallax angle, the better the captured 3D information.

123 Next, we revisit the basic equations that govern the FLMic image capture. First, the field of
 124 view (FOV) of captured EIs is

$$FOV_{EI} = \frac{1}{M_T} p. \quad (5)$$

125 where

$$M_T = \frac{f_L f_{R1}}{f_{ob} f_{R2}}. \quad (6)$$

126 is the lateral magnification between the ROP and the sensor.

127 The resolution limit of captured EIs is [34]

$$\rho_{EI} = \max \left\{ \frac{\lambda}{2NA_{ef}} + \frac{\delta}{M_T}, \frac{2\delta}{M_T} \right\} \quad (7)$$

128 where δ is the sensor pixel size. Note that ρ_{EI} is the minimum distance between resolvable points
 129 and is usually expressed in microns. However, since the resolution capability of optical systems
 130 is usually evaluated in terms of the USAF resolution chart, it is common to use the inverse of
 131 ρ_{EI} , which is usually expressed in line pairs per millimeter (lp/mm).

132 Finally, the depth of field of captured EIs is given by [23]

$$DoF_{EI} = \frac{\lambda}{NA_{ef}^2} + \frac{\delta}{NA_{ef} M_T}. \quad (8)$$

133 3. Depth Reconstruction

134 The use of FLMic aims to achieve any, or all, of the three following purposes. The first is using,
 135 directly, the captured EIs for composing a movie in which the sample is watched from different
 136 perspective angles. The second is the calculation of refocused images at different depths. Third
 137 is the computation of 3D point clouds. These three purposes are closely linked. For example,
 138 from accurate point clouds, it is possible to generate new perspective views, which than can be
 139 watched free of occlusions [35]. Behind these algorithms, there is a protocol that is based on
 140 shifting the EIs and compound their pixels. The primary refocusing algorithm, the one named
 141 as the shift and sum (S & S) algorithm, is the result of shifting and summing the pixels of the
 142 EIs [36]. This process is illustrated in Fig. 2. When all the EIs are stacked with no relative
 143 shifting between them ($n_s = 0$) and the pixel values are summed, the irradiance distribution at
 144 the ROP is rendered. In the general case, any EI is shifted out a number of pixels n_s with respect
 145 to its neighbor. There is a linear relation between the number of pixels of the relative shifting, n_s ,
 146 and the depth position, z_R , of the refocused plane. The relation is

$$z_R = \frac{n_s \delta_{rop}}{\sigma_p}, \quad (9)$$

147 with $-N < n_s < N$, being N the number of pixels contained, along a Cartesian direction, by any
 148 EI. Here δ_{rop} is the sensor pixel size as back-projected onto the ROP, $\delta_{rop} = \delta/M_T$ (δ being the
 149 actual pixel size) and $\delta = p/N$. As shown in Fig. 1(b), z_R takes its origin at the ROP and is
 150 positive for planes towards the MO.

151 A denser depth sampling can be obtained by simply resizing the EIs by an integer factor n , so
 152 that now the EIs have $N' = n.N$ pixels. This artificially makes the pixels smaller by a factor n ,
 153 $\delta' = \delta/n$, and therefore makes the depth refocusing denser in depth by the same factor. The main
 154 drawback of this is the increment in computation time [37].

155 Finally, to avoid obtaining refocused images with different sizes, all the computed images are
 156 cropped at the ROP image size (shown in yellow in Fig. 2). This is possible provided that the
 157 region of interest of the sample is just in front of the central EI.

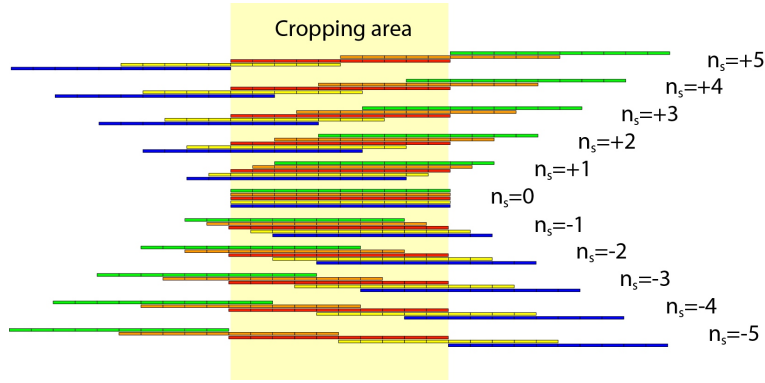


Fig. 2. Scheme of the shift & sum algorithm. Here we have represented a number of EIs (5 in this case) with a different colour each.

158 4. Setting up the FLMic

159 Aiming to build a FLMic in the laboratory, first one has to select its optical components according
 160 to the resolution, DoF, and FOV requirements. Also one should adapt to her/his stock of elements
 161 and to off-the-shelf ones. In our case, for example, the limiting element is the MLA, since
 162 we have only a few. For this experiment, we selected one with pitch $p = 1.0 \text{ mm}$ and focal
 163 length $f_L = 6.43 \text{ mm}$ (manufactured by Advanced Microoptic Systems GmbH). Making use of
 164 the software provided in [33], we selected the other elements: (a) An MO with magnification
 165 $M_{ob} = 20\times$ ($f_{ob} = 9.0 \text{ mm}$) and $\text{NA} = 0.40$; (b) A relay system composed by lenses of focal
 166 lengths $f_{R1} = 100 \text{ mm}$ and $f_{R2} = 50 \text{ mm}$; (c) An iris diaphragm with diameter $\phi_{FS} = 7.8 \text{ mm}$;
 167 and (d) A colour CMOS with pixel size $\delta = 2.2 \mu\text{m}$. With these elements, it is expected to
 168 capture EIs with $\rho_{EI} = 4.24 \mu\text{m}$, $\text{DoF} = 62.5 \mu\text{m}$, and $\text{FOV} = 699.8 \mu\text{m}$.

169 Then, one must follow the next steps, which are summarized in the video [Visualization 1](#). The
 170 lenses used must be set according to the optical conjugation requirements and NA matching. In
 171 this practical guide, the image of the shear plate and the images of light pointers being imaged by
 172 the image sensor are a confirmation procedure to find the optimal position of elements precisely
 173 and efficiently.

174 4.1. Setting up the collimated beam

175 First, we need to implement a collimated light, which is used for the alignment and adjustment of
 176 forthcoming elements. We use a converging lens that collects the light proceeding from a fiber
 177 coupled to a laser, or by an LED. Such a collimating lens (with focal length $f_C = 50 \text{ mm}$ in our
 178 case) provides the plane wave. It is checked with the help of a shear plate (see Fig. 3).

179 4.2. Setting up the MLA and the image sensor

180 Next, the MLA and the sensor should be set parallel to each other and perpendicular to the optical
 181 axis. To fix the distance between the MLA and the sensor accurately, the sensor position is tuned
 182 so that an array of light points is captured. This ensures that the sensor is at the MLA back FP
 183 (see Fig. 4).

184 4.3. Setting up the telecentric relay system

185 The telecentric relay is composed of three elements; lens $R2$, iris diaphragm, and lens $R1$, which
 186 should be set sequentially. The first element to set is lens $R2$. As shown in Fig. 5, the lens is set
 187 in the optical bench perpendicular to the parallel beam and centered in height. To make sure

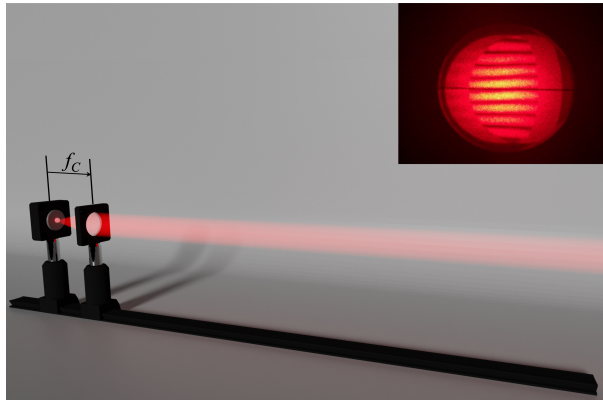


Fig. 3. Setting up the collimated beam.

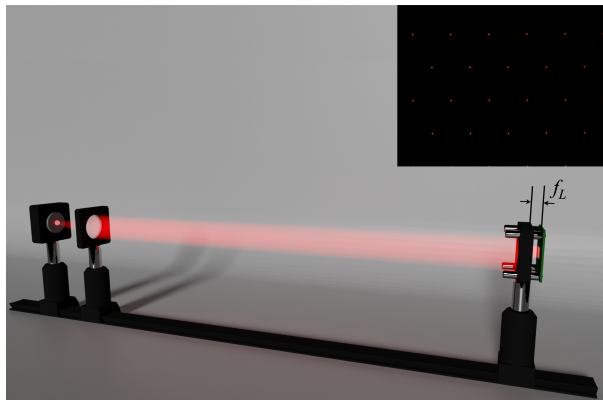


Fig. 4. Setting the MLA and the image sensor.

188 that the MLA is at the $R2$ back FP, the axial position of $R2$ is tuned till only one microlens is
 189 illuminated, which happens when the sensor records sharply a single hexagon.

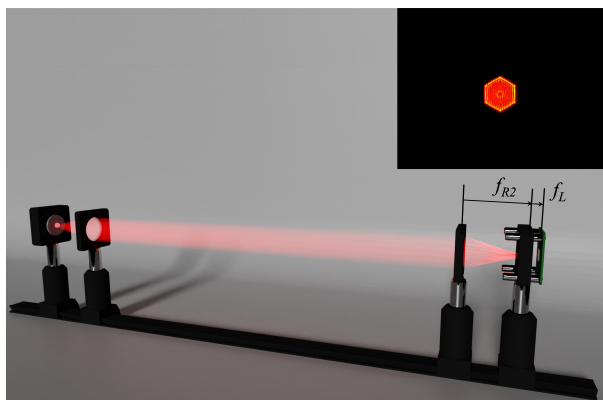


Fig. 5. Setting the lens $R2$.

190 The iris diaphragm, acting as a field stop, is an important element in the system since it helps

191 to avoid the overlapping between elemental images. It must be placed, properly centered, at the
192 front FP of $R2$. In that case, the iris and the sensor are on conjugate planes. To make this, the iris
193 is closed to a small diameter, and axially tuned till a sharp tiny circle is recorded (see Fig. 6).

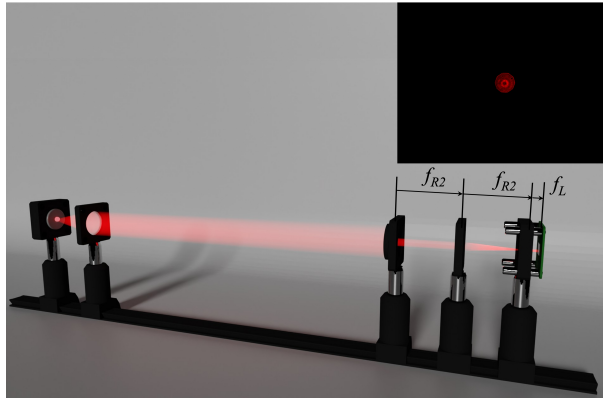


Fig. 6. Setting the iris.

194 Lens $R1$ must conform a telecentric relay together with $R2$. To ensure this, lens $R1$ should be
195 placed, properly centered, in the optical bench, and its axial position tuned till the array of light
196 spots is captured again by the sensor (see Fig. 7).

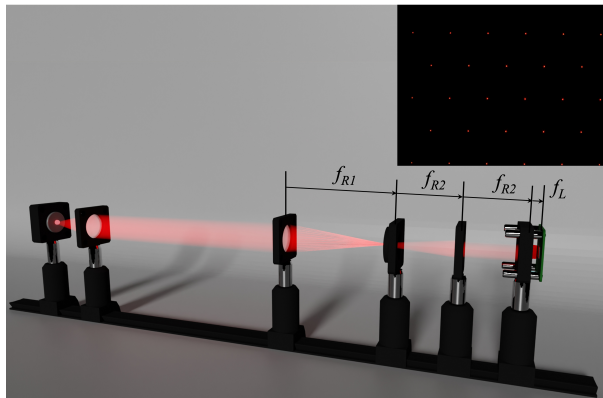


Fig. 7. Setting lens $R1$.

197 4.4. Setting up the microscope objective

198 The MO should be set telecentrically with lens $R1$. To ensure this, the MO should be placed,
199 properly centered, in the optical bench, and its axial position tuned till only one microlens is
200 illuminated, which happens again when the sensor records sharply a single hexagon (see Fig. 8).

201 4.5. Obtaining elemental images from the built FLMic.

202 Now one can record EIs after placing the sample on the front FP of the MO as shown in Figure
203 9. Similarly, it is possible to freely install the necessary light source in the illumination part
204 according to the sample requirement.

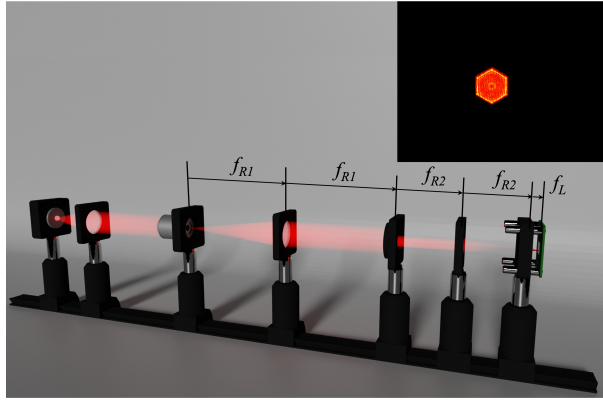


Fig. 8. Setting the MO.

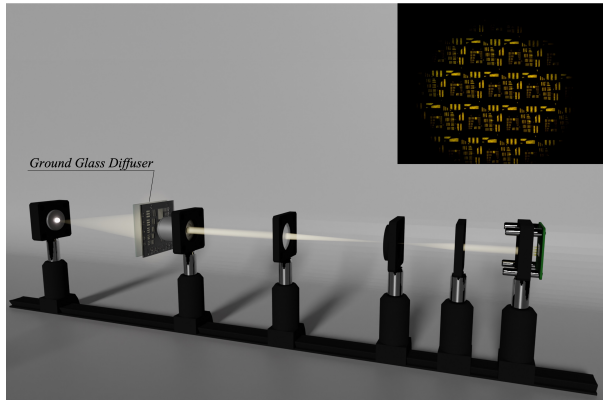


Fig. 9. Capturing the elemental images.

205 **5. FLMic Performance Results**

206 In order to verify the setup, one can evaluate the optical performance of the FLMic by using the
 207 system built following the previous section. According to the above formulae, the number of the
 208 EIs captured, along the horizontal direction, by our setup is $N_{EI} = 3.6$. Each EI has a circular
 209 shape with a diameter of 455 pixels.

210 **5.1. The spatial resolution of FLMic**

211 To confirm the spatial resolution of FLMic, we imaged the USAF 1951 target. Fig. 10(a) shows the
 212 captured raw images and it is also shown the central EI detailed in Fig. 10(b). The area visible in
 213 the selected image in Fig. 10(b) corresponds to Group 7 in the USAF target. Fig. 10 (c) shows the
 214 normalized profile of Group 7. It is possible to identify targets up to element 5 (E5), and through
 215 this, the highest spatial frequency of the USAF test calculated is 203 lp/mm ($\rho_{EI} = 4.9 \mu\text{m}$).
 216 From Eq. (7) the expected value of resolution is $\rho_{EI} = 4.24 \mu\text{m}$. In [Visualization 2](#) a video
 217 shows, sequentially, the captured EIs. From this video, it is apparent that each EI has captured a
 218 slightly different region of the USAF chart. This is because indeed the chart was not set exactly
 219 at the ROP but at some distance from it. Probably this is the reason for not having reached the
 220 expected resolution limit.

221 To confirm this, we applied the S & S algorithm and found that the USAF chart was reconstructed
 222 sharply only for a shift $n_S = -9$, corresponding to $z_R = -62.4 \mu\text{m}$. Fig. 11 shows the result of

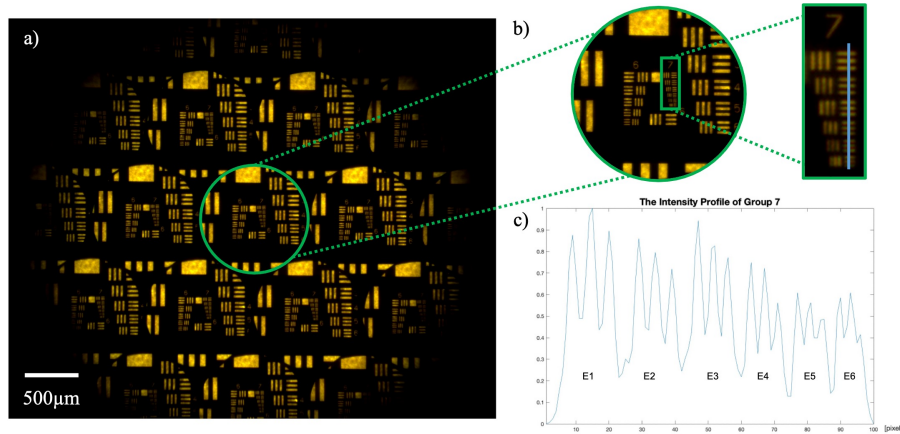


Fig. 10. The spatial resolution of Elemental images from FLMic system. (a) The captured raw elemental image of the USAF 1951 target (b) The central EI from raw image (c) The normalized profile along the blue line crossing Group 7.

223 the refocused image. Likewise, when checking Group 7 of the reconstructed image, it can be seen
 224 that the contrast is slightly reduced by the operation, but it still has the same spatial resolution as
 225 the captured EIs.

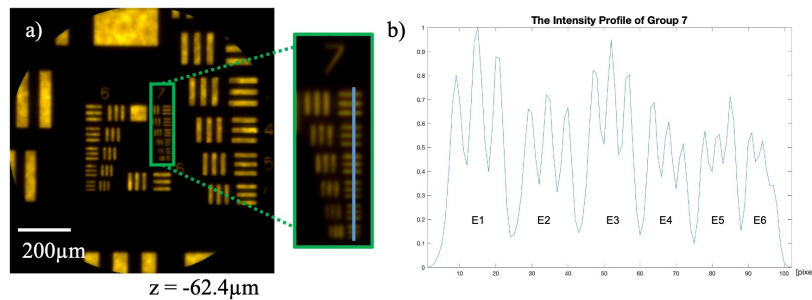


Fig. 11. The reconstruction result by using EIs of USAF 1951 test at the refocused plane $z_R = -62.4 \mu m$.

226 5.2. The depth Reconstruction of FLMic

227 To confirm the range of reconstructed depths in the same setup, we used a 3D bio-sample, which
 228 is a leg of a grasshopper. Fig. 12 (a) shows the captured EIs. Additionally, in [Visualization 3](#) a
 229 video shows, sequentially, the captured EIs. Again we used the S & S algorithm to reconstruct a
 230 3D image. Specifically, reconstructed images correspond to 10 refocused planes with a spacing
 231 of $6.9 \mu m$, see Fig. 12 (b). It can be seen that the DoF ranges from $z = -55.4 \mu m$ to $z = +6.9 \mu m$
 232 ($62.3 \mu m$ in total). In [Visualization 4](#) a video shows the computed depth images sequentially.

233 5.3. FLMic application with fluorescence sample

234 Next, as a second example, we used the FLMic to handle a fluorescent sample. Aiming to
 235 obtain more perspective images we have changed the MO (now $M_{ob} = 20\times$, $f_{ob} = 10.0 mm$
 236 and $NA = 0.50$) and the lenses of the relay so that $f_{R1} = 200 mm$, $f_{R2} = 100 mm$. With this

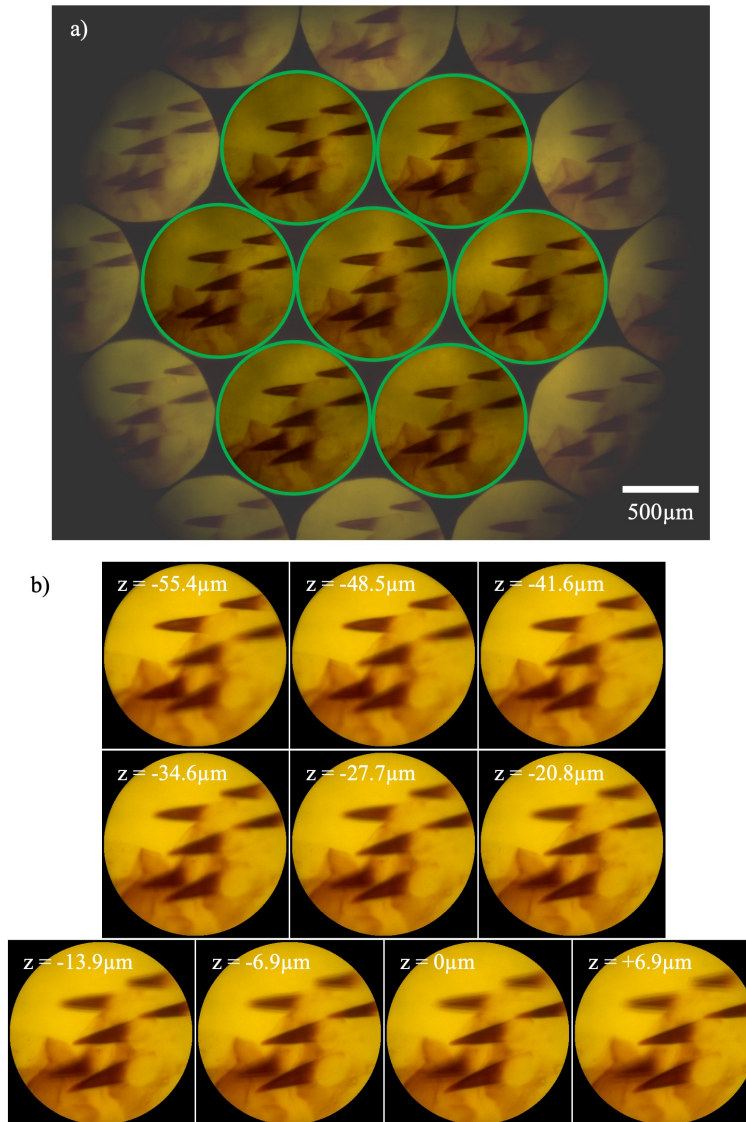


Fig. 12. (a) The captured raw elemental image of the 3D sample, leg of a grasshopper. (b) The reconstructed depth images.

237 new configuration, the expected figures about EIs are $N_{EI} = 5$, $\rho_{EI} = 4.7 \mu m$, $DoF = 77 \mu m$,
 238 and $FOV = 0.78 mm$. Again the EIs have a circular shape with a diameter of 455 pixels. In
 239 Fig. 13(a) we show the captured EIs, where the ones that we use for the depth reconstruction are
 240 enhanced. Also, in [Visualization 5](#) a video shows, sequentially, the captured EIs. This video
 241 makes apparent the high parallax achieved with the FLMic.

242 To calculate the depth refocused images, we used the (S & M) algorithm [18]. This algorithm
 243 is quite similar to the (S & S) one, but multiplying, instead of summing, the pixels of shifted EIs.
 244 When working with sparse fluorescent samples this algorithm is highly recommendable. The
 245 results obtained with this algorithm are shown in Fig. 13(b), where 11 depth images are shown.
 246 Finally, in [Visualization 6](#) a video shows the computed depth images sequentially. The depth
 247 images are reconstructed from $z = -68.4 \mu m$ to $z = +17.1 \mu m$ and those are a total of 11 planes

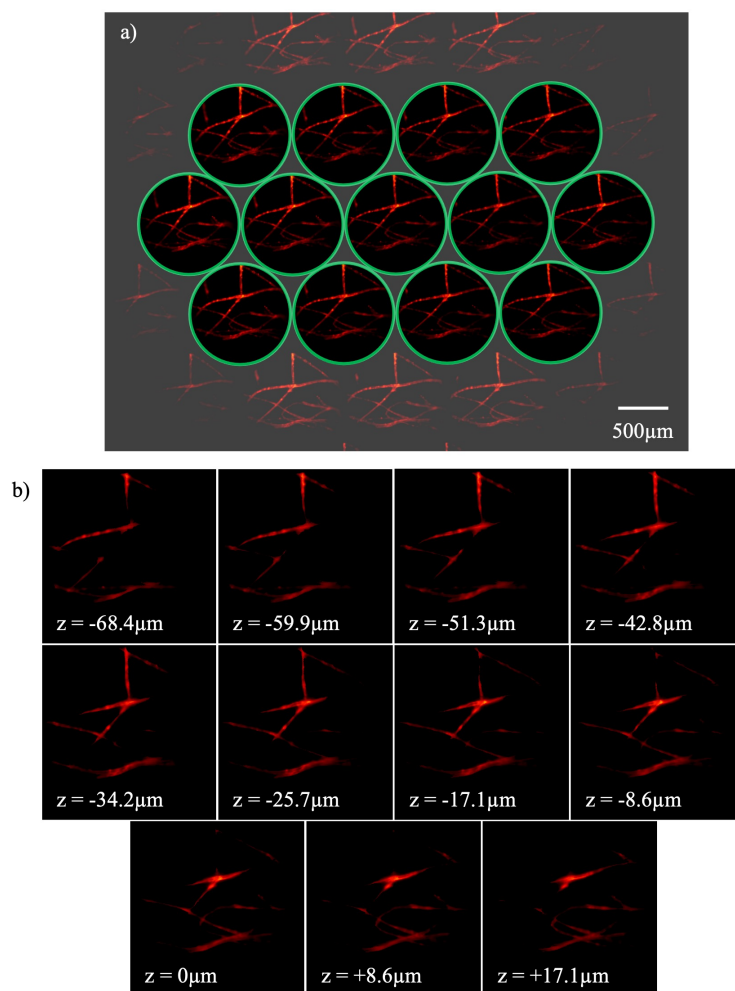


Fig. 13. FLMic with 3D fluorescence cotton fiber sample (a)The captured raw elemental image. (b)The reconstructed depth images.

248 constructed according to the spacing $8.6\mu m$.

249 6. Conclusion

250 This practical guide has provided a comprehensive overview of setting up the FLMic. We have
 251 covered FLMic's key concepts and techniques, including the optical feature of FLMic and the
 252 implementation process to meet the requirements. By following the step-by-step instructions
 253 provided in this guide, the reader will now have a solid understanding of how to face the accurate
 254 implementation of FLMic. Therefore, we hope that it has helped readers apply their newfound
 255 knowledge to their own work.

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259 **Disclosures.** The authors declare no conflicts of interest.

260 **Data Availability Statement.** The data presented in this study are contained within the article.

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