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Nanoindentation study of the mechanical and damage behaviour of suspension plasma sprayed TiO₂ coatings

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Abstract

TiO₂ coatings can be used as self-cleaning surfaces owing to their photocatalytic and

hydrophilic properties. Suspension plasma spray (SPS) has proven to be a feasible and

cheap technique for producing self-cleaning surfaces with acceptable photo-activity.

This paper presents a nanoindentation study of the mechanical properties (hardness,

Young's modulus and scratch resistance) of photoactive layers of suspension plasma

sprayed TiO₂ coatings applied on to glass substrates. Microstructure observation

showed that the rutile grains were surrounded by fine anatase crystals. Under the

same spraying conditions, the resulting anatase/rutile concentrations varied

depending on the cooling rate (the substrate being either cooled with water or in air).

The results showed that higher concentrations of anatase, which is softer than rutile,

reduced the scratch damage and increased the friction coefficient.

Keywords: Suspension Plasma Spray, Nanoindentation, TiO₂, Microstructure characterisation, Photocatalysis.

1. Introduction

TiO₂ semiconductors are used in solar cells, optical devices, and in photocatalytic reactors which references can find elsewhere [1-5]. The photocatalytic property is generated when TiO₂ is exposed to UV light, owing to its band gap centred between 3.0 eV and 3.2 eV, though this energy can be tuned to be sensitive to visible light by means of specific dopants [6, 7]. The liberated electrons previously excited by light radiation can reach the TiO₂ surface and then react with the organic matter deposited on the photoactive layers, degrading the organic molecules [8]. This degradation produces free active radicals, which can react or dissolve in water (in a solution configuration). In addition, activated TiO₂ is very hydrophilic and the contact angle of water is very low, creating a slippery surface. These properties make such materials highly appropriate to be employed as self-cleaning [9-11] surfaces. Other recent applications include wastewater treatment and disinfection [12, 13].

TiO₂ coatings can be produced by various techniques, such as atmospheric plasma spray, APS. APS is a particularly appropriate technique because a large area of TiO₂ can be easily deposited without any special requirements, such as vacuum pressures or reactive atmospheres [14-17]. In the APS technique, the material is fed in powder form into a high-energy flame and the melted particles are deposited on to the substrate, forming the coating. When very fine or nanometre-sized particles are sprayed, the material needs to be in the form of aggregates because the low acceleration of such very small masses is insufficient to allow them to reach the substrate. In the suspension plasma spray, SPS, used in this study, nanoparticle kinetic flight was improved by using a liquid carrier suspension containing the dispersed nanoparticles [18]. According to the literature [19-21], the SPS coatings obtained using nanopowder feedstock exhibit improved characteristics, because these coatings contain less porosity than APS and have a denser nanostructure. In recent studies on nanostructured TiO₂ coatings produced by SPS [17], photocatalytic activity was reported on observation of methylene blue degradation under UV radiation [23, 24].

TiO₂ can be found in amorphous, anatase, and rutile phases. Independently of the technique used to generate the TiO₂ coatings, high concentrations of anatase are required to obtain high ratios of photocatalytic activity [25, 26]. However, the compositional balance between these phases affects the mechanical properties of the coatings, making it necessary to find a compromise between optimal photocatalytic activity and good mechanical response. Lech Pawlowski *et al.* [27] conducted a nanoscratch study on sprayed TiO₂ coatings and examined the critical load required to generate coating failure on a substrate. Studies are unavailable in the literature, however, on the nanomechanical and tribological behaviour of such coating components.

The present study was undertaken to characterise the nanomechanical properties and damage resistance of suspension plasma sprayed TiO_2 coatings. The studied coatings were chosen from a series of suspension plasma sprayed TiO_2 coatings obtained in a previous work [28]. The following two coatings, which were sprayed under the same conditions, were chosen: the first was applied on to a substrate cooled in air, which gave rise to a homogenous anatase-rutile phase distribution; the second was applied on to a substrate cooled with water, which yielded a segregated anatase-rutile phase distribution. Nanoindentation tests were then performed on these coatings: the results from the scratch tests were correlated with the hardness (H) and Young's modulus (E) of the phase distribution. The constituent microstructures and phases were observed using a field-emission scanning electron microscope (FE-SEM).

2. Experimental Conditions

2.1. Materials and coatings preparation

 TiO_2 supplied by Evonik Industries under reference Aerodisp W 740 X was used in an aqueous suspension at 40 wt%. Aggregates smaller than 100nm made up of 20-30 nm nanoparticles of 90 wt% anatase + 10 wt% rutile provided the suspension with a viscosity below 1000 mPaS and a density of 1.41 g/cm³.

The coatings were deposited using a F4-MB monocathode torch (Sulzer Metco, Wolhen Switzerland) with a 6 mm internal diameter anode. The substrates were preheated at 300 °C to enhance coating adhesion.

Suspension injection was performed through a calibrated diaphragm of 150 μ m diameter. The plasma gas was a mixture of He and Ar with flow rates of 10 I/min and 50 I/min, respectively. Arc intensity was kept constant at 400 A. The surfaces of the deposited material were cooled either by spraying water (8 mls^{-1}) or by spontaneous cooling along the projection procedure.

Pyrex glass specimens in the form of 25 mm diameter disks were used as substrates. The substrates were cleaned with ethanol and dried in air prior to coating deposition. After deposition, cross-sections of the resulting specimens were polished down to 0.25 μ m abrasives. Surface roughness, measured by a standard surface roughness tester, was $Ra = 1.1 \pm 0.2 \mu$ m for the coatings obtained under both types of cooling conditions. Further details on the photoactivity behaviour and composition characterization by Raman microprobe analysis on the cross-sections are given in a previous paper [28].

2.2 Sample characterisation procedure

An Agilent G-200 nanoindenter was used to analyse the H and E of the resultant polished coating cross-sections with a calibrated Berkovich indenter. The indentations were performed at constant depth mode. The stiffness used for the H and E calculation was obtained by continuous stiffness measurement [29, 31] CSM, in the 45-50 nm average depth range. The scratch tests were conducted with the same apparatus, using a lateral force sensing module and a spherical sapphire indenter with a 100 μ m diameter. The scratches were made on the sample surface applying a dynamic load from 0 mN to 100 mN along a 100 μ m distance. Cross-section microstructure and wear tracks were observed using a HITACHI S-4100 field-emission scanning electron microscope (FE-SEM).

3. Results and discussion

Figure 1 shows the cross-section FE-SEM images of the two types of coatings. These images show that the thicknesses reached were between the 30 μm to 40 μm. Figs. 1a and 1b, the latter being at higher magnification, show that the coatings cooled in air exhibited a microstructure made up of (*I*) harder and larger grains surrounded by (*II*) softer and smaller grains. These morphologies were well characterised by Raman microprobe analysis in a previous work [28] and correspond to rutile and anatase TiO₂ phases, respectively. Fig. 1b shows that the coating consisted of dense material without measurable porosity. Hereafter, this specimen is designated *A+R* (*Anatase + Rutile on surface*). In contrast, the water-cooled samples (Fig. 1c) displayed a phase distribution in the form of a bi-layer structure. A great rutile grain concentration was found at the substrate surface, while the anatase microstructure lay at the coating outer surface. Hereafter, this specimen is designated *A* (*only Anatase on surface*).

This bi-layer structure may be explained as follows: the high temperature reached in the flame (3000-8000 K) melted all sprayed material. Subsequent fast cooling caused a significant amount of particles to crystallise as anatase phase, despite the rutile transformation occurs at 700-800 °C. In previous studies [32, 33] this transformation was reported when the TiO₂ suspension was sprayed directly into water, producing a high TiO₂ content in the form of anatase. However, the material sprayed close to the substrate was transformed into rutile owing to the higher temperature of the substrate and the subsequently deposited hot material. A previous study [28] confirmed this double-layer structure of anatase-rutile, independently of whether steel or glass was used as substrate material.

The H and E features of the observed microstructures were analysed by means of a square grid of 300 nanoindentation tests on the sample cross-section with homogeneously distributed anatase and rutile (A + R specimen). The distance between each imprint was programmed to be 1 μ m. This sample was chosen because of the more homogeneous anatase and rutile distribution throughout the coating. The distribution of the mechanical properties was then represented by histogram distributions and surface mappings in which each H and E result was plotted on the

axis coordinates with the same dimensions and locations as in the tested area. The distribution of the H and E results at 40-50 nm depth, is shown in Figure 2. As this type of plot depends to a great extent on the choice of bin size, the distributions were also plotted by the normal probability distributions acquired previously by fitting the cumulative results. This procedure has been described previously in similar studies [34, 35]. The H distribution clearly showed two main values centred at 8.5 GPa and 16.5 GPa. These results are close to those reported for TiO_2 anatase and rutile respectively [36]. The E histogram was difficult to deconvulate owing to the similar E values expected for both phases and their greater elastic stress field beneath the indenter [37]. The E and E maps acquired on the E sample are shown in Figure 3. The foregoing results confirm that the microstructure of the larger grains, which consisted of rutile, displayed the harder behaviour. These grains were surrounded by the anatase matrix that, though retaining its initial nanostructure, was the softer phase.

In order to compare the tribological properties of the A and A + R specimen surfaces, scratch tests were performed on those surfaces. FE-SEM images of the tracks produced under the test conditions used are shown in Figure 4. The maximum load attained corresponded to the bottom of the wear track, the experiment starting at zero load at the top. The friction force (F_{μ}) and coefficient of friction (μ) recorded during the scratch tests are plotted in Figure 5. The linear behaviour of F_{μ} under the test conditions used assured that no critical load was reached. The increase in friction when scratch load rose agreed with Nosonovsky and Bhushan's observation [38, 39] that is, at small contact sizes, μ increased when contact size and the applied load rose.

The recorded μ at the experimented conditions was higher on the A specimen surface, resulting an average value of μ = 0.7, compared with μ = 0.3 on the A+R surface. This behaviour may be explained by the theory of multi-asperity contacts put forward by Zhang et~al. [40, 41]. According to this theory, when two surfaces are in contact, a part of the load is distributed on the contact area of the asperities and/or on the contact area of debris particles. Thus, the resultant μ consists of the sum of three components: adhesion (1- $\beta)\mu_{adhesion}$, asperity ploughing $\beta\mu_{asperity}$, and debris ploughing μ_{debris} . The ' β ' coefficient is a value that depends on surface roughness. The spherical indenter used in this study assured that multiple-asperity contact conditions were in place, in which

there was a mechanical interlocking between the contacting surfaces, despite the low applied loads.

The main friction component on the A specimen was $(1-\beta)\mu_{adhesion}$. This was justified by observing the slide pattern, in which no evidence of asperity or debris ploughing was found. The wear track is shown at higher magnifications in the FE-SEM images of Figure 6. On the specimen A wear track (Fig. 6a), several transverse lines crossing the slide pattern as a plastic/adhesive wear mechanism may be observed, which explains the higher recorded friction.

On the other hand, Fig. 6b shows that a number of particles were pulled out of the A + R specimen. This was probably the result of small clusters of rutile particles detaching from the anatase matrix when the cohesion of the plastically deformed matrix failed. It may, further, be observed that the asperities were levelled inside the wear track: the inter-asperity voids were presumably (i) filled with the pushed material and (ii) reduced by a polishing effect. These assumptions would corroborate the main friction components on the A + R specimen surface being the sum of $\mu_{asperity}$ and μ_{debris} . In any event, the friction components produced a lower friction than that found on specimen A, owing to coating adhesion.

Plots of penetration depth versus load along the scratch are shown in Figure 7. The penetration curves were automatically calculated by subtracting the original morphology from the scratch and residual profile data using the nanoindenter Testworks^(R) software. The penetration curves exhibited a resultant track depth of 3 μ m and 4 μ m at maximum scratch load for the A and A + R specimens, respectively. These results indicate that the damage observed on the A + R specimen was greater than that on the A specimen. The generation of wear debris particles, visible as bright spots at higher magnifications in Figure 8, probably produced the arising damage as a result of a polishing mechanism of the surface asperity.

Archanta *et al.* [42, 43] reported that, in this type of tribosystem, wear particles continued to form during the subsequent sliding test cycles, some of those particles agglomerating and being pulled out from the wear track as large wear particles. In the present study, the rutile grains were expected to act as abrasive material or as a tribo-

layer, but no evidence was found in this regard. Several cyclical scratch experiments at constant load would reveal the wear mechanism that occurred under these test conditions and further research is needed on this issue.

The above findings show that the damage resistance and friction behaviour of the studied TiO_2 layers depended on how the microstructures were distributed in the coating surface. Although the resultant hardness of the A+R coating was higher than that of the A specimen surface, the tribological properties displayed different behaviour owing to the nature of the slide and wear mechanism. In photocatalytic applications, high anatase content is essential to reach the required photocatalytic activity. This scenario needs to be taken into account when photoactive surfaces are deposited, independently of the technique involved, because a comprise needs to be found between the mechanical and the photocatalytic properties by controlling the microstructure and phases contained in the layers.

Conclusions

In this study, suspension plasma sprayed TiO₂ coatings, which were cooled either in air or with water, exhibited a homogeneous anatase and rutile phase distribution or recrystallised anatase on surface, respectively. Under the plasma spray test conditions used, all the feedstock melted, temperatures being reached above that at which the material undergoes rutile transformation. However, depending on the cooling rate, the melted material was also able to re-crystallise into anatase, this being the case with the coating obtained on the water-cooled substrate.

The nanoindentation technique proved to be a useful method of characterising the arising phases, which consisted of anatase nano-crystals and rutile micro particles that displayed a hardness of 8.5 GPa and 16.5 GPa, respectively. The nanoscratch experiments confirmed that coatings with uniformly distributed rutile exhibited lower scratch resistance than the coatings with re-crystallised anatase, owing to the abrasive behaviour of the harder rutile phase. The higher friction coefficient obtained on the anatase surface $(\mu=0.7)$ compared with that obtained on the anatase + rutile surface

 $(\mu=0.3)$ also needs to be taken into account. The spherical indenter used in the scratch tests could be suitably used in further wear research because the linearity of the friction behaviour assures detection of any cohesive or adhesive failure.

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