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1 **PREDICTING STRAND TRANSFER LENGTH IN PRETENSIONED**
2 **CONCRETE: EUROCODE VERSUS NORTH AMERICAN PRACTICE**

3 José R. Martí-Vargas¹, and W. Micah Hale, M.ASCE²

4 **Abstract**

5 Prestressing strands are commonly used in pretensioned prestressed concrete bridges
6 construction. Transfer length is an important parameter for structural design. This paper
7 presents a comparative study on strand transfer length provisions from Eurocode-2 and North
8 American practice, and identifies similarities and differences between both models. A
9 database of measured transfer lengths according to several authors has been compiled and
10 compared with predictions according to code provisions. The intervals of predictions are
11 smaller than those corresponding to the experimental results, and they are smaller when code
12 provisions are more simplified: the interval from Eurocode-2 is greater than that from ACI-
13 318 which, in turn, is greater than the interval from AASHTO. The number of underestimated
14 cases is lower for Eurocode-2 because of the higher predicted values, but situations in which a
15 short transfer length is unfavorable are neglected by all models because they are not good
16 predictions of shorter measured transfer lengths. When a transfer length estimation criterion is
17 based on an allowable free end slip, more cases are excluded from the ACI-318 provisions.

18 **CE Database subject headings:** Bridge; Prestressed concrete; Bonding; Effective stress

19 **Author keywords:** Bridge; Concrete; Strand; Bond; Prestress; Transfer length; Transmission
20 length

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21 **Introduction**

22 The use of prestressing strands is commonplace in the construction of pretensioned concrete
23 structures and bridges. There are two procedures for prestressing a concrete member through
24 strands: post-tensioning and pre-tensioning. The manufacturing process for pretensioned
25 concrete members by pre-tensioning includes: tensioning the prestressing strands between
26 abutments using provisional end anchorages; casting concrete around the prestressing strands;
27 releasing the strand tension once the concrete achieves sufficient strength thereby transferring
28 the prestress force to the member. The prestressing force in the strands is transferred to the
29 concrete by bond in the end regions of the member. In each end region, the stress in the
30 prestressing strand varies from zero at the end of the member to a constant maximum value
31 (effective stress), which is achieved at a certain distance from the member end. Fig. 1 offers
32 an idealization of the prestressing strand stress profile in a pretensioned prestressed member
33 after prestress transfer.

34 According to ACI-318 –ACI: American Concrete Institute– (ACI 2011), the distance over
35 which the strand should be bonded to the concrete to develop the effective prestress in the
36 prestressing strand is defined as transfer length. Eurocode-2 calls this length transmission
37 length (CEN 2004 –CEN: Committee European of Normalization–).

38 Transfer length is an important parameter for pretensioned concrete structural design (Russell
39 and Burns 1996; Barnes et al. 2003). In the precast prestressed concrete industry, obtaining a
40 good product within a short period of time is essential. Therefore, it is necessary to achieve
41 the required concrete compressive strength as soon as possible so that the member can accept
42 the transfer of the prestressing force at detensioning, and the member can be removed from
43 the bed. The accuracy of any attempt to check the actual material stresses in the end region of
44 pretensioned members depends upon the transfer length estimation. In addition, transfer
45 length represents the first portion of the development length (in ACI-318; anchorage length in

46 Eurocode-2) over which the prestressing strand should be bonded so that a stress in the
47 prestressing strand at nominal strength of the member, f_{ps} , may develop.

48 Consequently, it is necessary to contemplate some implications for bridge designs according
49 to strand transfer length:

50 a) A short transfer length increases stresses and the risk of cracking (by concrete splitting,
51 bursting or spalling) in the end regions. This may result in complete bond loss, especially if
52 there is no confining reinforcement (den Uijl 1995). In these cases, it is possible to
53 redevelop effective prestressing force by bond at a distance from the damaged location
54 (Kasan and Harries 2011).

55 b) A long transfer length reduces the available member length to resist bending moment and
56 shear, and therefore increases member cost.

57 Moreover, design strength provided by a pretensioned member shall be taken as the nominal
58 strength multiplied by the strength reduction factors in sections within the transfer length
59 (also within the development length). If a critical section occurs within these regions -where
60 the strand is not fully developed- failure may occur by bond slip (ACI 2011). Thus, web shear
61 cracks, which extend into the transfer length, can cause a bond-slip failure of the prestressing
62 strands (Reed and Peterman 2004).

63 Strand transfer length depends on the properties of both the prestressing strand and the
64 surrounding concrete, and also on several design and manufacture parameters (FIB 2000 –
65 FIB: International Federation for Structural Concrete–; PCI 2011 –PCI: Precast/Prestressed
66 Concrete Institute–). Some of the most important properties and parameters are: concrete
67 strength at the time of detensioning, level of prestress force at detensioning, concrete cover,
68 strand spacing, size of the cross-section, type of strand, strand diameter, strand surface
69 condition (clean, oiled, rusted, epoxy-coated), detensioning method (sudden, gradual),

70 confining reinforcement around the strand, concrete consolidation around strands, time-
71 dependent effects, and vertical strand location in the concrete section.

72 There is also no consensus as to the main parameters to be considered in the models and
73 equations predicting transfer length (Martí-Vargas et al. 2007a, 2012b). A perfect example of
74 this is the case of the North American practice [ACI-318 (ACI 2011); AASHTO LRFD BDS
75 –American Association of State Highway and Transportation Officials, Load and Resistance
76 Factor Design, Bridge Design Specifications– (AASHTO 2012)] and Eurocode-2 (CEN
77 2004): provisions for transfer length are not a function of concrete strength in ACI-318 and
78 AASHTO LRFD BDS, while Eurocode-2 provisions include concrete properties.

79 This paper presents the findings of a research project that examined the differences in
80 predicted transfer length when using the Eurocode-2 and codes typically used in North
81 America. A carefully selected database spanning a variety of experimental transfer length
82 results has been compiled. Based on the data collected, strand transfer length predictions
83 based on different provisions have been examined.

84

85 **Background: transfer bond model and strand stress changes**

86 For prestressing strands, there are three bond mechanisms (FIB 2000): adhesion, friction and
87 mechanical action. A very small slip destroys adhesion. Then activation of the friction
88 mechanism and mechanical action takes place, while radial compressive stresses around the
89 prestressing strand causes bond stresses due to the prestress transfer. These radial
90 compressive stresses are the response of the surrounding concrete to both the strand diameter
91 increase and the displacement of the prestressing strand when a slip occurs. Mechanical action
92 in prestressing strands notably differs from that in wires because their helical shape allows for
93 increased bond stress when a greater slip occurs. As consequence, the longitudinal contraction

94 of the prestressing strand results in a radial expansion of the tendon which is known as the
95 Hoyer Effect (FIB 2000; Barnes et al. 2003).

96 Janney (1954) was one of the pioneers to research bond characterization and its relation with
97 the transfer length of prestressing strands. The results obtained by Janney (1954) showed an
98 inelastic response of the surrounding concrete with radial microcracking along almost the
99 entire transfer length. On the other hand, according to Guyon (1953), the hypothesis of
100 uniform bond stress distribution is an unattainable limit since there will always be a zone
101 exhibiting elastic behavior along the transfer length. An analytical transfer bond model that
102 considers both a longer plastic zone and a smaller elastic zone located at the end of the
103 transfer length was proposed by Cousins et al. (1990). However, several authors have reported
104 a plastic response along almost the entire strand transfer length (Janney 1954; Barnes et al.
105 2003; Martí-Vargas et al. 2007a). Consequently, authors and codes such as Eurocode-2 and
106 ACI-318 generally assume bond models by considering uniform bond stress distribution
107 (linear variation of the prestressing stress; see Fig. 1) along the transfer length.

108 In order for equilibrium to occur, the prestressing strand force must be equal to the force
109 developed in the prestressing strand over the transfer length by assuming the uniform bond
110 stress according to Eq. (1):

$$111 \quad f_s A_p = L_t P_p U_t \quad (1)$$

112 where f_s is the effective stress (strand stress after transfer), A_p is the cross-sectional area of the
113 prestressing strand, L_t is transfer length, P_p is the perimeter of the prestressing strand, and U_t
114 is the average bond stress along the transfer length.

115 Based on Eq. (1), researchers have proposed several equations to predict transfer length based
116 on experimental results and theoretical studies. Normally, regression analyses and statistical
117 models provide descriptions of the effects of the aforementioned properties and parameters on
118 transfer length (Martí-Vargas et al. 2006b; García-Taengua et al. 2011). The majority of these

119 equations predicting transfer length take a parametric form in accordance with the structure of
120 Eq. (2) (Martí-Vargas et al. 2007a):

$$121 \quad L_t = \left[\left(\frac{f_{sx}^n A_p}{(k_1 \pi d) U_t} + k_2 \right) \cdot \chi \right] \cdot \lambda \quad (2)$$

122 where (only an additional notation) f_{sx} is the prestressing strand stress, n is an exponent, k_1 is
123 the perimeter factor ($k_1 = 4/3$ for a seven-wire strand, $k_1 = 1$ for a circular cross-section), d is
124 the nominal diameter of the prestressing strand, k_2 is an adjustment constant, χ is a factor to
125 account for the type of release, and λ is a factor to obtain bound values for transfer length.

126 Wan et al. (2002a) proposed the application of a top bar effect factor, and Martí-Vargas et al.
127 (2012a) reported the effects of concrete composition on bond stress. An additional factor, ζ ,
128 for transfer length models has been proposed to account for time-dependent increases in
129 transfer length (Caro et al. 2012) based on strand stress changes relating to the manufacturing
130 process of pretensioned prestressed concrete members, as follows: a) strands are tensioned in
131 a casting bed from zero to $f_{s,jack}$ –strand stress at jacking–, which decreases to $f_{s,bed}$ –strand
132 stress at anchoring– by seating at provisional strands anchoring; b) the concrete member is
133 cast around the strands, and $f_{s,bed}$ diminishes to f_{s0} –strand stress just before prestress transfer–
134 because of strand relaxation losses; c) at release, strands shorten and the surrounding concrete
135 shortens with them: prestress losses due to concrete elastic shortening range from f_{s0} to f_{si} –
136 initial effective stress, just after prestress transfer– occur in the central zone of the member
137 (see Fig. 1); and d) several time-dependent prestress losses gradually occur by concrete creep
138 and shrinkage and strand relaxation and, consequently, effective stress changes from f_{si} to a
139 final value f_{se} –effective stress after allowing for all prestress losses–.

140

141 **Code provisions for transfer length**

142

143 ***Eurocode-2***

144 According to Eurocode-2 (Section 8.10.2, CEN 2004), the prestress may be assumed to be
145 transferred to the concrete by a constant bond stress f_{bpt} , as follows:

146
$$f_{bpt} = \eta_{pl} \eta_1 f_{ctd}(t) \quad (3)$$

147 where η_{pl} is a coefficient that takes into account the type of tendon and the bond situation at
148 release (3.2 for 3- and 7-wire strands), η_1 accounts for the tendon position during casting (1.0
149 for good bond conditions, and 0.7 otherwise), and $f_{ctd}(t)$ is the design value of strength at time
150 of release.

151 The basic transmission (transfer) length (l_{pt}) value is given by:

152
$$l_{pt} = \alpha_1 \alpha_2 \phi \sigma_{pm0} / f_{bpt} \quad (4)$$

153 where α_1 accounts for the release procedure (1.00 for gradual release, 1.25 for sudden
154 release), α_2 is a tendon area factor (0.25 for tendons with circular cross-sections, 0.19 for 3-
155 and for 7-wire strands), ϕ is the nominal tendon diameter, and σ_{pm0} is the tendon stress just
156 after release.

157 The transfer length should be taken as the less favorable of two values (l_{pt1} , l_{pt2}), depending on
158 the design situation:

159
$$l_{pt1} = 0.8l_{pt} \quad (5)$$

160
$$l_{pt2} = 1.2l_{pt} \quad (6)$$

161 Normally, the lower value is used to verify local stresses at prestress transfer, whereas the
162 higher value is for ultimate limit states.

163 The upper design value of transfer length is within the anchorage length. Fig. 2 illustrates the
164 strand stresses according to the Eurocode-2 transfer length model.

165 This model coincides with Model Code 2010 –MC-2010- (FIB 2010) which also provides two
166 values for transfer length. However, both models differ in relation to the obtained bound
167 values, as follows:

- 168 • in the Eurocode-2 model, Eq. (4) initially computes a mean transfer length value, and Eq.
169 (5) and Eq. (6) produces the lower bound and upper bound values, respectively; the
170 upper/lower ratio is $1.2/0.8 = 1.5$.
- 171 • in the MC-2010 transfer length model, the action effect that needs verifying in the design
172 is considered by a factor α_{p2} ($\alpha_{p2} = 1$ to calculate anchorage length when considering
173 moment and shear capacity; $\alpha_{p2} = 0.5$ to verify the transverse stress in anchorage zone);
174 the upper/lower ratio is $1/0.5 = 2$. With a non-specified value of $\alpha_{p2} = 0.75$ (by averaging
175 the established values $\alpha_{p2} = 1$ and $\alpha_{p2} = 0.5$), corresponding to a mean transfer length
176 value, the calculation of the transfer lengths from MC-2010 and Eurocode-2 coincides.

177

178 **ACI-318**

179 Current ACI-318 provisions on transfer length first appeared in ACI Code 318–63 (ACI
180 1963) and derive from Eq. (1) using (Tabatabai and Dickson 1993): $f_s = f_{se}$; $A_p = 0.725\pi d^2/4$;
181 $P_p = 4\pi d/3$; and $U_t = 400$ psi (2.76 MPa), resulting in (ACI-318, Section 12.9, the first part of
182 Eq. 12-4):

$$183 \quad L_t = \frac{f_{se} d_b}{3000} \quad (f_{se} \text{ in psi}) \quad (7a)$$

$$184 \quad L_t = \frac{f_{se} d_b}{20.7} \quad (f_{se} \text{ in MPa}) \quad (7b)$$

185 where f_{se} is the effective stress in the prestressing strand after allowing for all prestress losses,
186 and d_b is the nominal diameter of the prestressing strand.

187 According to the ACI Code 318-63 (ACI 1963) Commentary, it is worth noting that this
188 relationship estimates average transfer length. This equation remains to date in ACI Code
189 318-11 (ACI 2011) in spite of a considerable number of proposed modifications (Floyd et al.
190 2011). In addition, several authors consider that the use of the term f_{si} in Eq. (7a-7b) rather
191 than f_{se} for design purposes is more rational as transfer length is established at the release of
192 prestress (Shahawy et al. 1992; Deatherage et al. 1994).

193 As a reasonable limit for the higher transfer length values, Russell and Burns (1996)
194 recommended Eq. (8a-8b) for design applications:

$$195 \quad L_t = \frac{f_{se} d_b}{2000} \quad (f_{se} \text{ in psi}) \quad (8a)$$

$$196 \quad L_t = \frac{f_{se} d_b}{13.8} \quad (f_{se} \text{ in MPa}) \quad (8b)$$

197 Fig. 3 shows the relationship between strand stress and the distance over which the strand is
198 bonded to the concrete, as represented by Eq. (7a-7b). Fig. 3 includes the effects of
199 considering f_{si} rather than f_{se} , and of predicting transfer length by Eq. (8a-8b), which implies
200 $U_t = 267$ psi (1.84 MPa).

201 On the other hand, the transfer length requirement mentioned in the ACI-318 shear provisions
202 (Section 11.3.4) is 50 strand diameters, while the transfer length may be taken as 60 strand
203 diameters according to AASHTO LRFD BDS (AASHTO 2012) provisions for prestressing
204 strand development (Section 5.11.4.1).

205

206 ***Allowable free end strand slip***

207 Variation in strand stress along the transfer length at prestress transfer involves slips between
208 the strand and the surrounding concrete. It is possible to use these slips as an indirect method
209 to estimate transfer length (Martí-Vargas et al. 2007b). Anderson and Anderson (1976) used
210 this method as a simple non-destructive assurance procedure to monitor bond quality within

211 precasting plants. Guyon (1953) proposed the following equation for uniform bond stress
 212 distribution:

$$213 \quad L_t = 2 \frac{\delta E_p}{f_{s0}} \quad (9)$$

214 where δ is the strand end slip, E_p is the strand modulus of elasticity, and f_{s0} is the strand stress
 215 immediately before prestress transfer.

216 Several authors (Anderson and Anderson 1976; Petrou et al. 2000; Wan et al. 2002b) have
 217 established an allowable free end slip ($\delta_{allowable}$), which results in a transfer length equal to that
 218 computed by the ACI-318 provisions for transfer length. By setting Eq. (9) to be equal to Eq.
 219 (7a-7b), the implied allowable end slip value by Eq. (10a-10b) is:

$$220 \quad \delta_{allowable} = \frac{1}{6000} \frac{f_{s0}}{E_p} f_{se} d_b \text{ (Customary units)} \quad (10a)$$

$$221 \quad \delta_{allowable} = \frac{1}{41.4} \frac{f_{s0}}{E_p} f_{se} d_b \text{ (SI units)} \quad (10b)$$

222 It is possible to extend Eq. (9) by setting it to equal Eq. (4) by considering the Eurocode-2
 223 provisions, as follows:

$$224 \quad \delta_{allowable} = \frac{1}{2} \frac{f_{s0}}{E_p} \alpha_1 \alpha_2 \phi \sigma_{pm0} / f_{bpt} \text{ (SI units)} \quad (11)$$

225

226 **Eurocode-2 versus North American practice**

227 There are similarities between the Eurocode-2 (CEN 2004) and ACI-318 (ACI 2011)
 228 provisions for transfer length: a) both models consider uniform bond stress; b) transfer length
 229 depends directly on the nominal strand diameter -also in AASHTO LRFD BDS (AASHTO
 230 2012)-; and c) the effective stress after allowing for all prestress losses (f_{se} in ACI-318, $\sigma_{p\infty}$ in
 231 Eurocode-2) is the maximum strand stress considered along the transfer length to calculate
 232 development length. Table 1 summarizes the differences between both models.

233

234 ***Influence of concrete strength***

235 Fig. 4 presents the predicted transfer length values of several prestressing strand nominal
236 diameters. Eq. (4), Eq. (7a-7b) and the AASHTO LRFD BDS (AASHTO 2012) provisions
237 provide these lengths. In order to calculate transfer length, the following relationships have
238 been used: $f_{s0} = 0.75f_{pu}$ [f_{pu} : nominal strand strength; $f_{pu} = 1860$ MPa (270 ksi)], $f_{si} = 0.9f_{s0}$,
239 and $f_{se} = 0.8f_{s0}$. Since the Eurocode-2 includes the effects of concrete strength, specified
240 concrete compressive strengths of 50 MPa (7.25 ksi) and 100 MPa (14.50 ksi) at 28 days of
241 age were used for comparison.

242 As seen in Fig. 4, transfer length decreases when concrete strength increases for the lengths
243 predicted from Eurocode-2. The simplified model from AASHTO LRFD BDS provides
244 higher transfer length values than the ACI-318 provisions. Similar transfer length values were
245 obtained from the ACI-318 and Eurocode-2 when using a specified concrete compressive
246 strength at 28 days equal to 100 MPa (14.50 ksi).

247

248 ***Data provided from tests***

249 The transfer length may be determined experimentally, and over the years, there have been
250 several experimental research programs examining the bond of prestressing strands (by way
251 of example, see references included in Table 2). There are several experimental methods
252 frequently used to determine transfer length: the longitudinal concrete surface strain profile
253 (Russell and Burns 1997), the prestressing strand end slip (Guyon 1953), the bond strength
254 determination by push-pullout test (Hegger et al. 2007), and the prestressing strand force at
255 several cross-sections (Martí-Vargas et al. 2006a, 2012c).

256 A data set of measured transfer lengths was compiled from an extensive review of the
257 literature. All transfer lengths were measured using one of the three previously mentioned

258 techniques. The data set includes measured transfer lengths and establishes several
259 requirements for materials and manufacture parameters: nominal strand strength of 1860 MPa
260 (270 ksi), strand diameter of 12.5 mm (0.49”) to 13 mm (0.51”), and initial strand stress level
261 of 70-80% of nominal strand strength.

262 A total of 12 different sources reporting all the aforementioned input variables and spanning a
263 variety of practical transfer length prediction situations were selected for the study which
264 resulted in 202 transfer length samples. Table 2 summarizes this data, and Fig. 5 shows the
265 measured transfer length versus the concrete compressive strength at the time of prestress
266 transfer for this data.

267 In this data set, concrete strength at prestress transfer (f'_{ci}) covers a wide range (from 20 to 55
268 MPa [2.9 to 8 ksi]). In general, transfer length decreases when f'_{ci} increases. Fig. 5 includes
269 trend lines of the test results for some sources showing this relationship. The range of
270 measured transfer lengths for a single concrete compressive strength is ample. Furthermore,
271 the range of concrete compressive strength values varies considerably for a single transfer
272 length. The high transfer length results obtained by Cousins et al. (1990) -which may have
273 been caused by additional unreported factors such as strand surface condition- are an anomaly
274 in relation to the other test results.

275

276 ***Predicting strand transfer length from measured parameters***

277 The experimental results provided above have been compared with the theoretical predictions
278 obtained from the Eurocode-2 and ACI-318 provisions (Eq. (4) and Eq. (7a-7b), respectively.
279 Fig. 6 shows the transfer lengths predicted from Eurocode-2 provisions, and Fig. 7 provides
280 those from ACI-318 and it also offers the AASHTO LRFD BDS prediction ($60 \cdot 12.7 = 762$
281 mm [30”]) as a reference. As observed, the predicted transfer lengths from Eurocode-2 vary
282 between 650-1300 mm (25.6”-51.2”) (Fig. 6), whereas ACI-318 gives predictions within a

283 600-800 mm (23.6"-31.5") interval (Fig. 7). This small interval is because ACI-318 does not
284 consider concrete properties; indeed, only slight variations based on strand stress and
285 diameter affect transfer length predictions for this model. The AASHTO reference appears as
286 a top value (Fig. 7).

287 With the Eurocode-2 predictions (Fig. 6), it can be again observed the higher measured values
288 by Cousins et al. (1990). However, the Eurocode-2 predicted transfer lengths using Cousins
289 et al. data that are within a typical range of values.

290 Figs. 8, 9 and 10 show the transfer length ratios (calculated/measured) obtained from
291 Eurocode-2, ACI-318, and AASHTO, respectively, versus the measured transfer lengths.
292 These figures also depict the average value and the standard deviation of these ratios. For all
293 cases, the ratios decrease as measured transfer lengths increase. The obtained ratios are
294 grouped closer together when the transfer length models are simplified. The results are
295 grouped closest together when the AASHTO equation is used followed by the ACI-318 and
296 then the Eurocode-2 equations. The 80% of the results are within the corresponding average \pm
297 standard deviation range for all three models, although practically all the measured transfer
298 lengths by Cousins et al. (1990) are excluded of these ranges for being greater, and some
299 results obtained by den Uijl (1995) and by Rose and Russell (1997) are excluded because they
300 are smaller.

301 The higher ratios correspond to Eurocode-2, followed by AASHTO and ACI-318.
302 Consequently, the number of underestimated transfer lengths (ratio < 1) is smaller for
303 Eurocode-2: practically the only underestimated lengths are the measured transfer lengths by
304 Cousins et al. (1990). However, AASHTO and ACI-318 also underestimate the measured
305 transfer lengths obtained by other authors.

306 Based on the transfer length predicted from the measured parameters, Fig. 11 depicts the
307 average value \pm standard deviation for the three models, and also includes the experimental

308 values. The predicted values are greater than the experimental value in all cases. Once again,
309 it can be observed that the higher value corresponds to Eurocode-2, followed by AASHTO
310 which, in turn, comes before ACI-318. The intervals average value \pm standard deviation are
311 smaller than those corresponding to the experimental results, and they are smaller when code
312 provisions are more simplified: the interval from Eurocode-2 is greater than the interval from
313 ACI-318 which, in turn, is greater than that from AASHTO.

314 Fig. 11 offers the lower and the upper bound values of predicted transfer lengths, when
315 available: lower and upper bound values from Eurocode-2 according to Eq. (5) and Eq. (6),
316 respectively, and the upper bound value from the North American practice according to Eq.
317 (8) proposed by Russell and Burns (1996). As observed, the lower and upper bound values
318 from Eurocode-2 range the interval average value \pm standard deviation of the Eurocode-2
319 predictions. On the other hand, the lower bound value from Eurocode-2 coincides with the
320 average value from AASHTO.

321 Fig. 11 also shows that both the upper values are greater than those of the greater measured
322 transfer lengths (average value + standard deviation). However, no model offers good
323 predictions of the shorter measured transfer lengths (average value – standard deviation): the
324 North American practice does not offer this prediction and the lower bound value from
325 Eurocode-2 is much greater than the shorter measured transfer lengths (this lower bound
326 value is also greater than the average measured transfer lengths). Therefore, situations in
327 which a short transfer length is unfavorable are neglected, as are the verifications of local
328 stresses at prestress transfer.

329

330 ***Predicting allowable free end strand slip***

331 Based on the compiled experimental data set, the sources reporting measured values of
332 transfer length and free end strand slip for comparison purposes have been selected. Figs. 12

333 and 13 depict the measured transfer lengths versus the corresponding free end slip recorded in
334 beams by several authors. The allowable free end slip according to Eq. (11) and the average
335 transfer length value predicted from measured parameters according to Eurocode-2 have been
336 plotted in Fig. 12. Analogously the allowable free end slip according to Eq. (10a-10b) and the
337 average transfer length value predicted from measured parameters according to ACI-318 have
338 been plotted in Fig. 13.

339 Both figures show the percentages of the results included in each sector. As observed in the
340 figures, there is a wide range of end slips that correspond to the same transfer length.
341 Moreover, there is wide range of transfer length values for a given end slip.

342 Figs. 12 and 13 also depict that when the measured transfer length is shorter than the
343 predicted transfer length, the allowable free end strand slip limit is exceeded in 0.6% of the
344 cases (by applying the Eurocode-2 provisions) and in 2.8% of the cases (by applying the ACI-
345 318 provisions). On the other hand, for the measured free end slips that are less than the
346 allowable free end strand slip, measured transfer lengths are longer than the predicted transfer
347 length in some cases: 0.6% of the cases (by applying the Eurocode-2 provisions) and 4.6% of
348 the cases (by applying the ACI-318 provisions). Consequently, the use of an assurance
349 procedure for bond quality based on a limit value for the allowable free end slip is not
350 completely reliable, and these criteria exclude more cases when applying the ACI-318
351 provisions.

352

353 **Conclusions**

354 This research offers a comparative study on transfer length provisions from Eurocode-2 and
355 North American practice. Both models consider a uniform bond stress, strand diameter, and
356 the effective stress after allowing for all prestress losses is used for calculating development
357 length. The differences between the models include strand stress (just after release in

358 Eurocode-2, and after all the prestress losses in ACI-318), type of transfer length value
359 (bound values in Eurocode-2, and average values in ACI-318), and concrete strength at
360 release, tendon type, tendon position and release procedure (parameters only included in the
361 Eurocode-2).

362 The experimental data used in the study was composed of measured transfer lengths
363 determined by several authors. These results were compared with the theoretical predictions
364 from Eurocode-2 and North American practice. The predicted transfer lengths from ACI-318
365 were very similar (600-800 mm [23.6"-31.5"]) which was expected since this model considers
366 only the strand parameters. The predicted values from the Eurocode-2 vary vastly (between
367 650-1300 mm [25.6"-51.2"]) due to the fact that the model considers concrete properties. On
368 average, the predicted values are greater than the experimental values in all the transfer length
369 models. Higher values correspond to Eurocode-2 (it would be a good estimation of the longer
370 measured transfer lengths), followed by AASHTO, and then ACI-318 (the best prediction of
371 the average experimental values).

372 Predicted transfer length values result in smaller ranges than those corresponding to the
373 measured transfer lengths, and these ranges are smaller when code provisions are more
374 simplified: the range from Eurocode-2 is greater than the range from ACI-318 which, in turn,
375 is greater than that from AASHTO.

376 The Eurocode-2 bound values practically range the interval average value \pm standard
377 deviation of the Eurocode-2 predictions. The lower bound value from Eurocode-2 is similar to
378 the average AASHTO value. However, situations in which a short transfer length is
379 unfavorable are neglected because no model offers good predictions of shorter measured
380 transfer lengths: the North American practice does not offer this prediction and the lower
381 bound value from Eurocode-2 is greater than the measured transfer lengths.

382 The transfer length ratio (calculated/measured) according to Eurocode-2 and North American
383 practice shows a tendency in which these ratios decrease when the measured transfer lengths
384 increase. The number of underestimated cases is smaller for Eurocode-2 because of the higher
385 resulting ratios.

386 Finally, the use of a transfer length criterion based on the allowable free end slip excludes
387 more cases when applying the ACI-318 provisions.

388

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393

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