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Payri, R.; Salvador Rubio, FJ.; Carreres Talens, M.; De La Morena, J. (2016). Fuel temperature influence on the performance of a last generation common-rail diesel ballistic injector. Part II: 1D model development, validation and analysis. *Energy Conversion and Management*. 114:376-391. doi:10.1016/j.enconman.2016.02.043.



The final publication is available at

<http://doi.org/10.1016/j.enconman.2016.02.043>

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Additional Information

1 **FUEL TEMPERATURE INFLUENCE ON THE PERFORMANCE OF A LAST**  
2 **GENERATION COMMON-RAIL DIESEL BALLISTIC INJECTOR.**

3 **PART II: 1D MODEL DEVELOPMENT, VALIDATION AND ANALYSIS**  
4

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22 **ABSTRACT**

23 A one-dimensional model of a solenoid-driven common-rail diesel injector has been developed in  
24 order to study the influence of fuel temperature on the injection process. The model has been  
25 implemented after a thorough characterization of the injector, both from the dimensional and the  
26 hydraulic point of view. In this sense, experimental tools for the determination of the geometry of  
27 the injector lines and orifices have been described in the paper, together with the hydraulic setup  
28 introduced to characterize the flow behaviour through the calibrated orifices.

29 An extensive validation of the model has been performed by comparing the modelled mass flow  
30 rate against the experimental results introduced in the first part of the paper, which were performed  
31 for different engine-like operating conditions involving a wide range of fuel temperatures, injection  
32 pressures and energizing times. In that first part of the study, an important influence of the fuel  
33 temperature was reported, especially in terms of the dynamic behaviour of the injector, due to its  
34 ballistic nature. The results from the model have allowed to explain and further extend the findings  
35 of the experimental study by analyzing key features of the injector dynamics, such as the pressure  
36 drop established in the control volume due to the control orifices performance or the forces due to  
37 viscous friction, also assessing their influence on the needle lift laws.

38 **KEYWORDS**

39 diesel, injection, computational, 1D modelling, fuel temperature

40 **LIST OF NOTATION**

41  $A_o$  orifice outlet area

42  $C_d$  discharge coefficient

43  $c_f$  fuel speed of sound

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- 44  $D_{cl}$  clearance diameter
- 45  $D_i$  orifice inlet diameter
- 46  $D_o$  orifice outlet diameter
- 47  $D_{pist}$  piston diameter
- 48  $D_{rod}$  rod diameter
- 49  $D_{spire}$  diameter of a spring's single spire
- 50  $D_{spring}$  spring diameter
- 51  $E$  elastic modulus
- 52  $F_{pist}$  piston force
- 53  $F_{visc}$  viscous friction force
- 54  $F_{\Delta P}$  force due to the pressure difference at both sides of the needle
- 55  $G$  shear modulus
- 56  $K_{eq}$  equivalent stiffness
- 57  $K_{spring}$  spring stiffness rate
- 58  $k\text{-factor}$  orifice conicity factor
- 59  $L$  length of contact
- 60  $\dot{m}$  fuel mass flow rate
- 61  $\dot{m}_{th}$  theoretical fuel mass flow rate

- 62  $N_{spires}$  number of spires of a spring
- 63  $P$  pressure
- 64  $P_b$  discharge backpressure
- 65  $P_{dw}$  downstream pressure
- 66  $P_i$  injection pressure
- 67  $P_{up}$  upstream pressure
- 68  $P_v$  vapour saturation pressure
- 69  $p$  perimeter
- 70  $Re$  Reynolds number
- 71  $T_i$  fuel injection temperature
- 72  $t_d$  delay between SOE and SOI
- 73  $t_{inj}$  injection time
- 74  $u$  flow velocity
- 75  $u_{eff}$  effective velocity
- 76  $u_{th}$  theoretical velocity
- 77 **GREEK SYMBOLS:**
- 78  $\Delta P$  pressure drop
- 79  $\mu_f$  fuel absolute viscosity

80  $\nu_f$  fuel kinematic viscosity:  $\nu_f = \frac{\mu_f}{\rho_f}$

81  $\rho_f$  fuel density

82 **ABBREVIATIONS:**

83 ET Energizing Time

84 IRDCI Injection Rate Discharge Curve Indicator

85 OA Control volume outlet orifice

86 OZ Control volume inlet orifice

87 SEM Scanning Electron Microscope

88 SOE Start of Energizing

89 SOI Start of Injection

90

91 **1. INTRODUCTION**

92 The fuel injection system has attracted the interest of researchers in the diesel engine field due to  
93 the importance of key aspects such as nozzle geometry, fuel injection pressure or ambient  
94 conditions on the air-fuel mixture, combustion efficiency and emissions [1][2][3][4][5][6]. These  
95 are key features in the frame of the new standards and regulations in the automotive world, the  
96 increasing environmental awareness and the cost of the fossil fuels [7][8]. It is then of crucial  
97 importance to understand the diesel injection process in order to propose alternatives that make it  
98 possible to optimize its aforementioned outcomes.

99 In this context, it is helpful to develop computational tools that allow to predict the behaviour of the  
100 injection system under several operating conditions, properly catching their influence on the fuel  
101 rate of injection and even shaping it as desired [9]. In this sense, one-dimensional modelling seems  
102 to be a suitable solution due to its low computational cost as compared to full 3D-CFD approaches,  
103 which for this reason are typically focused on specific parts of the injector, such as the nozzle  
104 [10][11]. In fact, 1D modelling has already been successfully applied by the authors to study the  
105 hydro-dynamic behaviour of the injection system, both in its piezo [12] and solenoid-driven  
106 [13][14] variants.

107 It is important to understand how fuel temperature affects the fuel injection rate, since it is more  
108 difficult to control it during the engine operation than it is to control other relevant parameters such  
109 as the injection pressure or energizing time. Indeed, fuel temperature strongly affects the fuel  
110 properties [15], thus influencing the injected mass flow rate and spray development [16][17], as also  
111 noted in the first part of this study. This influence is even more important at extremely low  
112 temperatures, representative of cold start conditions [18][19].

113 Therefore, the computational models need to incorporate the effect of fuel injection temperature to  
114 their simulation capabilities in order to increase the accuracy of their predictions. Previous works by  
115 the authors regarding fuel injector 1D modelling were restricted to a single fuel temperature  
116 [12][13][14]. Different approaches were undertaken by several researchers in order to include fuel  
117 injection temperature variations in the simulations. Seykens et al. [20] investigated the effects of the  
118 fuel properties on the injection rate by means of a computational 1D model that made it possible to  
119 compare the performance of a diesel fuel and a biodiesel fuel at room temperature. Nevertheless,  
120 the difference among the properties of these fuels is not representative of the ones that could be  
121 induced by differences in temperature when running a diesel engine on its wide range of operating  
122 conditions. A similar work by the same authors involved the investigation of a model for a single

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123 fuel assuming adiabatic flow inside the injector, but the temperature variations studied were only in  
124 the range from 293 to 313 K [21]. Catania et al. [22] emphasized the importance of the effect of the  
125 fuel temperature evolution along high-pressure injection systems, also considering temperatures at  
126 room conditions or above, as Mohammed et al. [23] also did for the case of hydrogen fuel injection.  
127 On the other hand, Plamondon et al. [24] studied the problem for a piezo-driven injector without  
128 considering viscous friction, whose effects are deemed to be important on a solenoid injector at low  
129 pressure conditions. Different approaches were performed by Rafidah et al. [25], who implemented  
130 a 1D model of the whole engine to study the direct effect of the fuel properties on macroscopic  
131 variables like fuel consumption, without paying much attention to the injection event itself; or Shi et  
132 al. [26], who only focused on the lower part of the nozzle without considering the influence of the  
133 control volume orifices performance or the needle movement on the flow, which could also be  
134 affected by fuel temperature.

135 This work aims at the implementation of a 1D model to serve as a tool to predict the performance of  
136 a solenoid-driven common-rail ballistic injector (Bosch CRI 2.20), with special attention to the  
137 proper modelling of the inlet fuel temperature effects on the injection rate. The model is  
138 implemented in the multidisciplinary modelling platform AMESim [27] and validated against data  
139 experimentally gathered for a wide range of injector operating conditions (namely injection  
140 pressure, energizing time and injection temperature), as described in the first part of the paper. The  
141 fuel injection temperature ranges from 253 to 373 K, thus ensuring a proper behaviour of the model  
142 within the whole range of engine-like conditions, including cold start. The isothermal approach is  
143 considered for the flow, which means that for each simulation the fuel temperature is assumed to be  
144 constant along the injector and equal to the one at the injector inlet. Thus, the fuel properties also  
145 remain constant within the same simulation. However, the validation highlights that the model is  
146 still able to exhibit accurate results while reducing the simulation computational costs, even though



147 the ballistic nature of the injector makes its dynamics more sensitive to the changes in fuel  
148 properties (as opposed to previous generations of solenoid-driven injectors studied by the authors  
149 [13][14] in which the needle lift was limited to a value - 250  $\mu\text{m}$  - easily achieved during its regular  
150 operation, which led to the injector dynamics not being strongly affected by the fuel properties).

151 Once the model is validated, the simulation results will be used to confirm and explain the findings  
152 of the first part of the paper by means of an analysis of the physical processes behind the dynamic  
153 behaviour of this kind of injector under extreme temperature conditions. In this respect, the  
154 influence of fuel temperature on key features such as the pressure drop established in the control  
155 volume, due to the control orifices performance; or the forces on the needle, due to viscous friction,  
156 is studied. This allows to link them to the influence on the needle lift laws and the mass flow rate  
157 response.

158 The paper is divided in 6 sections. Section 2 deals with the explanation of the experimental tools  
159 used for the injector characterization needed to develop the computational model. This includes  
160 both a dimensional and a hydraulic characterization of the injector. Next, Section 3 describes how  
161 the different parts of the injector are modelled and implemented into the AMESim software. Section  
162 4 shows the results of the model validation against the experimental results presented in the first  
163 part of the paper. Following, in Section 5, the results from the model simulations will be analysed  
164 and discussed in order to justify the effect of the fuel temperature on the injection performance.  
165 Finally, Section 6 will gather the main conclusions of the study.

166

## 167 **2. EXPERIMENTAL TOOLS**

168 The need for a detailed characterization of the injector in order to obtain a reliable model has  
169 already been pointed out in Section 1. Both the internal geometry and the hydraulic behaviour of the

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170 most important flow restrictions need to be properly implemented in the model. In that regard,  
171 efforts must not be spared on obtaining the relevant parameters by experimental means.

172 The dimensional characterization involves gathering information about the internal lines, orifices,  
173 volumes and movable elements of the system, whereas the hydraulic characterization deals with the  
174 determination of parameters governing the flow (such as the discharge coefficient behaviour, the  
175 detection of cavitation and critical cavitation conditions in such event, etc.) by means of an  
176 experimental setup that makes it possible to isolate the flow through one sole restriction at a time. In  
177 addition, mass flow rate measurements need to be performed in order to validate the computational  
178 model in a wide range of operating conditions.

## 179 **2.1 Mass flow rate measurements**

180 The main output of the 1D computational model described in this work is the mass flow rate signal.  
181 Thus, the validation task needs to ensure that the model responds properly to any change in the  
182 injector operating conditions, namely the injection pressure, the fuel temperature and the energizing  
183 time. For this reason, mass flow rate results for a wide range of conditions need to be available. The  
184 experimental measurements used for validation in the present study were presented in the first part  
185 of the paper, covering the conditions summarized in Table 1. These measurements were taken with  
186 a commercial IRDCI (Injection Rate Discharge Curve Indicator) placed in a special setup, with  
187 particular efforts taken to ensure a proper fuel temperature control. Further details on the IRDCI  
188 working principle, setup and signal treatment are given in the first part of the paper, together with  
189 the exhibition of the mass flow rate results obtained and used as a basis in the present paper.

## 190 **2.2 Dimensional characterization**

191 The geometry of the internal ducts and orifices of the injector has been determined by introducing a  
192 silicone into the injector body. The silicone methodology to determine nozzle geometries is

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193 described by Macián et al. [28], and has been extended to other parts of the injector as shown in Fig.  
194 1. Therefore, silicone moulds of the different parts of the injector are extracted and visualized by  
195 either an optical microscope or a SEM (Scanning Electron Microscope), depending on the size of  
196 the samples. Thus, the moulds corresponding to larger internal passages can be introduced in the  
197 optical microscope. Other large parts of the injector, such as the internal springs, can also be  
198 directly visualized in this microscope. Moulds of the small calibrated orifices (such as the inlet  
199 orifice – OZ – and the outlet orifice – OA –) and the injector nozzle are visualized in the SEM. Due  
200 to the SEM working principle, a gold coating needs to be applied to these samples so that they are  
201 able to evacuate the energy of the electron beam. This gold coating is thin enough (in the order of  
202 nanometres) not to affect the geometry determination.

203 Digital pictures of the samples obtained from both the optical microscope and the SEM are  
204 processed with a CAD software in order to perform the proper measurements. A summary of the  
205 geometrical parameters obtained for the nozzle and the control volume orifices of the injector  
206 through this methodology is shown in Table 2. The *k-factor* introduced in the table is defined by Eq.  
207 (1) and highlights the high degree of convergence of the OZ and the nozzle orifices, whereas the  
208 OA orifice is essentially cylindrical. This means that the former orifices are not prone to cavitate, as  
209 opposed to the latter [29]. This finding is confirmed by the hydraulic characterization (Section 2.3)  
210 and taken into account on the modelling.

$$k - factor = \frac{D_i - D_o}{10} \quad (1)$$

### 211 **2.3 Hydraulic characterization**

212 The main purpose of the hydraulic characterization of an orifice is to determine its flow behaviour  
213 depending on the operating conditions of the injector. This characterization can be performed by

214 analysing the continuous flow through the orifice under several conditions of upstream and  
215 downstream pressure. To this end, the experimental setup depicted in Fig. 2 has been used. An  
216 electrically-driven fuel pump extracts the fuel from a tank and pressurizes it after going through a  
217 filter, providing continuous flow. Since the fuel heats up due to its pressurization, a fuel-water heat  
218 exchanger is used to cool down the flow before reaching a commercial common-rail, where the  
219 pressure is controlled thanks to a manual regulation valve located upstream of the rail. The  
220 hydraulic restriction to be characterized (either the nozzle or a control volume orifice) is disposed  
221 downstream of the rail, inside a test rig that isolates the corresponding orifice, avoiding any leakage  
222 to other paths. Details on the test rigs for the nozzle and the control volume are given in Sections  
223 2.3.1 and 2.3.2. Fuel flows through the hydraulic restriction into a discharge chamber, where the  
224 backpressure is controlled by means of another manual regulation valve located downstream of the  
225 chamber, and is finally injected into a glass deposit where the fuel mass instantaneously injected  
226 can be measured thanks to a scale. After a short stabilization time for each measurement, the mass  
227 flow rate is determined by averaging it for a period of 100 seconds.

### 228 **2.3.1 Nozzle test rig**

229 Fig. 3 shows the test rig for the hydraulic characterization of the nozzle, which ensures proper  
230 sealing. The nozzle is introduced without the needle, so that only the flow features through the  
231 orifices themselves are accounted for.

232 As stated in the first part of the paper, the mass flow through an orifice is given by the mass  
233 conservation equation, in which the discharge coefficient is introduced to take the losses into  
234 account:

$$\dot{m} = \rho_f A_0 u_{th} C_d \quad (2)$$

235 with  $u_{th}$  being the theoretical velocity through the orifice, derived from Bernoulli's equation taking  
236 the assumption of negligible upstream velocity, as described by Eq. (3):

$$u_{th} = \sqrt{\frac{2\Delta P}{\rho_f}} \quad (3)$$

237 where  $\Delta P = P_{up} - P_{dw}$ . The discharge coefficient can then be obtained as:

$$C_d = \frac{\dot{m}}{A_0 \sqrt{2\rho_f(P_{up} - P_{dw})}} \quad (4)$$

238 The discharge coefficient strongly depends on the theoretical Reynolds number, defined as:

$$Re = \frac{\rho_f u_{th} D_0}{\mu_f} \quad (5)$$

239 In order to ensure a wide range of Reynolds numbers, two values of upstream pressure (10 and 20  
240 MPa) are tested, whereas a sweep of downstream pressures from atmospheric pressure to 8 MPa  
241 (mechanical limit of the test rig) is carried out for each upstream pressure.

242 Results from the nozzle hydraulic characterization are depicted in Fig. 4. The left side of the figure  
243 shows the mass flow rate against the square root of the pressure drop. A linear trend is observed for  
244 both values of upstream pressure, as expected [4]. The fact that a mass flow rate collapse is not seen  
245 points out that the nozzle orifices do not work under cavitating conditions, confirming what was  
246 stated in Section 2.2 as suggested by their high  $k$ -factor [29]. With regard to the behaviour of the  
247 discharge coefficient with respect to the Reynolds number, shown at the right side of the figure, the  
248 asymptotic trend expected from the literature [30] can also be guessed by the experimental results.  
249 The discharge coefficient tends to a maximum value of about 0.96. This value is important for the

250 model since AMESim takes it as a reference and uses the so-called critical Reynolds number  $Re_{crit}$   
251 (Reynolds number at which the discharge coefficient is 95% of the maximum value) as the  
252 transition between laminar and turbulent flow, implementing the following  $C_d$  vs  $Re$  law [27]:

$$C_d = C_{d_{max}} \tanh\left(\frac{2Re}{Re_{crit}}\right) \quad (6)$$

253 In the case of the nozzle orifices,  $Re_{crit}$  takes a value of 5600. The evolution of  $C_d$  with  $Re$  predicted  
254 by AMESim according to Eq. (6) and the parameters that have been found through the hydraulic  
255 characterization are also shown in Fig. 4, revealing a proper fit to the experimental points.

### 256 **2.3.2 Control volume orifices test rig**

257 The test rig for the hydraulic characterization of the control volume orifices is shown in Fig. 5  
258 together with the injector control volume itself. There are two different configurations in which the  
259 test rig can be mounted in the experimental setup described in Fig. 2. In order to characterize the  
260 OA orifice, the port at the left side of the test rig in the figure is locked, and the test rig is mounted  
261 on the experimental setup so that the fuel flows from the bottom of the control volume to the top.  
262 The same test rig can be used for the OZ orifice characterization by locking the upper port of the  
263 test rig and making the fuel flow from the OZ orifice entrance to the lower part of the test rig.

264 Fig. 6 shows the results of the OA orifice hydraulic characterization. As it was done for the nozzle  
265 orifices, the left side of the figure shows the mass flow through the orifice against the square root of  
266 the pressure drop. A linear trend is also observed until a mass flow rate collapse is noticed for each  
267 upstream pressure, indicating cavitation inside the orifice, as expected due to its cylindrical shape  
268 reported in Section 2.2. The conditions at which the mass flow starts being choked are the critical  
269 cavitation conditions and also need to be provided to the AMESim model. Since cavitation is  
270 observed for all the tested values of downstream pressure (from atmospheric pressure to 8 MPa, as

271 tested for the nozzle orifices) for the upstream pressure of 20 MPa, an intermediate level of  
272 upstream pressure (15 MPa) has also been tested, so that the critical cavitation conditions  
273 determination is more reliable. The right side of the figure shows the behaviour of the discharge  
274 coefficient against the Reynolds number. It can be seen that, when the orifice works under non-  
275 cavitating conditions, the same trend that was analysed for the nozzle orifices is observed.  
276 However, for each upstream pressure, the discharge coefficient drops abruptly once the orifice starts  
277 cavitating. This fact highlights the need to properly describe the transition from non-cavitating to  
278 cavitating conditions in order to predict the injector behaviour in an accurate way.

279 The proneness of an orifice to cavitate has been described in the literature through different  
280 approaches. The cavitation number,  $CN$ , introduced by Soteriou et al. [31] is used in the present  
281 work:

$$CN = \frac{P_{up} - P_{dw}}{P_{dw} - P_v} \quad (7)$$

282 where  $P_v$  is the saturation vapour pressure of the fuel. This term is usually neglected due to its low  
283 value when compared to the others, thus leading to:

$$CN = \frac{P_{up}}{P_{dw}} - 1 \quad (8)$$

284 For each value of upstream pressure, the critical cavitation number  $CN_{crit}$  is defined as the cavitation  
285 number for the downstream pressure that leads to cavitation conditions, which can be determined  
286 from Fig. 6. The behaviour of the discharge coefficient in non-cavitating conditions, where it  
287 depends on the Reynolds number, has already been discussed. However, in cavitating conditions, its  
288 behaviour can be described as a function of the cavitation number, as reported in the literature  
289 [31][32] and stated in Eq. (9):

$$C_d = C_c \sqrt{1 + \frac{1}{CN}} \quad (9)$$

290 where  $C_c$  is the contraction coefficient, which describes the loss in discharge coefficient associated  
291 to the lower effective area in an orifice due to the presence of vapour bubbles.  $C_c$  can be obtained  
292 by applying Eq. (9) for the particular case of the critical cavitation conditions, for which both  $C_d$   
293 and  $CN$  are known.

294 A summary of the relevant parameters obtained from the hydraulic characterization of both the  
295 nozzle orifices and the control volume orifices (OA and OZ) is given in Table 3. It is important to  
296 note that cavitation has not been noticed for the OZ orifice, as expected due to its high *k-factor*  
297 reported in Section 2.2.

298

### 299 **3. INJECTOR MODELLING**

300 As stated before, AMESim has been used as the platform to implement the injector model [27]. It is  
301 a commercial simulation software for one-dimensional modelling and analysis. This software  
302 consists of a set of components from predefined libraries that belong to the different physical  
303 domains. Thus, the assembly of components makes it possible to simulate and analyse multi-  
304 domain systems. In the case of the injector, libraries from the electrics, mechanics and hydraulics  
305 fields are used, among others. For illustrative purposes, the model implemented in this work is  
306 divided in three parts that are described in the present Section: the injector holder, the solenoid  
307 valve and the nozzle. The implementation of the fuel properties is also described here.

#### 308 **3.1 Injector holder**

309 Fig. 7 shows a sketch of the injector holder together with its model representation. A pressure



310 source element is used in order to simulate the high pressure pump, which raises the pressure in a  
311 volume that represents the common-rail upstream of the injector inlet. Right at the injector inlet, the  
312 flow travels through the high pressure filter, modelled as a flow restriction. From here, the flow  
313 passes through the line HL1 until it reaches a bifurcation: part of the fuel enters the injector control  
314 volume HV1 through the OZ orifice. The pressure on this volume is used to compute the pressure  
315 force on the upper part of the needle, mechanically modelled as the element P1. The flow is also  
316 allowed to leave the control volume through the HL2 line linked to the OA orifice, connected in  
317 turn to the HV2 volume that links the injector holder to the solenoid valve. The rest of the fuel after  
318 the bifurcation downstream of the HL1 line travels to the nozzle through lines HL3, HL4 and HL5  
319 in order to be injected into the cylinder. This fuel also encounters the volumes HV3 and HV4,  
320 where the pressure forces on other parts of the needle are computed.

321 It is important to note that the main parameters of the hydraulic lines are their length and diameter.  
322 For those cases in which the hydraulic line is not circular (such as lines HL4 and HL5, which are  
323 annular ducts), the hydraulic diameter defined in Eq. (10) is used instead:

$$D_{hydr} = \frac{4 \cdot A}{p} \quad (10)$$

324 where  $A$  is the cross-sectional area of the duct and  $p$  the associated perimeter.

325 As far as the mechanical elements of the injector holder are concerned, the upper part of the needle  
326 is modelled by the elements P1, NLF, P2, 1/2 NM, ND and NSP. The piston P2 computes the  
327 pressure forces due to a change in area in the needle that generates an annular surface on which the  
328 pressure in the HV3 volume acts, trying to push the needle upwards. Any piston element computes  
329 the pressure forces from the pressure  $P$  in its associated volume as:

$$F_{pist} = \frac{\pi}{4} P (D_{pist}^2 - D_{rod}^2) \quad (11)$$

330 The element 1/2 NM accounts for half of the needle mass, since the other half will be linked to the  
 331 nozzle part due to compatibility among AMESim elements. Friction in the mass elements is taken  
 332 into account through a static friction term that needs to be overcome prior to the mass movement,  
 333 and a viscous friction term that is a direct function of the fluid viscosity. Moreover, the NLF  
 334 element accounts for internal leakages and viscous friction that take place due to the small clearance  
 335 among the needle and the injector holder itself in certain parts of the injector. Flow through this  
 336 clearance is considered with the Poiseuille law, assuming laminar regime. The viscous friction is  
 337 then computed as stated by Blackburn et al. [33]:

$$F_{fric} = -\Delta P \cdot \pi \cdot \frac{D_{cl} \cdot (D_{pist} - D_{cl})}{4} + 4 \cdot \pi \cdot \mu_f \cdot u \cdot L \cdot \left( \frac{D_{pist}}{D_{cl}} - 1 \right) \quad (12)$$

338 where  $D_{cl}$  is the clearance diameter among the needle and the injector holder,  $u$  is the mean flow  
 339 velocity,  $L$  is the length of contact along which the needle and the injector holder are only separated  
 340 by a small gap and  $\Delta P$  is the pressure difference across the element. In the case of the needle, this  
 341 pressure difference is the one set among the volumes HV1 (control volume) and HV3. During the  
 342 normal operation of the injector, the pressure in the control volume will depend on the pressure  
 343 drop across the OZ orifice, whereas the pressure in the HV3 volume is approximately the rail  
 344 pressure, since no important flow restrictions are found in the high pressure filter or the HL1 and  
 345 HL3 lines. Thus, the pressure drop in the control volume and the fuel viscosity are key on  
 346 understanding the friction forces on the needle.

347 In addition, NSP represents the spring that tries to hold the needle against its seat and opposes to its  
 348 lift. The stiffness rate of all the springs in the model has been calculated from their geometry

349 through the equation established by Adler and Bauer [34]:

$$K_{spring} = \frac{G \cdot D_{spire}^4}{8 \cdot N_{spires} \cdot D_{spring}^3} \quad (13)$$

350 where  $G$  is the shear modulus of the material (steel),  $D_{spire}$  is the diameter of a single spire of the  
351 spring, i.e. its thickness,  $D_{spring}$  is the diameter of the whole spring and  $N_{spires}$  is the spring total  
352 number of spires.

353 Finally, the element ND represents the elastic deformation of the needle, especially relevant prior to  
354 the injection event, when the needle is closed against its seat and the high pressures of the system  
355 lead to deformations that need to be recovered before the needle effectively opens once the injector  
356 is energized. These deformations are computed through an equivalent spring whose stiffness rate is  
357 calculated by means of the equation established by Desantes et al. [35]:

$$K_{eq} = \frac{1}{\frac{1}{E} \sum \frac{L_i}{A_i}} \quad (14)$$

358 where  $E$  is the elastic modulus of the material, whereas  $L_i$  and  $A_i$  are the length and cross section of  
359 each segment of the needle with the same cross-sectional area, respectively.

360 A summary of the most important parameters introduced in this part of the model is presented in  
361 Table 4. These parameters were gathered as described in Section 2.2. Details on the control volume  
362 orifices were presented in Section 2 and thus are here omitted.

### 363 **3.2 Solenoid valve**

364 A detail of the solenoid valve part of the injector together with a zoom to the magnetic path and the  
365 corresponding AMESim sketch proposed are shown in Fig. 8. The mechanical elements (piston) of

366 the valve are in charge of avoiding any flow from the control volume (HV1) through the OA orifice  
367 when the injector is not energized. When current arrives to the solenoid coil, it induces a magnetic  
368 flux through the magnetic core (represented by the elements SM1, SM2 and SM3) that crosses the  
369 air gap AG towards the upper side of the valve piston (SM4). This magnetic flux depends on the  
370 material, length and area of the elements it trespasses, which are obtained thanks to the injector  
371 dimensional characterization. The main parameters of the magnetic part of the solenoid valve are  
372 summarized in Table 5. The magnetic coil resistance has been determined by means of a  
373 commercial digital multimeter.

374 The resulting magnetic flux is responsible for the generation of a force that attracts the valve piston,  
375 letting the fuel flow from the control volume through an orifice, whose cross-sectional area grows  
376 as the valve piston moves up. Hence, this orifice has been modelled as the SO1 restriction, whose  
377 hydraulic diameter is a function of the valve piston lift (which is limited to 20  $\mu\text{m}$ ) and is linked to  
378 the injector holder part of the model through the OA orifice. Therefore, when the injector is  
379 energized, the set consisting of the OA and SO1 orifices evacuates fuel from the control volume,  
380 thus dropping its pressure and letting the needle rise, producing the injection. The fuel leaving the  
381 control volume flows to the return line through the SO2 orifices carved at both sides of the upper  
382 part of the control volume piece. From there, it travels through the SO3 orifices, drilled on the valve  
383 piston, and leaves the injector through the lines SL1 and SL2 and the orifice SO4, which represent  
384 the return duct. Along this path, the fuel also encounters the volumes SV1, SV2 and SV3, whose  
385 pressure acts on the pistons SP1, SP2, SP3 and SP4 that generate the forces that help opening or  
386 closing it against the SO1 orifice, in an analogous way to the piston forces on the needle explained  
387 in Section 3.1. These pistons, together with the valve mass VM, shape the valve piston mechanical  
388 part. A displacement sensor VDS is also introduced in the model to transfer the valve piston lift to  
389 the SO1 orifice at all times, establishing its variable area. In addition, the SLF element accounts for

390 the internal leakages and viscous friction in this section of the injector, in a similar way to the one  
391 described for the needle in Section 3.1.

392 Once the injector stops being energized, the valve piston closes the SO1 orifice thanks to the force  
393 imposed by the SS spring. In this situation, the OZ orifice refills the control volume, restoring its  
394 pressure and making the needle close against the nozzle seat, cutting the injection.

395 A summary on the most important parameters of the solenoid mechanical part is shown in Table 6.

### 396 **3.3 Nozzle**

397 Fig. 9 shows the nozzle together with its AMESim equivalent sketch. The fuel comes from the  
398 injector holder part through three parallel lines NL1 resulting from the quasi-triangular needle  
399 cross-section. For each of the lines, an additional hydraulic orifice NO1 has been introduced due to  
400 an increase in the needle cross-section, which results in an important restriction to the flow that may  
401 lead to important pressure changes. After these orifices, the fuel keeps travelling along parallel  
402 ducts NL2, until they encounter each other in the NV1 volume, from where it flows to the nozzle  
403 orifices through the nozzle channel NL3. The volume at the lower part of the nozzle is divided into  
404 the NV2 and NV3 volumes, since the latter exclusively represents the sac, considered from the  
405 needle seat point onwards. The NV1 and NV2 volumes are associated to the pistons NP1 and NP2  
406 that will simulate the pressure forces pulling the needle upwards. The nozzle seat NST is  
407 represented by a conical seat element that accounts for both the needle tip and the seat, and thus  
408 computes an additional pressure force associated to the sac (NV3 volume). The rest of the needle  
409 mass NM is associated to this part of the model. When the needle lifts, it discovers the 7 orifices of  
410 the nozzle, leading to the fuel being injected to a tank at a given backpressure.

411 The determination of the parameters associated to the nozzle seat NST is especially critical. Thanks  
412 to the dimensional characterization technique explained in Section 2.2, it is possible to obtain them

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413 by overlapping optical microscope pictures of both the needle and the nozzle silicone mould, as  
414 shown in Fig. 10.

415 The main parameters introduced into the nozzle part of the model are shown in Table 7. Details on  
416 the geometry of the nozzle orifices were already given in Section 2.2 and summarized in Table 2.

### 417 **3.4 Fuel properties**

418 As stated in the first part of the paper, the fuel used for the mass flow rate measurements that  
419 comprise the basis for the validation of the computational model proposed in this work is a standard  
420 winter fuel. Its properties were determined for a wide range of temperatures at atmospheric pressure  
421 and are available for the model. It was already stated in the Introduction section that the model will  
422 introduce the hypothesis of isothermal flow, thus keeping the temperature at the inlet as a constant  
423 along the injector, without changes in the fuel properties within the same simulation. Table 8  
424 reminds the values of density and absolute viscosity that were used for the temperatures for which  
425 the model has been validated.

426

## 427 **4. MODEL VALIDATION**

428 In order to ensure a proper behaviour of the model at the wide conditions of engine operation, the  
429 model has been validated against the experimental results of mass flow rate obtained in the first part  
430 of the paper, whose conditions are summarized in Table 1.

431 Fig. 11 shows a comparison of the mass flow rate curves obtained from the model versus the  
432 experimental ones at different injection pressures for each injection temperature. Three curves  
433 corresponding to different ET (0.5, 1 and 2 ms) are depicted for each  $P_i$  and  $T_i$ . It can be seen that  
434 the model properly reproduces the injector behaviour for most of the tested conditions. The

435 stationary mass flow rate follows the observed trends with the injection pressure and temperature,  
436 with a small underprediction for the highest temperature tested. With regard to the injection  
437 duration, the trends are also preserved except for the prediction of shorter durations for the  
438 energizing times of 0.5 ms for the temperatures of 303 K and higher. The analysis of the opening  
439 slope reveals a good reproduction of reality by the model, which appropriately follows the observed  
440 trend with the injection temperature. The worst results are obtained for the lowest injection  
441 temperature, for which the model assumes a slower opening slope. This fact can be attributed to the  
442 assumption of isothermal flow, which is not totally representative of the injector internal flow due  
443 to the heating that may take place especially through the small calibrated orifices (i.e. control  
444 volume and nozzle orifices), where viscous friction effects are deemed to be important. Thus, the  
445 isothermal assumption works properly for temperatures over 273 K due to the small changes in the  
446 relevant fuel properties (i.e. density and viscosity) associated to fuel heating in that case, whereas  
447 the behaviour is slightly worse for the cold temperature range, for which the viscosity follows an  
448 exponential trend (Table 8).

449 Since it is also important for engine modellers to be able to accurately predict the total mass  
450 injected into the cylinder, the reliability of the model is assessed in these terms in Fig. 12, where the  
451 values of total mass injected obtained from the model are compared against the experimental ones.  
452 Results show a fair prediction for the majority of points studied. More than 80% of the points are  
453 within a deviation lower than 10%. The highest deviations are noticed at low injection temperatures,  
454 representing up to 7% in the case of long injections (energizing times of 1 ms and 2 ms) or 35% in  
455 the case of the short injections (energizing times of 0.25 and 0.5 ms), where small deviations in  
456 absolute terms lead to a high percentage of deviation even if the injection rate shape is properly  
457 predicted. On the contrary, for the highest injection temperature, differences are lower than 10% for  
458 all the tested points. These findings are a direct consequence of the differences in mass flow rate

459 curves observed in Fig. 11.

460

## 461 **5. RESULTS AND DISCUSSION**

462 Fuel temperature is expected to influence the flow along the injector, especially through the most  
463 important restrictions (nozzle and control volume orifices), due to the different density and viscosity  
464 values induced. The density affects the mass flow rate through the restriction, in addition to  
465 controlling the flow regime together with the viscosity through the Reynolds number. These facts  
466 were already analyzed in the first part of the paper from the point of view of the stationary mass  
467 flow rate at the injector outlet. However, they are also deemed to play a key role on injector  
468 dynamics. In this case, a deeper analysis of the internal flow is required in order to explain the  
469 differences associated to the fuel temperature. The present Section aims at the internal exploration  
470 of the injector by means of the implemented computational model, further analyzing the simulations  
471 corresponding to the operating conditions used for validation, in order to identify and assess the  
472 causes for the differences related to fuel temperature.

473 Fig. 13 shows a simplified sketch of the injector depicting the main phenomena involved during the  
474 transient stages of the injection. On the one hand, injector dynamics are influenced by the force due  
475 to the pressure difference between the upper part of the needle (control volume) and its lower part.  
476 This pressure difference is governed by the performance of the control volume orifices, since the  
477 flow rate through them determines both the ability to evacuate the control volume when the  
478 solenoid valve is energized (thus reducing the pressure at the upper part of the needle, making it rise  
479 discovering the nozzle orifices) or to refill it when the injector stops being energized (recovering the  
480 pressure at the upper part of the needle and making it close against its seat). These features can be  
481 studied through the internal analysis of the injector allowed by the computational model. On the



482 other hand, needle dynamics are influenced by the force generated by viscous friction in the  
483 clearance between the needle and the injector wall, especially when this clearance is small. This  
484 viscous friction depends on the fuel viscosity, as stated by Eq. (12), which in turn depends on the  
485 fuel temperature. The fact that this friction force also depends on the pressure difference established  
486 between the control volume and the rail (as justified in Eq. (12)) makes it difficult to isolate the  
487 effects of the fuel temperature exclusively related to the control volume orifices performance from  
488 those related to the change in fuel properties. However, they will be hereby analyzed and linked to  
489 the needle lift evolution during the injection event, which should explain the findings from the  
490 experimental mass flow rate measurements.

#### 491 **5.1. Analysis of the hydraulic parameters of the flow through the control volume orifices**

492 As it has been mentioned, the hydraulic parameters of the control volume orifices play a key role on  
493 injector dynamics, since they determine the ability to effectively fill or empty the control volume,  
494 generating the pressure difference that drives the needle. During the opening stage, the OA orifice is  
495 uncovered and becomes responsible for evacuating the fuel from the control volume, whereas the  
496 losses through the OZ orifice, which is always active, determine the pressure drop in the control  
497 volume. During the closing stage, the OA orifice is locked and the discharge capabilities of the OZ  
498 orifice determine the ability of the control volume to recover its pressure. Attention to the discharge  
499 coefficients of both orifices must be given in order to shed light on these phenomena, keeping in  
500 mind that the OZ orifice is not expected to cavitate for any of the engine operating conditions due to  
501 its high conicity (recall Section 2), whereas the OA orifice is prone to cavitate.

502 Fig. 14 shows the simulated discharge coefficients of the control volume orifices as a function of  $Re$   
503 (OZ orifice and non-cavitating region of the OA orifice) and the  $CN$  (cavitating zone of the OA  
504 orifice), representing where the tested conditions are located. In the case of the OA orifice, it can be

505 seen that the orifice is cavitating ( $CN > CN_{crit}$ ) for all the tested conditions, but the non-cavitating  
506 part of the curve has been respected for illustrative purposes. No influence of the fuel temperature  
507 on the discharge coefficient has been found for temperatures higher than 303 K. In the case of the  
508 OZ orifice,  $Re$  is above  $Re_{crit}$  for all these conditions, directly leading to  $C_{dmax}$ . For the OA orifice,  
509 the pressure drop across the orifice remains the same regardless the nominal injection pressure,  
510 since the flow will experience subsequent pressure drops downstream the orifice due to the presence  
511 of further restrictions (SO1) before reaching the atmospheric pressure at the return line. An  
512 influence of the fuel temperature is however noticed at low temperatures. In the case of the OZ  
513 orifice, the high fuel viscosities associated to the low fuel temperatures (recall Table 8) lead to  
514 changes in the flow regime for the  $T_i = 253$  K and  $T_i = 273$  K cases, making the orifice work under  
515 the laminar regime in the former, whereas it acts on the laminar-turbulent transition on the latter.  
516 This results in a drastic reduction of the flow discharge capabilities across the OZ orifice, which is  
517 expected to lead to low pressures in the control volume during the opening. In the case of the OA  
518 orifice, the fuel temperature has only been found to affect  $CN$  for the lowest temperature tested, in a  
519 more important manner for the lower injection pressures. However, the associated differences in  
520 discharge coefficient are less significant.

521 Fig. 15 shows the evolution of the pressure at the control volume for the whole range of  
522 temperatures studied and two different injection pressures, focusing on the cases of  $ET = 1$  ms. The  
523 pressure values have been normalized with respect to the nominal injection pressure. Results for  $T_i$   
524 = 353 K have been omitted due to their similarity with the ones at  $T_i = 373$  K. The figure shows that  
525 the depression generated at the control volume at the opening stage is more important the lower the  
526 fuel temperature. This result can be explained due to the differences in mass flow rate expected at  
527 both control orifices. On the one hand, these differences come from the fact that the fuel density  
528 decreases linearly when increasing the fuel temperature (recall Table 8). However, Fig. 15 shows

529 that the differences in the pressure drop at the control volume at different temperatures become  
530 more important at the lowest temperatures, which suggests a non-linear trend. This is consistent  
531 with the findings about the discharge coefficients shown at Fig. 14, where the changes in flow  
532 regime induced by the lowest temperatures lead to further limitations on the OZ orifice discharge  
533 capabilities, producing extra losses on the orifice and therefore lower pressures set downstream.  
534 The performance of the OA orifice was already demonstrated to be only slightly affected by fuel  
535 temperature in the most extreme cases. Another factor that cannot be neglected when analyzing the  
536 pressure changes in the control volume is the fact that the needle lift evolution is expected to be  
537 different depending on the fuel temperature, thus modifying the actual size of the control volume,  
538 which therefore will lose or recover pressure at a different rate. No significant differences are  
539 appreciated among injection pressures, although it can be seen that a lower relative pressure drop is  
540 achieved for the highest injection pressure. This can be explained due to the fact that a higher mass  
541 flow rate enters the control volume through the OZ orifice, hindering the process to evacuate it.

542 It is important to note that the sole effect of the discussed control volume orifices hydraulic  
543 parameters would lead to a faster response of the injector at low temperatures, due to the more  
544 accused pressure drop at the control volume, which generates a higher unbalance at both sides of  
545 the needle. However, as stated before and highlighted by Fig. 13, the effect of the friction force also  
546 needs to be analyzed.

## 547 **5.2. Analysis of the friction force opposing the needle movement**

548 As shown by Eq. (12), the friction forces appearing on the needle when trying to lift through the  
549 fuel depend both on the pressure drop along the needle and the fuel viscosity, with opposed effects.  
550 Fig. 16 shows the evolution of the needle friction force for all the range of temperatures studied and  
551  $P_i = 70$  MPa (results for  $P_i = 180$  MPa have been omitted since the trend has been found to be the

552 same), focusing on the cases of  $ET = 1$  ms. Values have been normalized with respect to the case of  
553  $T_i = 303$  K, representative of ambient temperature. The figure only shows the time range  
554 corresponding to the stage in which the needle is rising. It can be seen that the friction forces are  
555 extremely affected by fuel temperature, getting higher the lower the temperature. Analyzing the two  
556 terms of Eq. (12), the higher pressure drops in the control volume observed at low temperatures  
557 (recall Fig. 15) would act in the sense of reducing the friction force. However, the increase in fuel  
558 viscosity at low temperatures acts with an opposite sense. The exponential trend of the fuel  
559 viscosity at low temperatures (recall Table 8) is able to overcome the effect of the pressure drop and  
560 justifies the higher friction forces observed in those cases. Thus, it is possible to state that the net  
561 effect of increasing the fuel temperature is a reduction in the friction force, which would in turn act  
562 in the sense of a faster needle opening.

### 563 **5.3 Analysis of the combined effect of control volume pressure drop and friction forces on** 564 **needle dynamics**

565 As highlighted by Fig. 13, injector dynamics are influenced, on the one hand, by the force due to the  
566 pressure difference between the control volume and the nozzle sac, being affected by the friction  
567 force on the other side. As it has been demonstrated in Sections 5.1 and 5.2, a lower fuel  
568 temperature would lead to a faster injector opening if only the pressure forces were considered,  
569 whereas it would lead to a slower opening by the sole effect of viscous friction. The present  
570 subsection aims at the analysis of the net effect of both phenomena in order to understand how the  
571 fuel temperature influences needle dynamics.

572 Fig. 17 shows the needle lift evolution obtained from the simulations for the whole range of  
573 temperatures studied and two different injection pressures, focusing on the cases of  $ET = 1$  ms.  
574 Needle lift values have been normalized with respect to the injector's mechanical limit ( $850 \mu\text{m}$ ).

575 The figure shows that the time at which the injector closes depends on the fuel injection  
576 temperature, as concluded in the first part of the paper due to the ballistic nature of the injector. It is  
577 observed that the needle opening is slower the lower the fuel temperature. In order to explain the net  
578 effect of the fuel temperature on the opening stage, Table 9 summarizes the effects of the fuel  
579 temperature on the control volume pressure and the friction force for the case of  $P_i = 70$  MPa at a  
580 time after SOE of 0.7 ms. Values have been extracted from Fig. 15 and Fig. 16 and normalized  
581 taking the case of  $T_i = 303$  K (representative of ambient conditions) as a reference. It can be seen  
582 that, in the end, the effect of the fuel temperature on the friction force is more important than the  
583 one on the control volume pressure through the differences in flow through the control volume  
584 orifices. Thus, the opening stage of the injection event is governed by the friction force appearing  
585 on the needle due to viscous effects, resulting in a slower opening the lower the fuel temperature is.

586 Fig. 17 shows that a slower needle opening results in lower top positions reached by the needle  
587 during an injection event. Hence, during the closing stage, the needle falls from these lower  
588 positions for low injection temperatures, which results in shorter times needed for the needle to  
589 close against its seat and cut the injection.

590 Fig. 18 summarizes the highest position reached by the needle for all the tested operating  
591 conditions. The expected trends in the view of Fig. 17 are followed except for high injection  
592 pressures ( $P_i \geq 120$  MPa) and long energizing times ( $ET > 1$  ms), where the needle already reaches  
593 its mechanical limit. This explains the fact that, at the longest energizing times (2 ms), the injection  
594 duration does not always follow the same trend with the injection pressure, as had already been  
595 noticed in the first part of the paper through the experimental measurements, and can be observed in  
596 Fig. 11: in general, for a given energizing time, the injection duration is longer the higher the  
597 injection pressure, due to the higher maximum positions of needle lift reached due to the pressure  
598 forces. This is no longer true when there are several injection pressures for which the limit needle

599 lift is achieved, since in those cases the needle falls from the same position and the only effect on  
600 injection duration is the one due to the needle closing speed, related to the previously mentioned  
601 phenomena.

602

## 603 **6. CONCLUSIONS**

604 The fuel temperature influence on injector dynamics has been assessed in this paper through a  
605 computational 1D model of a last-generation common-rail diesel ballistic injector implemented in  
606 the AMESim platform. The methodology to develop such a model through a careful  
607 characterization (both dimensional and hydraulic) has been presented, and its validity has been  
608 demonstrated in a wide range of fuel temperature conditions, from 253 to 373 K, obtaining a  
609 reasonable reproduction of the mass flow rate curves. Results have been analyzed through  
610 simulations at those temperature conditions and different levels of injection pressure and energizing  
611 time.

612 The main conclusions of the study are summarized in the following points:

- 613 • Injector dynamics are mainly affected by the pressure difference established between the  
614 control volume and the nozzle sac on the one hand, and the friction force generated between  
615 the needle and the fuel due to viscous effects on the other hand.
- 616 • The pressure established at any time in the control volume depends on the performance of  
617 the control volume orifices (OZ and OA), since they are responsible for evacuating the  
618 control volume when the injector is energized or to refill it when the solenoid stops being  
619 energized. The main hydraulic features of these orifices have been identified for several  
620 operating conditions, making it possible to explain the fact that the pressure drop in the

621 control volume is higher the lower the fuel temperature, due to the change in the flow  
622 regime induced in the OZ orifice through the Reynolds number. The influence of the fuel  
623 temperature on the OA orifice performance has been proved to be lower than the one on the  
624 OZ orifice, due to the fact that the former always operates in cavitating conditions. Thus, the  
625 sole effect of the pressure difference established in the control volume would lead to a faster  
626 response of the injector the lower the injection temperature.

627 • The friction force opposing the needle movement depends on the pressure drop across the  
628 needle and the fuel viscosity. Simulations have allowed to conclude that this phenomenon is  
629 mostly governed by the fuel viscosity, especially at low temperatures, due to the its  
630 exponential increase in those conditions. Thus, the effect of the friction force itself would  
631 lead to a slower response of the injector the lower the injection temperature.

632 • Needle lift laws have been reproduced in order to establish the net effect of the fuel  
633 temperature on injection dynamics. Viscous friction has been proved to be the phenomenon  
634 dominating the opening stage of the injection, since its variations with temperature have  
635 been demonstrated to be larger than those of the pressure drop in the control volume. Thus,  
636 the opening stage of the injection is slower the lower the fuel temperature. This, in turn,  
637 leads to lower top positions achieved by the needle during its rise due to the ballistic nature  
638 of the injector, also resulting in shorter injection durations due to the shorter distance to be  
639 travelled by the needle in order to close against its seat.

640

641

642

643 **ACKNOWLEDGEMENTS**

644 This work was partly sponsored by “Ministerio de Economía y Competitividad” in the frame of the  
645 project “Comprensión de la influencia de combustibles no convencionales en el proceso de  
646 inyección y combustión tipo diesel”, reference TRA2012-36932. The equipment used in this work  
647 has been partially supported by FEDER project funds "Dotación de infraestructuras científico  
648 técnicas para el Centro Integral de Mejora Energética y Medioambiental de Sistemas de Transporte  
649 (CiMeT), (FEDER-ICTS-2012-06)", in the frame of the operation program of unique scientific and  
650 technical infrastructure of the Ministry of Science and Innovation of Spain. This support is  
651 gratefully acknowledged by the authors.

652 The authors would also like to thank José Enrique del Rey and Santiago Lacruz for their technical  
653 help on the setup of the experimental tools and their support during the measurements.

654



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756 Table 1: Operating conditions for the experimental mass flow rate measurements used for validation.

757 Table 2: Summary of nozzle and control orifices geometrical parameters.

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759 Table 4: Summary of the main parameters of the injector holder.

760 Table 5: Summary of the main parameters of the magnetic side of the solenoid valve.

761 Table 6: Summary of the main parameters of the mechanical side of the solenoid valve.

762 Table 7: Summary of the main parameters of the nozzle.

763 Table 8: Fuel properties at atmospheric pressure and the temperatures used for model validation.

764 Table 9: Effect of the fuel injection temperature on the control volume pressure and the friction  
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789 Figure 18: Normalized maximum needle lift reached for all the tested injector operating conditions.

790

$T_i$ [K]	$P_i$ [MPa]	$ET$ [ms]	$P_b$ [MPa]
253	40	0.25	4
273	70	0.5	
303	120	1	
353	180	2	
373			

791 Table 1: Operating conditions for the experimental mass flow rate measurements used for validation.

Orifice	$D_i$ [ $\mu\text{m}$ ]	$D_o$ [ $\mu\text{m}$ ]	$k$ -factor [ $\mu\text{m}$ ]
Nozzle (7 orifices)	146 $\pm$ 2	117 $\pm$ 1	2.8 $\pm$ 0.2
OZ	308	290	1.8
OA	256	259	-0.3

792 Table 2: Summary of nozzle and control orifices geometrical parameters.

Orifice	$C_{dmax}$	$Re_{crit}$	$CN_{crit}$	$C_c$
Nozzle (7 orifices)	0.96	5600	-	-
OZ	0.94	7000	-	-
OA	0.95	7200	1.24	0.71

793 Table 3: Summary of the relevant parameters obtained from the hydraulic characterization.

Element	Length [mm]	Diameter [mm]	Volume [mm <sup>3</sup> ]	Mass [g]
Rail	-	-	24000	-
Filter	-	0.8	-	-
HL1	7.38	1.38	-	-
HV1	-	-	13.5	-
HL2	8.75	1.1	-	-
HV2	-	-	1.85	-
HL3	17.05	1	-	-
HL4	40.64	1.5	-	-
HL5	49.9	1.5	-	-
HV3	-	-	81	-
HV4	-	-	25	-
1/2 NM	-	-	-	4.6
Element	Piston diameter [mm]		Rod diameter [mm]	Spring rate [N/m]
P1	4.3		0	-
LF	4.3		4.292	-
P2	4.3		4	-
ND	-		-	8.5 $\cdot$ 10 <sup>7</sup>
NSP	-		-	5250

794 Table 4: Summary of the main parameters of the injector holder.

Element	Length [mm]	Area [mm <sup>2</sup> ]
SM1	6.725	136.07
SM2	3	108.38
SM3	6.725	51.25
SM4	3	108.38
AG	0.08	31.82



Element	No. coils [-]	Resistance [ $\Omega$ ]
Coil	40	7.46

795 Table 5: Summary of the main parameters of the magnetic side of the solenoid valve.

Element	Length [mm]	Diameter [mm]	Volume [ $\text{mm}^3$ ]	Mass [g]
SO2	-	1.255	-	-
SO3	-	5.233	-	-
SO4	-	1.0	-	-
SL1	8.25	5.0	-	-
SL2	23.25	5.0	-	-
SV1	-	-	23	-
SV2	-	-	522.2	-
SV3	-	-	5.3	-
VM	-	-	-	3.1
Element	Piston diameter [mm]		Rod diameter [mm]	Spring rate [N/m]
SP1	3.6		1.6	-
SP2	4.3		3.6	-
SP3	12.5		4.3	-
SP4	12.5		1.5	-
SLF	4.5		4.3	-
SS	-		-	38070

796 Table 6: Summary of the main parameters of the mechanical side of the solenoid valve.

Element	Length [mm]	Diameter [mm]	Volume [ $\text{mm}^3$ ]
NL1	3.5	0.7	-
NO1	-	0.37	-
NL2	20.75	0.7	-
NV1	-	-	2.68
NL3	5	0.5	-
NV2	-	-	6.36
NV3	-	-	0.3
NST	-	0.6	-
Element	Piston diameter [mm]	Rod diameter [mm]	Mass [g]
NP1	4	3.16	-
NP2	3.16	1.81	-
1/2 NM	-	-	4.6

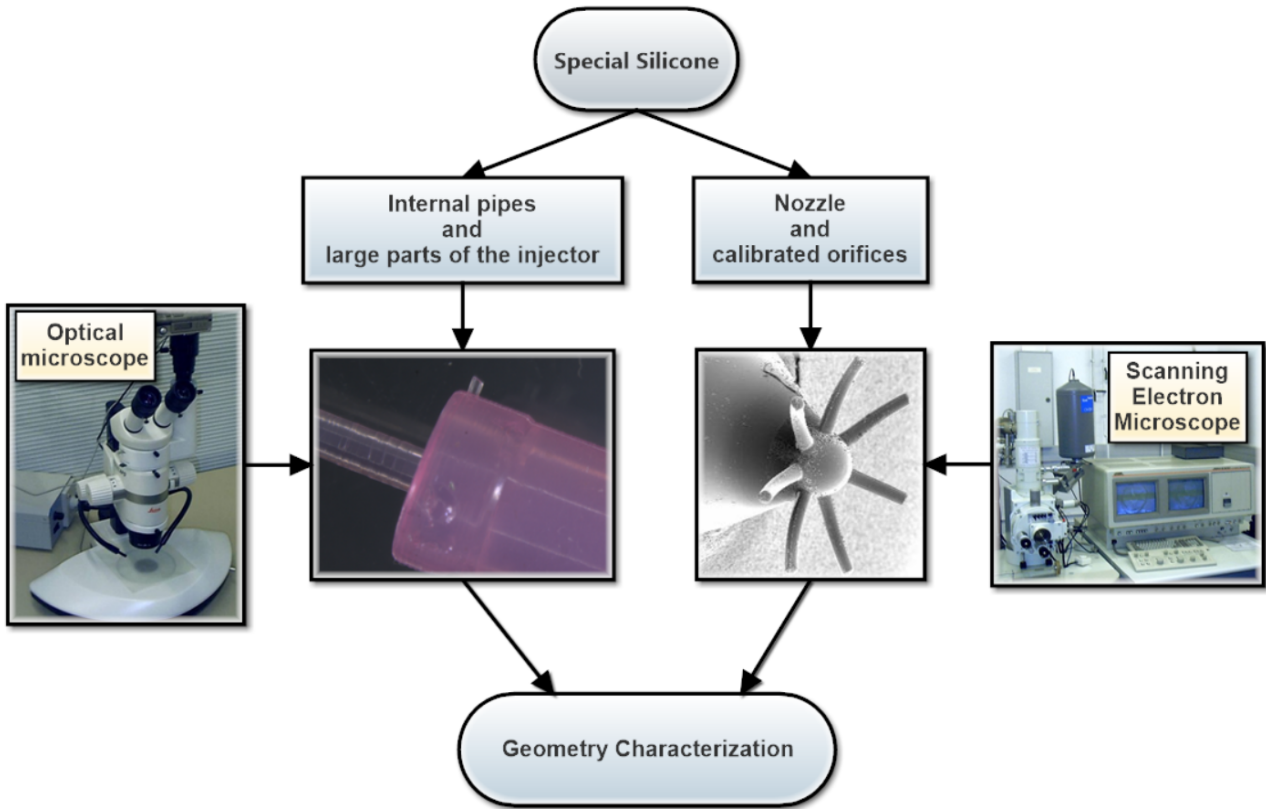
797 Table 7: Summary of the main parameters of the nozzle.

Fuel temperature [K]	Density [ $\text{kg/m}^3$ ]	Absolute viscosity [cP]
253	851	15.32
273	838	5.87
303	820	2.71
353	785	1.1
373	775	0.85

798 Table 8: Fuel properties at atmospheric pressure and the temperatures used for model validation.

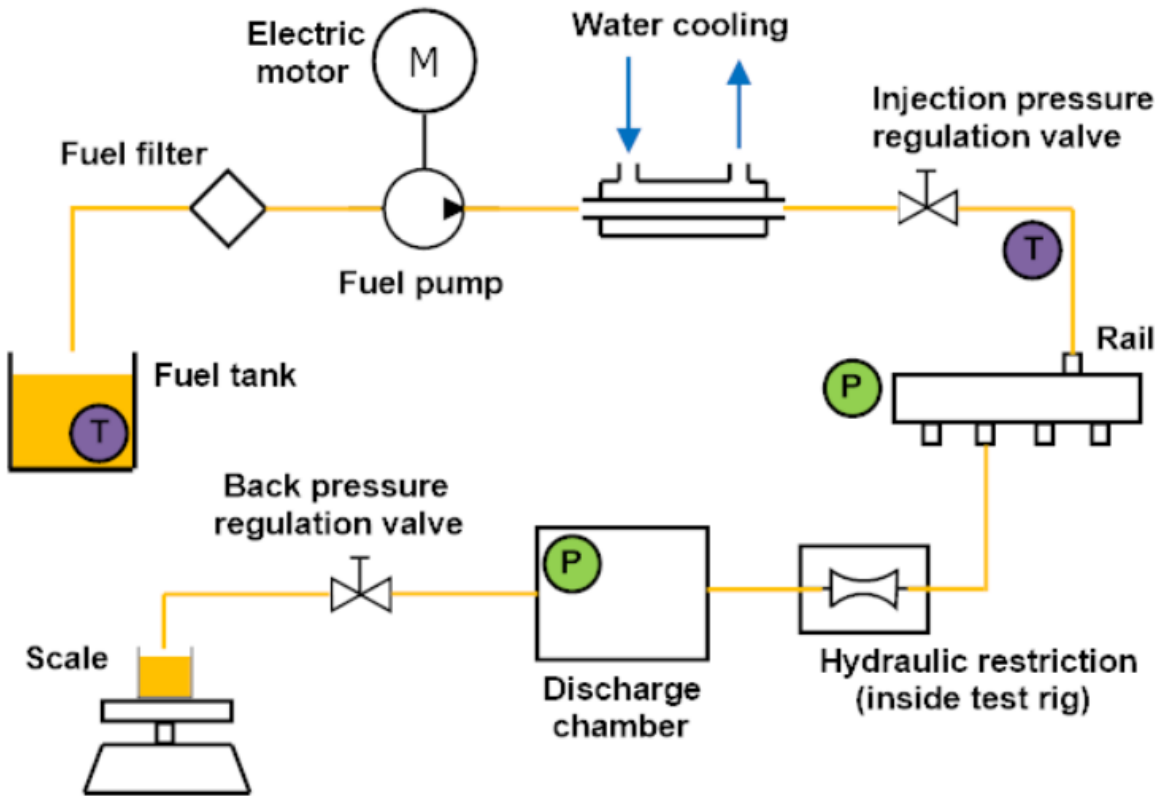
$T_i$ [K]	$\frac{P_{cv}}{P_{cv_{303K}}}$		$\frac{F_{fric}}{F_{fric_{303K}}}$	
253	0.852	↓	2.224	↑↑↑
273	0.952	↓	1.757	↑↑
303	1		1	
353	1.002	≈	0.415	↓↓
373	1.005	≈	0.346	↓↓↓

799 Table 9: Effect of the fuel injection temperature on the control volume pressure and the friction  
800 forces during the opening stage of the injector (time after SOE = 0.7 ms). Reference:  $T_i = 303$  K.



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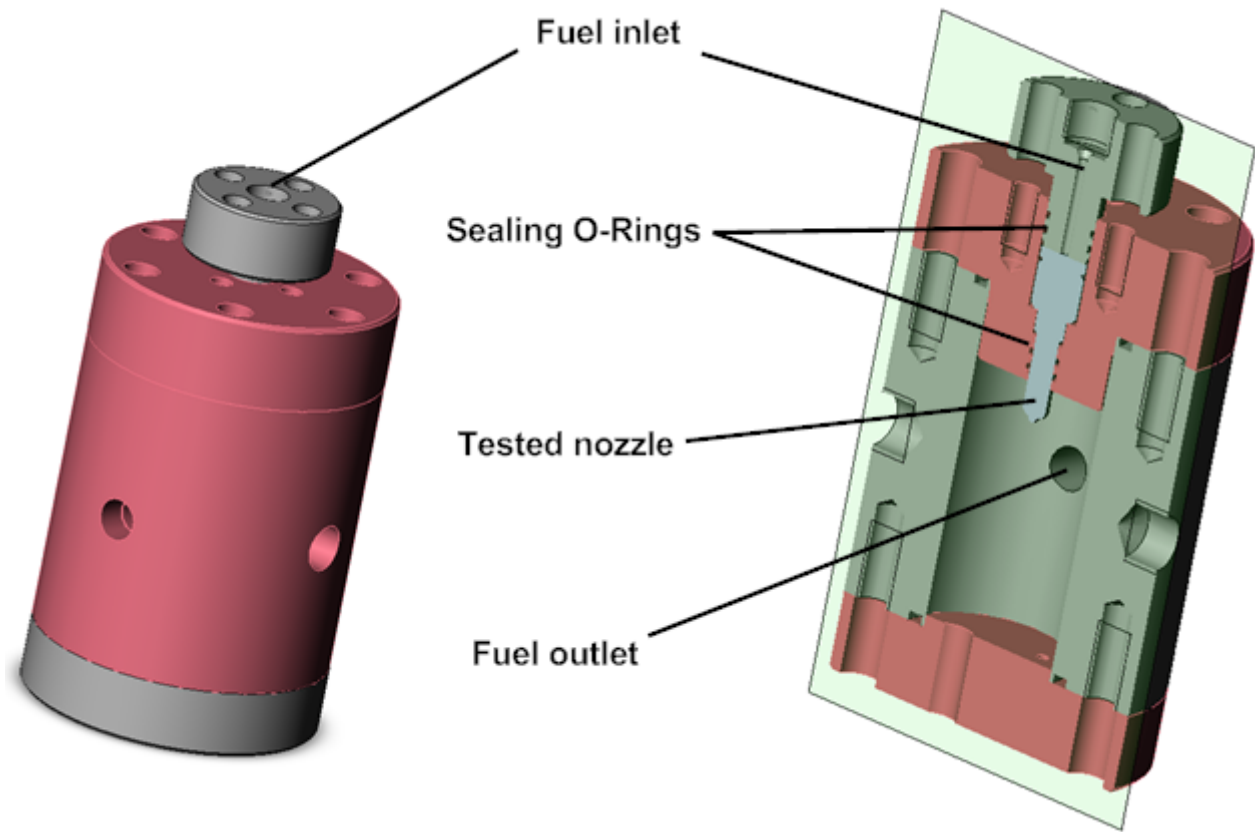
802 Figure 1: Injector dimensional characterization through the silicone methodology.



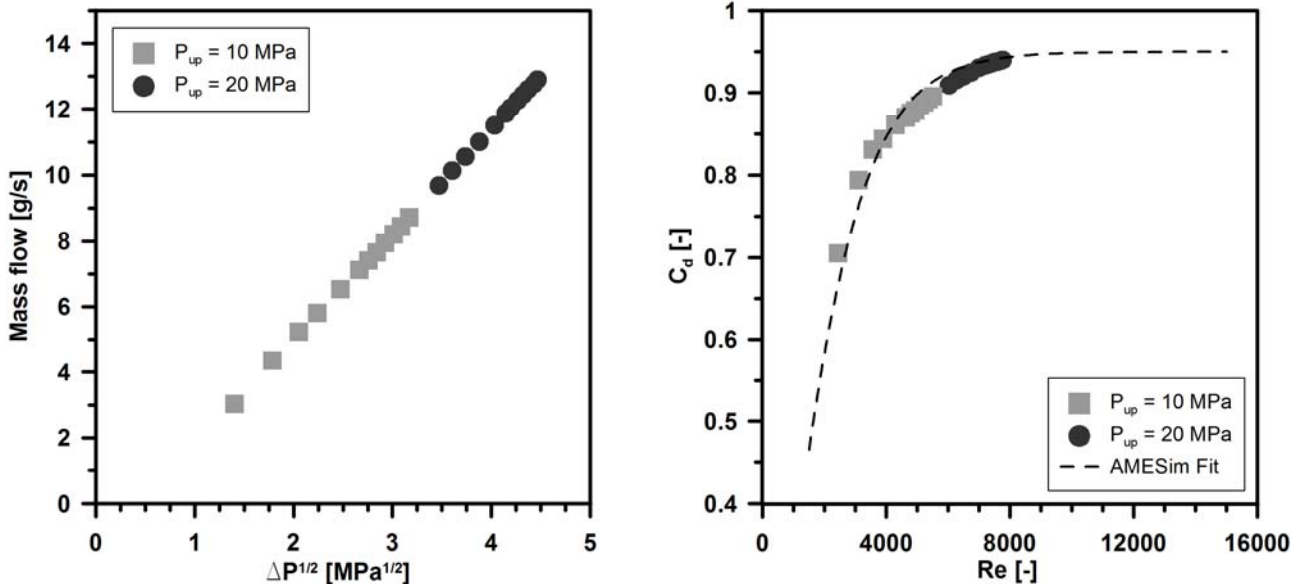
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804 Figure 2: Hydraulic characterization experimental setup.

Payri, R., Salvador, F.J., Carreres, M., De la Morena, J., "Fuel temperature influence on the performance of a last generation common-rail diesel ballistic injector. Part II: 1D model development, validation and analysis".

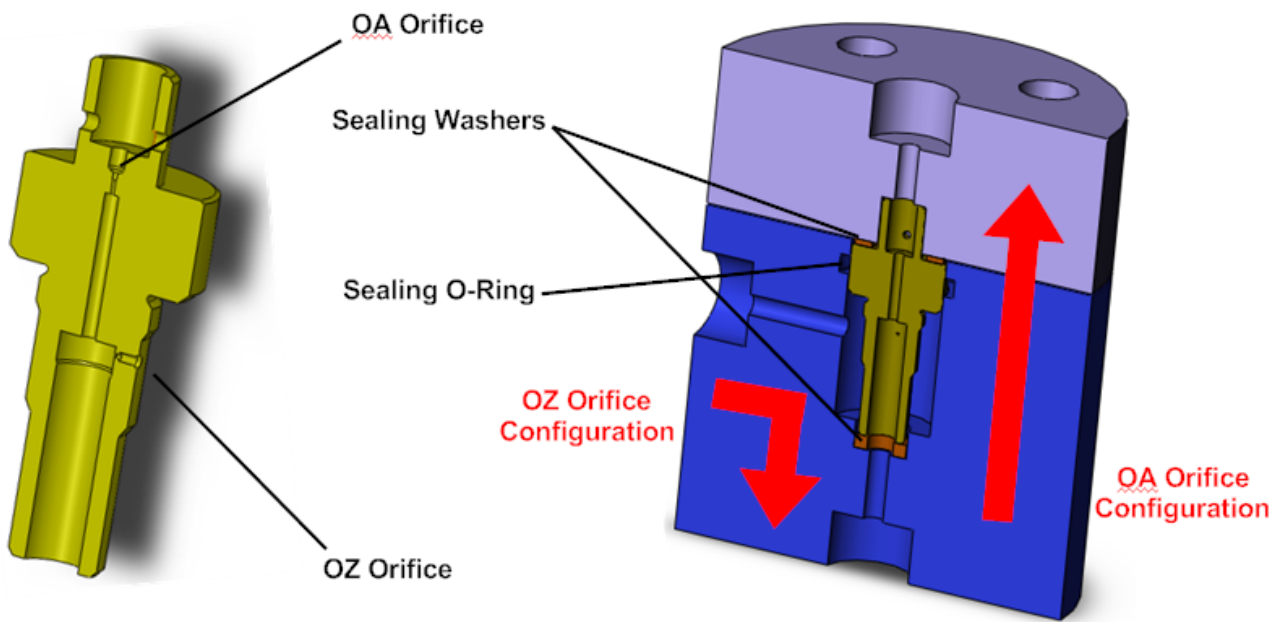


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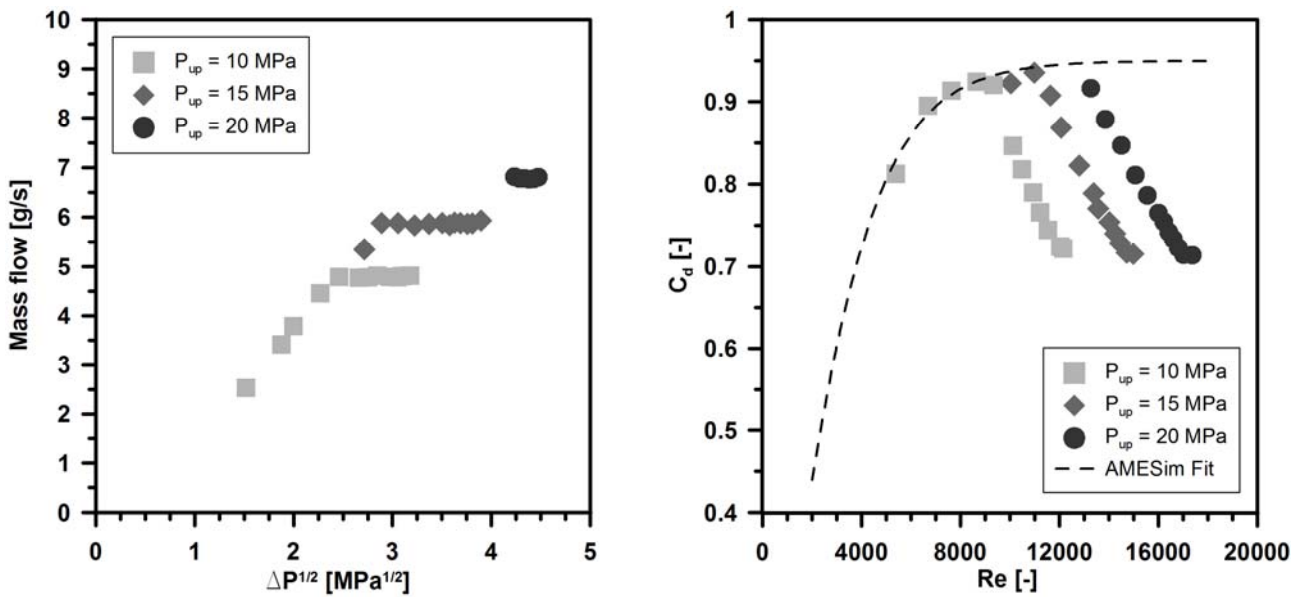
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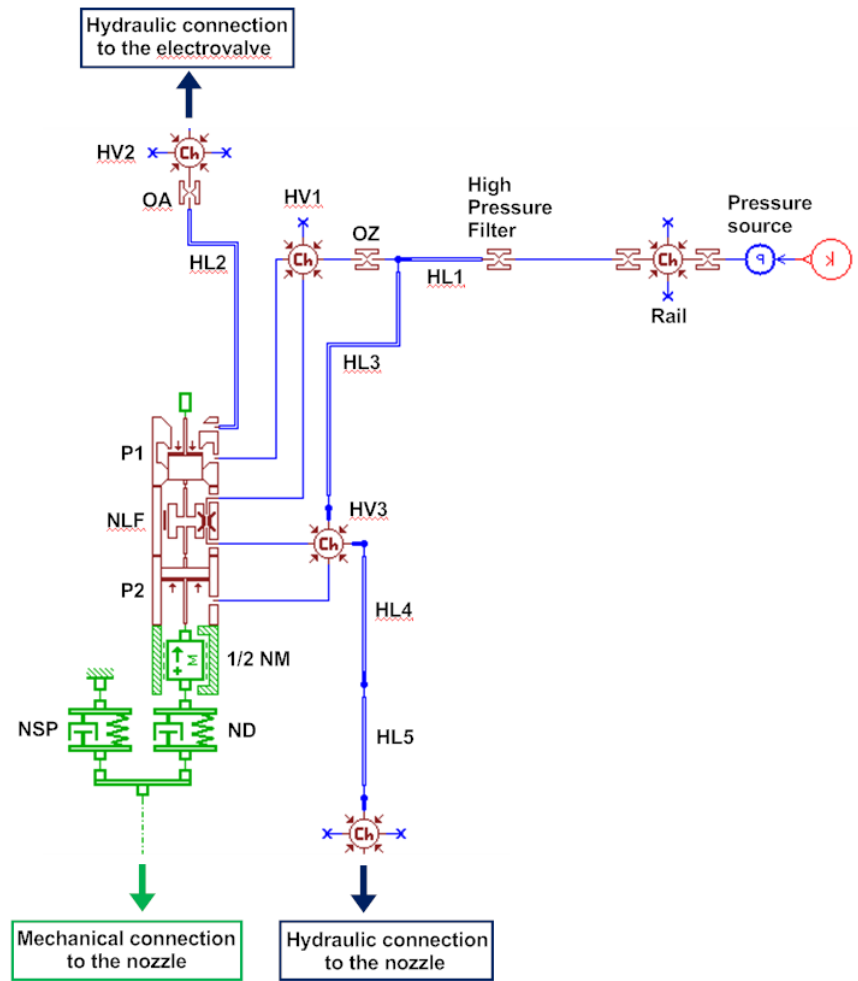
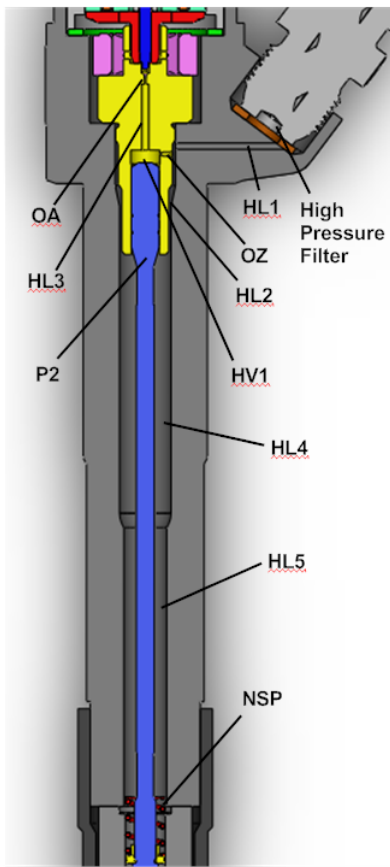
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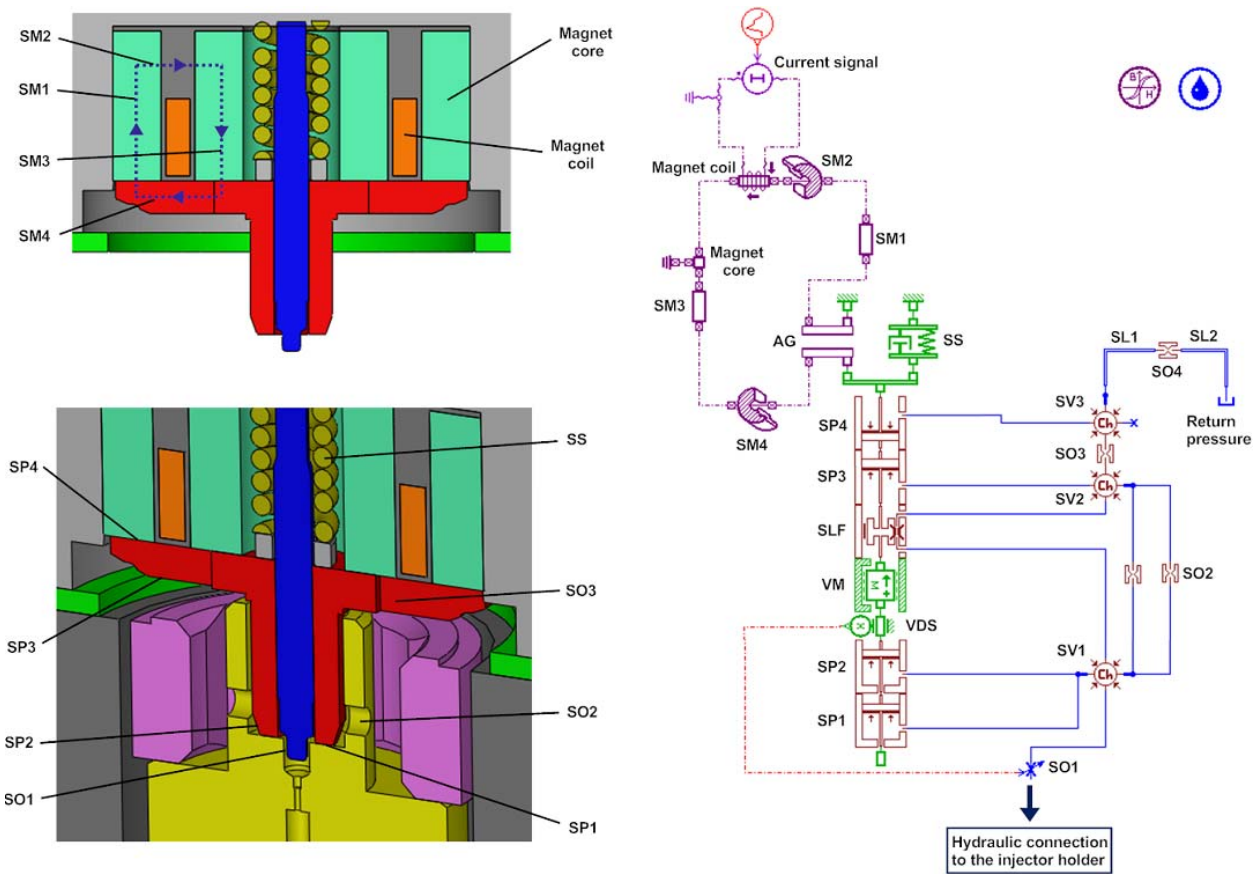
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816 Figure 7: Injector holder detail and model sketch.

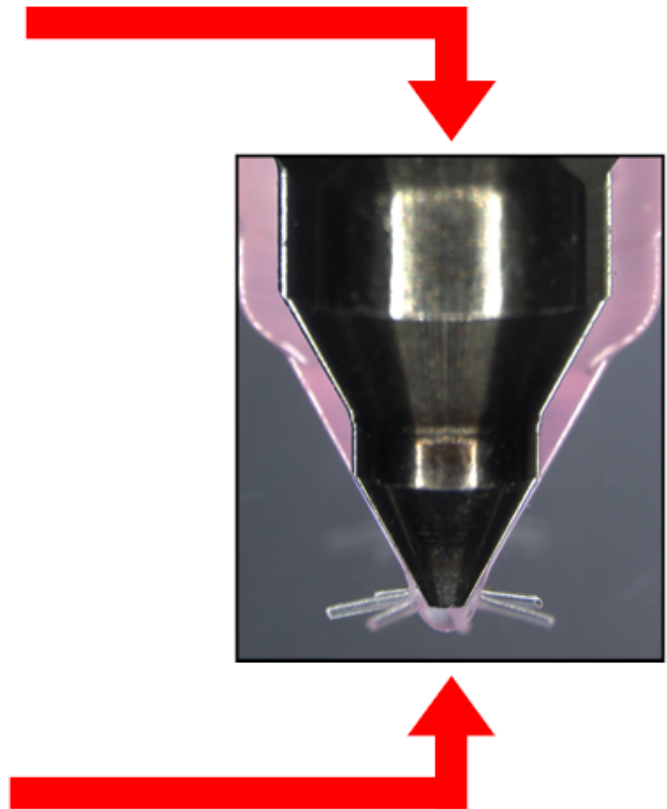
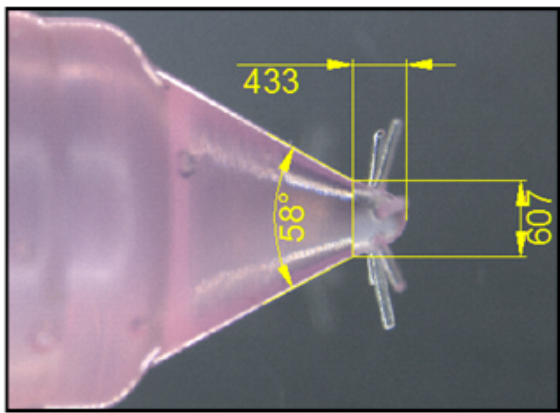
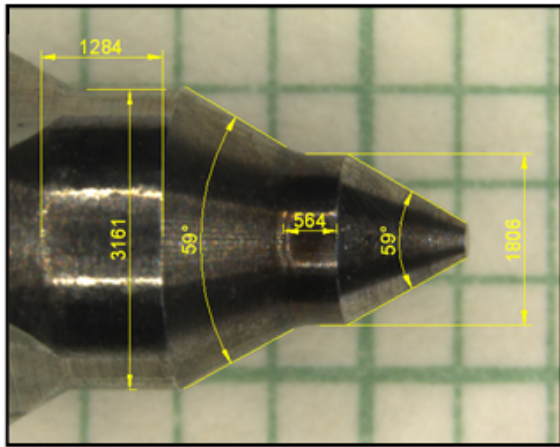


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 819 and model sketch (right).

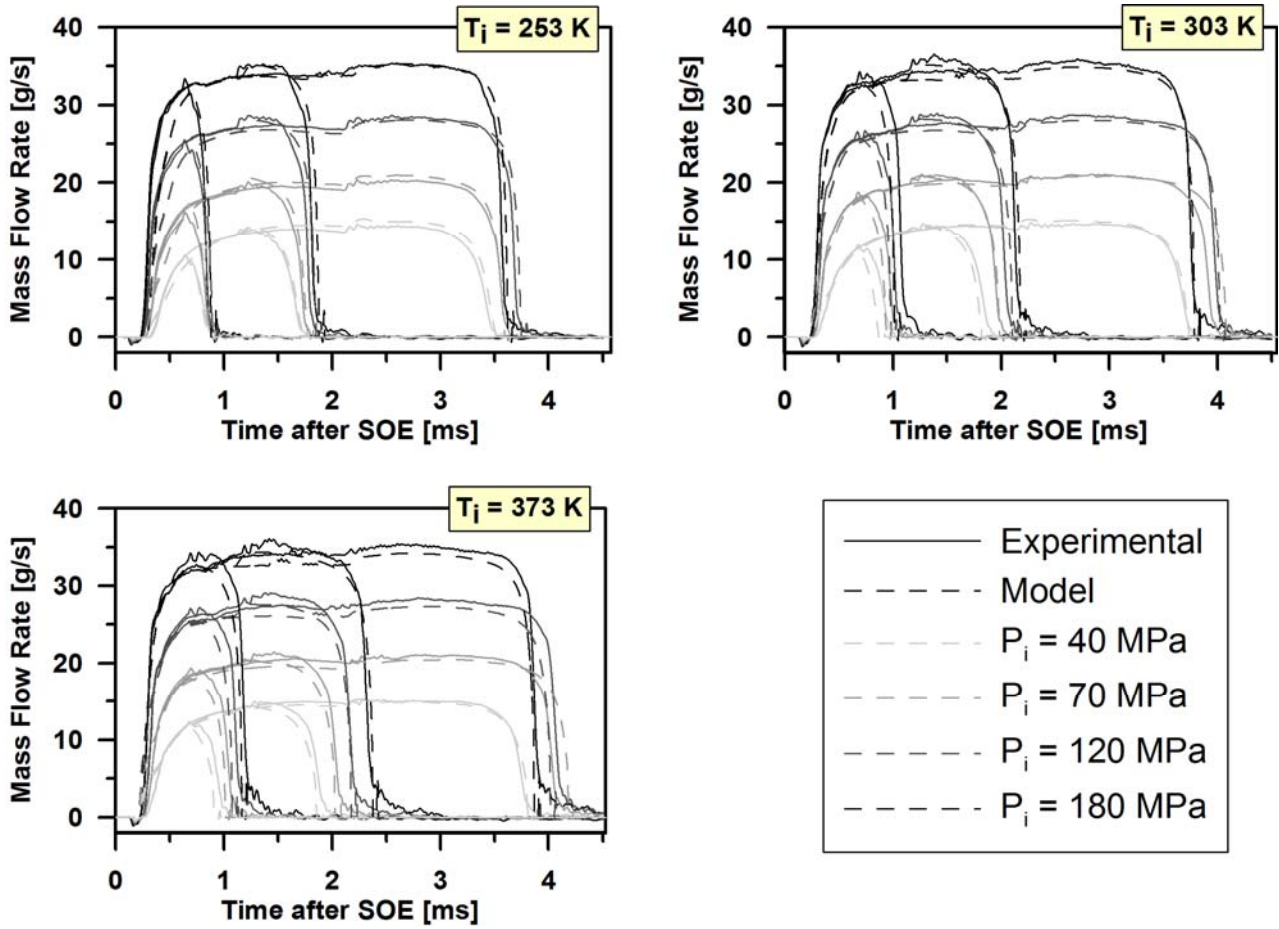






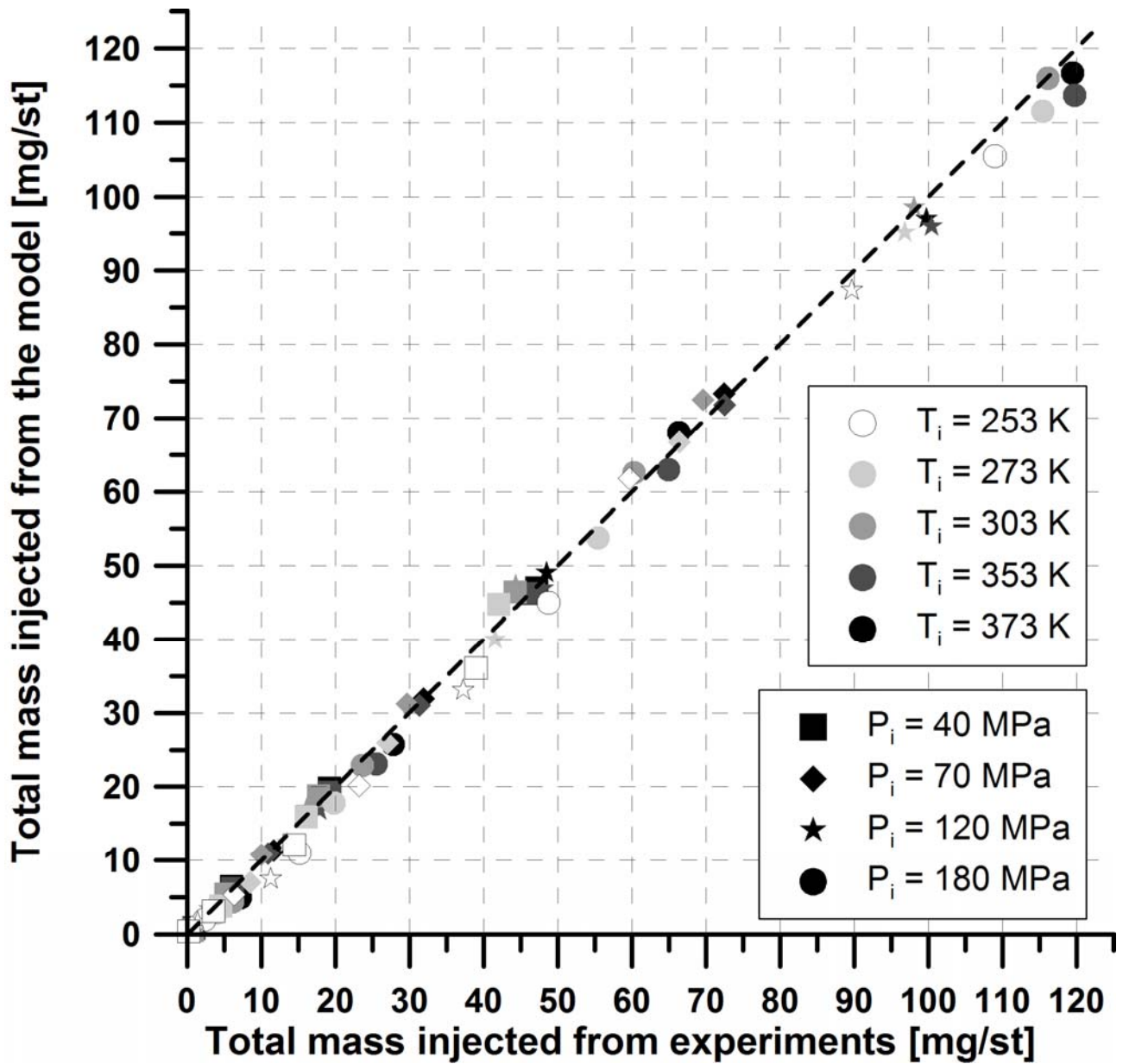
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823 Figure 10: Needle and nozzle optical microscope pictures overlapping.



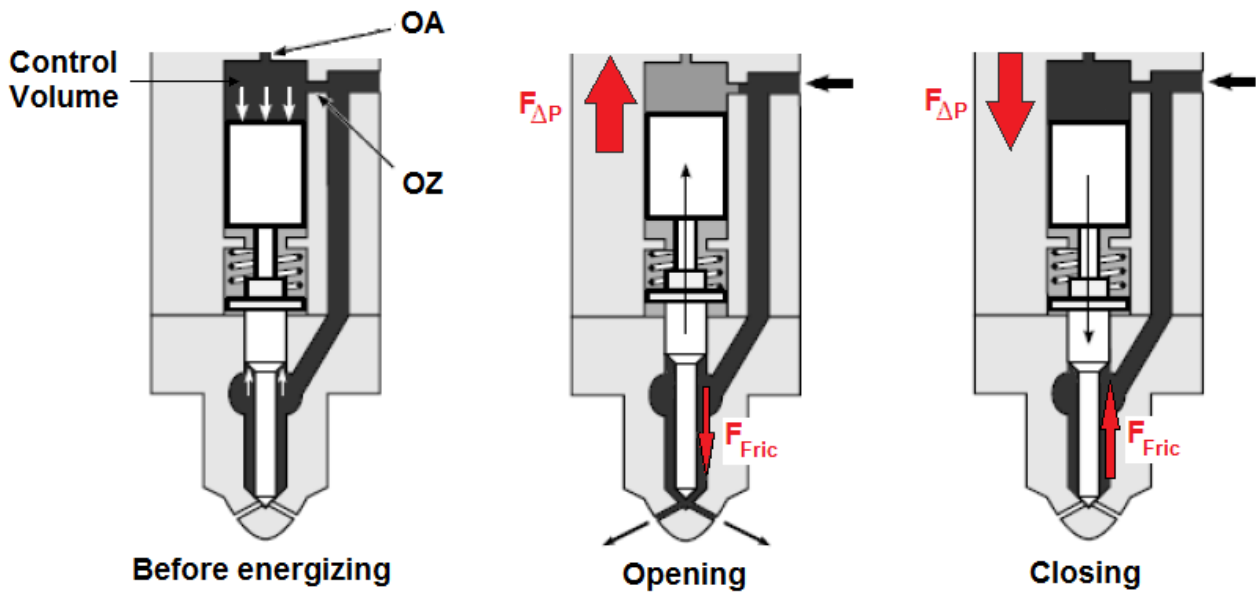
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825 Figure 11: Mass flow rate model versus experimental results comparison.



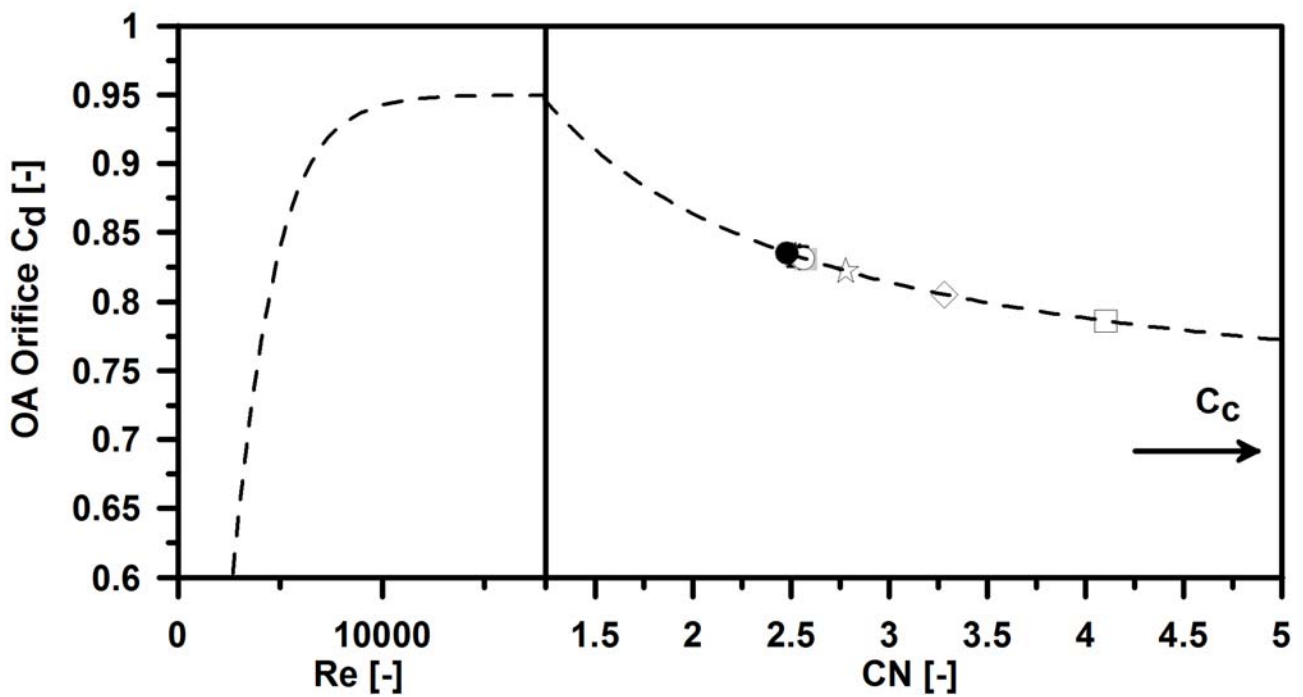
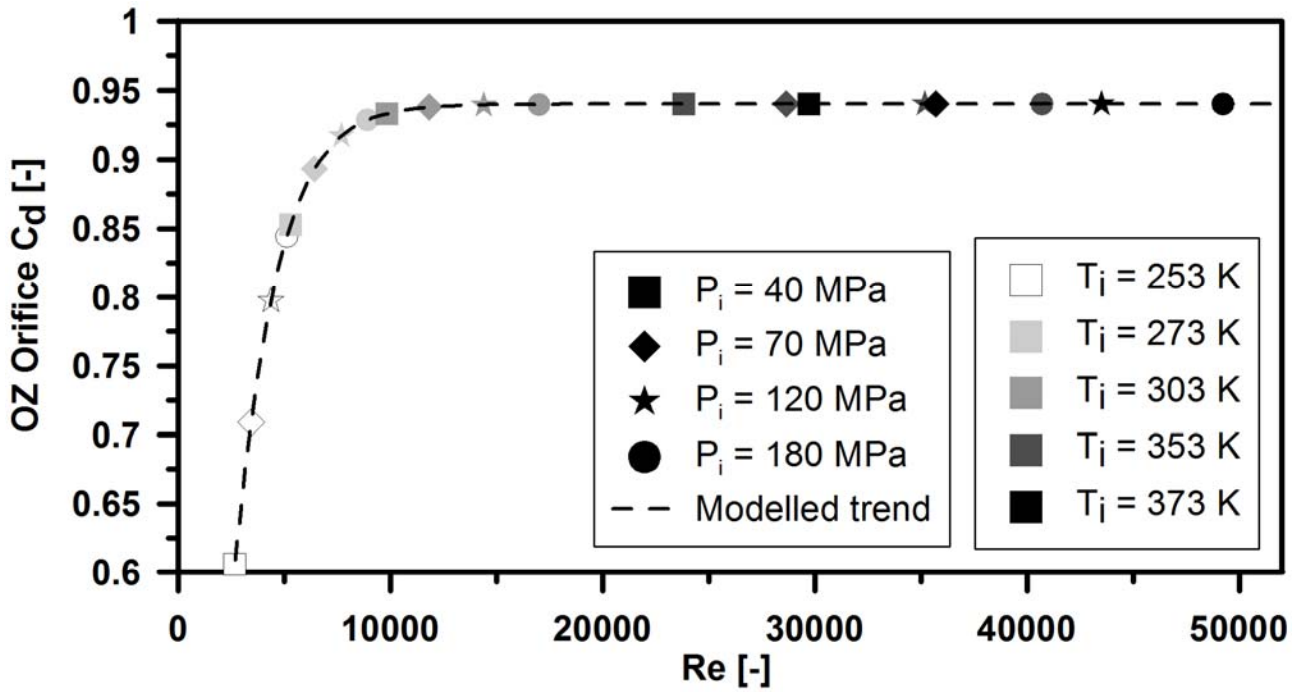
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827 Figure 12: Total injected mass: model versus experimental results comparison.



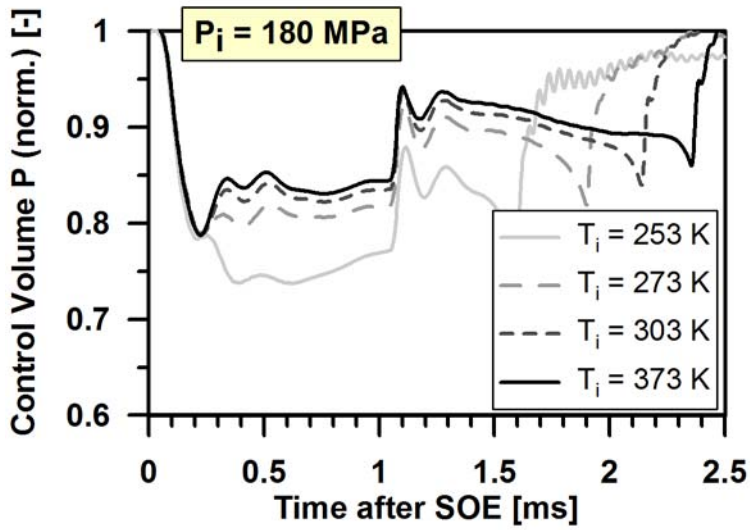
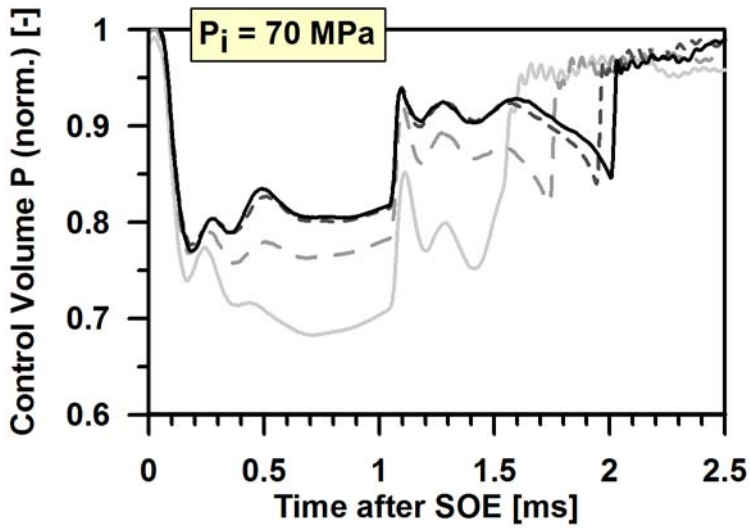
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829 Figure 13: Simplified sketch of the injector during several stages.



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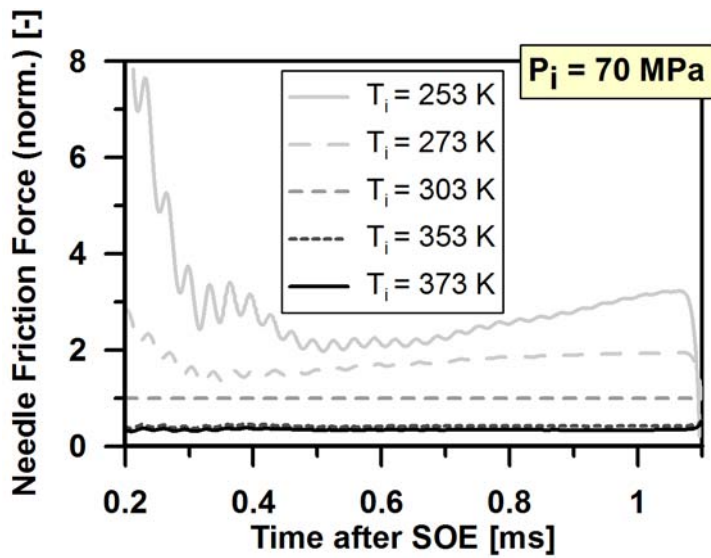
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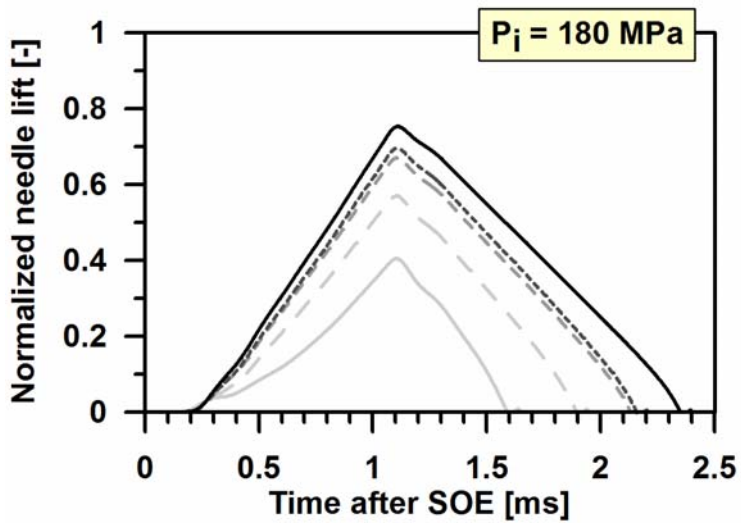
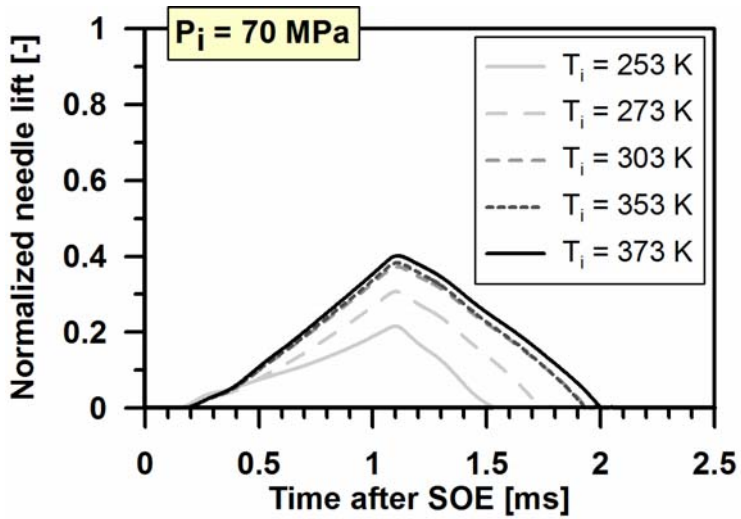
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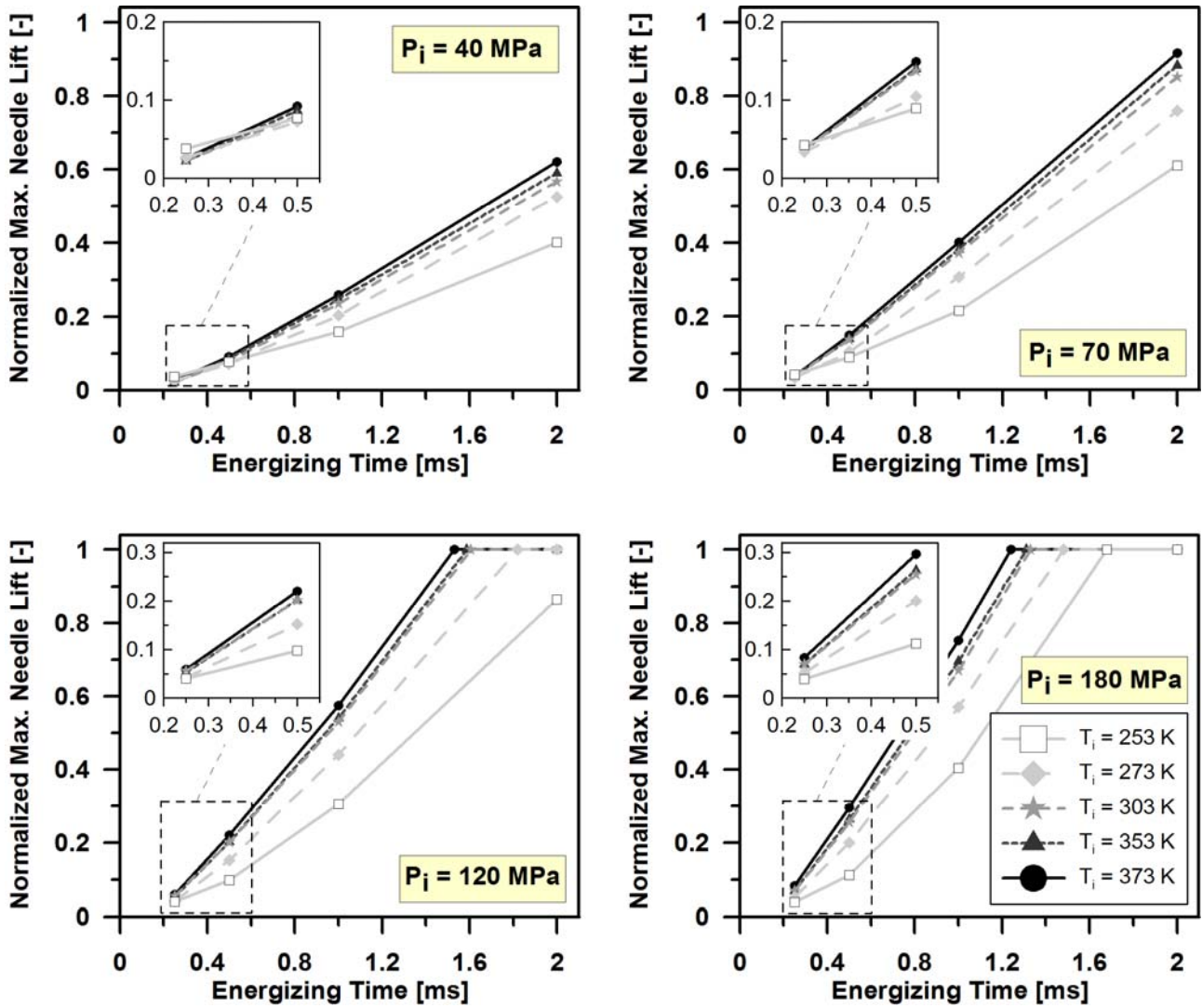
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842 Figure 17: Needle lift evolution for  $ET = 1 \text{ ms}$  and  $P_i = 70 \text{ MPa}$  (top) and  $180 \text{ MPa}$  (bottom) at the  
 843 different fuel temperatures tested.





844

845 Figure 18: Normalized maximum needle lift reached for all the tested injector operating conditions.