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## An energy-efficient metro speed profiles for energy savings: application to the Valencia metro

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### Abstract

Nowadays one of the main priorities for metro line operators is the reduction of energy consumption, due to the environmental impact and economic cost. In order to achieve this objective different strategies can be applied, normally focused into rolling stock, infrastructure and/or operation. Considering short-term measures and related to the traffic operation strategies, different approaches are being researched. One of the most effective strategy which reduce net energy consumption is the use of efficient driving techniques. These techniques produce a speed profile between two stations that requires the minimum net energy consumption, without degrading commercial running times or passenger comfort. In this paper, a computer model for calculating the metro vehicles speed profiles minimizing the energy consumption was developed. The equations considered in the model represent the behavior of a single vehicle operated under manual driving, subject to different constraints such as the headway, cycle time, distances and acceleration limits. The proposed model calculates different commands to be systematically executed by the driver. The resulting simulator has been tuned by means of on board measurements of speed, accelerations and energy consumption obtained along different lines in Metro de Valencia network. For this purpose, different scenarios are analyzed to assess the achievable energy savings. In general terms and comparing with the actual energy consumption, the solutions proposed can reduce the net energy consumption around 19%.

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## 1. Introduction

Nowadays metros systems are playing important roles in modern cities. Since metro systems consume huge amounts of energy each day, reducing the intensity of traction energy cost can lead to great economic growth and environmental protection benefits.

In order to reduce traction energy, two main methods are timetable optimization and energy-efficient driving (eco-driving). On the first case, considering that most trains are equipped with regenerative-braking systems, timetable optimization is focused on synchronize the movement of trains to reduce the global energy consumption from substations by maximizing the use of regenerative energy. A large number of timetable optimization models have been developed with different objectives, such as trip time by Szpigel (1973), passenger waiting time by Nachtigall (1997), transport demand by Cordonea and Redaelli (2011), energy consumption by Nourbakhsh and Ouyang (2010), delay time by Liebhena et al. (2010), reliability by Salicr a et al. (2011), operation cost by Li et al. (2013), and robustness by Cacchiani and Toth (2012). However, most of these techniques only considered the determination of the optimal timetable without some disturbances, which are very frequently and modifies substantially the effectivity of the solution.

On the other hand, the objective in eco-driving techniques is the reduction of the traction energy by optimizing speed profiles. The optimal speed contains an effective combination of four basic train regimes: acceleration, cruising at constant speed, coasting and deceleration.

As previously, an important number of projects and test were been developed in terms of speed profiles by Asnis et al. (1985), Calderaro et al. (2014) and Gong et al. (2014), manual driving for freight trains by Lukaszewicz (2001), genetic algorithms by Khmelnsky (2000) and Bigharaz et al. (2014) and high speed driving speed profiles by Sicre et al. (2012). In addition, other recent researches were focused on the use of energy storage systems by Fournier, (2014) and Wang et al. (2014).

Unlike the above studies, the motivation for this work is to approach reduction in traction energy on an experimental approach. Therefore, an energy measurement system is presented, which acquires the most important quantities on-board the train, as a first step to determine the best approach to reduce energy consumption. Then an algorithm based on simulation of the single train motion is proposed in order to design optimal speed profiles, considering the regenerative braking energy. The algorithm has been constructed and validated with real measures obtained.

## 2. Characterisation and energy flow of Valencia metro network

Energy costs represent a considerable financial burden for transport companies, and after staff is the second largest budget item for operators. The energy consumption on metropolitan rail networks consists of two principal aspects: the traction energy for the tractions of its trains and the additional energy to supply systems and for example, lightening or elevators in stations, energy for depots, and so forth.

The share of the traction energy is normally much more than half of the total energy consumption. For each rail network, the traction energy consumption is determined by many dynamic factors such as driving techniques, characteristics of the trains, alignments and natural environment of the tracks, operation management, etc.

### 2.1. Valencia metro network

Valencia metro operator agency is called Ferrocarrils de la Generalitat Valenciana (FGV), which operates nine narrow-gauge lines (equal to 1000 mm). Its network consists of more than 156 km, of which around 27 km is underground (see Fig. 1). The tension in metro lines are 1500 V DC and total annual energy consumption is around 64.5 GWh.



Fig. 1. Detail of FGV metro city center network. Source: FGV.

The underground section of the lines (which represents around 17 % of the total length) are equipped with automatic train operation (ATO), in which responsibility for operation management of the trains is transferred from the driver to the train control system. For each inter-station, a set of four speed commands are possible, obtaining four different travel times and energy consumptions. In this work, only ATP segments will be analyzed and performed due that ATO system incorporates some operational and technical constraints that have not been able to study.

2.2. Rolling stock

The metro Valencia lines are based on the Vossloh 4300 series, composed by four or five cars. As regards the maximum operation performances, it is able to reach a maximum speed equal to 80 km/h, with acceleration and deceleration maximum rates of 1.1 m/s<sup>2</sup> and 1.2 m/s<sup>2</sup>, respectively. Other principal characteristics, for the four carriages unit, are summarized in table 1.

Table 1. Rolling stock characteristics.

Rolling stock (Vossloh series 4300)	Column A (t)
Tension	1.500 V DC
Total traction power	1480 kW
Weight	122,85 t
Length	60,49 m
Composition	M-R-R-M
Capacity	588 passengers (116 seating and 472 standings)

3. Energy measurement campaign

Despite urban rail operators' desire to measure the energy consumption of its rolling stock, a standardized measurement procedure is not yet fully implemented to assist with this process.

In order to gather reliable data for the analysis of energy consumption optimization, three monitoring devices were installed on a single metro train operating in the Metro Network of Valencia. The devices were three DC voltage and current measuring systems developed by Mors Smitt (model MSAV-DC), as seen Fig.2.



Fig. 2. DC voltage and current measuring device installed on metro roof

These devices were placed in the train so as to measure the main energy consumptions, including the overall energy transmitted from the catenary to the train (energy consumed) and backwards (energy regenerated), the train auxiliary systems (i.e. heating, lights, automatic doors, etc.) and the energy consumed by the rheostatic braking system according to European Standards (EN-50463). The sampling frequency of the electric devices is 1 Hz, while the speed was measured at 100 Hz. All the data gathered from these devices was stored in a laptop placed in the train cabin. Additionally, the train speed was measured by means of an odometer and stored in the same laptop.

#### 4. Energy consumption model

Energy-efficient train operations is a very difficult optimization problem due that timetables and speed profiles should be controlled to reduce the tractive energy consumption under dynamic constraints such as speed limits, train interactions, travel times and distances. To maintain the actual level of service, actual travel times between two consecutive stations have not been modified. The model includes three independent modules (train dynamics, motor, and energy consumption), with an automatic generator of every possible speed profile.

##### 4.1. Train dynamics

Railway movement is seen as a one-dimensional problem located in the longitudinal direction of the track. The train motion is governed by the equation 1:

$$F_T - F_B - F_R - F_C - F_G = m_{eq} \cdot a \quad (1)$$

where  $F_T$  is the traction force from the motors,  $F_B$  is the braking force,  $F_R$  is the running resistance,  $F_C$  is the running resistance when negotiating curves,  $F_G$  is the gradient resistance,  $m_{eq}$  is the equivalent mass of the train (which includes the passenger mass and the rotational inertia of the rotating masses) and  $a$  is the train acceleration.

##### 4.2. Traction force

This term includes the force applied by the motor on the wheels. This force is transmitted to the rail through the wheel-rail contact. The traction force of the motors can be calculated as expressed in equation 2:

$$F_T = P_{total} \eta / v \quad (2)$$

where  $P_{total}$  is the total traction power,  $\eta$  is the efficiency of the full traction chain and  $v$  is the running speed.

#### 4.3. Braking force

This term represents the force applied in order to decrease the speed of the train. The force is transmitted through the wheel and rail interface, so its magnitude, is limited by the adhesion of interfaces, as in the previous case. The 4300 Vossloh train is equipped with dynamic and mechanic brakes. The total braking force is the summation of all the braking systems acting in each moment.

On the one hand, the dynamic braking is performed by the motors; so the braking force is calculated following the model in equation 2, but with an opposite sign. Then, the dynamic braking power is limited by the total power of the motors and the dynamic braking force by the adhesion in the wheel-rail interfaces for the powered wheelsets. When the motors are acting as brakes, the recovered energy can be either returned to the overhead power supply lines or dissipated in resistances (braking resistances), depending on the conditions of the traffic. It is assumed that the maximum dissipated power in the braking resistances is equal to the total traction power of the motors.

#### 4.4. Running resistance

Running resistance is the summation of different forces caused by many factors and impede the forward motion of a train. Normally is obtained by adding all individual elements together and it can be calculated as shown in equation 3.

$$F_R = A + B \cdot v + C \cdot v^2 \quad (3)$$

where A, B, C are positive constants for a specific train and  $v$  is train velocity. A, B and C are usually obtained from field tests. In this study, values are provided by the manufacturer of the unit.

#### 4.5. Curve resistance

This term represents the resistant force which appears on the wheelsets of the train, when traversing a curve. When a train runs on a curved section its instantaneous moving direction is tangent to the curve and different external forces act on the vehicle and on its wheelsets. In this situation, wheelsets try to move laterally on the track and find the radial position whilst primary suspension opposes this movement. Then, extra resistance to motion is experienced by the train, and it is modelled in equation 4.

$$F_C = k/R \cdot m_t \quad (4)$$

where  $k$  is a constant which depends on the track gauge,  $R$  is the radius in meters and  $m_t$  is the total train mass in kilograms.

#### 4.6. Gradient resistance

Considering the gravity force, when the plane of the track is inclined two forces can be described: the force along the gradient and the force normal to the incline. The equation that gives the gradient resistance can be expressed as Equation (5).

$$F_G = m_t \cdot g \cdot \sin \alpha \cong m_t \cdot p_t / 1000 \quad (5)$$

where  $\alpha$  is the angle of gradient in radians,  $g$  is the acceleration of gravity in  $m/s^2$  and  $p_t$  is the coefficient of grade resistance (‰).

#### 4.7. Energy consumption

The estimation of total energy consumption is based on three terms: the energy used by the traction motors, the energy consumption of auxiliary systems, and the energy recovered from regenerative braking. For our purposes only traction and regenerative energy are considered, considering that energy used by auxiliary systems depends basically on travel time. In addition, the energy consumption model with regenerative braking systems usually implies an energy consumption model of the entire line in order to consider regenerate energy used by other train in the same electric stretch.

The purpose of this paper is to optimise speed profiles for a single train between two consecutive stations in order to minimise its energy balance. This means that the travel is constrained to its timetable and to the forecasted travel demand.

The energy consumption ( $E$ ) for single train running along a given track is calculated as the mechanical power delivered by the traction force minus the energy recovered from the dynamic braking, which is returned to the overhead power supply. These two terms are represented in equation 6.

$$E = \int F_T \cdot v \cdot dt - \int F_B^* \cdot v \cdot dt \quad (6)$$

where  $F_B^*$  is the dynamic brake force which is used to regenerate energy to the overhead power supply.

### 5. Model validation

In order to adjust and validate the simulator, the proposed model was applied to different lines with manual driving of the Valencia metro network under real operative constraints by adjusting the parameters. The results obtained have been compared with measured data registered in the monitoring campaign. The simulated running times differ on average 0.5 % from measured times, and the difference between net energy consumptions less than 2.5 % for all cases, as shown in table 2.

Table 2. Energy consumption comparison results.

Stretch	Measured values (kWh)	Simulated values (kWh)	Error (%)
L1 - Bétera/Seminari CEU	15.48	15.39	-0.60
L1 - Seminari CEU/Bétera	53.99	54.00	0.03
L2 - Liria/Eliana	17.94	18.08	0.79
L2 - Eliana/Liria	31.52	31.27	-0.80
L3 - Rafelbuñol/Almásera	42.43	43.28	2.01
L3 - Almásera/Rafelbuñol	62.48	62.12	-0.58
L7 - Val.Sud/Torrent	31.95	32.68	2.26
L7 - Torrent/Val.Sud	20.01	19.92	-0.42

### 6. Design of efficient speed profiles

Once validated, the model allow us to compare the speed profiles and energy consumption obtained with real examples, measuring the reduction in energy that model provides. To enable the simulation of manual driving strategies, different strategies can be managed with a set of configurable parameters such as acceleration-deceleration rates, coasting criteria and speed restrictions. The most efficient techniques to reduce the energy consumption are holding speed without braking and performing a coasting process before braking to reach a speed

limit or a stopping station. The model executes this commands taking into account the speed and running time constraints. Under these conditions, a wide range of solutions can be obtained and analyzed.

As example, in Fig. 3 the real and simulated speed profiles between two stations are reported. The simulation uses the real time travel as input, so the optimized curve does not significantly deviate from the reference run. The result obtained covers the single section length with a total running time of 87 seconds which is the actual running time for this stretch, and the savings in net energy consumption reaches 10 %.

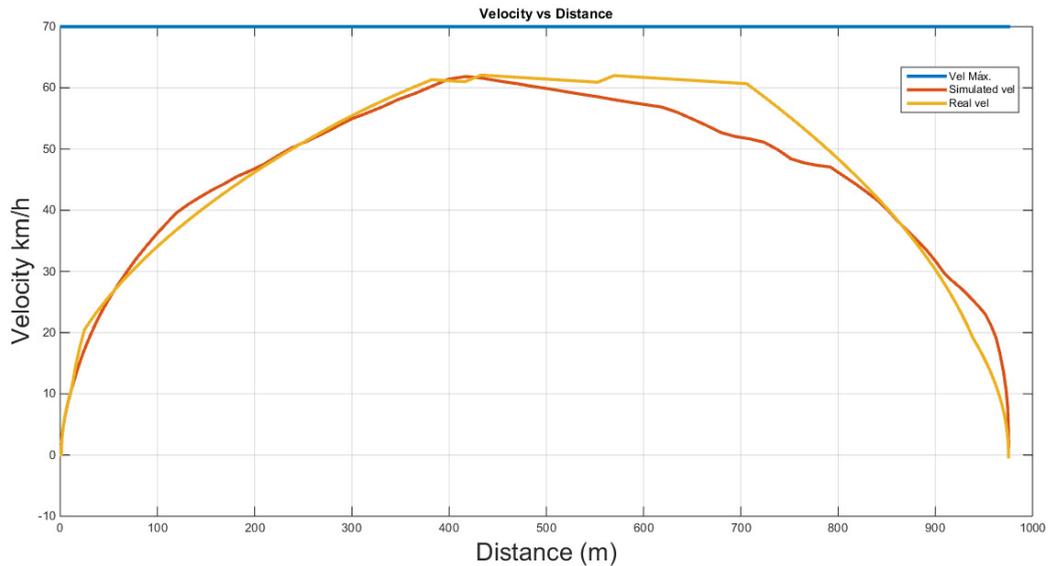


Fig. 3. Optimal speed profile (red) versus real speed profile (yellow).

Other results for different lines are showed in table 3. The energy reduction varies between 16% and 26%, depending on the track considered. Only in one case of study (L1) the energy optimization has not been possible.

Table 3. Energy savings obtained.

Stretch	Measured values (kWh)	Simulated values (kWh)	Error (%)
L1 - Bétera/Seminari CEU	4.23	4.23	0.00
L1 - Seminari CEU/Bétera	10.24	7.52	26.78
L2 - Lria/Eliana	7.41	5.88	20.59
L2 - Eliana/Lria	9.99	7.87	21.23
L3 - Rafelbunol/Almsера	4.20	3.33	20.66
L3 - Almsера/Rafelbunol	6.12	4.65	23.95
L7 - Val.Sud/Torrent	5.38	4.50	16.59
L7 - Torrent/Val.Sud	4.91	3.95	19.48

## 7. Conclusions

Previous works have already highlighted the importance of the optimal design of speed profiles, taking into account timetable constraints. In this paper, a model is proposed for the design speed profiles to minimize the energy consumption in the Valencia metro network under manual driving.

The tool presented is based on a mechanical and an electrical model. The mechanical model recalculates train speed and position in every simulation step. The acceleration parameter is obtained through the traction force, the aerodynamic resistance, the track gradient and curvature resistance, the braking force and the dynamic train mass.

The energy consumption is calculated knowing the traction force and the speed in all simulation steps. During the braking process is also possible to determine the energy recovered in the train.

Finally, the model proposed was tested on a real-scale case involving a suburban line. The simulations have shown to obtain a great reduction in the consumption of net energy of around 16 - 26 %.

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