Computational modeling of internally cooled wet (ICW) electrodes for radiofrequency ablation: Impact of rehydration, thermal convection and electrical conductivity

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Short running title: Modeling of internally cooled wet electrodes for RFA
Abstract

Purpose: 1) To analyze rehydration, thermal convection and increased electrical conductivity as the three phenomena which distinguish the performance of internally cooled electrodes (IC) and internally cooled wet (ICW) electrodes during radiofrequency ablation (RFA), 2) Implement a RFA computer model with an ICW which includes these phenomena, and 3) Assess their relative influence on the thermal and electrical tissue response and on the coagulation zone size.

Methods: A 12-minute RFA in liver was modeled using an IC electrode (17G, 3 cm tip) by an impedance-control pulsing protocol with a constant current of 1.5 A. A model of an IC electrode was used to compare the ICW electrode performance and the computational results with the experimental results.

Results: Rehydration and increased electrical conductivity were responsible for an increase in coagulation zone size and a delay (or absence) in the occurrence of abrupt increases in electrical impedance (roll-off). While the increased electrical conductivity had a remarkable effect on enlarging the coagulation zone (an increase of 0.74 cm for differences in electrical conductivity of 0.31 S/m), rehydration considerably affected the delay in roll-off, which, in fact, was absent with a sufficiently high rehydration level. In contrast, thermal convection had an insignificant effect for the flow rates considered (0.05 and 1 mL/min).

Conclusions: Computer results suggest that rehydration and increased electrical conductivity were mainly responsible for the absence of roll-off and increased size of the coagulation zone, respectively, and in combination allow the thermal and electrical performance of ICW electrodes to be modeled during RFA.
Keywords: Computer modeling, internally cooled electrode, radiofrequency ablation, electrical conductivity, rehydration

1. Introduction

Radiofrequency ablation (RFA) is a minimally invasive procedure using radiofrequency (RF) electrical currents to selectively heat tumors, causing their destruction by thermal coagulative necrosis [1,2]. The roll-off phenomenon is produced during heating and consists of a sudden increase in electrical impedance caused by the charring and dehydration of the tissue around the electrode [3]. When roll-off occurs the entire electrode is completely encircled by the dehydrated tissue, which obstructs energy diffusion and limits the coagulation zone size. Changing the electrode design can sometimes overcome this drawback; for instance, internally cooled (IC) electrodes prevent the adjacent tissue from charring and consequently can produce larger coagulation zones than conventional (dry) electrodes [4]. Although IC electrodes are commonly used, the coagulation zone obtained by them is limited to \(\approx 2.5 \text{ cm} \) [5]. In order to achieve larger coagulation volumes, wet electrodes infuse isotonic (0.9\% NaCl) or hypertonic (20\% NaCl) saline into the tissue through one or more perforations in the electrode surface [6,7]. This interstitial infusion enhances RF power deposition, improves electrical and thermal conductivity of tissue during ablation and prevents the tissue from vaporizing and charring [6-9]. Finally, internally cooled wet (ICW) electrodes combine saline infusion and internal cooling of the electrode [10] and have been clinically used for RFA of hepatic tumors [11]. Previous experimental studies have shown that ICW electrodes can create larger coagulation zones than IC and wet electrodes separately [12-14]. This could be explained by their electrical
performance, in particular by the delay or lack of roll-off. It is thought that rehydration could play a relevant role, i.e. infusion could compensate for desiccation by the continuous supply of liquid to the zone in which vaporization occurs, and consequently keep impedance low for a longer period, thus allowing the creation of larger coagulation zones [15,16]. Two other effects could also influence the capacity of ICW electrodes to create larger coagulation zones: 1) the increase in tissue electrical conductivity by infused saline and 2) the thermal convection produced by the flow of saline. The relative importance of these three phenomena (rehydration, thermal convection, and increased electrical conductivity) in the delay or total absence of roll-off and in coagulation zone size is an issue which remains to be clarified. Our aim was 1) analyze the biophysics associated with the thermal and electrical performance of ICW electrodes and identify the phenomena which distinguish the modeling of IC and ICW electrodes, and 2) implement a computer modeling including the identified phenomena and 3) study their effect on tissue electrical and thermal performance and coagulation zone size.

Since theoretical modeling can provide a comprehensive and detailed biophysical description of the electrical and thermal performance of ICW electrodes, we planned a study to assess the impact of each phenomenon separately. The computational results obtained were compared with the experimental results of previous studies [5,11,12,17,18] in terms of coagulation zone size and impedance evolution.

2. Methods

2.1. Background
An ICW electrode delivers RF current and saline simultaneously, which means these are mutually coupled phenomena. In electrical power application, RF current produces a temperature increase which has two main effects: 1) an increase in tissue electrical conductivity up to a limit temperature of \( \approx 100^\circ C \), and 2) above this limit temperature, tissue dehydration by water vaporization, which involves a drastic and sudden drop in electrical conductivity. The saline infusion chiefly causes: 3) rehydration of the previously dehydrated tissue (at temperatures around 100°C), 4) thermal convection by saline infusion into the tissue, and 5) the increased electrical conductivity of the tissue. All these phenomena are interrelated as follows: the tissue rehydrated by saline infusion partially impedes total dehydration due to vaporization, which occurs when the tissue temperature reaches \( \approx 100^\circ C \), since the water loss is balanced by the saline infusion. The secondary effects include: changes in electrical conductivity of the background tissue due to the saline infusion (with different electrical conductivity to non-infused tissue), modification of the temperature increase produced by RF currents, and hence the increased tissue electrical conductivity.

Phenomena 1) and 2), associated with the application of RF current, have been extensively considered in previous modeling studies [19,20]. However, there are very few studies on the modeling of phenomena 3), 4) and 5), related to saline infusion and its influence on RF delivery. Demazunder et al. [21] built a computational model of an irrigated electrode during RF cardiac ablation, but only modeled the thermal convection as a boundary condition along the electrode-tissue interface. Antunes et al. [22] built a model of an irrigated electrode during RFA in liver and focused on how the electrical and thermal
conductivities varied with saline content. Neither of these two studies simultaneously assessed all the phenomena associated with saline infusion and its effect on RF heating.

In a previous computational study we modeled the hypertonic saline infusion simply with a convective term in the governing equation and an electrical conductivity function that varied with distance from the infusion point [16]. Although the results reproduced a delay in roll-off, this was never totally absent. Neither was this model able to explain the low repeatability of the number of roll-offs and the time of their appearance, as observed experimentally. This suggests that a more realistic model of an ICW electrode for RFA should include a combination of additional issues.

2.2. General issues of the theoretical model

We considered RF hepatic ablation with a monopolar arrangement, in which RF current flows between an active electrode and a grounding patch placed on the patient’s body surface (dispersive electrode). We considered 1.5 mm diameter 17G ICW as active electrode with a 3 cm active tip, which combines an internally cooled circuit and an isotonic saline perfusion system (0.9% NaCl). Fig. 1 shows the geometry of the electrode and how it was simplified to a two-dimensional model by assuming that the problem presented axial symmetry. The dispersive electrode was modeled as an electrical condition on boundaries at a distance from the active electrode. Tissue dimensions were checked by a convergence test to be large enough to keep tissue surfaces at boundary tissue temperature and voltage. We used the value of the maximum temperature ($T_{\text{max}}$) reached in the liver at the first roll-off time as a control parameter in these analyses. When there was a difference
of less than 0.5% in $T_{\text{max}}$ between simulations we considered the former dimension as appropriate.

We assumed that saline exits through two 0.03 mm diameter microholes (Fig. 1A) [12], so their effective area was $(2\pi r^2 = 2\pi (0.015)^2 = 1.41 \times 10^{-3} \text{ mm}^2)$. Due to the axial symmetry, we mimicked these holes by means of a short segment on the surface of the electrode at the mid-point of its length, which is a cylinder in the real geometry. As the equivalent cylinder has to have the same area as the microholes $(2\pi r^2 L = 1.41 \times 10^{-3} \text{ mm}^2)$, so $L = 3 \times 10^{-4} \text{ mm}$, $r_2$ being the radius of the electrode (=0.75 mm). The model was based on a coupled electric-thermal problem, which was solved numerically on COMSOL Multiphysics software (COMSOL, Burlington, MA, USA). The thermal problem was solved using the bioheat equation:

$$\rho c \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + q + Q_p + Q_m$$  \hspace{1cm} (1)

where $\rho$ is tissue density, $c$ specific heat, $T$ temperature, $t$ time, $k$ thermal conductivity, $q$ heat source produced by RF power, $Q_p$ heat loss by blood perfusion and $Q_m$ the metabolic heat generation. This last term was not considered since it is negligible in RFA. The characteristics of materials used in the model are shown in Table 1 [23-26]. The RF power heat source was given by $q = \sigma |\mathbf{E}|^2$, where $\mathbf{E}$ is the electric field obtained from the electrical problem and $\sigma$ is the electrical conductivity. Equation $\nabla \cdot \sigma \nabla V = 0$ was the governing equation for the electric problem, $V$ being the voltage. The electric field was calculated from $\mathbf{E} = -\nabla V$. We used a quasi-static approach since the resistive current is much lower than the displacement current at RF ($\approx$500 kHz) [27]. The blood perfusion heat $Q_p$ is computed from:
\[ Q_p = \beta \rho_b c_b \omega_b (T_b - T) \]  

(2)

where \( \rho_b \) is density of blood (1000 kg/m\(^3\)) [20], \( c_b \) specific heat of blood (4180 J/kg·K) [28], \( T_b \) blood temperature (37ºC), \( \omega_b \) blood perfusion coefficient (0.019 s\(^{-1}\)) [29] and \( \beta \) is a coefficient which took the values of 0 and 1 according to the value of the thermal damage: \( \beta = 0 \) for \( \Omega \geq 4.6 \), and \( \beta = 1 \) for \( \Omega < 4.6 \). The parameter \( \Omega \) was assessed by the Arrhenius damage model [30], which associates temperature with exposure time by a first-order kinetics relationship:

\[ \Omega(t) = \int_0^t Ae^{\frac{\Delta E}{RT}} ds \]  

(3)

where \( R \) is the universal gas constant, \( A \) \((7.39 \times 10^{39} \text{ s}^{-1})\) is a frequency factor and \( \Delta E \) \((2.577 \times 10^5 \text{ J/mol})\) is the activation energy for the irreversible damage reaction [31].

Thermal boundary conditions were: Null thermal flux in the transversal direction to the symmetry axis and constant temperature of 37ºC in the tissue boundaries. The cooling effect produced by the liquid circulating inside the electrode was modeled on Newton’s law of cooling, using a thermal convection coefficient \( h \) with a value of 3127 W/K·m\(^2\) and a coolant temperature of 10ºC. The value of \( h \) was calculated by considering a length of 30 mm and a flow rate of 45 mL/min through an area equivalent to half of the cross section of the inner diameter of the electrode (see Fig. 1). Initial temperature of the tissue was considered to be 37ºC.

Electrical boundary conditions were: Zero current density in the transverse direction to the symmetry axis, in the tissue boundaries and inside the electrode, zero voltage in the dispersive electrode (bottom and top tissue surfaces) and current value of 1.5 A applied in the active electrode [32]. Once roll-off occurs, power is switched off for 15 s and then a
new current pulse is applied until the next roll-off [33]. This procedure is repeated for a period of 12 min.

The model mesh was heterogeneous, with a finer mesh size at the electrode-tissue interface, where the highest electrical and thermal gradients were expected. All the mesh elements used were triangular. In the case of the time-step we used an adaptive scheme since we let the time-stepping method choose time steps freely. The suitable mesh size and time-step were assessed by means of a convergence test with the same characteristics as those used for outer dimensions of geometry.

2.3. Modeling the phenomena associated with the RF power application

RF current produces heating in the tissue by ionic agitation. Increasing the temperature has two remarkable effects: first, as the temperature rises, tissue electrical conductivity ($\sigma$) also goes up to a limit temperature $\approx100^\circ C$. Secondly, this temperature value causes water vaporization and consequently tissue dehydration. Water vaporization implies a phase change, while the dehydration involves a drastic drop of $\sigma$ above this limit temperature ($\approx100^\circ C$). In order to include these phenomena in the modeling we used:

1) A mathematical piecewise function for $\sigma$ which uses different mathematical expressions according to the temperature range [19,20]. $\sigma$ increases with temperatures up to 100$^\circ C$ and at temperatures above 100$^\circ C$ vaporization occurs and desiccation implies a drastic drop in $\sigma$. In the present study we represented the temperature dependence of $\sigma$ by a function which assumes an exponential increase rate of $+1.5%/^\circ C$ for $T<100^\circ C$ and a linear drop by 2 orders of magnitude between 100 and 105$^\circ C$ for $T>100^\circ C$ [34], as shown in Fig. 2.
2) The enthalpy method was used to incorporate the phase change due to water vaporization [35,36]. The use of this method implies modifying the bioheat equation used as the governing equation for the thermal problem in the following way:

$$\frac{\partial (\rho h)}{\partial t} = \nabla \cdot (k \nabla T) + q + Q_p$$

(4)

where $h$ is tissue enthalpy. Enthalpy is related to tissue temperature by the following expression [35]:

$$\frac{\partial (\rho h)}{\partial t} = \frac{\partial T}{\partial t} \cdot \begin{cases} \rho_i c_i & 0 < T \leq 99^\circ C \\ h_{fg} C & 99 < T \leq 100^\circ C \\ \rho_g e_g & T > 100^\circ C \end{cases}$$

(5)

where $\rho_i$ and $c_i$ are density and specific heat of tissue respectively at temperatures below 100°C ($i=l$) and at temperatures above 100°C ($i=g$), $h_{fg}$ is the product of water latent heat of vaporization and water density at 100°C, and $C$ is tissue water content inside the liver (68%).

2.4. Modeling the phenomena associated with saline infusion

The phenomena associated with saline infusion are mainly: thermal convection by saline movement inside the tissue, rehydration of the tissue previously dehydrated, and the higher tissue electrical conductivity associated with the saline infusion pattern. The last two phenomena are related to the effects of applying the RF current mentioned above. Tissue rehydration partially blocks dehydration. Note that although vaporization does occur when the temperature reaches $\approx 100^\circ C$, the saline infusion balances the water loss. The changes in the electrical conductivity of the background tissue due to the saline also modify the
temperature rise produced by the RF current, and so the increase in $\sigma$. To include these phenomena we made the following modifications:

1) **Convection modification**: A new term was added to Equation (3) in order to model the thermal convection by saline motion into the tissue. The new formulation was:

$$\frac{\partial (\rho \dot{h})}{\partial t} = \nabla \cdot (k \nabla T) + q + Q_p - \rho \mathbf{u} \cdot \nabla T$$

(6)

$\mathbf{u}$ being the velocity field (m/s) of the saline inside the tissue, which depends on the infusion rate. The term $\mathbf{u}$ was computed by using the Darcy equation [37]:

$$\mathbf{u} = -\eta \nabla p$$

(7)

where $\eta$ is the hydraulic conductivity of the liver ($6.4 \times 10^{-15}$ m$^2$/Pa·s) [37] and $p$ the pressure inside it. Darcy equation was solved on COMSOL using a stationary study. We considered an infused saline flow rate of ($Q_s$) which varied from 0.05 mL/min (low infusion rate), to 1 mL/min (high infusion rate) [38]. The inlet condition was imposed on segment $L$ (see Section 2.2). The velocity field $\mathbf{u}$ obtained from Darcy’s problem was imposed as initial condition for the electric-thermal problem.

2) **Conductivity modification**: A modification was made to the $\sigma$ expression shown in Fig. 2, which consisted of considering higher values of $\sigma(37^\circ\text{C})$. We initially considered $\sigma(37^\circ\text{C}) = 0.19$ S/m for the liver tissue without the presence of saline. This value was in the range proposed for liver electrical conductivity at 37$^\circ$C [29] and matches with initial experimentally observed impedance values [16]. However, as liver $\sigma$ increases with the presence of saline [16], we assessed the impact of using higher values for $\sigma(37^\circ\text{C})$ in the tissue zone affected by saline. Since we used a constant current protocol, a higher value of $\sigma(37^\circ\text{C})$ implied a smaller impedance value and hence a smaller power value and
smaller coagulation zone. In order to estimate the real effect of the $\sigma(37^\circ C)$ value, we therefore modulated the applied current in order to have the same initial voltage value despite the changes of $\sigma(37^\circ C)$. We increased $\sigma(37^\circ C)$ up to a value whose corresponding current was 2 A, which is the maximum current applied by the generators usually employed in this type of ablation.

3) Phase-change modification: A modification was made to Equation (4) which assumes that a much greater amount of energy is needed to produce the change of phase, and could model the rehydration associated with continuous saline infusion:

$$ \frac{\partial (\rho h)}{\partial t} = \frac{\partial T}{\partial t} \cdot \begin{cases} \rho_i c_i & 0 < T \leq 99^\circ C \\ F h_{li} C & 99 < T \leq 100^\circ C \\ \rho_s c_s & T > 100^\circ C \end{cases} $$

where $F$ is a factor used to multiply latent heat. The higher the $F$ value is, the greater the amount of energy required. As far as we know, this parameter has never been used before and so we conducted a sensitivity analysis to assess the impact of different values in the interval $[1, 10]$.

Regarding the porosity of the desiccated tissue, i.e. changes in hydraulic permeability once the tissue has been completely denatured by heat, two interesting experimental studies [39, 40] reported that permeability decreases after RF application (a mean of $43 \pm 19.8\%$, [39]), which means that desiccated tissue does not completely lose its hydraulic permeability, so that in a first approach we can assume that rehydration is constant (i.e. factor $F$ is constant).
A value of $u=0$ m/s, $\sigma(37^\circ\text{C})=0.19$ S/m and $F=1$ represented the case in which there was no saline infusion and the electrode worked as an IC electrode. This was considered to be the control case (which will be used as a reference to assess the effect of introducing convection, conductivity and phase-change modifications).

2.5 Saline spatial distribution

Eqs. (6)-(7) were applied exclusively in the area in which the saline was distributed. Experimental studies have reported that saline follows a heterogeneous spatial distribution in tissue [38,41]. Since our objective was to assess the impact of each factor of saline infusion, we considered a general pattern represented by a circular distribution, assuming that saline was distributed symmetrically around the electrode, which represented an “ideal” distribution (see Fig. 1B). This circular area was assumed to be placed in the center of the electrode, had a radius of 0.015 m and covered the electrode, as has been observed experimentally [38].

2.6 Outcomes

The following outcomes were analyzed: 1) times when roll-offs occur and time between two consecutive roll-offs, 2) evolution of electrical variables (voltage, power and impedance), and 3) evolution of the short (also known as transverse) diameter of the coagulation zone. The representation of the coagulation zone by the Arrhenius damage model at 12 min provided by the numerical resolution produced a “very noisy” contour. According to [42] the 48-50°C isotherm correlates with the thermal damage contour $D_{99}$ to compute the lesion dimension contour, which corresponds to $\Omega = 4.6$ (99% probability of
cell death) after a 12 min protocol. In the present study we verified that the 50°C isotherm really matched with $\Omega = 4.6$ (differences were <2 mm) and the isotherm provided a better defined line and so decided to use the 50°C isotherm to measure the coagulation zone diameter.

3. Results

In the control case, we found that the first roll-off occurred 45 s after beginning the RFA, there was a total of 16 roll-offs in a period of 12 min, and the short diameter and volume of the coagulation zone was 2.98 cm and 17.53 cm$^3$, respectively (see Table 2). The evolution of impedance, voltage and power are shown in Figure 3.

Table 2 shows the short and axial diameters of the coagulation zone, its volume, the time of the first roll-off and the number of roll-offs at 720 s RFA in all the analyzed cases, except the cases with a convection modification. The results of these cases are not given, since when we only assessed the impact of thermal convection (at high and low saline infusion rates) we did not find any differences with the control case. In order to explain this finding, Figure 4 shows the velocity field \( u \) obtained from the Darcy problem using a high rate of saline infusion. It can be seen that the saline velocity is drastically reduced with distance from the infusion point, which confines the effect of saline convection to a radial area of \( \approx 0.1 \text{ mm} \) around the infusion point.

To assess the impact of increasing electrical conductivity, we first decided the \( \sigma(37^\circ\text{C}) \) values to be used. Initially, we thought of progressively raising the \( \sigma(37^\circ\text{C}) \) value in the control case by \( \approx 0.1 \text{ S/m} \) (i.e., 0.3, 0.4, 0.5… S/m). Changes in \( \sigma(37^\circ\text{C}) \) also implied changes in the current applied, which had to be modulated to obtain the same initial voltage
value as in the control case (≈110 V, see Fig. 3). This meant that we had to use currents of $I=1.85, 2.1$ and $2.4$ A for $\sigma(37^\circ C)$ values of 0.3, 0.4 and 0.5 S/m, respectively. Since the current value in RF generators cannot exceed 2 A, in these three cases we could only consider the case of $\sigma(37^\circ C)=0.3$ S/m (case B in Table 2). We also decided to include the case of the maximum current allowed ($I=2$ A), which was $\sigma(37^\circ C)=0.35$ S/m (case C in Table 2). We then considered an additional case corresponding to $\sigma(37^\circ C)=0.5$ S/m with a $I=2.4$ A (case D in Table 2). Since this current value exceeded the limit, there was a notable increase in $\sigma(37^\circ C)$ and therefore their effect would also be more notable.

Table 2 shows that coagulation zone size increases with the value of $\sigma(37^\circ C)$. For the case of $\sigma(37^\circ C)=0.35$ S/m and $I=2$ A (case C) the coagulation zone minor diameter was 7% bigger than the control case and 25% bigger in case D, and these differences were greater (≈40 and 60%) in terms of the coagulation zone volume. The electrical response also registered differences with respect to the control case, since in cases B, C and D there was a delay in first roll-off time (22, 25 and 26 s, respectively) and fewer total roll-offs (13, 13 and 12 roll-offs). Note that these differences were similar in the three cases, since the maximum difference in first roll-off time was 4 s, and 1 roll-off with respect to the total number of roll-offs. The initial impedance and voltage values were similar in the three cases as a result of modulating the current value.

About the effect of tissue rehydration (Cases E, G and H), we observed that the higher the $F$ values, the greater the changes in the different outcomes with respect to the control case. The coagulation zone volume increased by ≈50% of the control case (IC electrode) value and there was a considerable impact on the roll-off phenomenon: with a delay in the first
roll-off time of 133, 257 and 563 s and a reduction of 9, 12 and 15 in total roll-offs (Figure 25).

Finally, we varied $\sigma(37^\circ\text{C})$ and $F$ simultaneously. In case J we used $F=3$ and $\sigma(37^\circ\text{C})=0.35$ S/m, for which the corresponding current was 2 A and in case K we used $F=10$ and the $\sigma(37^\circ\text{C})=0.35$ S/m (current 2 A), as is shown in Table 2. The combination of both phenomena had a greater effect on all the analyzed outcomes than when they were considered separately. For example, when $\sigma(37^\circ\text{C})=0.35$ S/m and $F=10$ (case K), the coagulation zone minor diameter increased by 23% more than the control case, while the increase was 7 and 10% in the cases in which the phenomena were considered separately (change of $\sigma(37^\circ\text{C})=0.35$ S/m only, case C, and the change $F=10$ only, case H, respectively). The delay in first roll-off was 664 s when the phenomena were combined (case K) and 25 and 563 s when they were considered separately (cases C and H). In fact, in case K roll-off was practically absent (Figure 5). On the other hand, we did not find any changes with respect to the results of cases J and K, also adding the phenomena of convection. Overall, it is observed that both $\sigma$ and $F$ have a strong influence on number of roll-offs and coagulation zone volume. In this respect, Figure 6 shows the relationship between the number of roll-offs and the coagulation zone volume with variations in factor $F$ and the electrical conductivity values, respectively. The data in Figure 6 are extracted from Table 2 with the trend lines for every case. Both Figures A and B show that for the range of values and the electrical conductivity used for factor F, these variables show a strong influence on the number of roll-offs and coagulation size, which is supported by the high values of the square of the correlation coefficient ($R^2$). In both cases A and B $R^2$ is obtained from an exponential correlation for the graphs which represents the relationship of
Figure 7 shows the temperature radial distribution at line z=0.075 m for the control case (IC electrode) and case K (ICW electrode) for t=6 and t=12 min. These results show that ICW electrodes can reach high temperatures (above 50ºC) at points further away and consequently achieve a greater coagulation zone volume.

4. Discussion

In line with our objective, we identified the phenomena which distinguish the performance of IC and ICW electrodes, modeled these phenomena and assessed their relative influence on coagulation zone size and tissue electrical and thermal performance. We found rehydration, thermal convection and increased electrical conductivity to be the three phenomena associated with the use of ICW electrodes that are mainly responsible for their electrical and thermal performance being different from IC electrodes. Specifically, we found that greater coagulation zone size and delay in the occurrence of roll-off are the primary outcomes which characterized the use of ICW electrodes vs the IC.

We built a computational model of an ICW electrode by modifying the formulation of an IC electrode model in order to represent the above-mentioned phenomena. The saline convection was modeled by introducing a term of heat convection in the governing equation for the heat problem. This new term did not cause any changes in the results obtained with the IC electrode. We assessed two different saline infusion velocities $u$, but none of them was high enough to have a noticeable thermal effect on tissue. Rates of saline infusion higher than 1 mL/min are not usual in clinical practice. Higher values of $\sigma$ (and
current values modulated in concordance with $\sigma$ in order to have the same initial voltage value as the control case) were used to model the increase in electrical conductivity. The effect of this phenomenon was more noticeable in coagulation zone size. By increasing the value of electrical conductivity it was possible to obtain coagulation zone sizes in the range of those obtained experimentally [18]. However, the isolated phenomenon of higher electrical conductivity, even though it delayed roll-off time, was not able to eliminate it completely. On the other hand, rehydration, modeled by introducing factor $F$ into the enthalpy method of vaporization, had a notable effect on delaying roll-off, and could totally eliminate it at high enough $F$ values. It is important to note that by considering the rehydration phenomenon only, the computed coagulation zones did reach the range obtained experimentally. Only the simultaneous combination of increasing electrical conductivity and rehydration allowed the absence of roll-off and enlarged coagulation zone to be mimicked, as has been observed experimentally [5, 18].

In the case of an IC electrode, roll-off occurs when the 100ºC isotherm completely surrounds the electrode [43]. This is due to the abrupt drop in tissue electrical conductivity at temperatures higher than 100ºC. In contrast, although the temperature around the ICW electrode also goes up to 100ºC (Figure 7), the rehydration phenomenon (mimicked in this study by factor $F$) prevents the tissue from exceeding this limit and so reduces the tissue electrical conductivity and consequently roll off is delayed. With the rehydration a greater amount of energy is necessary to produce tissue phase-change, which means a lower amount of energy available to raise the tissue temperature (see Equation (4)). So, for higher $F$ values, a higher limitation to achieving tissue phase-change (and so, roll-off) is assumed. However, the relationship between the $F$ value and the coagulation zone volume was not
linear (see Figure 6), which means that the growth of the coagulation zone size with respect to \(F\) will be negligible for a specific \(F\) value. Likewise, although the electrical conductivity showed a strong influence on the number of roll-offs and the coagulation zone volume, their rate of change with \(\sigma\) decreases as \(\sigma\) increases.

We did not observe noticeable differences in the electrical performance of the cases in which we varied the value of electrical conductivity (cases B, C and D), however these cases presented noticeable differences with the control case (IC electrode modeling). The only difference in the modeling of all these cases was in the value of electrical conductivity and the corresponding modulated current value, so it was surprising that cases B, C and D presented differences with the control case but not with each other. A possible explanation for this fact may be found in [32], in which authors observed that differences in electrical performance were reduced when current was increased.

*Comparison with experimental and clinical results*

To validate our computer results we compared them with some previous experimental and clinical studies.

As regards the electrical performance of an IC electrode during RF ablation, in [16] the authors showed that in a typical impedance evolution throughout a 12-min ablation with an IC electrode, roll-offs appeared more or less equidistantly spaced in time, and the first roll-off appeared before the first 60 s (see Figure 4 of [16]). This pattern was also found in Fig. 3, which shows the impedance evolution obtained for the control case (IC electrode) by means of computer simulations. In the case of an ICW electrode, our results show that this electrode delays the first roll-off and may even eliminate it under certain circumstances, as
observed in case K (see Table 2 and Fig. 5). Romero-Méndez et al. in [16] also showed experimentally that the ICW electrode not only delays roll-off (Figure 6b in [16]), but can even make it disappear completely (Figure 5b in [16]). Similar results were also found in [43,44].

We selected four studies on the analysis of coagulation zone volume whose experimental conditions were identical to the physical situation considered in the computer model, i.e. a 17-gauge ICW electrode with 3-cm exposed tip, a couple of tiny side holes (0.03 mm diameter) to conduct the interstitial infusion of saline, and 12-minute ablation using impedance control [11,12,17,18]. With these conditions, the reported volumes ranged from 29.3±10.9 cm$^3$ [17] to 49.21±21.18 cm$^3$ [18]. We obtained coagulation zone volumes in the range of 26.31-40.62 cm$^3$ in the computer simulations, which is in the order of those obtained experimentally. This agreement was also found when we analyzed the coagulation zone volumes created with IC electrodes (case A in our study): values of 15.2±6.7 cm$^3$ and 11.05±4.27 cm$^3$ in experimental studies [11,12] versus 17.53 cm$^3$ in computer simulations. Note that the differences between coagulation zone volume produced by IC and ICW electrodes in experimental studies were 53% [11] and 50% [12], while computationally we obtained a difference of 56% by comparing the IC electrode case with case K.

Limitations of the study

1) We assumed the ideal circular distribution of saline around the electrode, which would maximize the effect of the phenomena studied. This means that that under conditions of heterogeneous or irregular saline distributions, the influence of increasing electrical conductivity and rehydration could be reduced. Despite these
limitations, the results suggest that the mathematical framework considered here could be included in modeling ICW electrodes. Moreover, we assumed the continuous rehydration of tissue during RFA, as employed in clinical practice [18]. It has also been reported that greater coagulation zones can be created when saline is infused prior to RFA [45, 46]. Even when the application is before RFA, the tissue remains hydrated during the RFA process, so that when modeling the biophysics of this process it would still be valid to consider the $F$ factor.

2) We propose the idea of a constant factor $F$ modulating the mathematical formulation associated with rehydration. The inclusion of $F$ is only one possible way of hindering tissue vaporization, as other mathematical approaches, e.g. based on a water-content function, could also be valid to model the rehydration associated with ICW electrodes. The results suggest that the proposed mathematical approach makes sense, at least in terms of observing a considerable delay in roll-off and increased coagulation volume as compared to the case without saline infusion. Future studies could be planned to give physical support to this mathematical approach, and even to correlate the exact value of $F$ with the hydraulic permeability of different tissue conditions (healthy, cirrhotic, extremely fatty, etc).

5. Conclusions

We made some changes in the formulation of an IC in order to model the phenomena which distinguish it from ICW electrodes: higher electrical conductivity, heat convection and rehydration. We also assessed the effect of these changes on coagulation zone size and the tissue electrical and thermal response and found that the combination of tissue rehydration
and higher electrical conductivity should be taken into account to increase coagulation zone size in RFA applications. However, it was not considered necessary to take into account the convection phenomenon to model an ICW electrode for the different saline infusion velocities used.

Acknowledgments
This work was supported by the Government of Spain through the "Plan Estatal de Investigación, Desarrollo e Innovación Orientada a los Retos de la Sociedad" with Grant Number TEC 2014-52383-C3-R (TEC 2014-52383-C3-1-R).

References


Table 1. Characteristics of the materials used in the theoretical model [23-26].

<table>
<thead>
<tr>
<th>Tissue/material</th>
<th>$\sigma$ (S/m)</th>
<th>$k$ (W/m·K)</th>
<th>$\rho$ (kg/m$^3$)</th>
<th>$c$ (J/kg·K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Electrode</td>
<td>$7.4 \times 10^6$</td>
<td>15</td>
<td>$8 \times 10^3$</td>
<td>480</td>
</tr>
<tr>
<td>Plastic</td>
<td>$10^{-7}$</td>
<td>0.026</td>
<td>70</td>
<td>1045</td>
</tr>
<tr>
<td>Liver</td>
<td>0.19$^{(1)}$</td>
<td>0.502</td>
<td>1080$^{(2)}$</td>
<td>3455$^{(2)}$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>370$^{(3)}$</td>
<td>2156$^{(3)}$</td>
</tr>
</tbody>
</table>

$\sigma$, electric conductivity; $k$, thermal conductivity; $\rho$, density; $c$, specific heat.

$^{(1)}$ Assessed at 37°C. $^{(2)}$ At temperatures below 100°C. $^{(3)}$ At temperatures above 100°C.
Table 2. Computer results for the internally cooled electrode (IC, case A), and internally cooled-wet electrode (ICW, cases B–K): diameters (a: short, b: axial) and volume (V) of the coagulation zone, time of first roll-off ($t_1$), and number of roll-offs (N).

<table>
<thead>
<tr>
<th>Cases</th>
<th>$\sigma$ (S/m)</th>
<th>$F$</th>
<th>I (A)</th>
<th>a (cm)</th>
<th>b (cm)</th>
<th>V (cm$^3$)</th>
<th>$t_1$ (s)</th>
<th>N</th>
</tr>
</thead>
<tbody>
<tr>
<td>IC electrode</td>
<td>A 0.19</td>
<td>1</td>
<td>1.5</td>
<td>2.98</td>
<td>4.1</td>
<td>17.53</td>
<td>45</td>
<td>16</td>
</tr>
<tr>
<td></td>
<td>B 0.3</td>
<td>1</td>
<td>1.85</td>
<td>3.11</td>
<td>4.91</td>
<td>27.86</td>
<td>67</td>
<td>13</td>
</tr>
<tr>
<td></td>
<td>C 0.35</td>
<td>1</td>
<td>2.0</td>
<td>3.2</td>
<td>4.96</td>
<td>29.73</td>
<td>70</td>
<td>13</td>
</tr>
<tr>
<td></td>
<td>D 0.5</td>
<td>1</td>
<td>2.4</td>
<td>3.72</td>
<td>5.38</td>
<td>40.62</td>
<td>71</td>
<td>12</td>
</tr>
<tr>
<td>IC + ↑$\sigma$</td>
<td>E 0.19</td>
<td>3</td>
<td>1.5</td>
<td>3.06</td>
<td>4.85</td>
<td>26.31</td>
<td>178</td>
<td>7</td>
</tr>
<tr>
<td></td>
<td>G 0.19</td>
<td>5</td>
<td>1.5</td>
<td>3.2</td>
<td>4.9</td>
<td>27.50</td>
<td>302</td>
<td>4</td>
</tr>
<tr>
<td></td>
<td>H 0.19</td>
<td>10</td>
<td>1.5</td>
<td>3.28</td>
<td>4.87</td>
<td>29.03</td>
<td>608</td>
<td>1</td>
</tr>
<tr>
<td>IC + ↑$F$</td>
<td>J 0.35</td>
<td>3</td>
<td>2.0</td>
<td>3.45</td>
<td>5.18</td>
<td>36.76</td>
<td>218</td>
<td>5</td>
</tr>
<tr>
<td></td>
<td>K 0.35</td>
<td>10</td>
<td>2.0</td>
<td>3.68</td>
<td>5.26</td>
<td>39.93</td>
<td>709</td>
<td>1</td>
</tr>
</tbody>
</table>

$\sigma$: Tissue electrical conductivity value (at 37°C); $F$: hydration factor (see text for details); I: applied current.
Figure 1. A) Three-dimensional scheme of the real geometry (out of scale and dimensions in mm). The domain is divided into three zones: plastic portion of the electrode, metallic cooled electrode and hepatic tissue. The zoom shows the ICW electrode system, in which the isotonic saline is infused into the tissue through two microholes (0.03 mm in diameter). Blue arrows show the direction of saline flow. B) Two-dimensional geometry used in the study. Dashed curve shows the spatial distribution of saline.
Figure 2. Electrical conductivity ($\sigma$) variation with temperature. The temperature dependence of $\sigma$ was represented by a function which assumes for $T < 100^\circ$C an exponential increase rate of $+1.5\%/^\circ$C and for $T > 100^\circ$C a linear drop by 2 orders of magnitude between 100 and 105$^\circ$C (Trujillo and Berjano, 2013).
Figure 3. Impedance, power and voltage evolution during a 12 min RFA for the control case ($\sigma(37^\circ C)=0.19$, $F=0$ and $u=0$) using a current value of 1.5 A.
Figure 4. Velocity field $u$ obtained from the Darcy problem using a high rate of saline infusion in the area of saline distribution (B) and with a zoom-in on the area of saline distribution around the infusion zone (A).
Figure 5. Impedance evolution during 12 minutes of RF ablation (1.5 A) and created coagulation zone diameters for the considered cases (see Table 2). A: case without saline infusion, i.e. without rehydration, corresponding with an IC electrode. In the case of ICW electrodes, a more and more effective rehydration, modeled by increasing values of the factor F (from 3 to 10, cases E, G and H) delays the appearance of the first roll-off (dashed rows represent this respect with to the case of an IC electrode) and allows larger coagulation zones to be created. Furthermore, when saline infusion allows increasing the background electrical conductivity (from 0.19 to 0.35 S/m), the maximum current to be applied during RF ablation can be augmented to 2.0 A, and as a result the first roll-off
delays a bit more and the created coagulation zone is even larger (case K). Gray zone represents the range of coagulation zone diameters reported in experimental studies using ICW electrodes.
Figure 6. Relationship between the number of roll-offs (squares) and the coagulation zone volume (circles) with respect to variations in factor $F$ (A) and electrical conductivity (B). Data are extracted from Table 2 and lines are the corresponding trend lines, $R^2$ being the square of the correlation coefficient.
Figure 7. Temperature profiles in the tissue at 6 and 12 min of RF ablation for IC and ICW electrodes (cases A and K, respectively). Black dashed line represents the 50°C isotherm.