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Additional Information

1 **Swirl Ratio and Post Injection Strategies to Improve Late**  
2 **Cycle Diffusion Combustion in a Light-Duty Diesel Engine**

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15

## ABSTRACT

16 Nitrogen oxides (NO<sub>x</sub>) and soot emissions are the most important pollutants from direct-  
17 injection diesel engines. In particular, soot formation and oxidation determine the net  
18 engine-out soot emissions. These phenomena are complex and competing processes  
19 during diesel combustion. Despite many researches implicate the mechanisms of soot  
20 formation with soot emissions, the enhancement of the late cycle soot oxidation is the  
21 dominant mechanism for a reduction of engine-out soot emissions. The mixing process  
22 and the in-cylinder bulk temperature are two important parameters in the development of  
23 soot oxidation process. The current research compares different engine strategies to  
24 enhance the late cycle mixing controlled combustion process and therefore enhance soot  
25 oxidation while maintaining similar gross indicated efficiency in a light-duty engine. For  
26 this purpose, a simplified methodology has been used, which analyzes the effect of mixing  
27 process and in-cylinder bulk gas temperature on soot oxidation during the late cycle  
28 combustion. For carrying out this research, theoretical and experimental tools were used.  
29 In particular, the experimental measurements were made in a single-cylinder direct-  
30 injection light-duty diesel engine varying the swirl ratio and the injection pattern as  
31 injection pressure, Start of Energizing (SoE), Energizing Time (ET) and number of  
32 injections events. To analyze soot emissions, the combustion luminosity was measured  
33 by an optoelectronic probe and the optical thickness parameter (KL) was evaluated by the  
34 two-color pyrometry method. The apparent combustion time ( $ACT^{-1}$ ) was used as mixing  
35 time tracer. Results show that an increase in swirl ratio implies an improvement on the  
36 mixing process and higher values of average bulk temperature during the late-cycle  
37 diffusion combustion. Both phenomena produce an enhancement in the soot oxidation  
38 process. In the lowest swirl ratio case, a suitable injection strategy based on multiple

39 injections, provides similar results of soot oxidation process (and therefore, the  
40 emissions) as high swirl ratio case.

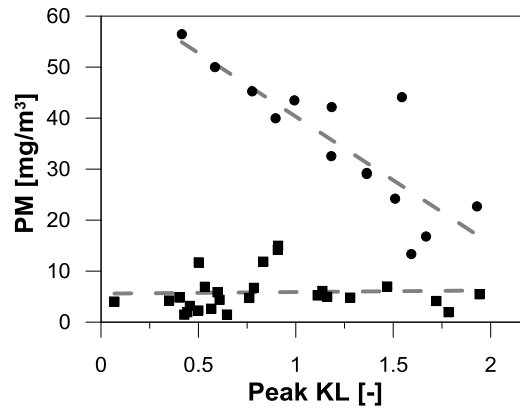
## 41 **1. INTRODUCTION**

42 Due to the increase of Greenhouse Gas (GHG) emissions produced by the Internal  
43 Combustion Engines (ICE), stringent regulations are being introduced all around the  
44 world to limit their exhaust emissions with the objective of decreasing their  
45 environmental impact. The automotive manufacturers and researchers focus their  
46 attention on the development of cleaner and more efficient powertrain engines. In  
47 particular, the nitrogen oxides (NO<sub>x</sub>) and particulate matter (PM) are the most important  
48 pollutants from direct-injection diesel engines. Thus, different strategies are implemented  
49 to reduce these emissions: high pressure fuel injection systems [1, 2], multiple injections  
50 [3], high boost pressure [4], exhaust gases recirculation [5], high swirl [6], new cleaner  
51 fuels [7] and new combustion concepts [8, 9]. The present research was focused on  
52 comparing different engine operating conditions, which can achieve a reduction in  
53 engine-out exhaust emissions.

54 Soot emissions in diesel exhaust depend on formation and oxidation processes. Both  
55 processes are distinct in temporal and spatial evolution. The soot formation process is  
56 more important during the fuel injection event and it is approximatively located in the  
57 region closest to the nozzle [10]. Large amount of soot forms quickly during the earliest  
58 combustion period due to high local equivalence ratio in the fuel-rich premixed burn  
59 region [11, 12, 13]. In this stage, soot oxidation is poor. From the End of Injection (EoI),  
60 the soot oxidation process becomes more relevant. The oxidation stage spans the range  
61 from EoI up to the End of Combustion (EoC). In this stage, the diffusion flame disappears,  
62 the soot formation decreases and the soot oxidation rate increases. In these conditions,

63 the mixing process and the in-cylinder bulk temperature govern the soot oxidation  
64 process. It is important to highlight that only a small amount of soot formed makes it into  
65 the exhaust. Figure 1 shows the correlation between the maximum amount of soot formed  
66 (peak value of soot concentration, KL) and concentration of PM emissions in the exhaust  
67 for different measured engine conditions [14]. Thus, two groups of results are clearly  
68 observed: on the one hand, the square symbols points out a group of results in which the  
69 PM emissions are similar and low independently on the peak value of soot concentration,  
70 KL and therefore independently on the value of soot formed in-cylinder. On the other  
71 hand, group of circle symbols indicate other results where the highest concentrations of  
72 soot formed, maximum of KL peak value correspond on lowest values of PM emissions,  
73 and vice versa. These trends are the opposite of those that would be expected if the PM  
74 emissions were explained by the amount of formed soot [15]. Gallo et al. have obtained  
75 a similar correlation. In their study [16], different operating conditions were measured in  
76 an optical engine and the laser extinction technique was used to evaluate the oxidation  
77 rates during the expansion stroke. They conclude that the amount of in-cylinder soot  
78 formed does not explain the engine-out soot emissions. Considering diesel fuel and  
79 operating conditions tested, the oxidation process is mainly responsible for the exhaust  
80 PM emissions in a CI diesel engine under real conditions.

81



82

83 *Figure 1. Concentration of exhaust PM versus the maximum value of KL for the different engine conditions*  
 84 *measured in [14].*

85 In literature, many researchers have studied the soot oxidation process. Dembinski et al.  
 86 [17] studied the impact of swirl ratio and injection pressure on the soot oxidation process.  
 87 Experimental measurements were made with two different optical techniques  
 88 (Combustion Image Velocimetry and two-color method) in an optical engine. This  
 89 research stated that the soot oxidation process improved when the swirl ratio and injection  
 90 pressure were increased due to an enhancement of in-cylinder turbulence. O'Connor and  
 91 Musculus [18] studied the effect of different engine parameters on the soot oxidation  
 92 process, concluding that a post injection can reduce engine-out soot by up to 45% at high  
 93 swirl ratios and 30% for low swirl ratios. Gallo et al. [16] analyzed the amount of PM  
 94 emitted by modifying the injection pressure, gas density and temperature at TDC as well  
 95 as engine speed and nozzle hole size by application of the laser extinction method. These  
 96 authors concluded that increasing the injection pressure, gas density, and reducing nozzle  
 97 hole size and the engine speed, the engine-out PM emissions were strongly reduced.  
 98 Arrègle et al. [19] showed different post-injection strategies for reducing soot emissions  
 99 in DI diesel engines. In this research, a broad experimental analysis was carried out to  
 100 explore the behavior of post-injection strategy on exhaust soot emissions under a certain  
 101 range of operating conditions and with different post-injection timings. These authors

102 concluded that the engine-out soot emissions were reduced when the post-injection event  
103 was added. Using a similar optical approach, Lopez et al. [20] also studied the in-cylinder  
104 soot oxidation process by means of the two-color method. In particular, the impact of  
105 swirl, EGR and injection timing were analyzed. These authors concluded that the soot  
106 oxidation process is degraded when swirl is decreased, EGR rate is increased or injection  
107 timing is delayed.

108 Thus, the main objective of this work was to compare different engine strategies to  
109 enhance the late cycle mixing controlled combustion process and therefore to improve  
110 the soot oxidation process while maintaining similar gross indicated efficiency in a light-  
111 duty engine. For this purpose, a simplified methodology defined in [14] was used, which  
112 analyzed the effect of mixing process and in-cylinder bulk gas temperature on soot  
113 oxidation during the late cycle combustion. Experimental measurements were made in a  
114 single-cylinder direct-injection light-duty diesel engine varying the swirl ratio and the  
115 injection pattern as injection pressure, Start of Energizing (SoE), Energizing Time (ET)  
116 and number of injections events. To analyze soot, the optical thickness (KL) parameter  
117 was used, which was measured by an optoelectronic probe based on the two-color  
118 pyrometry method. The apparent combustion time ( $ACT^{-1}$ ) was used as mixing tracer.  
119 This parameter is based on the injection rate profile and the experimental heat release.  
120 Finally, both strategies (swirl ratio and injection pattern) were evaluated with the goal of  
121 getting the maximum benefits in terms of the soot oxidation process.

122

## 2. EXPERIMENTAL TOOLS

### 2.1. Test cell and engine description

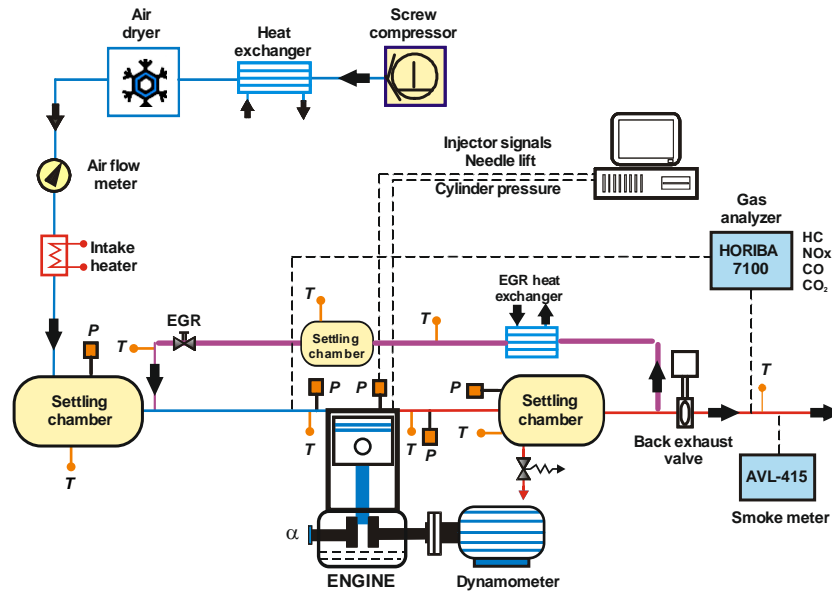
The experimental measurements were carried out in a single-cylinder light-duty diesel engine. It was equipped with a common-rail fuel injection system and a high-pressure exhaust gas recirculation. This engine is derived from a production GM 1.9L Diesel engine, which has four valves per cylinder, centrally located injector and a re-entrant type piston bowl. For performing this research, the engine was modified with two swirl flaps in the air intake port, which allowed for a variation in swirl ratio from 0 to 5. The important engine data as well as the injection system information are given in the table 1.

<b>Engine Type</b>	DI, 1-cylinder, 4-stroke	<b>Max. Power [kW]</b>	27.5 @ 4000 rpm
		<b>Max. Torque [Nm/min<sup>-1</sup>]</b>	80 @ 2000-2750 rpm
<b>Displacement[mm<sup>3</sup>]</b>	477	<b>Injection System</b>	Bosch Common Rail (solenoid)
<b>Stroke [mm]</b>	90.4	<b>Max. Rail Pressure [bar]</b>	1600
<b>Bore [mm]</b>	82	<b>Nozzle hole diameter [mm]</b>	0.141
<b>Combustion Chamber</b>	Re-entrant type	<b>Injector Nozzle Holes</b>	7
<b>Compression ratio</b>	17.1:1	<b>Hydraulic flow rate [cm<sup>3</sup> (30s) at 100 bar]</b>	440

Table 1. Engine and injection system specifications

The single cylinder engine was installed in a fully instrumented test cell with an auxiliary facility necessary for the operating, control and acquisition of raw data. Figure 2 shows the complete test-cell scheme.





136

137

Figure 2. Complete test cell set-up

138 The engine was connected to an electric dynamometer, to control engine speed and load.

139 To reach the desired intake air flow conditions, an externally driven screw compressor

140 was used to provide the necessary boost pressure before passing through the air dryer

141 system to control the relative humidity air. The air pressure and temperature were

142 regulated inside of intake settling chamber after mixing the EGR. The exhaust

143 backpressure was adjusted by means of a pneumatic valve to simulate the effect of the

144 turbocharger in the real engine. The exhaust pressure and temperature were controlled in

145 the exhaust settling chamber.

146 The concentrations various constituents in the exhaust gas were analyzed with a five gas

147 Horiba MEXA-7100 DEGR analyzer bench. To assure the accuracy of the measurements,

148 the different pollutant species were measured and averaged over 60 seconds after

149 attaining steady state operation. The smoke emissions were measured with an AVL 415

150 variable sampling smoke meter. Three consecutive measurements (1 litre volume each

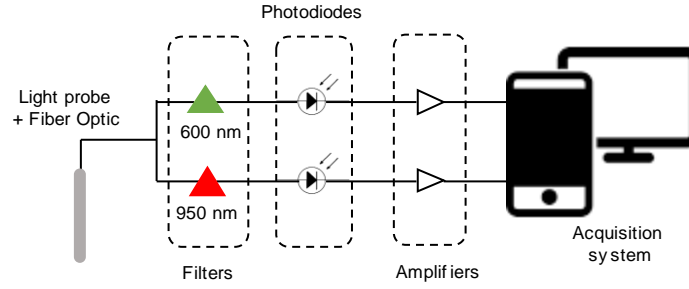
151 sample) were acquired and averaged supplying results directly in FSN (Filter Smoke

152 Number) units [21].

153 The in-cylinder pressure was measured during 400 consecutive cycles with a Kistler  
154 6125C glow-plug piezoelectric transducer coupled to a 4603B10 charge amplifier. The  
155 pressure signal was measured every  $0.5^\circ$  by a Yokogawa DL708E oscillographic recorder  
156 with a 16 bits A/D converter module. The common-rail fuel injection system was  
157 managed by a commercial DRIVVEN controller system [22]. The mean variables were  
158 acquired at a low sampling frequency of 100 Hz using SAMARUC, a CMT-developed  
159 test system that collects the signals of different sensors and controls the electric  
160 dynamometer [23].

## 161 **2.2.Optoelectronic probe**

162 The in-cylinder soot data were measured with an AVL optoelectronic signal converter  
163 based on the two color method, known as AVL VisioFEM with a selection of photodiodes  
164 and narrow band optical filters adapted for IC engines. Figure 3 shows a scheme of the  
165 light probe. At the tip of the probe, a sapphire lens records the luminous intensity from  
166 the flame in the combustion chamber with an angle view of  $90^\circ$ . The light is transported  
167 through optical fiber and it is split to two filters at wavelength of 600 and 950 nm (around  
168  $\pm 50$ nm FWHM each one). Photodiodes convert the intensity to a voltage signal. This is  
169 amplified and acquired every  $0.5^\circ$  CAD. The raw signals of the optoelectronic probe are  
170 referenced with a halogen lamp mounted to an integrating sphere, which provides a  
171 homogenously illuminated surrounding. The transmission of the light probe is obtained  
172 with the halogen lamp base by a methodology provided by AVL. Each operating point  
173 was recorded with 4 repetitions of 100 combustion cycles (400 cycles).



174

175

Figure 3. Signal path from flame to data acquisition device

176

Once the temporal evolution of the raw voltage signal was determined, the spectral

177

emission was calculated with the equation (1):

178

$$I_{soot} \left[ \frac{W}{m^2 \cdot m \cdot sr} \right] = \frac{\text{Voltage signal [V]} \cdot \text{Sensitivity} \left[ \frac{W}{m^2 \cdot m \cdot sr \cdot V} \right]}{\text{Gain [-]} \cdot \text{Transmission [-]}} \quad (1)$$

179

where  $I_{soot}$  is spectral emission, temporal voltage signal for each wavelength (600 and 950

180

nm) recorded by the optoelectronic probe, sensitivity is a constant of the pyrometer and

181

thus, the manufacturer provides it. The gain was fitted during the measured process

182

according to the light intensity.

183

Finally, the two color method was applied for obtaining the temperature and soot volume

184

fraction (KL). This technique establishes that the spectral emission emitted by the soot

185

particles ( $I_{soot}$ ) inside the combustion chamber is proportional to the intensity emitted by

186

a black body at the same temperature (equation 2). The proportional factor is determined

187

by the emissivity of the soot particles, which depends on the soot concentration, working

188

wavelength ( $\lambda$ ).

189

$$I_{soot}(\lambda, T, KL) = \varepsilon_{\lambda} I_{b,\lambda} = \left[ 1 - \exp\left(-\frac{KL}{\lambda^{\alpha}}\right) \right] \frac{1}{\lambda^5} \frac{c_1}{\left[ \exp\left(\frac{c_2}{\lambda T}\right) - 1 \right]} \quad (2)$$

190

Where  $c_1 = 1.1910439 \times 10^{-16} \text{ Wm}^2\text{sr}^{-1}$  and  $c_2 = 1.4388 \times 10^{-2} \text{ mK}$ . Zhao et al. [22]

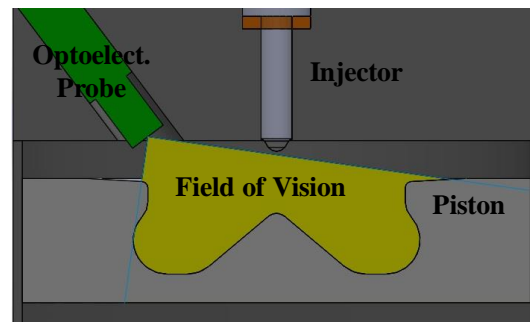
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reported that  $\alpha$  values are less dependent on the wavelength in the visible range than in

192

the infrared.

193 For the sake of clarity, figure 4 presents the optical set up when the optoelectronic  
194 pyrometer is used in the light duty engine. In this figure, the piston is located at 20 CAD  
195 after top dead center. It is possible to observe the injector, the optoelectronic flush  
196 mounted probe as well as its field of vision in the combustion chamber.



197

198 *Figure 4. Optoelectronic pyrometer set up on the light duty engine configuration*

### 199 **2.3. Test Matrix**

200 In this research, a study was carried out for evaluating the potential of swirl ratio and a  
201 dedicated injection strategy to enhance the late cycle mixing controlled combustion. For  
202 that, a reference operating condition was selected as baseline case for analyzing the effect  
203 of each strategy on the late cycle combustion and finally, to compare both strategies for  
204 selecting the best option. The engine was operated maintaining constant engine speed at  
205 2000 rpm and low load at 5 bar BMEP considering the flame transparency uncertainties  
206 imposed by the two-color method [14].

207 In addition, the temperature of the coolant and oil stayed constant for all the  
208 measurements at 86°C and 95°C, respectively. For each operating condition, 4 repetitions  
209 were measured and the results were averaged in order to minimize the experimental  
210 uncertainties.

211

212 **2.3.1. Baseline case**

213 The experimental engine operating conditions are represented in table 2. These operating  
 214 conditions were chosen for being representative of typical operating point for the derived  
 215 production GM 1.9L Diesel engine, which was set up to meet EURO IV emissions  
 216 regulations.

Operation condition	Baseline case		
Injection pressure [bar]	650	$T_{in}$ [K]	318
Fuel Flow [kg/min]	0.018	$P_{in}$ [bar]	1.306
SoE [°BTDC]	19.5 / 9.9 / 0.3	$P_{exh}$ [bar]	1.49
ET [ms]	0.310 / 0.310 / 0.587	Air Flow [kg/min]	0.659
		EGR [%]	0
SR [-]	1.5	CA50 [° aTDC]	13

217 *Table 2. Baseline engine operating conditions*

218 **2.3.2. Engine setting sweeps**

219 Table 3 presents the text matrix for the two different strategies studied in this work. In  
 220 the first strategy, the objective was to evaluate the effect of swirl ratio on late-cycle  
 221 combustion process. For that, the swirl ratio was varied from 0 up to 5, in steps of 1 unit  
 222 maintaining constant all other engine parameters The tests were performed with the same  
 223 trapped mass at the IVC. For that, the intake pressure was adapted in every test. While,  
 224 the intake air temperature and the exhaust pressure were kept constant. Regarding the  
 225 injection pattern, all parameters were kept constant except the SoE and ET for the main  
 226 injection event, which were modified for obtaining the same CA50 and fuel mass in all  
 227 cases.

228

<b>Operation condition</b>	<b>SR Sweep</b>	<b>Injection Strategy Optimization</b>
<b>Injection pressure [bar]</b>	650	800
<b>Fuel Flow [kg/min]</b>	0.018	
<b>SoE [°BTDC]</b>	19.5 / 9.9 / 0 - 0.5	19.2 / 9.6 / -0.5 / -4.7
<b>ET [ms]</b>	0.310 / 0.310 / 0.582 - 0.590	0.285 / 0.300 / 0.510 / 0.150
<b>Number of Injections</b>	3 (2 pilots and 1 main)	4 (2 pilots, 1 main and 1 post)
<b>SR [-]</b>	0 - 5	1.5
<b>T<sub>in</sub> [K]</b>	318	
<b>P<sub>in</sub> [bar]</b>	1.300 - 1.410	1.304
<b>P<sub>exh</sub> [bar]</b>	1.475	
<b>Air Flow [kg/min]</b>	0.659	
<b>EGR [%]</b>	0	
<b>CA50 [° aTDC]</b>	13	

229

*Table 3. Experimental engine operating conditions*

230 The aim of the second strategy was to produce the same RoHR for the high swirl case  
231 (SR=3), which implies the highest GIE. The baseline case was taken as reference point.  
232 To achieve the same RoHR, the parameters CA10, CA25, CA50, CA75 and CA90 must  
233 be very similar. Thus, some considerable changes of the injection strategy (injection  
234 pressure, duration and position of each injection and number of injection) were applied  
235 as table 3 shows.

236 Commercially available European diesel fuel was used for this work. Table 4 shows the  
237 main characteristics of the fuel used.

238

<b>Fuel</b>	<b>Diesel</b>
<b>Cetane Number</b>	50.8
<b>Density @ 313K [kg/m<sup>3</sup>]</b>	820
<b>Distillation @ 65/ 85/ 95% [K]</b>	568.3 / 601.4 / 624
<b>HC Ratio</b>	6.05
<b>Weight Molecular [g/mol]</b>	215.42
<b>Dynamic Viscosity @ 313K [cSk]</b>	2.38

239

*Table 4. Fuel properties at 1 atm and 40°C*

## 240 **3. THEORETICAL TOOLS**

### 241 **3.1. 0-D model: Calmec**

242 A 0-D single-zone thermodynamic model, called CALMEC, was used to perform the  
243 combustion analysis. This model is completely described in [25]. The in-cylinder pressure  
244 signal was the main input for the combustion analysis. The signal was measured with a  
245 pressure transducer linked with its corresponding charge amplifier. The pressure signal  
246 was measured from 400 consecutive combustion cycles to avoid the experimental  
247 uncertainties due to the cycle-to-cycle variation. Each individual raw pressure data was  
248 smoothed by means of a low-pass filter. Once all recorded cycles were filtered, the set of  
249 cycles was averaged in order to create a representative in-cylinder pressure trace, which  
250 was used to carry out the combustion analysis. The first law of thermodynamics was  
251 applied between IVC and EVO (during the closed cycle), considering the combustion  
252 chamber as an open system because of the blow-by and fuel system. In addition, the ideal  
253 gas equation of state was used to calculate the average gas temperature in the combustion  
254 chamber [26]. The main output of this tool was the RoHR, which allowed for calculating  
255 other important parameters such as Start of Combustion (SoC).

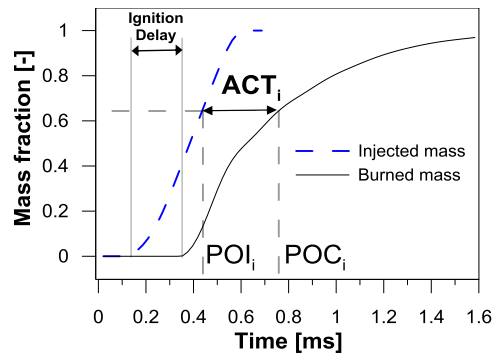
256

### 257 3.2.Apparent Combustion Time Concept

258 The Apparent Combustion Time (ACT) parameter was used to evaluate the amount of  
259 mixing during the combustion process [27]. Figure 5 illustrates that this parameter can be  
260 defined as the time interval between the instant when a determined percentage of the mass  
261 injected (point of injection,  $POI_i$ ) and the instant when the same percentage of fuel mass  
262 is burned (point of combustion,  $POC_i$ ). In a diffusion combustion process, it is noted that  
263 if a certain fuel mass is considered as a physical package, this package will not burn  
264 instantaneously at the instant POC. It will probably start to burn before the instant POC  
265 and it will finish burning after the instant POC. Therefore, the ACT (defined as  
266  $ACT=POC-POI$ ) has been considered as an approximation of the average time interval  
267 elapsed between the injection and the combustion for a particular fuel mass package. The  
268 ACT concept must be distinguished from the ignition delay. ACT matches with the  
269 ignition delay only in the first fuel injected package as figure 5 shows. Besides, the mixing  
270 time is different for the first fuel package and the last fuel package. Due to deterioration  
271 of the local thermodynamic conditions (gas density and oxygen molar fraction mainly),  
272 ACT presents an enlargement in its value when combustion process is evolving. Figure 6  
273 presents the temporal evolution of ACT (dashed blue line), which corresponds to the case  
274 showed in the figure 5. In addition,  $ACT^{-1}$  parameter is also presented in the figure 6. This  
275 parameter can be considered as a mixing capability tracer.

276

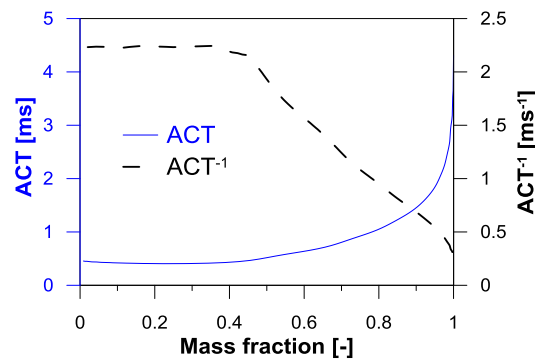




277

278

Figure 5. Definition for the Apparent Combustion Time (ACT)



279

280

281

Figure 6. Evolution of the ACT and  $ACT^{-1}$  parameter for the case shown in previous figure (single injection pulse)

282

## 4. RESULTS AND DISCUSSIONS

283

### 4.1. Impact of swirl ratio on late cycle combustion

284

An increase in swirl ratio causes an improvement in turbulence and vorticity due to the

285

higher rotational speed of the air flow and therefore, an acceleration of combustion rate

286

[28].

287

Figure 7 shows the apparent combustion time ( $ACT^{-1}$ ) parameter at 90% of total heat

288

released for the swirl ratio sweep, ranged from 0 to 5. This parameter was used as a mixing

289

capability tracer during the late cycle (from EoI up to EoC). Thus, it can be said that the

290

values present an increase in mixing capability when the swirl ratio raises up to a

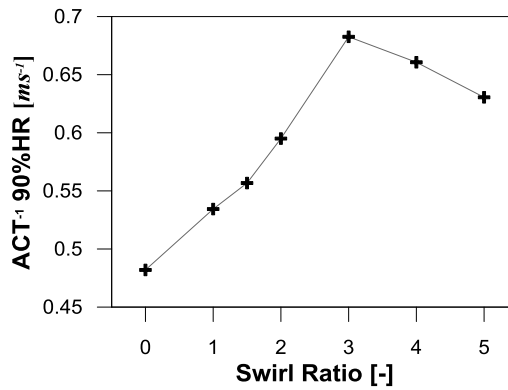
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maximum and later, a decrease in mixing parameter is produced. From  $SR=3$ , the

292

increase in swirl ratio produces presumably a deterioration of the combustion

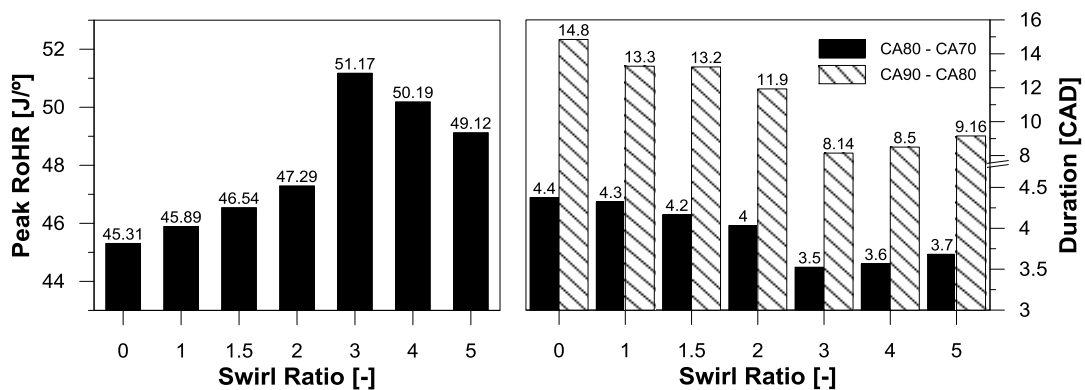
293 development due to excessive spray interaction and/or a displacement of the combustion  
 294 process towards the squish region [29]. In this sense, it is possible to state that SR= 3 is  
 295 the best condition in terms of mixing capability.



296

297 *Figure 7. ACT<sup>-1</sup> parameter at 90% of heat release for each swirl ratio at 2000rpm at 5bar BMEP.*

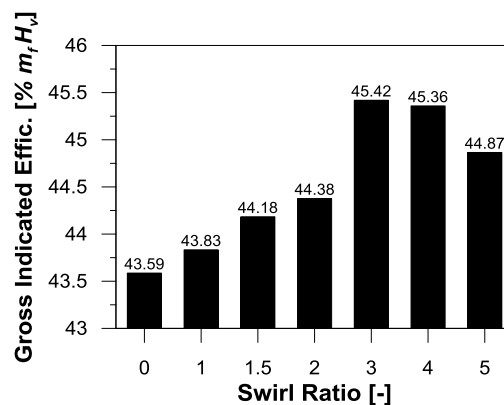
298 Figure 8 (left) represents the maximum values of RoHR for the same swirl ratio sweep.  
 299 When the swirl ratio increases, the peak of RoHR is higher due to a faster mixing process  
 300 up to the SR=3 (maximum mixing capability) due to an enhancement in the combustion  
 301 process. The figure (right) indicates the interval duration (in CAD) from 70 to 80% and  
 302 80 to 90% of the total heat release, respectively. These intervals represent approximately  
 303 the late cycle part of combustion event. The chart shows a reduction in both interval  
 304 durations when the swirl ratio is increased. It indicates that there is higher energy released  
 305 during expansion stroke, resulting a better thermal efficiency.



306

307 *Figure 8. Peak of RoHR and interval duration for swirl ratio sweep at 2000rpm at 5bar BMEP.*

308 According to the conclusion obtained in the previous figures, it is possible to conclude  
309 that, when SR is increases, the Gross Indicated Efficiency (GIE) should also be increased  
310 as shown the figure 9. This figure presents the Gross Indicated Efficiency for seven  
311 different swirl ratios. The trend is similar as figures 7 and 8. Finally, the SR= 3 condition  
312 is selected as optimum point considering that is the best SR condition for swirl sweep in  
313 terms of mixing capability, combustion process and GIE.



314

315

*Figure 9. Gross Indicated Efficiency for different swirl ratios.*

316 Once the “optimum” SR has been selected, the main goal of this section is to study the  
317 impact of SR on the soot oxidation process during the late cycle combustion, since the  
318 oxidation plays the main role in the final engine-out soot emissions. For this purpose, it  
319 was analyzed how the mixing process and bulk gas temperature affect to oxidation  
320 process for optimum SR compared with the baseline condition. For that, two tracers were  
321 used: on the one hand, the half-life time of  $ACT^{-1}$  evaluated the mixing capability and its  
322 effects on combustion process (and exhaust emissions), and on the other hand, the half-  
323 life time of optical thickness (KL) was proposed with the goal of evaluating the reduction  
324 in soot after de EoI. In addition, the average bulk gas temperature during the late cycle  
325 was also added to better understand the soot oxidation phenomenon.

326 Figure 10 (left) shows the temporal evolution of  $ACT^{-1}$  and its exponential fit  
 327 (discontinuous line) for the baseline (SR=1.5) and optimum (SR= 3) conditions. Each  
 328 curve represents the average of 400 cycles. The  $ACT^{-1}$  curves have been drawn after EoI  
 329 due to the late cycle combustion covered from EoI up to End of Combustion (EoC).

330 By definition, the half-life time of exponential  $ACT^{-1}$  curve is given by:

$$331 \quad ACT^{-1} = b \cdot e^{\frac{-\ln(2) \cdot x_{CAD}}{t_{1/2}}} \quad (3)$$

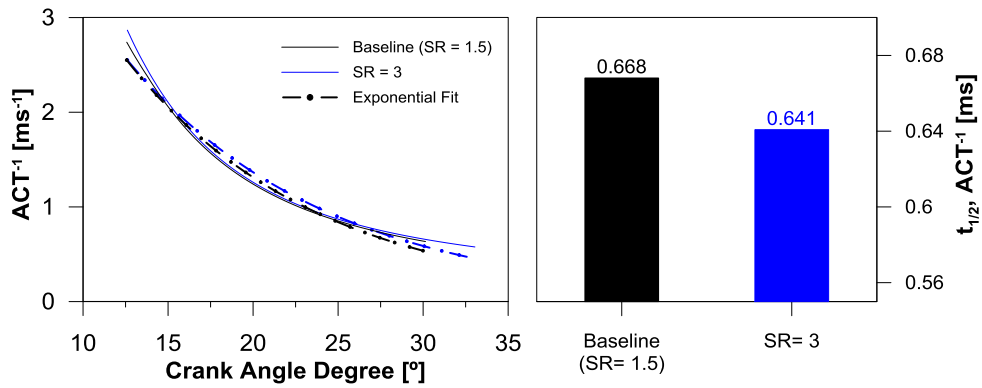
332 where  $b$  is a constant and  $x_{CAD}$  is the crank angle position aTDC in CAD. Then, the half-  
 333 life time concept was defined as the necessary time for the initial value for the variable  
 334 (in this case,  $ACT^{-1}$ ) decrease up to its half value.

335 Table 5 indicates the interval in which the  $ACT^{-1}$  curves has been fitted and the  $R^2$ -values  
 336 for the experimental fits. The exponential fits start around 13 CAD aTDC (approximately  
 337 the EoI) up to the point when the profiles approach zero.

ACT <sup>-1</sup>		
Point	Interval fitting [CAD]	R <sup>2</sup> -values
Baseline (SR= 1.5)	12.6 - 31	0.9747
SR= 3	12.6 - 33	0.9852

338 *Table 5. Interval fitting analyzed and R<sup>2</sup>-values for the experimental fits to ACT<sup>-1</sup> trace at different swirl*  
 339 *level cases.*

340 The figure 10 (right) represents the results of half-life times of  $ACT^{-1}$  for the baseline and  
 341 optimum SR case. When the swirl ratio increases, the half-life time of  $ACT^{-1}$ ,  $t_{1/2 ACT^{-1}}$ , is  
 342 reduced and so, the mixing process is improved. Maintaining constant conditions at intake  
 343 closing (air intake temperature and mass, without EGR) and the injection strategies for  
 344 both measured points, a higher value of swirl ratio is expected to enhance turbulence and  
 345 vorticity [17]. These phenomena explain a lower time to burn similar amount of injected  
 346 fuel. So, an improvement in the air/fuel mixing process was confirmed.



347

348

349

Figure 10. Temporal evolution of  $ACT^{-1}$  and its exponential fits (left) and half-life times of  $ACT^{-1}$  (right) obtained for different swirl level cases.

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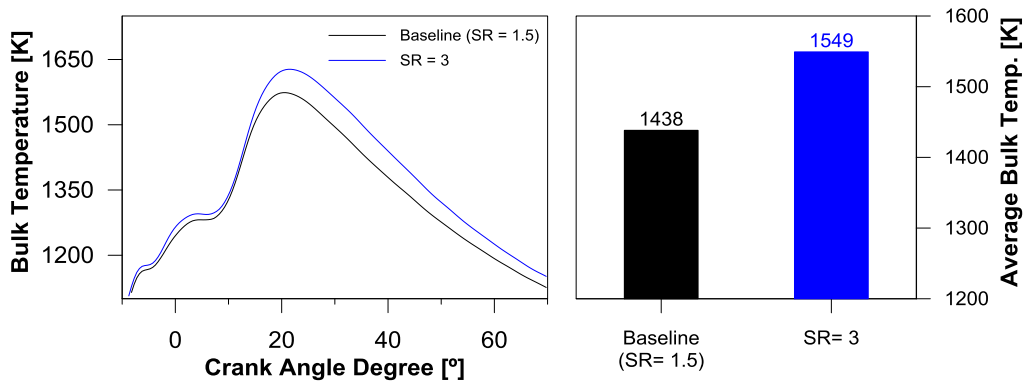
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Figure 11 shows the time evolution of gas temperature (left) and average bulk gas temperature (right) for the baseline and SR= 3 cases. This average was calculated in the same range as previously used to fit the half-life time of  $ACT^{-1}$ . Each curve represents the average of 400 cycles. As other researchers report [14], the bulk temperature has an important effect by increasing the reaction rates. Averaged bulk gas temperature value is higher for the SR=3 (approximately 100K). At higher temperatures, the soot oxidation process is expected to be enhanced in the flame sheath and then, it leads to a reduction in a both in-cylinder soot and exhaust particulate emissions.



358

359

360

Figure 11. Temporal evolution of bulk gas temperature (left) and averaged bulk gas temperature (right) obtained for different swirl level cases.

361 For evaluating the soot oxidation process, the half-life time parameter has been used  
 362 considering that KL curves take an exponential shape after the EoI. The half-life time of  
 363 KL was adjusted by an exponential fit and it is given by the following equation:

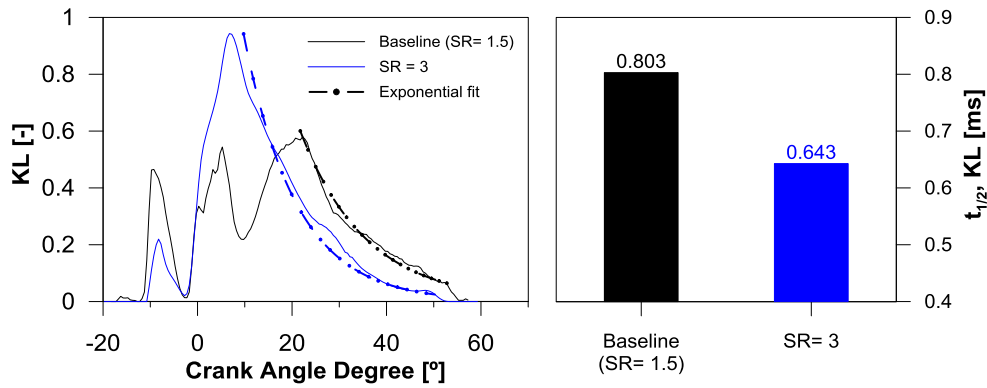
$$364 \quad KL = c \cdot e^{\frac{-\ln(2) \cdot x_{CAD}}{t_{1/2}}} \quad (4)$$

365 where  $c$  is constant and  $x_{CAD}$  is the crank angle position aTDC in CAD. So, the half-life  
 366 time of KL was determined as the time in which the soot concentration is reduced up the  
 367 half its initial value. Table 6 indicates the interval in which the KL curves have been fitted  
 368 and the  $R^2$ -values for the experimental fits. Due to higher swirl, the peak of KL is closer  
 369 the TDC than to the baseline and therefore, the onset of exponential fit is located at  
 370 different crank angle intervals.

KL		
Point	Interval fitting [CAD]	$R^2$ -values
Baseline (SR=1.5)	21 - 54	0.9503
SR= 3	11 - 51	0.9786

371 *Table 6. Interval fitting analyzed and  $R^2$ -values for the experimental fits to KL trace for the different swirl*  
 372 *level cases.*

373 Figure 12 (left) represents temporal evolution of KL and its exponential fit and the results  
 374 of half-life times of KL for the baseline and SR=3 case (right). Each curve represents the  
 375 average of 400 cycles. As it was expected [17], the half-life time of KL decreases with  
 376 the increase of swirl number, maintaining constant the rest of variables. For the optimum  
 377 SR case, the in-cylinder angular velocity is higher than the baseline. The enhanced  
 378 turbulence and vorticity produces a higher soot oxidation rate for the SR= 3 case  
 379 independently on the initial soot concentration.



380

381

*Figure 12. Temporal evolution of KL and its exponential fits (left) and half-life times of KL (right)*

382

*obtained for different swirl level cases.*

383

## **4.2. Impact of injection pattern on late cycle combustion**

384

The post-injection is a shorter injection pulse that follows the main injection, which

385

improves the mixing process and increases the temperature during the late cycle

386

combustion phase. Thus, the post-injection enhances soot oxidation leading to a reduction

387

in the engine-out soot emissions [30]. The effects of injection pressure and post injections

388

are well-known on the combustion process. An increase in injection pressure causes an

389

equivalence ratio reduction at the lift-off length (LOL) and thus, a reduction in soot

390

formation [10]. In the current section, the aim is to obtain similar RoHR to SR=3

391

(optimum GIE case) by using a reduced swirl ratio (baseline SR= 1.5 case) condition by

392

modifying only the injection settings (number of injection, injection pressure and duration

393

and position of each injection event).

394

Figure 13 explains how the injection settings were determined to obtain the similar

395

RoHR. Thus, to replicate the RoHR obtained with the highest swirl ratio tested using the

396

lowest swirl, different steps were proposed. First, the injection pressure was increased in

397

steps of 50 bar. Faster RoHR with higher peak was obtained after this process. In the

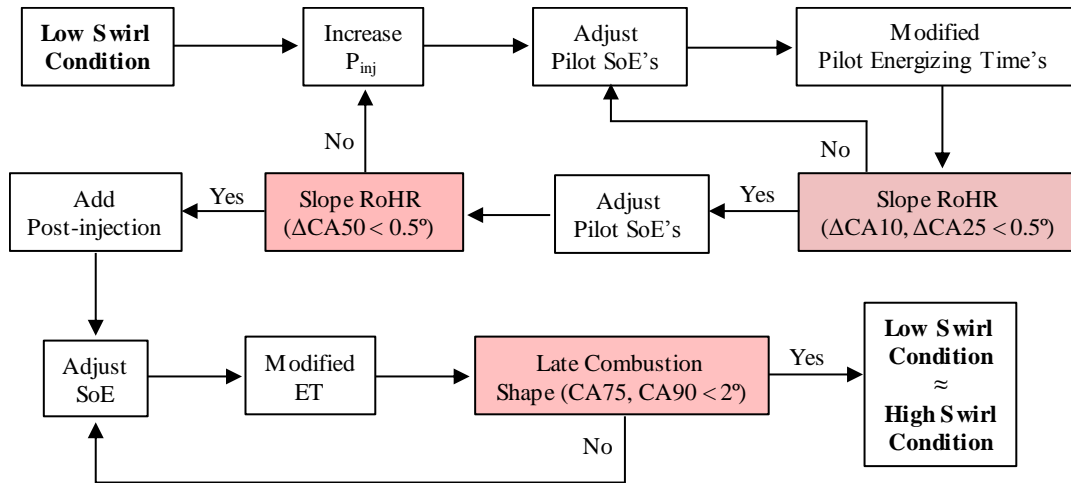
398

following step, the Start of Energizing (SoE) times, as well as the Energizing Times (ET),

399

were changed to adjust the CA10, CA25 and CA50 parameter for both operating

400 conditions (SR= 3 and post-injection case at SR = 1.5). Finally, a post injection event was  
 401 added to compensate the better mixing process at the late cycle combustion phase  
 402 achieved with the optimum SR=3 case. With this proposal, the differences between CA75  
 403 and CA90 were acceptable (less 2° CAD).



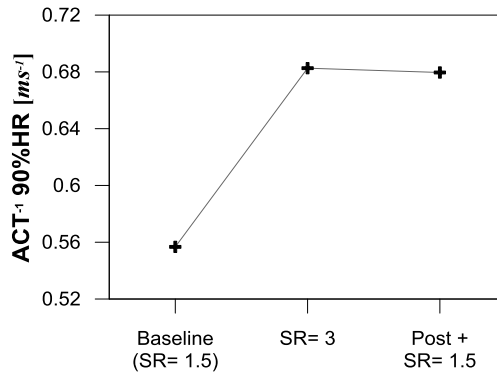
404

405 *Figure 13. Experimental methodology used to get similar RoHR of SR= 3 with baseline*  
 406 *condition (SR=1.5).*

407 Figures 14, 15 and 16 evaluate the mixing and combustion processes of the post injection  
 408 case at the baseline SR of 1.5 compared to the optimum (SR= 3) case.

409 Figure 14 shows the apparent combustion time (ACT<sup>-1</sup>) parameter at 90% of total heat  
 410 release for baseline, optimum and post injection cases. It is possible to note that the post  
 411 injection case presents a similar mixing capability to the SR=3 case and, as it has been  
 412 explained in the previous sub-section, both operating conditions show an increase in  
 413 mixing capability when compared to the baseline case.

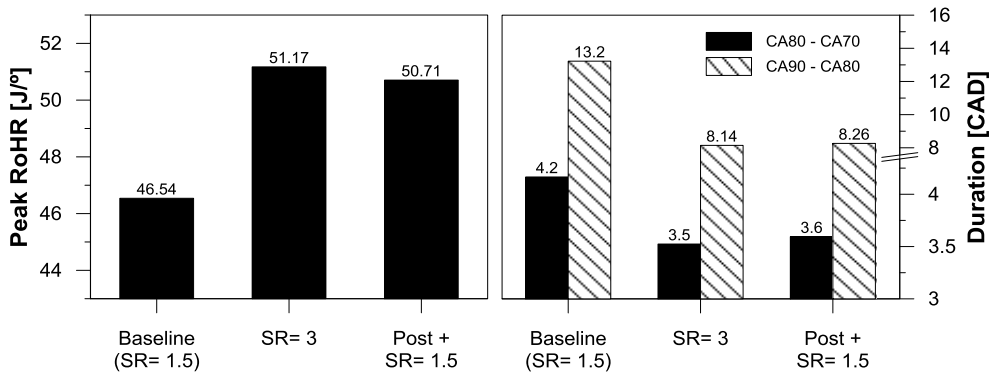




414

415 *Figure 14. ACT<sup>-1</sup> parameter at 90% of heat release for the baseline, optimum SR and post injection case.*

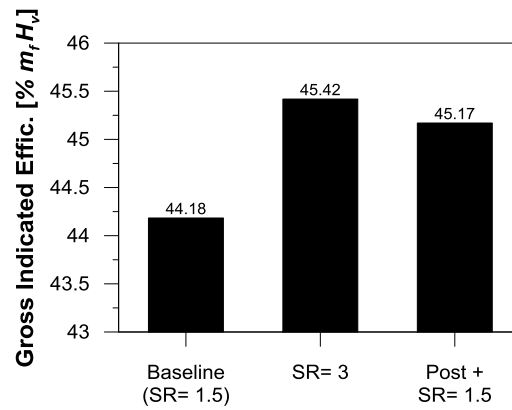
416 In addition, the peak of RoHR is slightly higher at SR= 3 than the post injection case  
 417 (approximately 1 J/°) as shown in the figure 15. This fact could be due to the small  
 418 differences in the RoHR fit. Considering the interval duration from 70 to 80% and 80 to  
 419 90 % of the total heat release, the trend follows the same shape. The values of SR= 3 and  
 420 post-injection case are very similar and the interval durations are shorter compared to the  
 421 baseline case.



422

423 *Figure 15. Peak of RoHR and interval duration for the baseline, optimum SR and post injection case.*

424 Figure 16 presents the GIE for the three different operating conditions. According to the  
 425 conclusion obtained in the two previous figures, SR= 3 and post injection case present  
 426 similar values of GIE. It can be therefore concluded that the selected injection strategies  
 427 replicate the optimum case (SR= 3).



428

429

*Figure 16. Gross Indicated Efficiency for the baseline, optimum SR and post injection case.*

430

Once the post injection case has been selected, it is necessary to study the impact of the

431

injection pattern on the soot oxidation during the late cycle combustion. Following similar

432

work scheme as the swirl ratio section, the relationship of mixing process and bulk gas

433

temperature on the soot oxidation process for post injection and baseline cases was

434

studied.

435

Figure 17 (left) shows the temporal evolution of  $ACT^{-1}$  and its exponential fit

436

(discontinuous line) for the baseline and post injection conditions. Each curve represents

437

the average of 400 cycles. The crank angle ranges and  $R^2$ -values for the exponential fit

438

are presented in table 7. Figure 17 (right) presents the half-life times of  $ACT^{-1}$  for the

439

baseline and post injection case. The half-life of  $ACT^{-1}$  with the post injection pulse is

440

lower than the baseline case due to mainly two phenomena: the injection pressure and the

441

post injection event. On the one side, if the injection pressure increases, the half-life time

442

of  $ACT^{-1}$  is reduced. A higher injection pressure produces an increase in the movement

443

of the in-cylinder air environment due to the higher momentum of the spray and so, this

444

air movement enhances the air/fuel mixing process during the late cycle combustion [14].

445

On the other side, the mixing process is improved by adding the post injection. The post

446

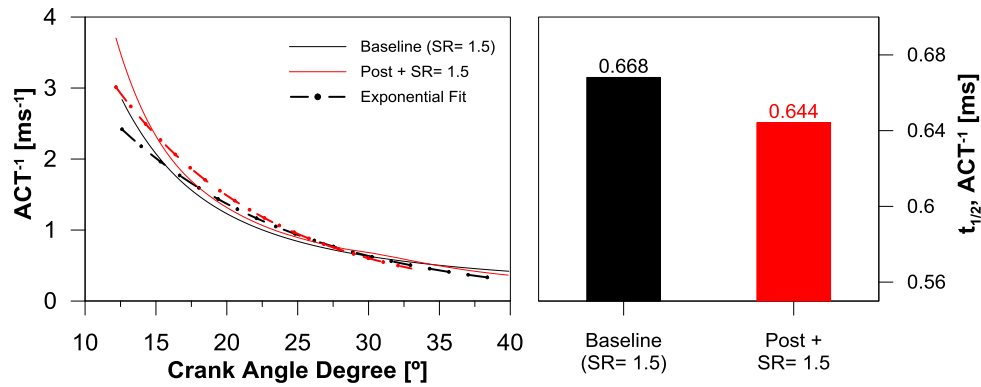
injection redistributes the fuel from the main injection, generating a more well mixed

447

air/fuel distribution [19].

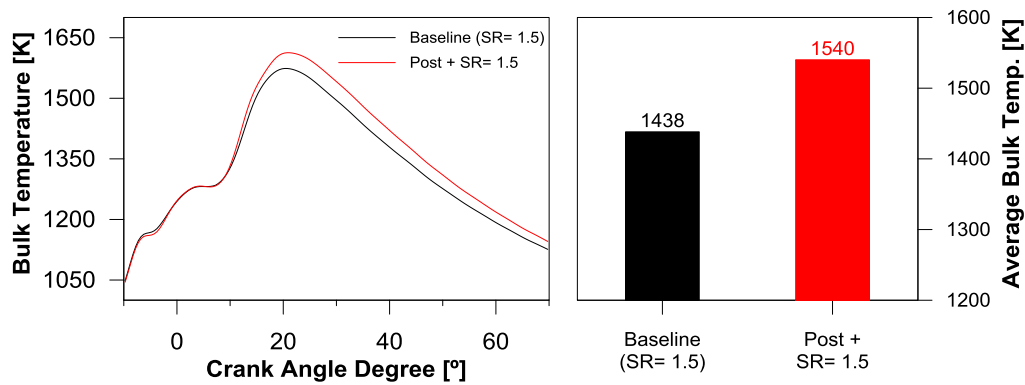
ACT <sup>-1</sup>		
Point	Interval fitting [CAD]	R <sup>2</sup> -values
Baseline (SR=1.5)	12.6 - 33	0.9747
Post + SR=1.5	12.1 - 33	0.9299

448 Table 7. Interval fitting analyzed and R<sup>2</sup>-values for the experimental fits to ACT<sup>-1</sup> trace for the different  
 449 injection pattern



450  
 451 Figure 17. Temporal evolution of ACT<sup>-1</sup> and its exponential fits (left) and half-life times of ACT<sup>-1</sup> (right)  
 452 obtained for different injection pattern

453 Figure 18 shows temporal evolution of gas temperature (left) and average bulk gas  
 454 temperature (right) during the late cycle for the baseline and post injection conditions.  
 455 Each curve represents the average of 400 cycles. The average bulk temperature for the  
 456 post injection case is higher than the baseline case (around 100K). As in the previous sub-  
 457 section, soot oxidation process is enhanced when the bulk gas temperature is higher.



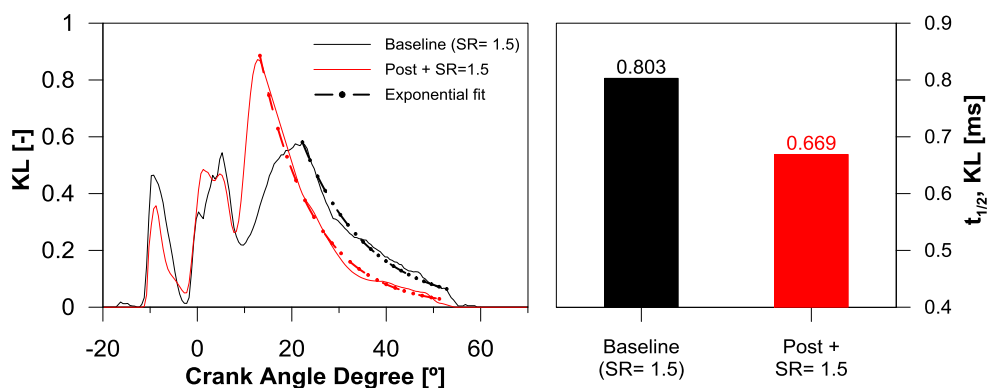
458  
 459 Figure 18. Temporal evolution of bulk gas temperature (left) and averaged bulk gas temperature (right)  
 460 obtained for different injection pattern.

461 Once the mixing process and bulk gas temperature were studied, it was necessary to  
 462 evaluate the soot oxidation process.

463 Figure 19 (left) represents temporal evolution of KL and its exponential fit for the baseline  
 464 and post injection cases. Each curve represents the average of 400 cycles. The selected  
 465 crank angle ranges for the exponential fit and  $R^2$ -values are presented in table 8. Figure  
 466 19 (right) shows the results of half-life times of KL for the baseline and post injection  
 467 case. As expected, the half-life time of KL for the post injection case was lower than the  
 468 baseline case. An increase in injection pressure enhances the mixing process during the  
 469 late cycle combustion and thereby, the soot oxidation process. As other researches have  
 470 reported in the literature [31, 32], post injection enhances mixing of soot from the main  
 471 injection and available in-cylinder air/O<sub>2</sub> and the oxidation of this soot is enhanced due  
 472 to combustion of the post-injection fuel.

KL		
Point	Interval fitting [CAD]	R <sup>2</sup> -values
Baseline (SR= 1.5)	21 - 54	0.9503
Post + SR= 1.5	12 - 51	0.9742

473 *Table 8. Interval fitting analyzed and R<sup>2</sup>-values for the experimental fits to KL trace for the different*  
 474 *injection pattern.*

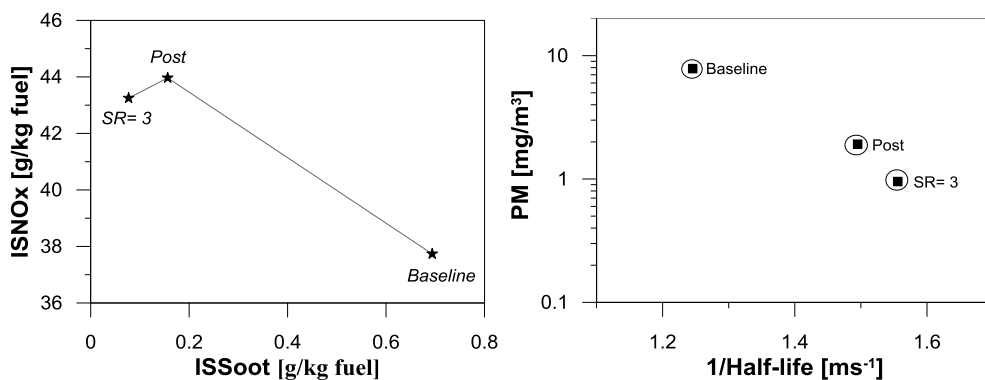


475  
 476 *Figure 19. Temporal evolution of KL and its exponential fits (left) and half-life times of KL (right)*  
 477 *obtained for different injection pattern.*

478 **4.3. Emissions comparison of optimized swirl ratio and post**  
479 **injection strategies on late cycle combustion**

480 Once the soot oxidation has been analyzed independently for the two different strategies  
481 versus the baseline case, this section aims to compare the optimum swirl ratio and post  
482 injection cases during the late cycle combustion. This comparison has been used to  
483 identify the best engine strategy.

484 Figure 20 (left) shows the engine-out NO<sub>x</sub> and soot emissions for baseline, optimum SR  
485 and post-injection conditions. The expected soot-NO<sub>x</sub> trade-off is found. Considering  
486 that combustion process between optimum SR and post injection case is quite similar, it  
487 is also expected to have similar engine-out emissions. A negligible difference in NO<sub>x</sub>  
488 emission (approximately 0.7 g/kg fuel) was measured. In addition, these conditions  
489 present higher values than the baseline case. This fact is maybe due to a faster combustion  
490 process and thus higher local combustion temperatures for the maximum GIE cases than  
491 the baseline case. Regarding soot emissions, it is interesting to remark that the post-  
492 injection soot is quite similar to the SR= 3 case and significantly lower than the baseline  
493 case due to an improvement of mixing and oxidation processes.



494  
495 *Figure 20. Left) The ISNO<sub>x</sub> vs ISSoot emissions for the 3 different point at 2000rpm@ 5bar BMEP. Right*  
496 *Soot emissions versus half-life time of KL for each swirl ratio at 2000rpm at 5bar BMEP*

497 Figure 20 (right) presents engine-out emissions versus the inverse of half-life time of KL  
498 ( $1/t_{1/2,KL}$ ) on a semi-logarithmic scale for swirl ratio sweep and post-injection case. The  
499 three conditions studied in this research have been marked with black circles. It is  
500 observed that the soot emissions are drastically reduced for the SR= 3 and post injection  
501 cases, where the soot oxidation rate (and mixing capability) was improved. A linear  
502 relationship is established between the soot emissions and the oxidation rate. Therefore,  
503 engine-out soot emissions are governed mainly by oxidation process. In conclusion, it is  
504 possible to improve the late cycle diffusion combustion (and thus, soot oxidation process)  
505 with an appropriate injection strategy for a low SR condition.

## 506 **5. CONCLUSIONS**

507 The main objective of this work was to compare different engine strategies to enhance  
508 the late cycle mixing controlled combustion process and therefore, to improve the soot  
509 oxidation while maintaining similar gross indicated efficiency. The experimental  
510 measurements were made in a light-duty engine by modifying the swirl ratio and the  
511 injection strategy. In particular, experimental and theoretical parameters were used to  
512 carry out the research. The apparent combustion time ( $ACT^{-1}$ ) was used as mixing tracer.  
513 An exponential fit was applied to the temporal evolution of  $ACT^{-1}$ . This parameter is  
514 based on the injection rate profile and the experimental heat release. The soot oxidation  
515 process was evaluated with an exponential fit applied to the temporal evolution of optical  
516 thickness (KL). KL was obtained by applying the two color method using a dedicated  
517 optoelectronic pyrometer. Finally, both strategies (swirl ratio and injection pattern) were  
518 compared in terms of engine-out emissions. The conclusions of the study can be  
519 summarized as follows:

- 520 • An increase in swirl ratio is not directly related with an increase in mixing process  
521 during the late cycle combustion. Indeed, an excessive SR can lead a deterioration  
522 of the combustion development due to excessive spray interaction, which causes  
523 a slower and less powerful heat release process reducing the indicated efficiency.
- 524 • Half-life time of KL was revealed as a proper tracer for characterizing soot  
525 emissions in CI engines. This parameter is governed by mixing capability (half-  
526 life time of ACT-1) and bulk gas temperature. When half-life of ACT-1 is reduced  
527 due to higher SR and/or injection pressure and/or post injection addition, the  
528 average bulk gas temperature is increased. Both phenomena cause an  
529 improvement in the soot oxidation process (reducing half-life of KL).
- 530 • A proper injection pattern (increase of injection pressure and post injection  
531 addition) coupled with a low SR was showed as a suitable strategy to improve the  
532 late cycle diffusion combustion as well as soot oxidation while maintaining  
533 constant GIE.
- 534 • According to the emission results obtained, the expected soot-NO<sub>x</sub> trade-off was  
535 found. So, considering that combustion process between optimum SR = 3 and post  
536 injection case was quite similar, it was also expected to have similar engine out  
537 emissions. Thus, the soot reduction can be attained with higher swirl ratio and a  
538 proper injection strategy. On the contrary, NO<sub>x</sub> emissions increased appreciably  
539 when the mixing process is enhanced (SR = 3 and SR=1.5 adjusted). In addition,  
540 a linear relationship was established between the soot emissions and the soot  
541 oxidation process, which indicates that mainly the soot oxidation process governs  
542 the engine-soot emissions.

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## 654 **Abbreviations**

- 655 ACT: Apparent Combustion Time
- 656 BMEP: Brake Mean Effective Pressure
- 657 CA50: Crank Angle at 50% mass fraction burned
- 658 CAD: Crank Angle Degree

659 CI: Combustion Ignition

660 DI: Direct-Injection

661 EGR: Exhaust Gases Recirculation

662 EoC: End of Combustion

663 EoI: End of Injection

664 ET: Energizing Time

665 EVO: Exhaust Valve Open

666 FSN: Filter Smoke Number

667 FWHM: Full Width at Half Maximum

668 GHG: Greenhouse Gases

669 GIE: Gross Indicated Efficiency

670 ICE: Internal Combustion Engines

671 IVC: Inlet Valve Close

672  $I_{b,\lambda}$ : Spectral Intensity of Black Body

673  $I_{\text{soot}}$ : Spectral Intensity

674 KL: Optical Thickness

675 LOL: Lift-off Length

676 NO<sub>x</sub>: Nitrogen Oxides

677  $P_{\text{in}}$ : Intake Pressure

678 PM: Particulate Matter

679 POC: Point of Combustion

680 POI: Point of Injection

681 RoHR: Rate of Heat Release

682 SoE: Start of Energizing

683 SR: Swirl Ratio

684 TDC: Top Dead Center

685  $T_{in}$ : Intake Temperature

686  $\alpha$ : Absorptivity

687  $\varepsilon$ : Emissivity

688  $\lambda$ : Wavelength