

# Proposal of Strength Formula and Type Development of Composite Mega Column to Beam Connections with T-shaped Stiffener

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## Abstract

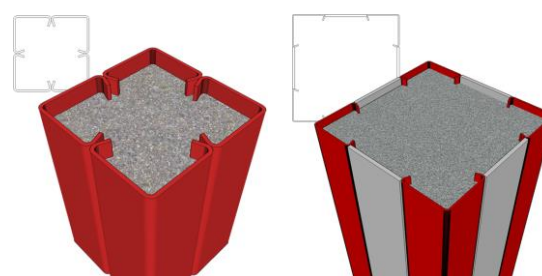
As buildings are becoming larger, demand for mega-sized composite columns (over 1-meter diameter) is increased. We have developed and commercialized welded built-up CFT column (ACT Column I) since 2005 which are structurally stable and economical using cold-formed steel with rib. However, there has a limit in size of cross section (618 X 618mm) by a fabrication facilities. And due to characteristics of closed cross section, there has a limit to construction of connection of moment frame. Composite mega column (ACT Column II) has same concept of forming closed cross section. But in order to enlarge cross sectional size, thick plate is inserted between cold-formed steels. Since composite mega column can control thickness and width of thick plate, steel or composite beams can be directly attached to the connection. In this study, we propose strength formula of composite mega column to beam connections with T-shaped stiffener as internal diaphragm and verified through finite element analysis and simple tensile experiment.

**Keywords:** *Welded built-up CFT column; Composite mega column; T-shaped Stiffener; Tensile strength formula*

## 1. Introduction

### 1.1. Background and purpose of study

Due to development of IT / logistics industry, internet transactions have risen and buildings have become larger for logistics storage and delivery. As a result, demand for large-sized composite columns for heavy loads also increased. In previous study, we have developed stable and economical welded built-up CFT column (ACT Column I) using cold-formed steel with rib. However, there has a limit in size of cross section (618mm X 618mm). And it is difficult to select inner diaphragm and through diaphragm because continuity of rib must be secured in order to demonstrate structural performance as a column. In addition, due to characteristics of closed cross section, there has a limit to construction of connection for moment frame. Fig. 1 (a) shows shape of welded built-up CFT Column.[1]



(a)Welded built-up CFT column (b)Composite mega column

Fig. 1. Shape of ACT Column

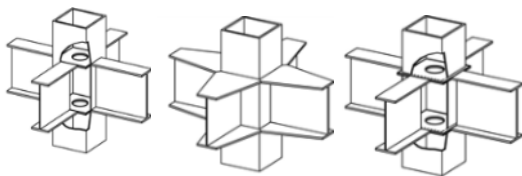
Then, in order to solve problems of welded built-up CFT column, composite mega column (ACT Column II) was developed while maintaining advantages of welded built-up column. Composite mega column has a closed cross section like welded built-up column, but thick plate is inserted between cold-formed steel to expand cross section size. Fig. 1 (b) shows shape of composite mega column. And because

stiffener can be pre-assembled to thick plate, there is an advantage that detail of connection is simplified. In addition, thickness and width of thick plate can be adjusted, steel or composite beams can be directly attached to the connection. Fig. 2 shows basic concept of composite mega column forming process.



Fig. 2. Basic concept of composite mega column

However, despite structural strength of composite mega column, characteristic of closed cross section make it difficult to reinforce connection and complicate construction of connection. Therefore, it is necessary to develop and study connection type that can secure strength of connection and take into consideration workability and economy. Currently, commonly used types of connections are classified into three types as shown in Fig. 3: through diaphragm, internal diaphragm, and external diaphragm.



(a) internal diaphragm (b) external diaphragm (c) through diaphragm

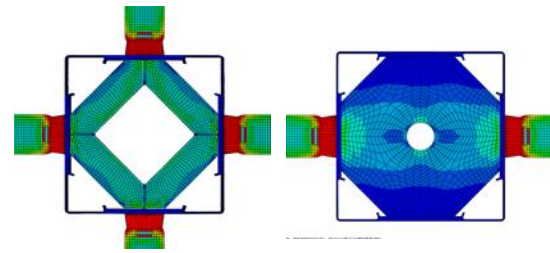
Fig. 3. CFT column to beam connection type

External diaphragm was applied to welded built-up CFT column to secure continuity of rib. However, if external diaphragm is applied to composite mega column with a width of 1m or more, amount of steel increases greatly and interference with finishing material occurs. Therefore, in this study, connection type is set as internal diaphragm, we will develop connection shape and propose strength formula.

## 2. Connection type of inner diaphragm

Composite mega column were applied to internal diaphragm connection to overcome problems of external diaphragm. In previous study, internal diaphragm is divided into two types, horizontal stiffener and T-shaped stiffener.

Shape of each internal diaphragm is shown in Fig. 4.[2]



(a) T-shaped stiffener (b) Horizontal stiffener

Fig. 4. Application shape of internal diaphragm

T-shaped stiffener is composed of two members, vertical member and horizontal member. In composite mega column, vertical member acts as anchor to induce concrete cone failure. Further, load transfer can be clarified through horizontal member. Horizontal stiffener is internal diaphragm having only a horizontal member, and larger amount of steel is used than T-shaped stiffener. Based on these characteristics, it is considered that T-shaped stiffener is effective diaphragm shape as compared with horizontal stiffener and is suitable for composite mega column. Therefore, we propose a strength formula of composite mega column connection with T-shaped stiffener.

### 2.1. Details of T-shaped stiffener

When beam flange is subjected to tensile force, T-shaped stiffener welded to inner surface of column transmits tensile force on opposite side with deformation. As shown in Fig. 5, T-shaped stiffener is divided into vertical member and horizontal member. Horizontal member determines size of cross section to resist tensile force, and vertical member determines height of concrete cone.

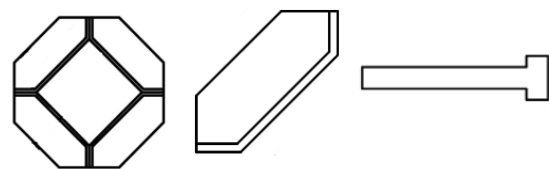


Fig. 5. Details of T-shaped stiffener

## 3. Proposal of composite mega column connection strength formula

Load resistance mechanism for each model is as follows. In case of concrete non-charging model, it is assumed that out-of-plane

deformation of steel pipe and yield strength of T-shaped stiffener resist load. In case of concrete charging model, since concrete controls out-of-plane deformation of steel pipe, it is assumed that it is resistant to load by concrete cone failure and yield strength of T-shaped stiffener.

### 3.1. Limitations for strength formula proposal

(1) Maximum strength of weld zone shall be greater than maximum strength of non-charging or charging steel pipe.

(2) Strength of proposed formula should be greater than beam flange tensile strength.

(3) In case of concrete charging model, it is assumed that tensile force transferred from beam flange is transferred to concrete cone and T-shaped stiffener.

### 3.2. T-shaped stiffener yield strength formula

Cross-sectional size of T-shaped stiffener can be expressed as Eq. (1). Yield strength of T-shaped stiffener is assumed to be tensile at all of cross sections. And as can be seen from the arrow in Fig. 6, tensile force transferred from flange acts as angle of  $\theta$ . Yield strength formula of T-shaped stiffener is shown in Eq. (2).

Tshaped Stiffener Cross sectional size

$$= b_s \times h_s \times t_{sh} \times t_{sv} \quad (1)$$

$$P_s = b_s \times t_{sh} \times f_{ys} \times 2 \times \cos \theta \quad (2)$$

$b_s$  : Width of horizontal member

$h_s$  : Height of vertical member

$t_{sh}$  : Thickness of horizontal member

$t_{sv}$  : Thickness of vertical member

$f_{ys}$  : Yield strength of T-shaped stiffener

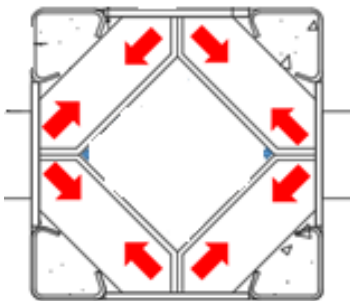


Fig. 6. Tensile force transfer in T-shaped stiffener

### 3.3. Concrete cone failure strength formula

Concrete cone failure resulting from tensile force transferred from T-shaped stiffener vertical member is based on assumption that cone failure occurs in 45 degree direction. Cone failure is assumed to occur simultaneously with deformation of T-shaped stiffener. Area of cone failure consists of area surrounded by line connecting column-side end of T-shaped stiffener to end of T-shaped stiffener vertical member.

(1) Cone failure area in column section

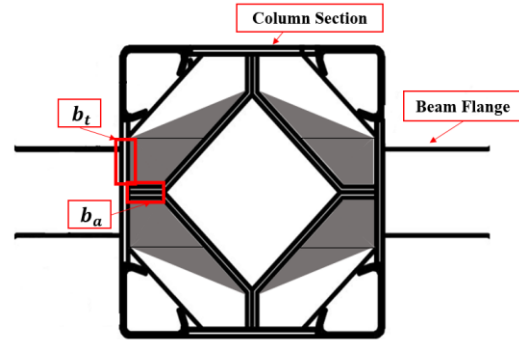


Fig. 7. Cone failure in column section

Concrete Cone failure area in column section is shown in Fig. 7. This area is assumed to be area surrounded by line connecting column-side end of T-shaped stiffener to end of T-shaped stiffener vertical member. Strength formula for concrete cone failure in column section is shown in Eq. (3).

$$P_{c1} = 2 \times \left[ \left( (\sqrt{2}b_s + b_a) \times b_t \right) + \left( \sqrt{2}b_s \times \left( \frac{b_c}{2} - t_{sv} - b_a - b_t \right) \right) \right] \times v_c \quad (3)$$

$b_a$  : Length of rib /  $b_c$  : Width of concrete

$b_t$  : Width of T-shaped stiffener attached to thick plate

$v_c$  : Shear strength of concrete

(2) Cone failure area at front of column

Cone failure area at front of column is area generated at 45 degree from end of T-shaped stiffener vertical member as shown in Fig. 8. Strength formula for concrete cone failure at front of column is shown in Eq. (4).

$$P_{c2} = 2f_t(h_c + h_s - 2t_{sh}) \times \left( \frac{b_c}{2} - t_{sv} \right) \quad (4)$$

$h_c$  : Height of concrete cone

$f_t$  : Tensile strength of concrete

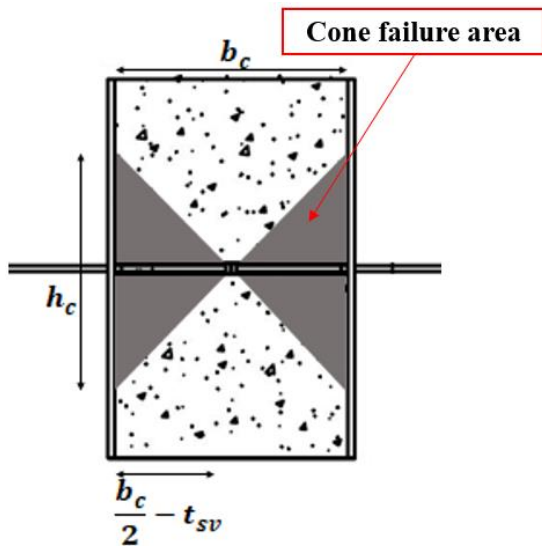
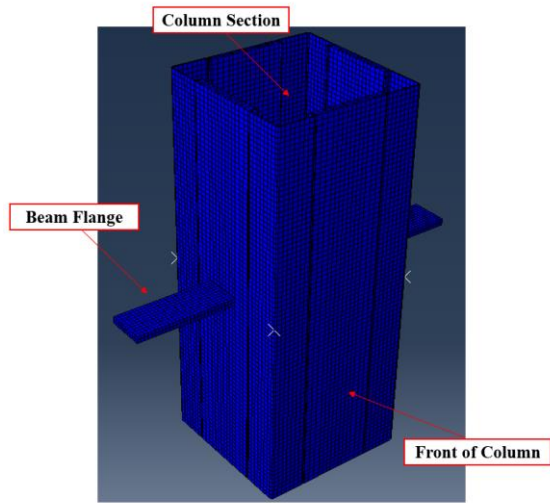


Fig. 8. Cone failure at front of column

#### 4. Finite element analysis for T-shaped stiffener yield strength formula verification

##### 4.1. Analysis overview

For verification of proposed strength formula, finite element analysis was performed using Abaqus 6.13. Analysis was carried out on simple tensile connection with beam flange (PL-300X55mm) attached to steel pipe of 1200X1200X3000mm in size. Analysis used solid element and boundary conditions were fixed at  $U_1, U_2, U_3=0$  on one flange and 500mm displacement control on  $U_1$  at the end of opposite flange. Yield strength of applied material is 325MPa and modulus of elasticity is 205GPa. Loading was performed by 500mm

displacement control and strength was evaluated by reaction force of flange.

Table 1. Finite element analysis object

Specimen	Parameter	
	reinforcement	Section size(mm)
4-1	X	-
4-2	O	157.06*110*55*55
4-3	O	135.84*110*55*55

##### 4.2. Analysis result

###### (1) Specimen 4-1

In case of specimen 4-1, since T-shaped stiffener was not reinforced, resistance was only caused by out-of-plane deformation of steel pipe. Since displacement was controlled to 500mm, load continued to increase, but yield of beam flange could not be reached. Fig. 9 shows analysis result of specimen 4-1.

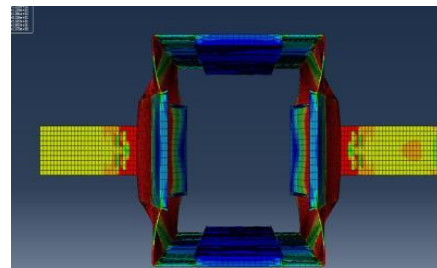


Fig. 9. Result of specimen 4-1

###### (2) Specimen 4-2

In case of specimen 4-2, T-shaped stiffener was reinforced. In the beginning, tensile force was transferred to T-shaped stiffener. After T-shaped stiffener yielded, out-of-plane deformation of steel pipe began to appear distinctly. Yield strength of T-shaped stiffener and resistance of out-of-plane deformation of steel pipe are larger than beam flange yield strength, resulting in beam flange yielding. Fig. 10 and 11 show yield and analysis result of specimen 4-2.

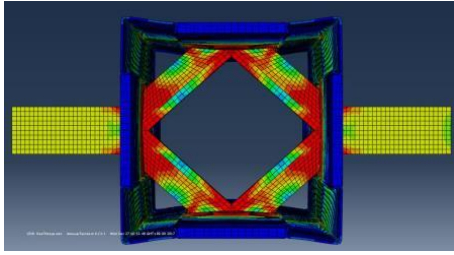


Fig. 10. Yield of specimen 4-2 T-shaped stiffener

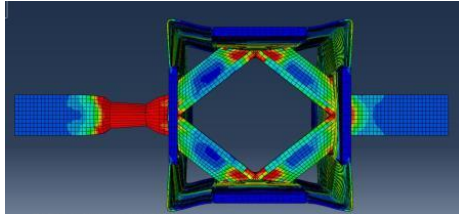


Fig. 11. Result of specimen 4-2

(3) Specimen 4-3

Specimen 4-3 showed same behavior as specimen 4-2, and yield strength of T-shaped stiffener was less than specimen 4-2 because width of T-shaped stiffener horizontal member was narrow. Fig. 12 and 13 show yield and analysis result of specimen 4-3.

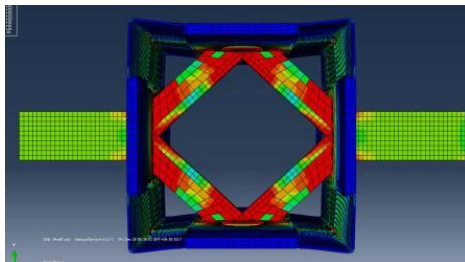


Fig. 12. Yield of specimen 4-3 T-shaped stiffener

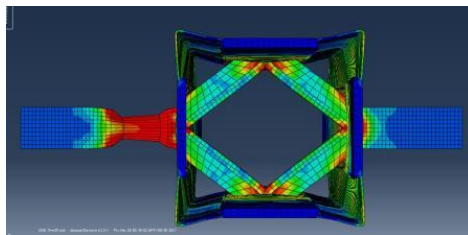


Fig. 13. Result of specimen 4-3

4.3. Analysis and discussion

Fig. 14. shows load-displacement relation for each specimen, and Table 2 shows T-shaped stiffener yield strength, beam flange yield strength and maximum load.

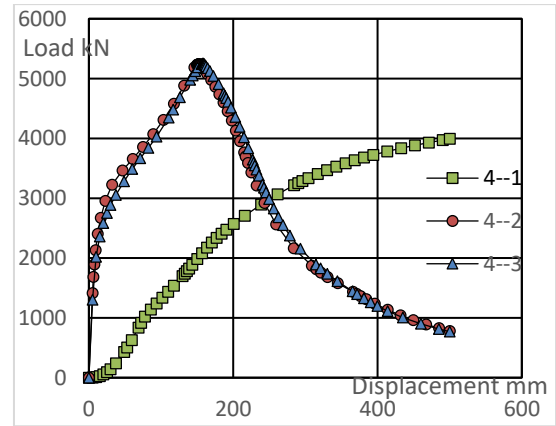


Fig. 14. Load-Displacement graph

Table 2. Result of finite element analysis

Specimen	T-shaped stiffener yield strength	Beam flange yield strength	Maximum load
4-1	-	-	3992.9kN
4-2	3856.92kN	5240kN	5240kN
4-3	3487.96kN	5250.1kN	5250.1kN

Yield strength of beam flange used in analysis is 5362.5kN by formula. Value according to T-shaped stiffener yield strength formula is 3970.33kN for specimen 4-2 and 3433.91kN for specimen 4-3. Table 3 and Table 4 compares analytical value with formula value.

Table 3. Comparison of T-shaped stiffener

Specimen	Analytical value	Formula value	Formula / Analysis
4-2	3856.92kN	3970.33kN	1.029
4-3	3487.96kN	3433.91kN	0.985

Table 4. Comparison of beam flange

Specimen	Analytical value	Formula value	Formula / Analysis
4-2	5240kN	5362.5kN	1.023
4-3	5250.1kN	5362.5kN	1.021

Yield strength of T-shaped stiffener and beam flange were compared with analytical value and formula value, respectively. As a result, in case of specimen 4-2, difference was 2.9% for T-shaped stiffener and 2.3% for beam flange. In case of specimen 4-3, difference was 1.5% for T-shaped stiffener and 2.1% for beam flange.

## 5. Tensile experiment of column-beam connection to confirm behavior of concrete and T-shaped stiffener

### 5.1. Plan of experiment

Columns of specimens used for column-beam connection tensile experiment were divided into three types according to width. Beam flange is divided into two types according to thickness, and T-shaped stiffener is divided into three types according to size. There are 5 types of experiment specimen, all using SM490. Unlike analysis, all experiments were charged with concrete and concrete strength was planned to be 24MPa. Experiment was applied tensile force on both sides of beam flange using 3000kN hydraulic universal testing machine(U.T.M). Load was applied to displacement control with 0.02mm/s of force speed until failure mode was confirmed after maximum load. Table 5 and Fig. 15 show specimen of Tensile experiment.

Table 5. List of experiment specimen

Specimen	Width of Column	Beam flange	T-shaped stiffener
5-1	500mm	150*14	106.07*28*14*14
5-2	500mm	150*10	106.065*20*10*10
5-3	500mm	150*10	80*20*10*10
5-4	650mm	150*14	106.07*28*14*14
5-5	800mm	150*14	106.07*28*14*14

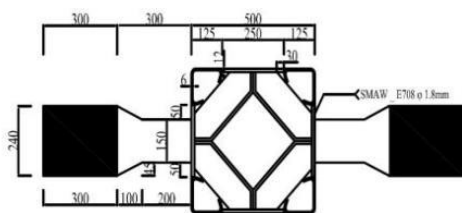


Fig. 15. Details of 500mm cross section

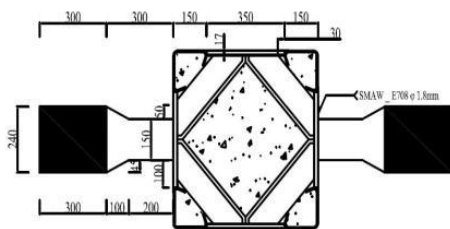


Fig. 16. Details of 650mm cross section

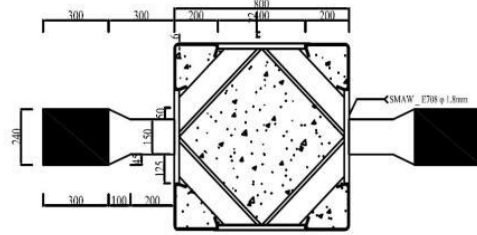


Fig. 17. Details of 800mm cross section

### 5.2. Result of experiment

#### (1) Result of material test

In order to investigate mechanical properties of steel used in this experiment, three tensile test specimens were cut and tested in accordance with KS B 0801 and 0802 standards. Material used is SM490 10mm, 14mm steel. Results of each test specimen are shown in Table 6. In addition, concrete specimens were subjected to 21day compressive strength test, and test results are shown in Table 7.

Table 6. Result of tensile test

Steel grade	Thickness	Yield strength	Tensile strength
SM490	10mm	450MPa	536MPa
	14mm	366MPa	478MPa

Table 7. Result of concrete compressive strength test

Design Strength	Size	Test Result
24MPa	Φ100 x 200	27MPa

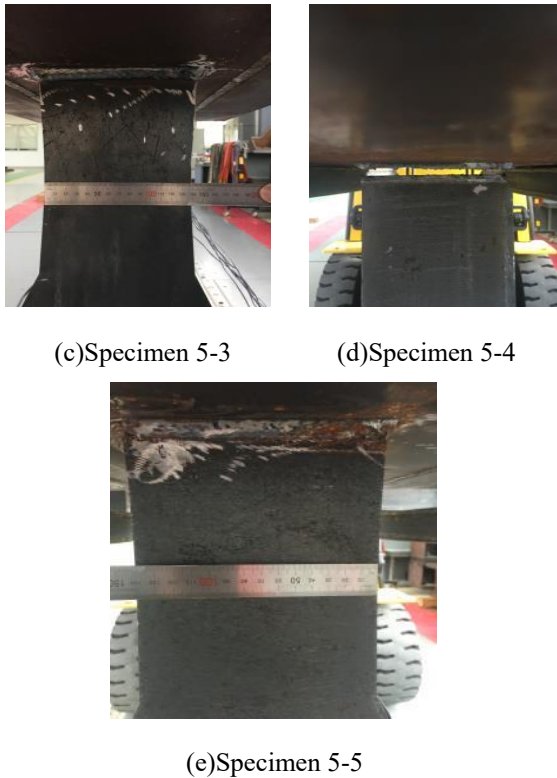
#### (2) Result of connection tensile experiment

Table 8 shows results of connection tensile experiment, and Fig. 18 shows failure mode of each specimen.



(a) Specimen 5-1

(b) Specimen 5-2



(c) Specimen 5-3 (d) Specimen 5-4

(e) Specimen 5-5

Fig. 18. Failure mode of each specimen

Table 8. Result of tensile experiment

Specimen	Yield load	Maximum load	Expected load
5-1	760kN	952kN	769kN
5-2	667kN	786kN	675kN
5-3	701kN	799kN	675kN
5-4	771kN	1029kN	769kN
5-5	771kN	1069kN	769kN

Expected load is value obtained by multiplying cross sectional area of beam flange by material test result, respectively. Yield load of experiment was within 3% error of expected load. Failure mode was observed at weld zone of beam flange-column steel pipe at specimen 5-1 and 5-4. Specimen 5-2, 5-3, 5-5 showed beam flange necking. Load-Displacement graph for each specimen is shown in Fig. 19 and 20.

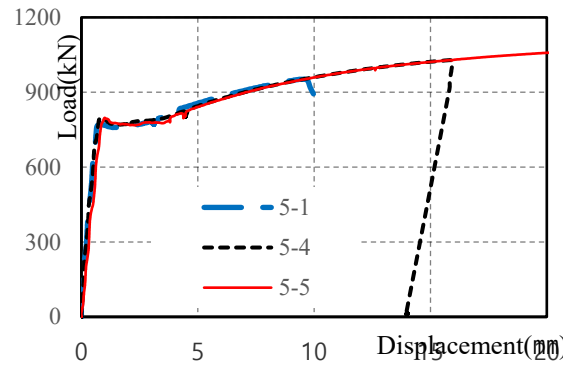


Fig. 19. Load-Displacement graph for specimen with flange 14mm

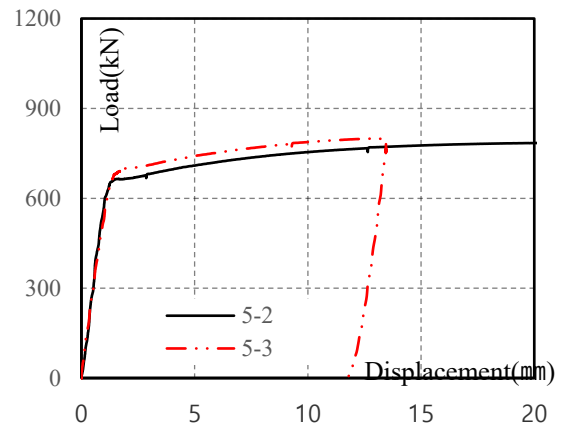


Fig. 20. Load-Displacement graph for specimen with flange 10mm

### 5.3. Analysis and discussion

T-shaped stiffener and concrete behave together from the moment tensile force acts. Therefore, it is considered that tensile strength to resist is different according to yield strength of T-shaped stiffener and ratio of strength due to concrete cone failure. Table 9 shows yield strength of T-shaped stiffener and cone failure and ratio between two by strength formula. Fig. 21, 22 and Table 10 show strain distribution and analysis for each load step of experiment specimen.

Table 9. Value by strength formula

Specimen	T-shaped stiffener yield strength	Concrete cone failure	T-shaped stiffener / Cone failure
5-1	768.6kN	288.84kN	2.66
5-2	675kN	294.95kN	2.29
5-3	509.1kN	283.49kN	1.8
5-4	768.6kN	483.28kN	1.59
5-5	768.6kN	795.08kN	0.97

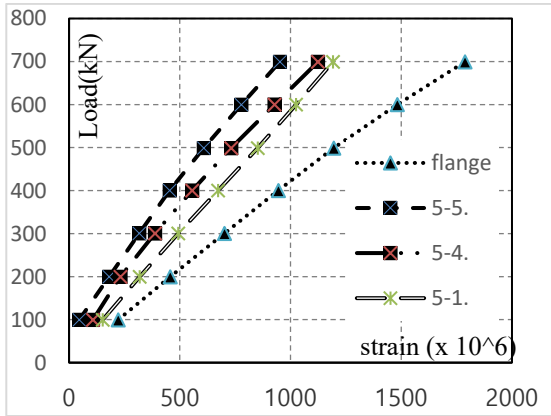


Fig. 21. Strain distribution by step of load for specimen with flange 14mm

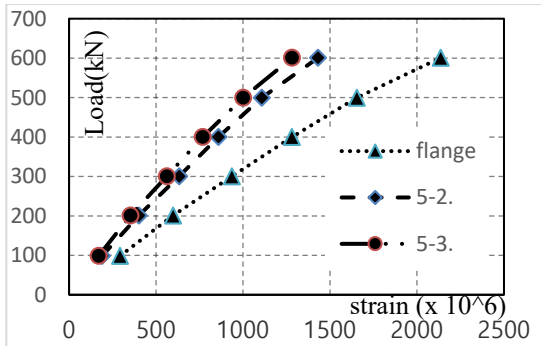


Fig. 22. Strain distribution by step of load for specimen with flange 10mm

Table 10. Ratio of T-shaped stiffener to cone failure

Specimen	Experiment value	Formula value	Formula / Experiment
5-1	2.16	2.66	1.23
5-2	2.03	2.29	1.13
5-3	1.5	1.8	1.2
5-4	1.63	1.59	0.98
5-5	1.04	0.97	0.93

As a result of comparing experimental value with formula value of ratio of T-shaped stiffener to cone failure in elastic range of beam flange, error of 5-1 specimen was 23% and the others were 13%, 20%, 2%, and 7%, respectively.

## 6. Conclusion

In this study, to develop shape and to propose strength formula of composite mega column to beam connection, finite element analysis and

connection tensile experiment were carried out. Through finite element analysis, load transfer mechanism through T-shaped stiffener in concrete non-charging steel pipe was confirmed and yield strength formula was verified. In addition, when T-shaped stiffener and concrete acted as composite section, through connection tensile experiment, load transfer mechanism and failure mode were confirmed. Conclusions of this study are as follows.

(1) Yield strength of T-shaped stiffener is determined by cross sectional area of horizontal member, and concrete cone failure is determined by area and height of T-shaped stiffener and column section size.

(2) Yield strength of composite mega column connection is determined by yield strength of T-shaped stiffener and concrete cone failure. In elastic range, tensile force resists according to ratio of T-shaped stiffener to cone failure. In other words, strength of connection is thought that large value of dominant T-shaped stiffener and cone failure.

(3) Strength formula verified by finite element analysis and tensile experiment of connection are as follows.

$$P_s = b_s \times t_{sh} \times f_{ys} \times 2 \times \cos \theta$$

$$P_{c1} = 2 \times \left[ \left( (\sqrt{2}b_s + b_a) \times b_t \right) + \left( \sqrt{2}b_s \times \left( \frac{b_c}{2} - t_{sv} - b_a - b_t \right) \right) \right] \times v_c$$

$$P_{c2} = 2f_t(h_c + h_s - 2t_{sh}) \times \left( \frac{b_c}{2} - t_{sv} \right)$$

$$P_{c1} + P_{c2} = P_c \tag{4}$$

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