

1 **COST OPTIMIZATION OF LOOPED NETWORKS WITH MULTIPLE PUMPING WATER SOURCES**

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14 **ABSTRACT**

15 The cost of pumping is one of the most significant operational expenditures in a water

16 distribution network. When a network has multiple water sources, which are associated to

17 pumping stations, it may be possible to optimize those costs. One way to minimize costs is to

18 determine the optimal flow rate for each pumping station and for every point of the temporal

19 demand curve, while keeping the energy cost minimized. This also requires that the required

20 minimum pressure at the critical point in the network to be satisfied. This paper introduces the

21 principle known as the setpoint curve as the key component of the network optimization

22 methodology. A direct search algorithm based on Hooke-Jeeves approach has been tested on

23 two case studies. Two key cost factors, the electric tariff and the cost of water production have
24 been considered for each water supply source. The model also considers the pressure
25 dependent consumption, which directly influences the setpoint curve. To test the methodology,
26 a software application has been implemented using the EPANET toolkit. The two case studies
27 demonstrate the benefits of the approach in developing optimal pump operating policies,
28 which would otherwise be difficult to infer.

29

30 **Keywords:** water, energy, pressure, optimization, network, costs

31

32 **INTRODUCTION**

33 The two main types of costs associated with managing water distribution networks are capital
34 (CAPEX) and operational expenditure (OPEX). Those costs can increase significantly in the future
35 if new water resources are required or water management efficiency has to be implemented to
36 mitigate against impact of demand increases. This in turn can significantly increase pressure on
37 water utility budgets, thus requiring all costs to be evaluated and optimized. In networks
38 containing pumps, capital costs may increase if a new pumping station is required, but also
39 operational costs can be affected mainly because system pressure must be readjusted. As
40 pumping energy represents a major OPEX cost, improved pump control must be considered as
41 a priority when a more efficient network operation is sought (Jowitt & Germanopoulos 1992).
42 Therefore, optimal operating conditions must be established for each pumping station and the
43 system overall. If that is done correctly, no new pumping stations may be needed even when
44 additional demand is encountered in the system. Optimal pumping operation then leads to

45 reduction the overall energy cost. It is well known that pump flow rate and pressure head
46 determine the amount of energy used by a pump. Therefore, the basic question is what are the
47 minimum flow rate and pumping head required to satisfy the flow and minimum pressure
48 requirements in the network (i.e., at each demand node). Thus, this paper focuses on improving
49 operations of a water distribution network by minimising energy costs of pumping.

50 For some time the emphasis has been on the need to develop more comprehensive analysis
51 and optimization tools for water networks to improve their efficiency and acceptance (Goulter
52 1992). To date, much of that effort has been invested in optimizing pumping in water networks.

53 Ormsbee & Lansey (1994) presented an overview of pump scheduling where different
54 approaches are analysed depending on the hydraulic network, demand forecast and optimal
55 control models. With regard to optimization models, it has been pointed out that energy-
56 consumption costs may be reduced by: decreasing either the quantity of water pumped or the
57 total system head; by increasing pumping efficiency by proper pump or pump combination
58 selection; by using tanks to achieve high efficiency in pump operations; or by shifting pump
59 operation to off-peak demand periods controlling storage levels and energy costs. Furthermore,
60 when pump maintenance costs are taken into account as a part of operational considerations,
61 optimization will attempt to minimize the number of pump switches.

62 Fundamentally, optimization methods (linear programming, dynamic programming, or nonlinear
63 programming) are mathematical models used to find the optimal values of some decision
64 variables. In pump control problems, the decision variables may be represented either directly
65 or indirectly. In the former case, a decision variable is expressed as the fraction of time that the
66 pump is operating over a time interval. Therefore, the objective is to minimize the energy cost

67 associated with the operation of each pump for each interval. In the latter case, a decision
68 variable is expressed in terms of a substitute variable, such as a tank level or pump station
69 discharge. This means that the aim is to find the least-cost tank level trajectory or the least-cost
70 time distribution of pump flows (or heads). Then that solution needs to be converted to a pump
71 operation policy. Both approaches have been used in the past to develop methodologies for
72 optimizing different pumping systems, i.e., those with single- or multiple-pumping stations with
73 no tanks, those with a single tank with single- and/or multiple-pump stations, and those with
74 multiple-tank and multiple-source systems. However, these methodologies have been
75 developed under the limitations of computational efficiency encountered at that time of their
76 development. As the computational resources advanced over time, the number of state and
77 decision variables has increased and new algorithms have been developed, such the harmony
78 search, genetic algorithms, ant-colony optimisation, and others (López-Ibáñez et al. 2008;
79 Błaszczuk et al. 2010; Henrique et al. 2015). Later studies have included the multi-objective
80 criteria in the search for the optimal pumping schedules. However, the inclusion of more
81 objectives are making the problem more complex and in some cases, they are unnecessary. On
82 the other hand, most previous methods were based on the use of fixed speed pumps, which
83 have as a major disadvantage that they produce pressures in a water distribution system that
84 are significantly higher than required and could exceed specifications (Lingireddy & Wood
85 1998). In those situations, hydraulic efficiency of keeping pressures low (and consequently
86 leakage) in the network is not addressed.

87 To improve hydraulic performance, the pump system efficiency curves should be adapted to be
88 as close as possible to the system characteristic curve (discharge and pressure head required by

89 the network), (Planells Alandi et al. 2005; Lamaddalena & Khila 2012). Therefore, the use of
90 variable-speed pumps can alleviate that problem and provide hydraulic and economic benefits
91 by reaching a high efficiency, as demonstrated by Lamaddalena & Khila (2013). In the same
92 way, Viholainen et al. (2013) formulated a new control strategy for variable speed-controlled
93 parallel pumps taking into account the relation between the preferable operating area (POA)
94 and pump energy efficiency to reach a high performance level. However, all these studies are
95 based on the system characteristic curve (resistance curve), which is usually difficult to
96 determine in drinking water distributions networks as it depends on the demand variations
97 both in time and space.

98 It should be noted that most of the optimization models start with pre-selected pumps,
99 meaning that once the pump discharge is known the required head is calculated from the pump
100 curve. Then, the objective function is used to search for the minimum cost value. In that way,
101 the cheapest pumping configuration that meets the established requirements is found
102 (economic limitations, physical limitations, others). Nevertheless, in that context, it is not
103 possible to find the maximum achievable cost saving since the optimal solution is restricted by
104 the existing pumps characteristics. Therefore, more cost-efficient solutions can be found if the
105 pump limitations are removed from the formulation either partially or totally. Following on
106 from that, it is assumed that optimal pump configurations that fit the water network are not
107 known. To obtain a greater degree of freedom with regard to the operation of the pumps,
108 Fernández García, et al. (2014) and Fernández García et al. (2016) represented pumps as
109 reservoirs in Epanet (Rossman 2000), considering the pump heads as decision variables. Their
110 approach has been applied to irrigation networks. However, the interaction among individual

111 reservoirs makes the behaviour and the optimization process much more complex. Thus, an
112 alternative approach would be to assume that the pumps at the sources are supply nodes
113 whose flow rates are decision variables, which is proposed in this work. In this way, the result is
114 neither the flow nor the head a certain pump can provide, but the flow rate and pumping head
115 required by the network.

116 The present work develops a new approach to achieving economic benefits through reducing
117 energy costs in pumping stations. It aims to identify the least-cost flows for each of the pumped
118 water sources in a supply network. To carry out the optimization process, two algorithms have
119 been implemented and the results compared: 1) Hooke-Jeeves (1961), and 2) Nelder-Mead
120 (1965). The algorithms are heuristic and do not guarantee that the global optimum can be
121 found. However, the aim is to find a near optimal solution in a reasonable time. A strategy is
122 employed to reduce the search space by discarding the infeasible solutions through the use of
123 constraints. The methodology was developed using the EPANET toolkit (Rossman 2000) and
124 Visual Basic via the Visual Studio 2010 platform. The objective function takes into account
125 electric tariffs, water production costs, and pumping efficiency. Finally, two case study
126 networks are analysed and the results and conclusions are presented.

127 **PROBLEM STATEMENT**

128 The approach uses the concept of a setpoint curve, where the most critical node in the network
129 is identified and all of the pumping station are represented as nodes (Iglesias-Rey et al. 2012;
130 Martínez-Solano et al. 2014; León-Celi et al. 2016). The critical node is used as a reference point
131 to optimise pressure heads at pumping stations and satisfy the pressure requirements in the
132 network, while keeping the energy consumption at the minimum. The critical node can change

133 depending on the changing demand in the network, therefore, it has to be found for each time
134 instant (step). By minimizing the pressure in the network, the leakage is also reduced and
135 associated additional benefits are achieved.

136 The setpoint curve concept does not require the real pump as a hydraulic machine with its own
137 pump characteristics (e.g., pump curve, efficiency curve, and power curve. It uses instead a
138 node that represents a conceptual (hypothetical) pump, where for a given flow rate to be
139 supplied at that node, the model determines the pressure head needed to supply the required
140 flow rate. The values of both flow rate and pressure head for the conceptual pump are limited
141 only by the required demand and the minimum pressure in the network.

142 As the setpoint curve deals with hypothetical pumps with not limitations on flow rate, it is not
143 possible to associate an efficiency curve with them. However, as that is important to determine
144 costs associated with flow rate and pressure head, the assumption taken here is that a constant
145 efficiency value can be applied.

146 Obviously, the flow rate provided by the sources must meet demand requirements in the
147 network. In the case of a network with several sources, the flow supplied by each source can
148 take many different values. Every flow combination defines a specific setpoint curve for every
149 source, which will also maintain the required minimum pressure. Hence, there are as many
150 setpoint curves as source discharge combinations that will meet overall demand, but there is
151 only one optimal setpoint curve. Thus, the cornerstone of this work is to find the optimal
152 setpoint curve that leads to the minimum energy cost through the formulation of a cost
153 objective function and the use of an optimization algorithm.

154 The basic assumptions of the methodology are as follows: (1) multiple water sources are
 155 available to supply water for consumption in the network; (2) each of the sources has its own
 156 pump(s); (3) storage is not available in the network and only snapshot hydraulic analysis is
 157 required to describe hydraulic behaviour of the system; (4) a setpoint curve for each pumping
 158 stations is obtained; and (5) the demand at nodes and demand patterns are known. This means
 159 that the flow rate and pressure head for each supply source is determined such that it satisfies
 160 both the demand in the network and the minimum pressure required.

161 **METHODS**

162 **Objective Function**

163 The least-cost solution is determined by optimizing the objective function that is formulated as
 164 the sum of the two cost terms. The first term represents the pump energy cost (Eq. 1) and the
 165 second is the cost of water treatment (Eq. 2). The analysis is developed for a 24 h time horizon
 166 with 1 h intervals. Therefore, 24 results are obtained at the end of the simulation period.

167 The first term in the objective function is obtained by multiplying the power consumption at the
 168 pumping station with the tariff unit charge and pumping time. In this case, the tariff function is
 169 represented as an average value per hour. Hence, it depends only on the energy consumed
 170 over the day.

$$EPC_i = \sum_{j=1}^{Nws} \frac{\gamma \times Q_{j,i} \times PH_{j,i}}{1000 \times \eta_j} \times ET_{j,i} \times t_i \quad (1)$$

171 Where EPC_i is the sum of the power consumption cost for each pumping station j at hour i (€);
 172 Nws is the number of water supply sources, γ is the specific weight of water (9810 N/m^3); $Q_{j,i}$
 173 is the flow rate for each pumping station j at hour i (m^3/s); $PH_{j,i}$ is the pressure head needed

174 at each pumping station j at hour i (m); η_j is the minimum efficiency estimated for each
 175 pumping station j depending if it is desirable to incorporate partially the characteristics of pre-
 176 existent pumps or whether it is a new pumping system, j taken as a fixed value; $ET_{j,i}$ is the
 177 energy tariff at hour i (kWh/€) at the source j ; t is the pumping time at hour i (h). The flow rate
 178 and the pressure head identify points on the setpoint curve for each pumping station. This
 179 concept will be explained with more detail in next section. It is important to note that as the
 180 proposed methodology involves simulation of the behaviour of unknown pumps, the efficiency
 181 value cannot be taken as flow rate dependent.

182 For the second term of the objective function, i.e., the cost of the treated water, is calculated as
 183 the product of the pumped flow rate and the cost of a cubic meter of treated water. Those
 184 costs are directly related to the volume of water produced.

$$TWC_i = \sum_{j=1}^{Nws} (TC_{j,i} \times Q_{j,i} \times t_i) \quad (2)$$

185 Where TWC_i is the sum of the treated water cost for each supply source j at hour i (€); $TC_{j,i}$ is
 186 the unit treatment cost for each water source j (€/m³) at time i . $TC_{j,i}$ could also depend on
 187 aspects such as disinfection chemicals, maintenance, energy for the plant devices, and others.

188 The objective function can be expressed as follow:

$$\sum_{i=1}^{24} Min f(x)_i = \sum_{i=1}^{24} (EPC_i + TWC_i) \quad (3)$$

189 There are two types of constraints in the problem. The first are those related to the hydraulics
 190 of the system: 1) flow and energy conservation constraints; 2) pressure constraints, and 3) no

191 negativity constraints for some variables. The second type of constraints are introduced to
192 avoid infeasible solutions being evaluated:

193 a) The addition of each flow rate supplied to the network must be equal to the total flow
194 rate(TFD_i) required at time i :

195

$$\sum_{j=1}^{Nws} Q_{j,i} = TFD_i \quad (4)$$

196 b) The total flow rate supplied by a water source cannot be greater than the total flow rate
197 required and must be greater than zero:

$$0 \leq Q_j \leq TFD_i \quad (5)$$

198 c) The pressure head at the critical node (PH_{c_i}) in the network cannot be lower than the
199 minimum head required (PH_{min}):

200

$$PH_{c_i} \geq PH_{min} \quad (6)$$

201 **Setpoint Curve**

202 A setpoint curve is a theoretical construct that allows setting both the specific flow rate and
203 pressure head at the water source, which are needed to satisfy the minimal pressure constraint
204 at the critical node. At the same time, it ensures that the water demand is met in full (León-Celi
205 et al. 2016). Thus, the setpoint curve is represented by two variables, the flow rate against the
206 pressure head. Furthermore, there is only one optimal setpoint curve for each water source.
207 For a network with only one water source, the flow rate for every point on the setpoint curve
208 will be the rate required at a particular time. With more than one supply sources, the problem
209 of finding the flow rate and pressure head for each of them becomes more difficult since it is

210 needed to determine both variables at the same time and there is normally interaction
211 between the two sources. Hence, to define the curve it is essential to fix one of the two
212 variables, either the flow rate or pressure head. The results obtained by employing the EPANET
213 software are used for calculating the setpoint curve.

214 An easy way to determine the setpoint curve would be to fix one of the variables, e.g., the
215 discharge from each water source. In other words, to determine a portion $x_{j,i}$ of the total
216 demand to be pumped by station j at time i (Eq. 7). For that to be possible, the pumping
217 sources need to be represented as nodes. By EPANET conventions, it also means that the flow
218 rate will have to be negative at these locations. This allows a lot more freedom for selecting
219 pump flows and heads than in the case with pre-existing pumps, because these values are not
220 unnecessarily constrained. Since EPANET needs at least one water source where the pressure
221 head is known, one of the sources must be represented as a fixed-head reservoir. This can be
222 assumed for any of the sources. The reservoir will be necessary for adjusting the pressure at
223 network nodes by varying its elevation.

$$Q_{j,i} = -x_{j,i} \times TFD_i \quad (7)$$

224 Where $x_{j,i}$ is the part of the total demand to be supplied by the water source j in time period i .
225 The process begins with the fixed-head reservoir node (PH_{RS}). Flow rates in other source nodes
226 are allocated according to the second type constraints previously mentioned (Eq. 4 and Eq. 5)
227 and the expression in Eq. (7). One additional constraint can be the maximum flow rate that a
228 water source is capable of supplying. The flow rate of the reservoir and the pressure head of
229 each water source will be calculated using this approach. Once variables have been initiated the
230 hydraulic model is solved. Then the pressure in each node is evaluated and the critical node,

231 having the minimum pressure (PH_{c_i}), is found. Note that the critical node may change its
232 position depending on demand variation over time. PH_{c_i} is compared to the minimum required
233 pressure (PH_{min}). If the required minimum pressure constraint is not satisfied, a correction to
234 the reservoir elevation has to be implemented. For a single source, this is accomplished by
235 increasing its value if higher pressure is needed or by decreasing it if it is lower, until the correct
236 value is achieved. The number of corrective steps depends on whether the consumption in the
237 network is considered pressure dependent or not. When the consumption is assumed not to be
238 pressure dependent, only one correction step is necessary. Pressure dependent consumption
239 makes the problem more complex due to two main reasons. Foremost, when the reservoir
240 elevation is modified, it changes the pressure at every node including the critical node, and
241 hence the demand flow rate. This often requires an iterative procedure. On the other hand, if
242 the demand changes throughout the network, the flow supplied by each of the sources needs
243 to be recalculated. For the cases studies the concept of emitters of EPANET was implemented
244 for modelling pressure dependent consumption. However, modelling of water losses is
245 considered beyond the scope of the present analysis and has not been implemented. The
246 process finishes when the minimum pressure required is reached at the critical node (Figure 1).
247 The optimization problem arises when the pump flows from each source need to satisfy the
248 minimal pressure head requirement and achieve the minimum costs are unknown. The
249 procedure has to take into account that the distribution of pump flows affects the lowest cost
250 that can be achieved. The problem can be addressed by testing a finite set of flow distributions
251 among the sources to find which is the cheapest. However, a trial-and-error procedure can take

252 a long time and still may not achieve the optimum. Therefore, the use of optimization
253 algorithms is advisable, as explained in the next section.

254 The optimization function (Eq. 3) makes this a non-linear multidimensional problem with
255 constraints. The number of dimensions is related directly to the number of water sources. The
256 constraints (Eq. 4-6) have been incorporated into the problem indirectly by selecting a suitable
257 flow distribution before the process begins and by correcting the elevation of the reservoir to
258 keep the pressure within desirable values. The problem cannot be solved analytically, hence a
259 search method is required. According to the requirements of the problem, two algorithms have
260 been tested: Hooke & Jeeves (1961) and Nelder & Mead (1965). The main reasons for using
261 these two algorithms is that they do not need complex mathematical operations and to
262 compare their results. The algorithms have been implemented on the Visual Studio 2010
263 platform using the Visual Basic programming language that allows EPANET toolkit to be used.
264 Both algorithms produced very similar results, thus only the results using the Hooke-Jeeves
265 algorithm (León-Celi et al. 2016) will be presented.

266

267 **CASE STUDIES**

268 Two distribution networks have been considered in this paper, both with pressure dependent
269 consumption. The first is the TF network (León-Celi et al. 2016), and the second is the COPLACA
270 network.

271 **TF network**

272 This is a small network with eighteen nodes and twenty-four pipes. There are three water
273 sources, P0, P16 and P17, in the system. In this case, the sources do not have flow constraints.

274 The source P16 is at an elevation of 4 m, and the elevation of the remaining sources is equal to
275 zero. The average elevation of the network is around 5 m. Therefore, it can be considered as a
276 flat distribution network. The emitter exponent used in this work is 0.5 and the emitter
277 coefficient for each node is 0.8. The input data is shown in Table 1. The minimal required
278 pressure is 45 m.

279 The electricity tariffs (Table 1) are different for each source and have been discretized into four
280 periods. The prices correspond to the energy term in the expression for the energy consumed
281 (Eq. 1). The maximum power has not been considered in this work. Both, the efficiency (η) and
282 the cost of the water treatment (TC) is given for each source and they are assumed constant
283 over time, P0 ($\eta = 60\%$, $TC = 0.30 \text{ €/m}^3$), P16 ($\eta = 75\%$, $TC = 0.25 \text{ €/m}^3$) and P17 ($\eta = 65\%$, $TC =$
284 0.20 €/m^3).

285 Once the optimization is carried out, the setpoint curves for the three sources are obtained
286 (Figure 3). Although source P16 is at a higher elevation than P0, the optimization results show
287 that P0 is preferred over P16, i.e., the minimum energy curve is associated with P0. In other
288 words, it is beneficial for source P0 to provide more water to the network than P16 in order to
289 minimize the operation costs. Therefore, this demonstrates that the problem of finding the
290 setpoint curves is a complex one, which cannot be understood by just observing pressure heads
291 at various sources, but can only be solved by using an optimization approach. The optimized
292 solution shows a flow distribution among the sources (Figure 4), which has not been obvious
293 before optimization. For the first seven hours of operation, the source P17 makes the largest
294 contribution to the system flows. This is logical as that is the source with the lowest electricity
295 tariff for the period. As the demand increases, the contribution from source P0 increases in

296 comparison to the other two sources. This happens despite it neither having the lowest tariff
297 rate nor the best efficiency. Therefore, this shows that operating policies that lead to greater
298 economic savings are difficult to infer. Although pumps selection is beyond the scope of this
299 work, these curves can be very useful in selecting the pumping system.

300 It should also be mentioned that the minimum pressure in network over the whole simulation
301 period is implicitly satisfied and guaranteed as part of the setpoint curve calculation process.
302 Hence, addition another search objective or a constraint to meet this goal is not necessary. As
303 consumption is pressure dependent it is important to keep the minimum pressure in the
304 network, so use the setpoint curve can mean significant savings, but the analysis of this aspect
305 requires further research.

306

307 **COPLACA network**

308 The model was built for a real city with a population of 25,000 (Figure 5). It has a seasonally
309 variable demand, which is particularly difficult to satisfy in the summer. The residential area
310 does not receive enough water due to the increased water demand. Therefore, the municipality
311 is considering additional water resources, which would involve reactivation of some old and
312 neglected wells. The distribution network consists of 1,032 nodes, 1,095 pipes (a total length of
313 133 km), and one reservoir. There are seven water sources, six of them are nodes that
314 represent pumping wells: P05, P06, P07, P11, P12, and P13. Each well has a maximum
315 extraction flow rate (Q_{max}) associated with it. Reservoir P10 represents a river source, which
316 supplies water through a pumping station. Consumption is considered pressure dependent. The
317 minimum required pressure is 20 m.

318 In this case, a minimum (Q_{min}) flow rate for each water source has been fixed to avoid solutions
319 with unrealistically low flow rates. The efficiency and the cost of water treatment of each
320 source are presented in Table 2. They are assumed to be constant over time, as it was done in
321 the previous case.

322 The demand curve was obtained for a period of 24 hours (Table 3). As in the previous case, the
323 electricity tariffs have been specified for three separate periods, for each time step and the
324 water source (Table 3). Prices are only a function of the electricity consumed.

325 In this case, it can be seen from Figure 6 that for most source the setpoint curves are flat and
326 some of those collapse into a single point. The setpoint curve for P10 is the only one spread
327 over the range of flows. This information can be used to support decisions on how to regulate
328 the pumping systems for each water source, i.e., whether it needs variable speed regulators
329 (e.g., P10) or can be kept as fixed-speed pumps. On the other hand, optimization (Figure 7)
330 shows that all sources are required to work together only during the peak demand periods.
331 Therefore, the results can lead to a better water management plan, including maintenance and
332 operation plans, because only some of the water sources are required to meet demand at
333 certain times of the day. As minimum pressures are also maintained, the consumption is kept
334 low as it is pressure dependent. The river source (P10) has not reached its maximum capacity
335 (Figure 6), thus allowing to eliminate need for additional sources. Hence, the existing network
336 has enough capacity to meet the daily demand.

337 It is worth noting that if the source production costs are considerable higher than the energy
338 costs and the differences among them are significant, the flows from different sources will be
339 distributed mainly according to those rates, i.e. from the lowest to the highest cost. In that

340 case, the energy cost may be less important. Therefore, optimization may arrive to an obvious
341 answer. However, through the methodology presented it is still possible to find the least-cost
342 flow distribution to be supplied by the different water sources.

343 **CONCLUSIONS**

344 This study considers pumping and treatment cost optimization required to determine the least-
345 cost utilisation of multiple sources, from which the water is pumped into a water distribution
346 system. For that purpose, the optimum flow rate must be found for each of the sources/pump
347 stations over the period of analysis (e.g., 24 hours). The key to the methodology is the setpoint
348 curve concept, which can be used with both pressure dependent and independent
349 consumption.

350 In addition to the energy consumption, the objective function developed in this work allows
351 consideration of additional aspects, such as water production costs, electricity tariffs, and the
352 minimum and maximum flow rates for the sources. It is also possible to add any other
353 consideration relevant for the particular network, e.g., water quality, as long as it can be
354 expressed in terms of cost. To optimize the objective function, the use of an optimization
355 algorithm is required. The algorithm must allow exploration of the wide range of water supply
356 combinations among the water sources associated with pumping stations. In this case a direct
357 search algorithms, Hooke-Jeeves, was chosen as it has been shown to be effective for nonlinear
358 multidimensional problems with constraints. Although the method can encounter problems
359 with local optima, it is efficient and quick to implement. Furthermore, the minimum pressure
360 constraint is implicitly satisfied over the whole simulation period by the setpoint curve

361 calculation process. As a consequence, there is no need to add another search criteria or an
362 explicit constraint to account for that, as it is the case with other optimization approaches.

363 The problem of determining the optimum flow and pressure heads for each source/pumping
364 station in a water distribution system is complex due to the non-linear nature of network
365 behaviour, its topology, pressure dependent consumption, and variable tariffs. Therefore, it is
366 difficult to infer optimal pumping operating policies without a formal optimization approach.

367 The case studies demonstrated the utility of setpoint curves as a method for determining a
368 suitable least-cost pumping policy. By representing water sources as nodes allows this
369 methodology much more freedom in selecting pumping policy that fits better network
370 characteristics. It is also important to note that, if water production costs are more significant
371 than energy costs, optimization will consider energy costs less important.

372 Further research will be directed to the assessment of benefits that supply source optimization
373 can bring while considering leaks in the system. Moreover, the joint application of zoning
374 strategies and management measures to improve the performance at the critical node have not
375 been yet addressed. Furthermore, control valves, network storage capacity, pump selection,
376 location of storage tanks, etc., have not been taken into account.

377

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428

429 Table 1. Demand curve and electric tariffs according to the hour and the water source (TF
 430 network).

Time (h)	1-5	6-7	8	9	10	11	12	13-14	15	16	17	18	19-20	21-22	23	24
Demand Factor (DF)	0.4	0.7	1	1.2	0.7	0.7	1.7	2	1.7	1	0.8	1.1	1.1	1.5	1.1	0.4
P0 (€/kWh)	0.094		0.133									0.166		0.133		
P16 (€/kWh)	0.092		0.131									0.164		0.131		
P17 (€/kWh)	0.090		0.129									0.162		0.129		

431 *Electric tariffs are variations of ENDESA (2017)

432 Table 2. Q_{max} , Q_{min} , performance and water treatment cost of the water sources of the network
 433 (COPLACA network).

Sources	P05	P06	P07	P11	P12	P13	P10
Efficiency (%)	60	75	65	70	80	60	70
Water treatment cost [€/m³]	0.34	0.38	0.36	0.27	0.30	0.30	0.25
Q_{max} [l/s]	9.0	3.0	7.0	17.0	15.0	15.0	80.0
Q_{min} [l/s]	0.5	0.5	0.5	0.5	0.5	0.5	0.0

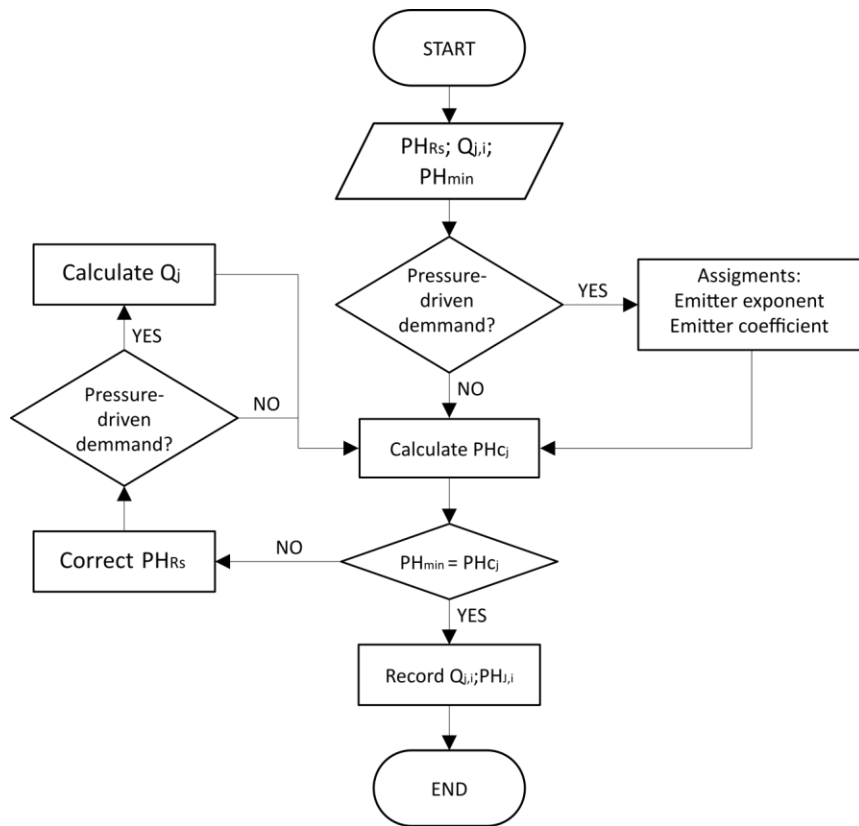
434

435 Table 3. Demand curve and electric tariffs according to the hour and the water source
 436 (COPLACA network).

Time (h)	1-4	5-6	7-8	9	10	11	12-14	15	16	17-18	19	20	21-22	23-24
Demand Factor (DF)	0.4	0.7	1.3	1.3	0.9	0.9	2.2	1.6	0.4	0.8	0.8	0.9	1.3	0.4
P05, P07, P13 (€/kWh)	0.090		0.129									0.162		0.129
P06, P11 (€/kWh)	0.092		0.131									0.164		0.131
P12, P10 (€/kWh)	0.094		0.132									0.165		0.132

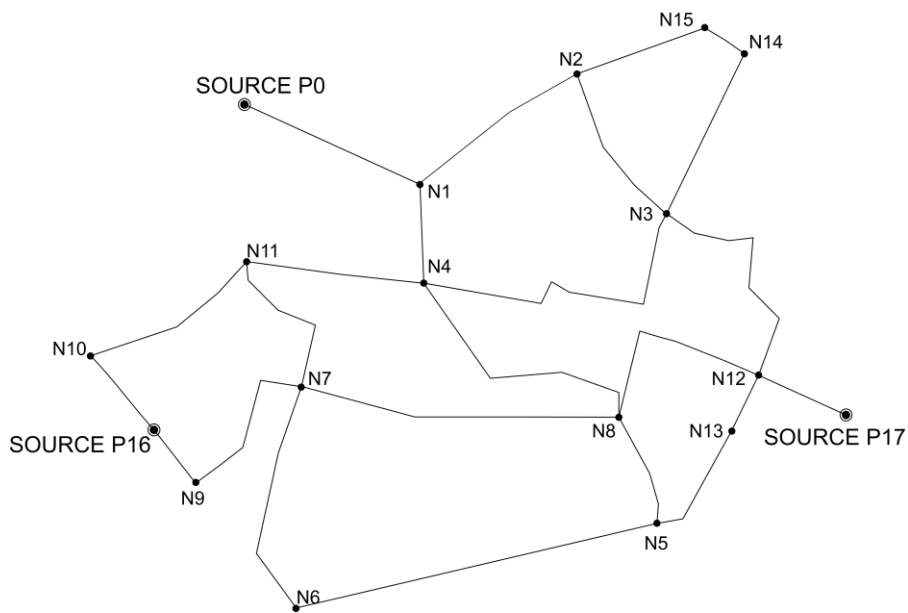
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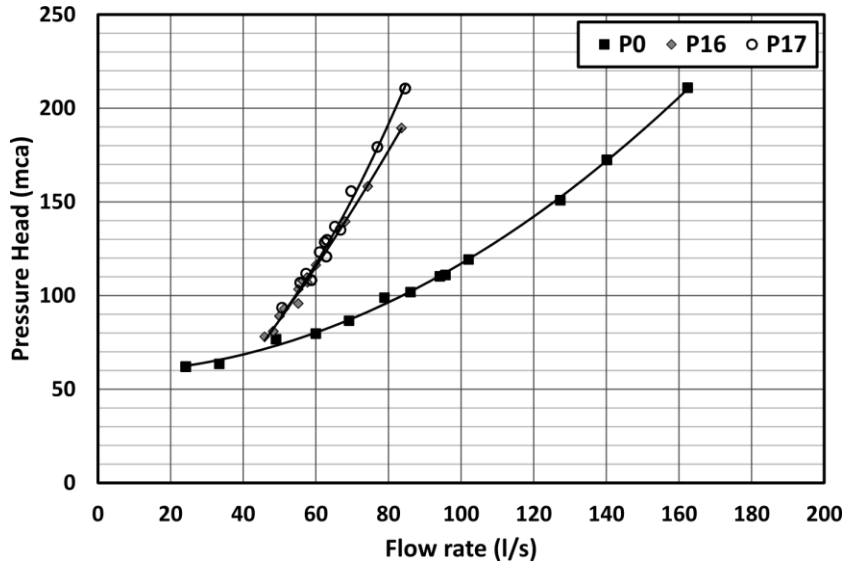
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440 Figure 1. Setpoint curve. Calculation process.



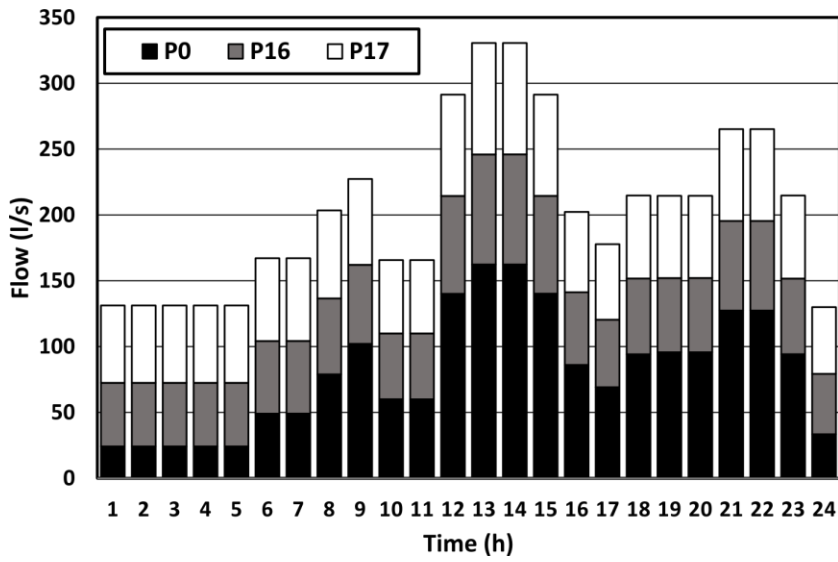
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442 Figure 2. TF Network.



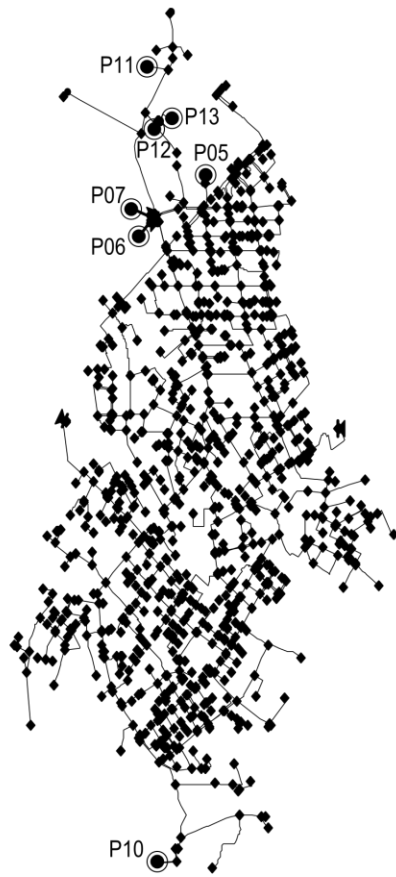
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444 Figure 3. Setpoint curves from the TF network sources.



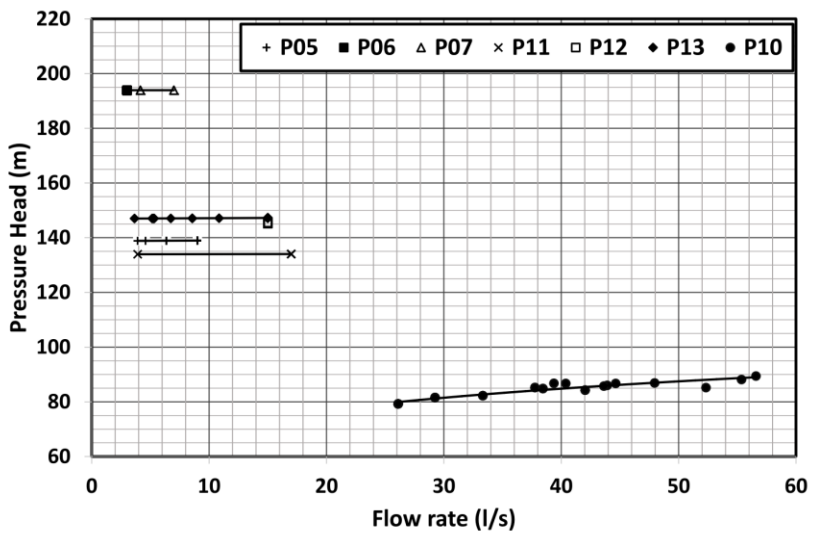
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446 Figure 4. Flow contribution of each source in the TF network.



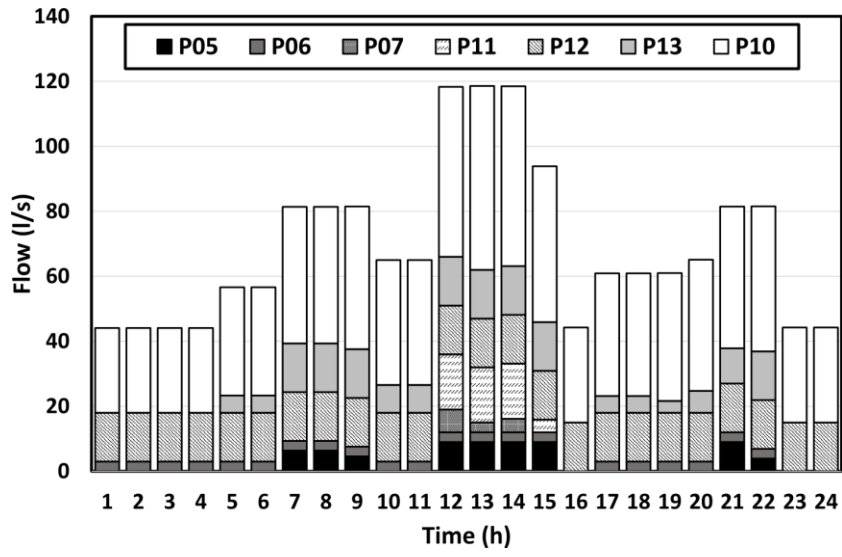
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448 Figure 5. COPLACA network.



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450 Figure 6. COPLACA network.



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452 Figure 7. COPLACA network.

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