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Galindo, J.; Guardiola, C.; Dolz, V.; Kleut, P. (2018). Further analysis of a compression-expansion machine for a Brayton Waste Heat Recovery cycle on an IC engine. *Applied Thermal Engineering*. 128:345-356. <https://doi.org/10.1016/j.applthermaleng.2017.09.012>



The final publication is available at

<https://doi.org/10.1016/j.applthermaleng.2017.09.012>

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Additional Information

1 **Further analysis of a compression-expansion machine for a Brayton Waste**
2 **Heat Recovery cycle on an IC engine**

3
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11 In order to comply with the legislation, car manufacturers are looking for a way
12 to lower the CO₂ emission by improving engine efficiency. About one third of the fuel
13 combustion energy is wasted through exhaust gasses. Waste Heat Recovery (WHR) could
14 improve engine efficiency by recovering a part of exhaust gasses energy. In this study,
15 the potential use of an open loop Brayton cycle with a volumetric compression expansion
16 machine for exhaust gas waste heat recovery was investigated. The use of the Brayton
17 cycle system with only two main elements, a heat exchanger and a volumetric machine,
18 could be very interesting due to its compactness and versatility. However, the publications
19 on this subject are scarce. The present paper aims at bridging this knowledge gap by
20 studying the cycle viability for passenger car application characterized by low
21 temperatures, variable working conditions and several restrictions of available space and
22 weight. The simulated vehicle was a Ford Mondeo family car with an Ecoboost 2.0
23 engine. The main components of the Brayton cycle WHR system model were a heat
24 exchanger and an alternating piston machine that was used both as a compressor and as
25 an expander. Theoretical studies were conducted in the compression-expansion machine
26 model in order to determine the main parameters that influence the cycle and optimise
27 those parameters in order to obtain the maximum recuperated power. The conclusion was
28 that the cycle viability is not clear because cycle losses are in the same order of magnitude
29 as the recuperated power. Considering future improvements of the compression-
30 expansion machine and the heat exchanger, the recuperated power could be positive.
31 Nevertheless, it is hard to expect that recuperated power would be sufficient to justify the
32 application of this WHR system in the vehicle.

33 Keywords: Brayton cycle, Waste Heat Recovery, WHR, Internal Combustion Engine

Nomenclature and abbreviations	
A	Area [m ²]
AirGasRatio	Ratio of air and exhaust gas mass flows
B	Bore [m]
BDC	Bottom Dead Centre
CA	Closing Angle
Cp	Isobaric heat capacity
c _x	Aerodynamic drag
D	Diameter [m]
F	Force [N]
f	Friction coefficient
f _{mep}	Friction mean effective pressure [Pa]
g	Gravitational acceleration [m/s ²]
HE	Heat Exchanger
HP	High Pressure
ht	Heat transfer
ICE	Internal Combustion Engine
J	Moment of inertia [kg·m ²]
k	Thermal conductivity [W/(m·K)]
l	Length [m]
LP	Low Pressure
m	Mass [kg]
\dot{m}	Mass flow [kg/s]
n	Number of parts
NEDC	New European Driving Cycle
Nu	Nusselt number
OA	Opening Angle
p	Pressure [Pa]
P	Power [W]

Q	Heat energy [W]
Re	Reynolds number
ρ	Density [kg/m ³]
S1, S2, S3	Pressure sensors
S _p	Mean piston velocity [m/s]
T	Temperature [K]
T	Torque [N·m]
TDC	Top Dead Centre
TR	Transmission
WHR	Waste Heat Recovery
η	Efficiency
ν	Kinematic viscosity [cSt]
ω	Rotational velocity [rpm]

34

Subscripts	
aero	Aerodynamic
amb	Ambient conditions
bc	Bearing crankshaft
br	Bearing connecting rod
bv	Bearing camshaft
dr	Driving
E	Engine
exh	Exhaust gasses
FD	Final drive
GB	Gear box
HE	Heat Exchanger
HT	Heat transfer
in	Inlet
out	Outlet
p	Piston
pump	Pumping loss
val	Valve

veh	Vehicle
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wh	Wheel
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36 1 Introduction

37 By the current European regulation, car manufacturers must lower the average
38 fleet CO₂ emission below 95 g/km by the year 2020 [1]. Some car manufacturers would
39 not comply with the regulation if they would keep the same trend of CO₂ emission
40 reduction as in the period 2008-2014 [2]. Even the ones whose trend would allow them
41 to reach the objective would probably have to use technologies that are currently not on
42 the market in order to achieve the desired emission. Waste Heat Recovery could be a
43 technology that would provide the reduction of CO₂ emission without negatively
44 influencing the emission of other pollutants.

45 When IC engines operate in the zone of good efficiency, around one third of the
46 energy obtained by fuel combustion is wasted through the heat of the exhaust gasses.
47 There are different known technologies available for Waste Heat Recovery (WHR) to
48 improve the mechanical power of the engine [3] and other technologies for heat
49 management improvements into the engine [4] [5] [6] [7]. Two technologies that have
50 been extensively studied are the Organic Rankine Cycle (ORC) and the Thermoelectric
51 Generator (TEG). While the ORC provides good efficiency [8], it is complex, heavy and
52 requires a lot of space. Generally, research about the ORC focuses on efficiency and
53 viability of the system [9] [10], different proposals for the system layout [11] [12],
54 technologies for the expander machine [13] and the working fluid [14]. On the other hand,
55 TEG systems have a low efficiency, low specific power and their materials are very
56 expensive, [15] but they are simple and robust systems. It is a topic of high interest.
57 Published studies on this topic deal with issues related to the materials and the layout of
58 thermoelectric elements [16] and the viability to recover energy from the exhaust gasses
59 of a car engine [17] [18]. Considering these studies on these two systems, a Brayton cycle
60 could possibly be a compromise solution that could offer relatively good efficiency and
61 simplicity without occupying much space or adding a significant weight into the vehicle.
62 Nevertheless, publications about the application of the Brayton cycle system for WHR in
63 a passenger car are scarce. In general, Brayton cycles are studied to improve the energy
64 recovered from solar power plants. It is possible to find numerous studies about the cycle
65 layout design for closed Brayton cycles working with CO₂ in solar plants can be found
66 [19] [20] [21], the interest of regenerative and inverse Brayton cycles [22] [23] and the
67 turbine design for the Brayton cycle of these solar plants [24]. In addition, WHR using
68 Brayton cycles in IC engines for industrial applications, where space requirements and
69 dynamic conditions are less restrictive, has been studied [25]. However, studies about this
70 system applied to IC engines in vehicles are lacking. Nevertheless, because it is a topic
71 of high interest, some authors begin to consider Brayton cycles for WHR in car engines.
72 Banglin et al. [26] studied the viability of this system assisted with a steam generator by
73 using a theoretical model in GT-Power, concluding that it could be a viable system.

74 Considering this growing interest in WHR issues for car engines using very
75 compact Brayton cycles, the objective of this paper is to estimate the viability of the WHR
76 Brayton cycle by using a very compact layout, in order to minimize the space and weight
77 requirements of the system. To reduce these requirements, a very simple open loop cycle
78 is proposed using only two main elements, first a heat exchanger to take the heat from the
79 exhaust gasses and second, a newer design of a volumetric compression-expansion

80 machine, in order to minimize the space requirements of the machine for the compression
81 and expansion processes. This paper represents the continuation of the authors' previous
82 research on Brayton cycle WHR system [27], where it was estimated that the recuperated
83 power could be 1515 W for the engine working condition that corresponds to car velocity
84 of 120 km/h.

85 2 Model description

86 The car that was used in the study was a Ford Mondeo with an Ecoboost 2.0 engine
87 which is a typical European D segment family car. Car engine was a 2 litre turbocharged
88 gasoline engine that at 120 km/h produces 22548 W at 2623 rpm. For this paper the same
89 vehicle, engine and operating point were used. It was considered that the model that was
90 used in current study could be further improved in order to obtain a more realistic Brayton
91 cycle model. Some of the conclusions from the first paper will serve as an initial condition
92 for this study. The most important ones are that the same piston machine will be used
93 both as a compressor and expander and that the diameter of the piston will be 120 mm.

94 The modelled Brayton cycle is an open loop thermodynamic cycle that consists of
95 five main processes: compression, heat addition, expansion, exhaust process and intake
96 process. Regarding the processes of compression and expansion, it was estimated that for
97 both processes alternating piston could be a promising technology to use. Furthermore,
98 similar piston diameter was estimated for both processes. In the present paper, in order to
99 reduce size and weight of the machine, it was considered that one alternating piston could
100 be used for both processes, while compression process would take one piston stroke the
101 expansion process would continue during the next stroke. At the end of expansion the air
102 temperature is higher than ambient air. For the process of heat rejection two more piston
103 strokes were used. These two strokes would be used to expel the hot air from the previous
104 cycle and admit the fresh air for the new cycle. Regarding the process of heat addition,
105 heat is introduced into the cycle through the heat exchanger by a heat exchange process
106 between the air (gas cycle) and the ICE exhaust gasses.

107 The engine used in this study was tested by modelling the car. The main engine
108 parameters were measured for car velocity of 120 km/h, as it is a regular speed of the
109 vehicle with a high rate of heat energy into the exhaust line. The most important engine
110 characteristics are presented in [Table 1] while the most relevant engine characteristics
111 for the studied engine operating point are presented in Table 2.

Characteristic	Value
Displacement [cm ³]	1999
Maximum Power [kW]	149
Maximum Torque [Nm]	300

112 Table 1. Engine characteristics

Characteristic	Value
Exhaust gas mass flow [g/s]	27.01
Exhaust gas temperature [°C]	733
Rotational speed [rpm]	2623
Effective power [W]	22548

Engine efficiency [%]	29.66
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113

Table 2. Engine operating point characteristics

114

From the engine operating point data and assuming 25 ° C as the reference ambient temperature (T_{amb}), the available heat power of exhaust gasses (P_{exh}) can be estimated as:

115

$$P_{exh} = \dot{m}_{exh} \cdot C_{pexh}(T_{exh} - T_{amb}) = 19353 \text{ W}$$

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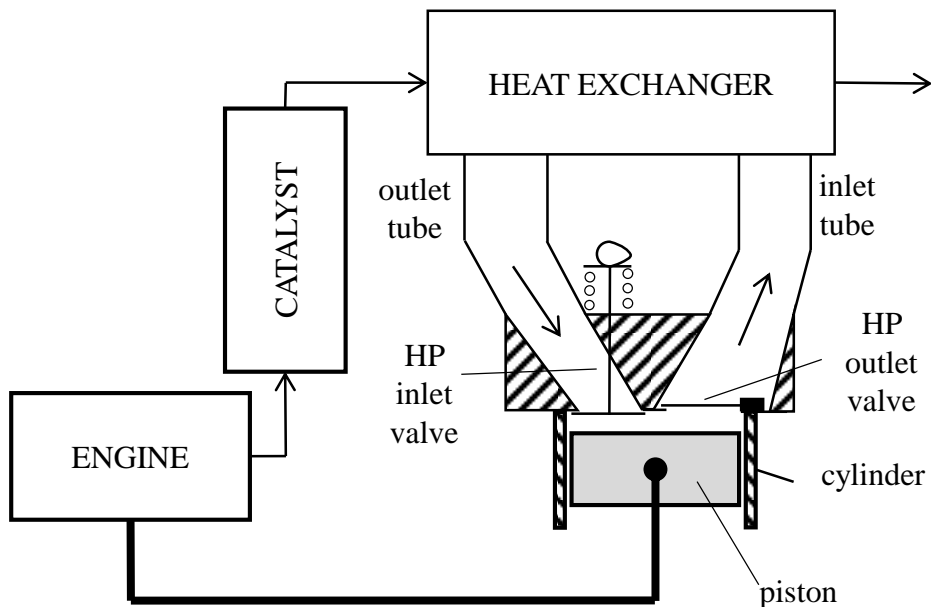
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Where \dot{m}_{exh} is the exhaust gas mass flow, T_{exh} is the temperature of exhaust gasses and C_{pexh} is the isobaric mass heat capacity of exhaust gasses. Considering these values, the present Brayton cycle system consists of two main elements: the heat exchanger and the compressor-expander machine. Regarding the first element, heat exchanger model was validated by using experimental measurements on a prototype. For the piston machine, there was no prototype made instead the model uses empirically confirmed relations from the similar technology of reciprocating internal combustion engines. In this study some machine design parameters and dimensions were defined. Valve timing and stroke were used as variables that provide variation of heat exchanger pressure and air to exhaust gas mass flow ratio in order to maximize the recuperated power and to analyse the viability of the cycle. Figure 1; **Error! No se encuentra el origen de la referencia.** shows the schematic of the cycle and naming convention that was used. Figure shows only the High Pressure (HP) valves while there are two more Low Pressure (LP) valves, that are not shown, that connect the piston machine with the ambient. Figure shows the configuration used in the model. A HP outlet valve that connects the piston machine with the heat exchanger is presented as a reed valve and a HP inlet valve that connects the heat exchanger with the piston machine is a poppet valve.



134

135

Figure 1. Brayton cycle schematic

136

137 2.1 Heat exchanger model

138 Heat exchanger model was validated by experimental measurements of a
 139 prototype. The prototype of the heat exchanger was a gas-gas, cross flow, plate-fin
 140 recuperator. Overall dimensions of the heat exchanger were 311x282x103 mm in order
 141 to obtain a compact design minimizing size and weight. Heat exchanger was tested on a
 142 steady flow test bench in order to estimate heat exchanger efficiency and pressure drops
 143 on air and gas side. The model of heat exchanger was implanted in the WHR recovery
 144 system along with the piston machine. To model the behaviour of this element two
 145 phenomena have been considered, heat transfer and pressure drop.

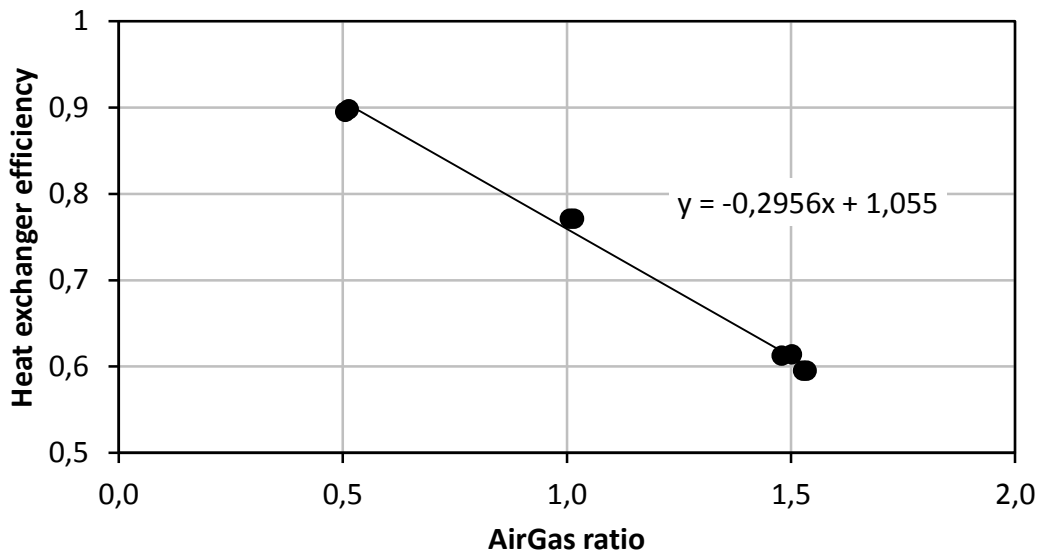
146 *Heat transfer*

147 To determine the heat transfer through the heat exchanger the parameter of heat
 148 exchanger efficiency has been used, this parameter is defined as:

149
$$\eta_{HE} = \frac{T_{air,out} - T_{air,in}}{T_{gas,in} - T_{air,in}}$$

150 Temperatures of air and gas at the inlet were imposed on the test bench along with
 151 the mass flows of air and gas. Temperatures of the air and gas at the outlet were measured
 152 and heat exchanger efficiency was correlated by using these experimental measurements.
 153 Heat exchanger efficiency was measured for various ratios of air and exhaust gas mass
 154 flows (AirGasRatio). Figure 2 shows that the relation between heat exchanger efficiency
 155 and AirGasRatio was very linear so it was defined in the model as:

156
$$\eta_{HE} = -0.2956 \text{ AirGasRatio} + 1.055$$



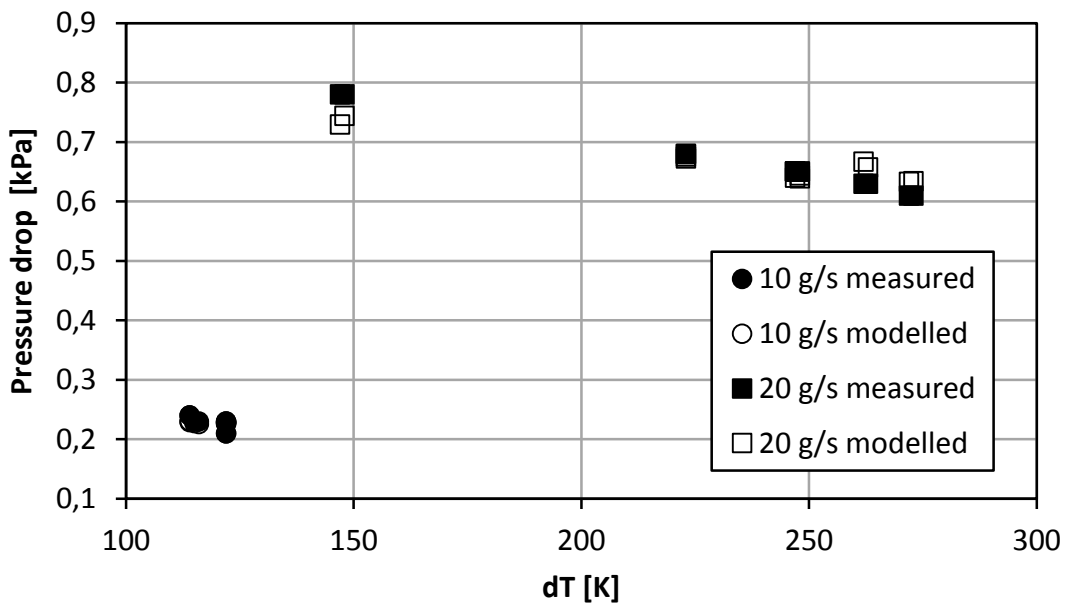
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158 Figure 2. Heat exchanger efficiency as a function of AirGasRatio

159 *Pressure drop*

160 Pressure drop is the difference in pressure at the heat exchanger inlet and outlet.
 161 It represents the resistance of flow through the heat exchanger. Pressures were measured
 162 at the heat exchanger inlet and outlet, for both air and gas side, for different mass flows

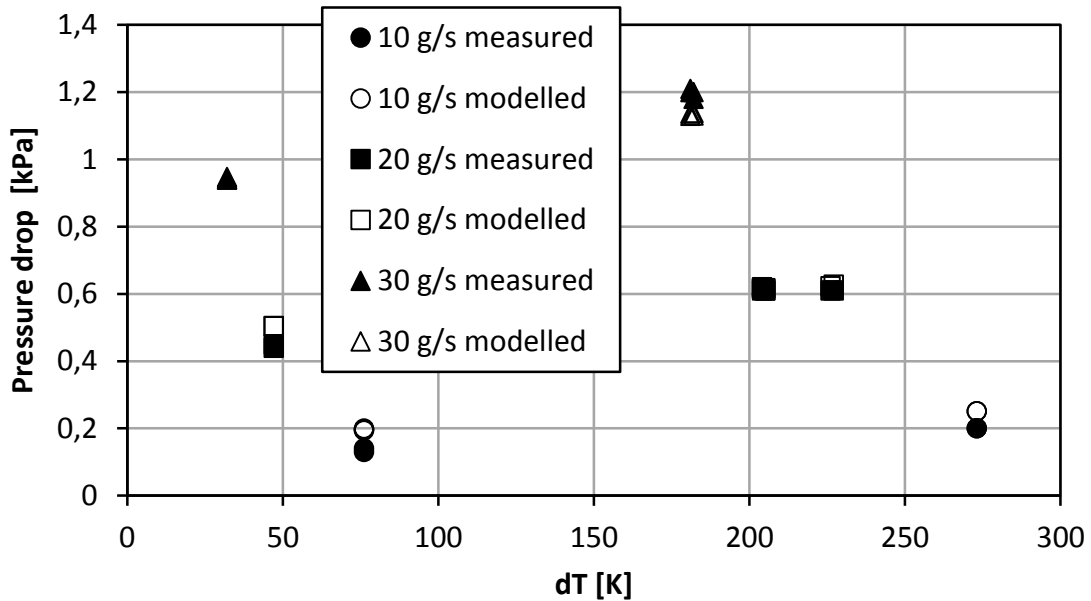
163 and temperatures. Heat exchanger is modelled by using the geometrical dimensions of
 164 the heat exchanger and pressure drop estimations [28]. The pressure drops in the air and
 165 gas sides were modelled by using separate discharge coefficients for each of the
 166 components along the heat exchanger model. The air side of the heat exchanger model
 167 was composed of five components: inlet diffuser, 90 degrees inlet bend, heat exchanger
 168 core, 90 degrees outlet bend and outlet diffuser. On the other hand, the model of the heat
 169 exchanger gas side was composed by a volume as its geometry was simpler. Comparison
 170 of measured and modelled pressure drops is represented in Figure 3 for the gas side and
 171 Figure 4 for the air side. In these figures horizontal axis represents difference of
 172 temperatures ΔT at the heat exchanger inlet and outlet. The fit between the measured and
 173 modelled pressure drop for the gas side is very good and apart from one point, when
 174 relative difference is 11%, for all other points the difference is less than 10%. For the air
 175 side, the fit is not very good for small mass flow (10 g/s) when relative difference between
 176 measured and modelled pressure drop is as high as 50%. For medium (20 g/s) and high
 177 (30 g/s) mass flow rate, that better represent the working conditions when WHR system
 178 could be used, the fit is very good and except for two points when it is around 15% for
 179 all other points it is less than 6%. Model of air side pressure drop was used in the model
 180 of Brayton cycle WHR system. Model of gas side pressure drop was used to estimate the
 181 internal combustion engine power loss because of additional exhaust back pressure
 182 (pumping losses) caused by the placement of heat exchanger in the exhaust line.



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Figure 3. Pressure drop gas side



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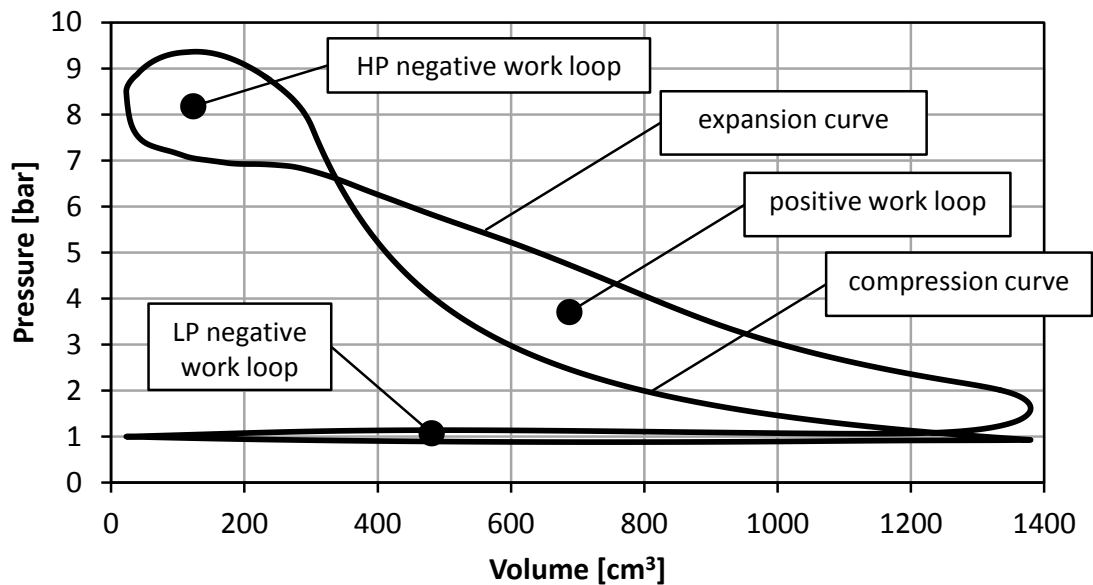
Figure 4. Pressure drop air side

187 2.2 *Piston machine*

188 The compression-expansion piston machine is similar to four stroke internal
 189 combustion engine cycle but in this case the machine has an external combustion. In ICE
 190 the heat is added by the combustion of fuel that is very fast while in the WHR cycle air
 191 has to be moved to heat exchanger where it gets warmed by the exhaust gas. The piston
 192 machine cycle starts when piston is at the lowest position called Bottom Dead Center
 193 (BDC), this position is represented as the 0 crank angle degrees. Piston then starts rising,
 194 all the valves are closed and the air that is inside the machine is being compressed. This
 195 is the compression stroke that consumes work. In some moment, before reaching the
 196 highest position, HP outlet valve opens and air starts moving from the machine to the heat
 197 exchanger. Piston reaches the TDC (180 degrees) and starts descending. In some moment,
 198 HP inlet valve opens, HP outlet valve closes and air starts moving from the HE to the
 199 machine. In some moment during the descending stroke, the HP inlet valve closes and the
 200 expansion begins producing a positive work. Piston reaches the BDC (360 degrees) and
 201 starts rising. Both LP valves open and air leaves the machine and goes out to the ambient,
 202 this is the exhaust stroke. Then, piston reaches the TDC (540 degrees) and starts
 203 descending. LP valves remain open and fresh ambient air is admitted for new machine
 204 cycle. This is the admission stroke. When this stroke ends, the LP valves close and the
 205 cycle ends. As the average pressure during the exhaust process is higher than the average
 206 pressure during the intake process this low pressure loop will consume work.

207 The main differences, comparing to ICE cycle, is that same LP valves could be
 208 used to exhaust the air from the previous cycle and admit the fresh air as there are no
 209 products of combustion and the natural movement of the air around the machine facilitates
 210 the renewal of the air. Although, this temperature is lower than in ICE it is still higher
 211 than the temperature of a fresh air. It was assumed in this study that the air is admitted at
 212 the ambient temperature. Another difference is that at the end of compression in case of
 213 ICE all the valves are closed while for WHR piston machine, the HP valves are open. If
 214 some valve is open while piston is at TDC, cylinder pressure would not rise significantly

215 even if high compression ratio is used. In this case compression ratio would not be limited
 216 by the pressure but by the clearance between the piston and valve or cylinder head. As
 217 this clearance could be very small very high compression ratio can be achieved.



218
 219

Figure 5. Typical Brayton cycle pV diagram

220 Figure 5 shows the typical pressure-volume diagram of the proposed piston
 221 machine. HP negative work represents the pumping work that was consumed by the
 222 system to move the air from the piston machine to the HE and back.

223 To model this element, the machine cycle has been modelled as a 0D variable
 224 volume with two open loops to move the air with negative work (one at high pressure and
 225 the other at low pressure) and one closed loop with positive work. Piston diameter was
 226 defined in Introduction to be 120 mm but the stroke was not yet defined. Piston stroke
 227 defines the displaced volume and greatly affects the air mass flow through the heat
 228 exchanger. Pumping losses of both LP and HP cycle parts also have a big influence.
 229 Initially, the value for stroke was taken from the recommendation of bore to stroke ratio
 230 for ICE. Heywood [29] suggests stroke to bore ratio in the range of 0.9-1.1 for the
 231 passenger car application. The mean value of this range, the value of 1 was decided for
 232 stroke to bore ratio. Thereby, stroke was defined to be 120 mm. The model of valves was
 233 then made allowing for estimation of pumping losses and air mass flow. Stroke was later
 234 used as a variable to analyse the system behaviour. Because the cycle is very similar to
 235 ICE cycle, the first type of valves that was studied was the poppet valve actuated by
 236 camshaft that is the standard valve kind for ICE.

237 *Poppet valve*

238 It was decided to use four valves. Two valves would be in charge for low pressure
 239 (LP) part and two valves for high pressure (HP) part. It was assumed that valves for the
 240 same pressure part have the same size. Valves should be as large as possible to lower
 241 pumping losses. Valve size is limited by the minimum clearance between the valve and
 242 cylinder and minimum distance between the valves. In the cylinder head, minimum
 243 distance between valves was 0.12Dp as a recommended value for ICE [30]. Where, Dp

244 is the piston diameter. Minimum clearance between the valve and cylinder was 2.5 mm
 245 as a typical value for ICE [31]. Other valve dimensions were taken from
 246 recommendations [29]. Cam profile for valve opening and closing and coefficients of
 247 discharge for valves were taken from [31]. High pressure valves are specific because of
 248 their short timing. While low pressure valves have full piston stroke to open and close,
 249 duration of high pressure valve is closer to half the piston stroke. Valve lift of high
 250 pressure valves had to be proportionally reduced in order to respect the recommended
 251 values of valve acceleration, deceleration and avoid high impact between valve and valve
 252 seat. The pressure drop and the mass flow through these valves were modelled by using
 253 discharge coefficients of similar valves measured in an air test bench and correlating these
 254 coefficients with the opening lift of the valves. Considering that higher pumping losses
 255 could be expected at HP valves it was believed that it should be beneficial if HP valves
 256 are bigger than LP valves.

	Case 1	Case 2	Case 3	Case 4	Case 5	Case 6	Case 7
HP diameter [mm]	39	40.5	42	43.5	45	46.5	48
LP diameter [mm]	39	37.5	35.8	34.5	31.7	29.8	26

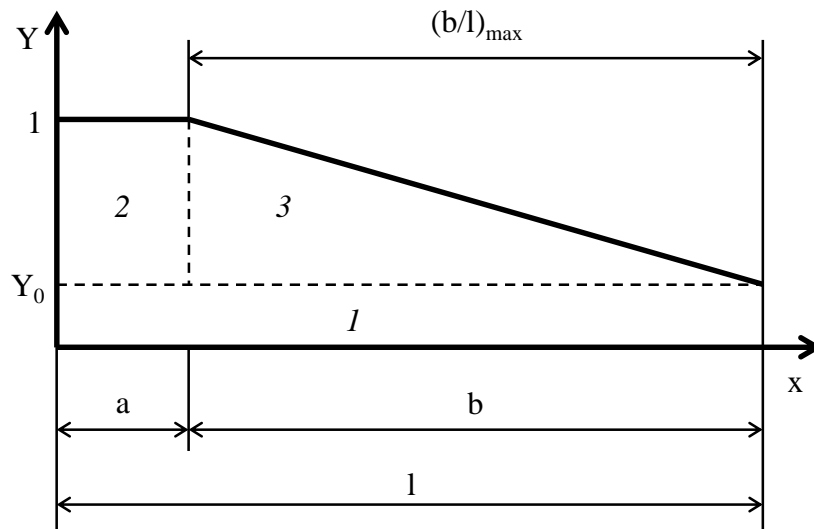
257 Table 3. Poppet valve diameters

258 Table 3 shows the 7 cases with different valve diameters that were considered in
 259 the study in order to optimize them to the processes of compression and expansion. LP
 260 valve diameters were the maximum diameter that could fit respecting selected HP
 261 diameter and already mentioned limitations.

262 *Reed valve*

263 The used reed valve model consider the reed valve as a rigid flap rotating around
 264 one of its edges. Load on the flap was defined by defining the pressure distribution on
 265 each side of the valve. Moment of the inertia for the model was calculated knowing the
 266 dimensions and density of the material. Reed valve stiffness was modelled as a torsional
 267 spring. Torsion coefficient of the spring was a parameter for optimisation in order to fit
 268 better the model to the experimental values. The maximal rotation angle is limited by the
 269 maximum aperture of the valve's free end. Pressure distribution on each valve side was
 270 modelled according to Flecks model [32]. When the valve is closed overall pressure
 271 differential is uniform along the petal and it is equal to the difference between upstream
 272 and downstream pressure. When the valve starts to open some part of the pressure
 273 distribution remains uniform while the other part has a triangular distribution. At very
 274 low lift, pressure differential along the petal length follows the overall differential except
 275 at the very end. At high lift, the pressure distribution tends to have a more triangular
 276 shape. Figure 6 shows a generic pressure distribution along the reed valve. Horizontal (x)
 277 axis represents the distance along the petal length (l) while vertical axis represents the
 278 pressure defined by $Y = \Delta p(x) / \Delta p$. Where Δp is the difference of pressures on each side of
 279 the reed valve. Fleck estimated that one part of the distribution remains uniform
 280 regardless of valve lift. This part was marked as Y_0 in Figure 6. In the present work the
 281 value of $Y_0 = 0.3$ was used as this was the value used by Fleck et al. Figure 6 shows the
 282 three load areas marked 1-3. Each of the loads creates a torque that contributes to total
 283 torque that makes the petal rotate. When the valve is closed the pressure distribution is
 284 uniform and b is equal to zero. When valve starts opening length b starts augmenting from

285 zero to the maximum value defined by ration $(b/l)_{\max}$. The value of $(b/l)_{\max}=1$ was used
 286 because it offered the better fit with the experimental values. In other words, when the
 287 valve is fully open b is equal to l .

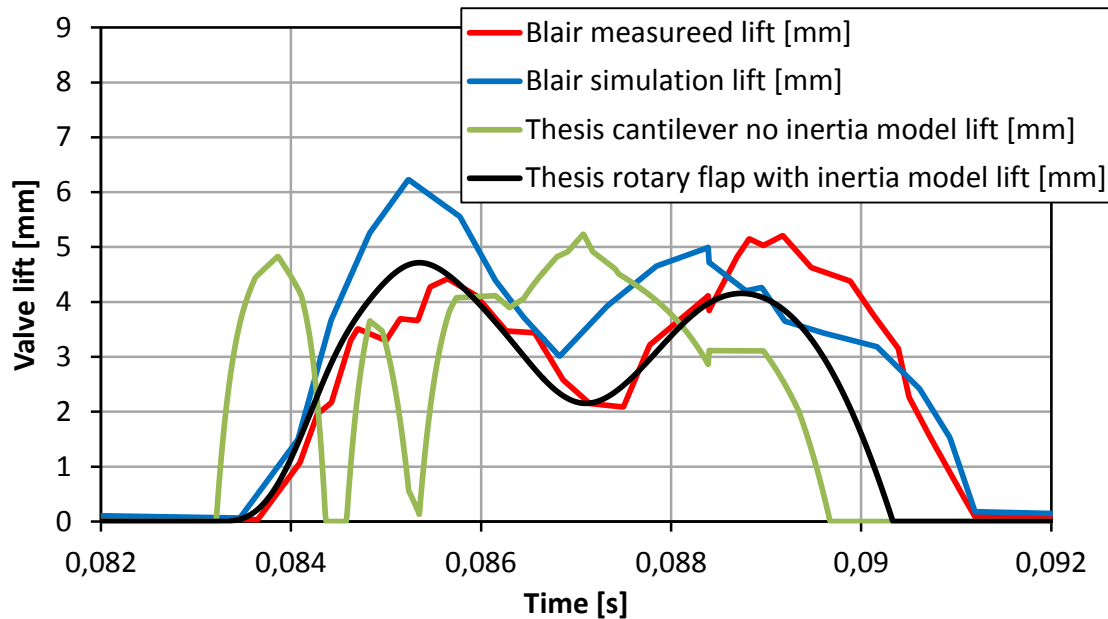


288
 289

Figure 6. Reed valve pressure distribution

290 Reed valve model was validated using the data from Blair's experiments [33].
 291 Pressures measured on both sides of the reed valve and petal tip aperture were used to
 292 parametrize the model. He also modelled the valve as a cantilever beam and compared
 293 his simulation results with measured values. To validate the present thesis's model, same
 294 pressures measured by Blair were imposed in the model. Same dimensions, material and
 295 mass for reed valve were also used in the model as in the Blair's experiment.

296 Figure 7 shows the valve lift as a function of time for imposed pressures on each
 297 petal side. Red curve represents Blair's measured lift while blue curve represents the
 298 results of the Blair's model of cantilever valve with inertia. Black curve represents results
 299 of authors' model of rotary flap with inertia. Green curve represents the authors' model
 300 of cantilever beam without inertia that was given for a comparison. It can be seen that the
 301 valve lift of the rotary flap model used in the present study fits very well with the
 302 experimental values of Blair. Rotary flap model does not predict precisely the timing of
 303 closing the valve but it does generally predict better the valve lift than Blair's model of
 304 cantilever beam. The figure shows that authors' cantilever beam model without inertia
 305 does not predict well the valve lift and stresses the importance of using the model with
 306 inertia. This proposed model with inertia is the model chosen for the present study.



307
308

Figure 7. Reed valve lift simulation and measurements

309 *2.3 Heat transfer model*

310 Heat transfer from the hot air trapped in the cylinder to colder cylinder walls can
 311 be the cause of significant efficiency losses. This heat loss lowers the temperature of the
 312 air which comes from the heat exchanger, and consequently the pressure during the
 313 expansion, which leads to less work. During the last part of expansion, temperature of the
 314 wall gets to be higher than temperature of the air and there is a positive effect of heat
 315 transfer but it is to be expected that this part is small. During the compression, pressure
 316 and temperature in the cylinder rise. While the temperature of air is less than the cylinder
 317 wall temperature, the heat is being transferred from the wall to the air. This warms the air
 318 and raises the pressure, which leads to higher work needed for compression. During the
 319 last part of compression it is possible that the wall temperature gets lower than air
 320 temperature and positive effect of heat transfer occurs but it is reasonable to believe that
 321 would be the small part. During the expansion process a similar phenomenon occurs but in
 322 the opposite direction. In order to take these important effects into account, a heat transfer
 323 model was applied. The model of Annand [34] for four stroke ICE was used, so Nusselt
 324 number is defined as $N_u = 0.49Re^{0.7}$ where Re is the Reynolds number calculated by
 325 $Re = \frac{S_p D_p}{\nu}$. Where, S_p is the area for the heat transfer, considered as the sum of piston
 326 surface, head surface that is considered to be equal to piston surface and the area of
 327 cylinder whose height would depend of crank angle.

328 In the model, heat is transferred between the air and a single mass (node). This
 329 mass represented the sum of piston, cylinder and head equivalent mass. As all tests were
 330 for steady conditions, weight of this mass (thermal inertia) is not relevant. It was assumed
 331 that there was no heat transfer between this node and the ambient. It means that the global
 332 piston machine cycle is considered as an adiabatic process.

333 *2.4 Mechanical losses*

334 The model for the mechanical losses is based on the article by Sandoval and
 335 Heywood [35]. In this article authors estimate the mechanical losses for different
 336 components of gasoline engines. To take into account the difference between the WHR
 337 machine and ICE, from the different equations proposed by authors the ones that were
 338 obtained from the experiments without the combustion were selected. Mechanical losses
 339 greatly depend on part number and their dimensions: cylinder bore, stroke, diameters of
 340 bearing journals, lengths of journals, number of bearing, number of valves etc. As a first
 341 approximation dimensions of WHR machine were taken from the recommendations for
 342 ICE [30] and are presented in Table 4.

Dimension	Recommended range	Chosen value
cylinder bore B		120 mm
crankshaft bearing diameter D_{bc}	$(0.6-0.7)B$	70 mm
crankshaft bearing length l_{bc}	$(0.45-0.6)D_{bc}$	30 mm
number of crankshaft bearings n_{bc}		2
diameter of connecting rod bearing D_{br}	$(0.55-0.65)B$	65 mm
connecting rod bearing length l_{br}	$(0.45-0.6)D_{br}$	29 mm
number connecting rod bearings n_{br}		1
number of camshaft bearings n_{bv}		2
number of poppet valves n_{val}		3

343 Table 4. Recommended and chosen parameters for calculation of mechanical
 344 losses

345 2.5 Indirect losses

346 Indirect losses are not directly affecting the WHR cycle efficiency. Those losses
 347 take into account how application of Brayton cycle WHR system affects the efficiency of
 348 the internal combustion engine in the vehicle. As the objective of the WHR is to improve
 349 ICE efficiency and lower the fuel consumption of the vehicle those losses must be taken
 350 into account. Indirect losses can be divided in two sources: pumping losses because of
 351 the additional exhaust backpressure and fuel consumption increase because of the
 352 additional rolling friction of the vehicle with the ground due to the weight of Brayton
 353 cycle elements.

354 Exhaust backpressure pumping losses

355 Placing the heat exchanger in the exhaust line increases the exhaust back-pressure.
 356 This increases the ICE pumping losses because the pistons have to push the exhaust
 357 gasses harder to pass them through an additional resistance of heat exchanger. Pressure
 358 drop in the heat exchanger increases the negative work of the pumping losses. Equation
 359 from [36] was used to estimate the power loss in this process:

$$360 P_{pl} = \frac{\dot{m}}{\rho} \Delta p$$

361 Density ρ is the mean value of heat exchanger inlet and outlet density. Exhaust
362 gas was considered to have the characteristics of air as an ideal gas. Inlet and outlet
363 densities were calculated as a function of inlet and outlet temperature and pressures. Inlet
364 temperature was defined by the selected ICE operating point. Outlet temperature was
365 estimated from the heat exchanger energy balance.

366 *Additional weight*

367 Implementing the WHR system contributes to additional vehicle weight. With the
368 added weight engine would have to produce more power for the vehicle to travel at the
369 same velocity as it was without this additional weight. Engine power needed for desired
370 vehicle velocity can be calculated by:

$$371 \quad P_E = (F_{dr} + F_{aero}) \frac{1}{\eta_{TR}} v_{veh}$$

372 Where F_{dr} is the driving force, F_{aero} is the aerodynamic drag force, η_{TR} is
373 transmission efficiency and v_{veh} is the vehicle velocity.

$$374 \quad \text{Driving force is calculated by: } F_{dr} = \left(m_{veh} + 4 \frac{J_{wh}}{R_{wh}^2} \right) gf$$

375 Where m_{veh} is the vehicle mass, J_{wh} is the wheel moment of inertia, g is the
376 gravitational acceleration and f is the rolling friction coefficient.

377 Only the mass of vehicle is changing. Aerodynamic drag force, wheel moment of
378 inertia and wheel radius do not depend on vehicle mass so that the additional engine
379 power can be calculated by:

$$380 \quad \Delta P_E = \Delta m_{veh} gf \frac{1}{\eta_{TR}} v_{veh}$$

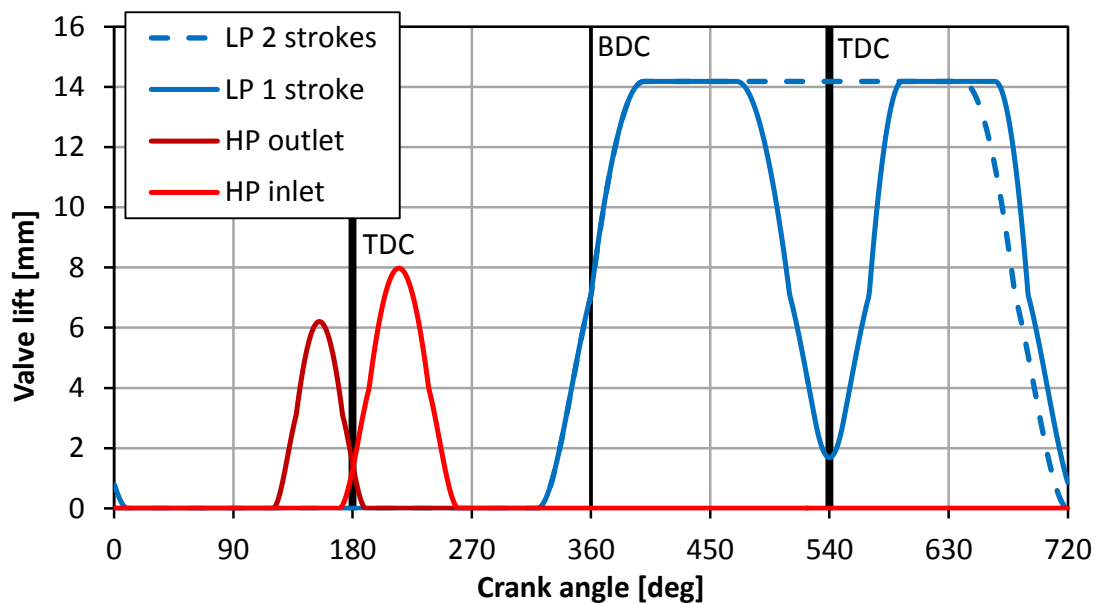
381 **3 Theoretical studies**

382 *3.1 Valve timing*

383 At first, it was considered that all four valves are poppet valves. As there are 4
384 valves but both LP valves use the same timing that leaves 6 parameters (opening and
385 closing angles) to be optimized.

386 In order to define a realistic lift, typical lift shapes of IC engine cam valves are
387 used to simulate a realistic lift on these elements. Two strategies were considered for LP
388 valve timing. By the first strategy (labelled as LP 2 strokes), valves open at the start of
389 exhaust stroke and remain open for two strokes. Because the valves are open when piston
390 is at TDC there must be slots (reliefs) in the piston crown for the valves in order to avoid
391 the contact between the piston and valves. These slots increase the dead volume which
392 negatively affects the volumetric efficiency. By the second strategy (labelled as LP 1
393 stroke), valves open at the start of exhaust stroke and close either fully or partially at the
394 TDC and then open again at start of admission and close at the end of admission. If the
395 valves close only partially there must be again reliefs in the piston crown but this time
396 much smaller because valve lift is less than full lift. For this study, a minimum lift of 2
397 mm has been considered on the TDC Closing the valves fully is not desirable because

398 high compression ratio causes high pressure rise and high negative work when valves are
399 closed.



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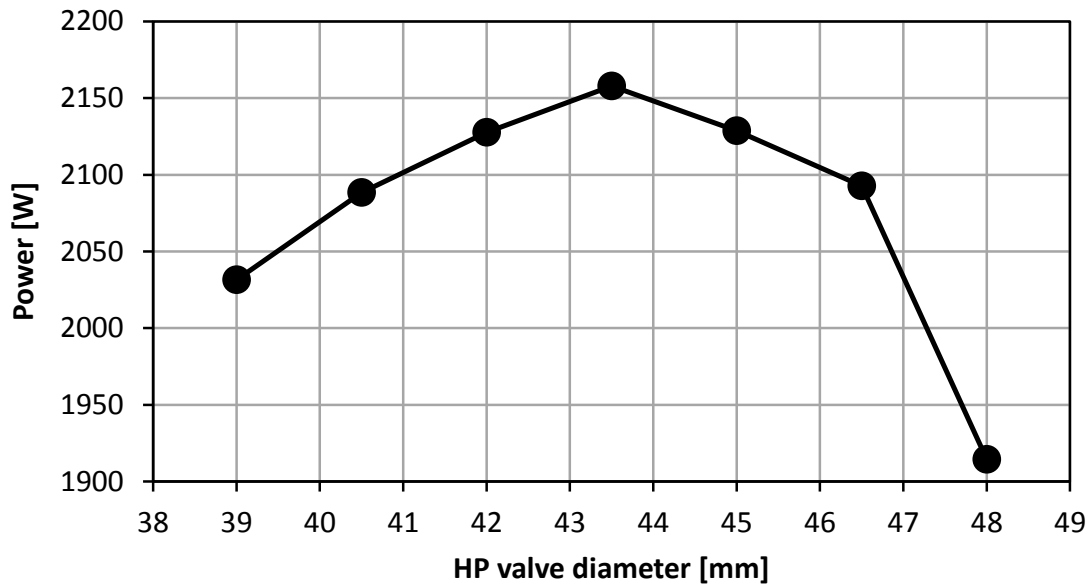
Figure 8. LP valve timing strategies

402 Figure 8 shows both LP valve strategies. LP 1 stroke strategy represents a better
403 solution than LP 2 stroke because stroke could be shorter for the same mass flow (110
404 mm for LP 1 stroke against 130 mm for LP 2 stroke). As it was already said, the reason
405 for this is the better volumetric efficiency of 1 stroke strategy because of smaller valve
406 reliefs. It can be seen that LP valves open before BDC. Opening the valves before BDC
407 (when pressure in the cylinder is higher than atmosphere pressure) helps expelling the air
408 out and lowers the exhaust pumping losses. By lowering the initial exhaust pumping
409 work, positive work also increases. Valves were opened 40 degrees before BDC. This
410 value was obtained as optimal by simulation varying the opening angle of the LP valves.
411 Earlier valve opening than this lowers the positive work of expansion. Later valve
412 opening than this increases the negative work. It can be seen also that HP valve lifts are
413 much shorter because there is not enough time to fully open the valves. Small HP valve
414 overlap is desirable in order to lower the high pressure rise that would occur as a
415 consequence of high compression ratio if both valves would be closed at TDC. In this
416 case, 20 degrees valve overlap was used. For smaller valve overlap, valves are open very
417 little and the piston cannot suck the air, the pressure in the cylinder decreases rapidly.
418 Higher values of valve overlap were avoided in order to avoid the reflow from the HP
419 inlet valve to HP outlet valve.

420 This way, there are only 2 parameters left for valve timing optimisation: HP outlet
421 valve open angle (OA) and HP inlet valve close angle (CA). HP outlet valve OA was
422 varied in the range 110-140 crank angle degrees with 10 degrees step. HP inlet valve CA
423 was varied in the range 240-280 crank angle degrees also with 10 degrees step. For the
424 study of maximum recuperated power it was decided to include two more parameters:
425 piston stroke and valve diameters. Piston stroke was varied in the range 70-100 mm with
426 steps of 10 mm. This variation of piston stroke allowed sufficient variation of air mass
427 flow to optimize the machine design. Air mass flow was varied in order to study the effect
428 of AirGasRatio (ratio of air and exhaust gas mass flows) on recuperated power which is

429 a variable that will affect the behaviour of the cycle. Different sizes of HP and LP valves
430 were tested in order to estimate the size that would offer better recuperated power. Valve
431 diameters used in the study were defined in the Table 3.

432 Figure 9 shows the recuperated power as a function of valve diameters. For each
433 point in this figure all other parameters were varied in their respective ranges. The
434 maximum recuperated power of 2157 W was obtained with HP valve diameter of 43.5
435 mm and LP valve diameter of 34.5 mm.

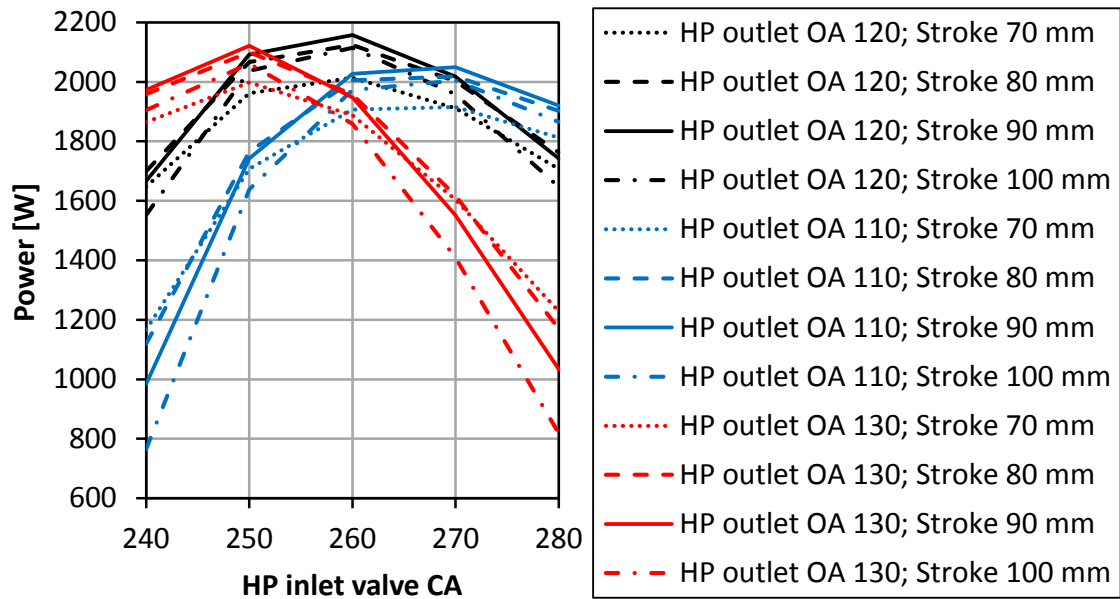


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Figure 9. Recuperated power as a function of valve diameters

438 The effects of valve timing and stroke length on recuperated power could better
439 be seen for fixed valve dimensions. Figure 10 shows the recuperated power as a function
440 of piston stroke, HP inlet valve CA and HP outlet valve OA for valve diameters that
441 provided the maximum power (HP valve diameter 43.5 mm, LP valve diameter 34.5 mm).
442 For the clarity, the plot shows only the three values of HP outlet valve OA that provided
443 the highest recuperated power. Results of the simulation show that for any HP outlet valve
444 OA the stroke of 90 mm always provides the highest recuperated power. The optimal HP
445 outlet valve CA changes with HP inlet valve OA. For the HP outlet valve OA of 120
446 degrees the optimal HP inlet valve CA is 260 degrees, but if the HP outlet valve OA
447 decreases to 110 degrees, the optimal HP inlet valve CA increases to 270 degrees.
448 Maximum recuperated power of 2157 W was obtained with HP outlet valve OA of 120
449 degrees, HP inlet valve CA of 260 degrees and stroke length of 90 mm.



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Figure 10. Recuperated power as function of stroke length, HP inlet valve CA

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and HP outlet valve OA

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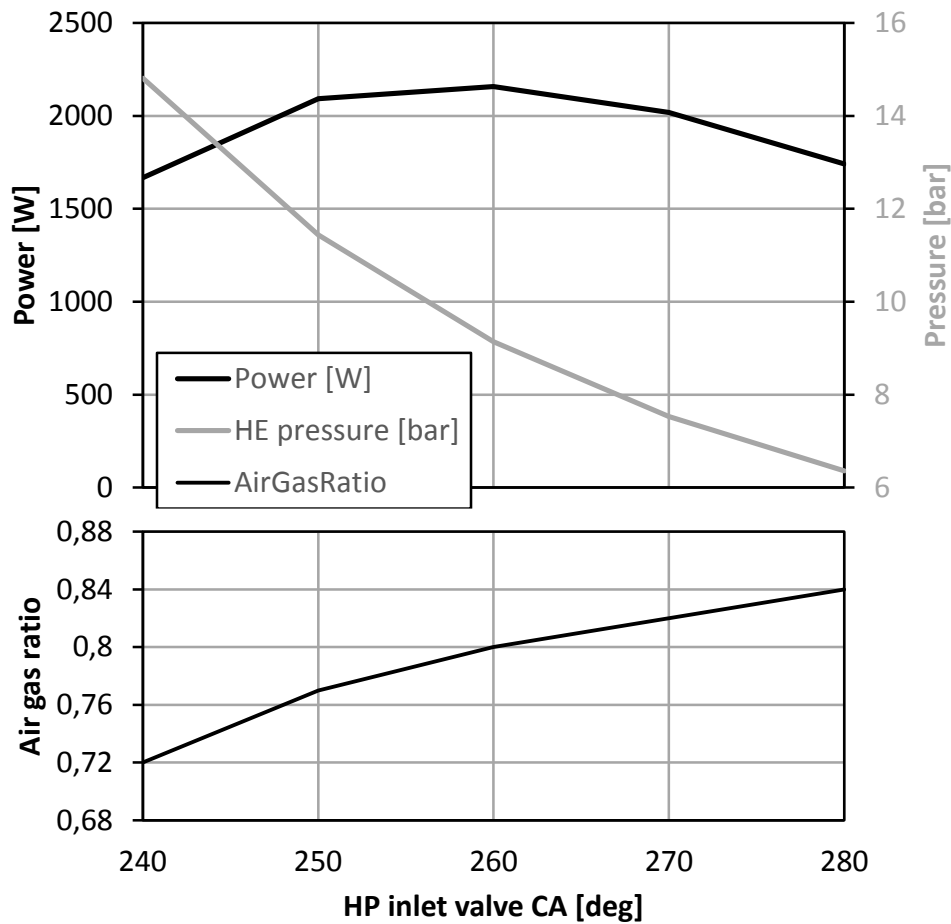
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For this optimal point with a fixed HP outlet valve OA of 120 degrees and a stroke of 90 mm, changing the HP inlet valve CA has a main effect on recuperated power and pressure in the heat exchanger with the secondary effect on air mass flow. This can be seen on Figure 11. HE pressure from the figure represents cycle mean value of the pressure in the heat exchanger. If the HP inlet valve closes later, pressure in the heat exchanger will be lower and air mass flow higher, producing an optimal value that results in highest recuperated power. Recuperated power is highest for HP inlet valve CA of 260 degrees and stroke of 90 mm when HE pressure is 9.14 bar and air gas ratio is a 0.8 approximately.



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Figure 11. Effect of HP inlet valve CA on pressure in the HE, AirGasRatio and

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power; stroke 90 mm; HP inlet valve OA 120 degrees

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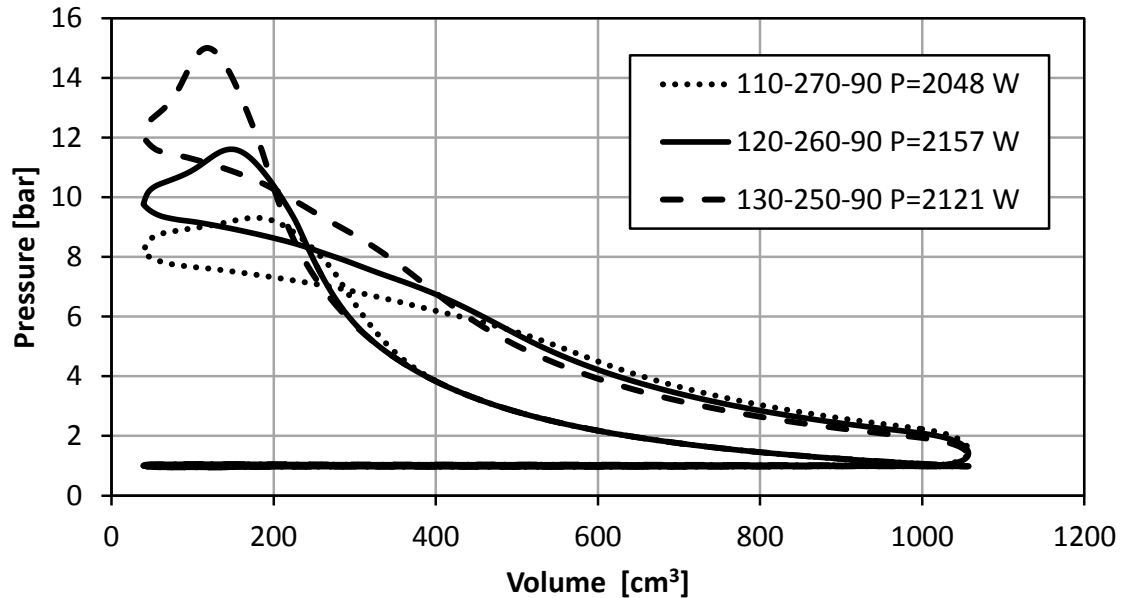
Figure 12 shows the comparison of pressure-volume diagrams for the three cases of HP valve timing. These cases are the points of maximum power for each HP outlet valve OA value from Figure 10. The curves from Figure 12 were named in the following style HP outlet valve OA-HP inlet valve CA-Stroke followed by the recuperated power for that valve timing. For example, the label “120-260-90 P=2157 W” represents the case with HP outlet valve OA of 120 degrees, HP inlet valve CA of 260 degrees and stroke of 90 mm. Highest recuperated power was obtained in this case with a HP inlet valve OA of 120 degrees as it was explained before. Earlier HP outlet valve opening results in the decrease of both HE pressure and cylinder peak pressure. While the difference in power between 120 and 110 HP inlet valve OA is small 109 W, the difference in HE pressure is more significant as the pressure decreases from 9.14 bar to 7.55 bar.

476

The HP negative work area from the Figure 12 is significantly big. For the case when the recuperated power was maximal (2157 W), HP pumping losses consumed 1220 W while the positive work generated 3517 W. HP pumping loss is very high and it should be further analysed how to reduce it. The reason for this big loss is that the big quantity of air must be moved from the cylinder to the heat exchanger in a short time period. This creates the high instantaneous mass flow rate that causes the high pressure drop in the HP outlet valve and HP inlet valve.

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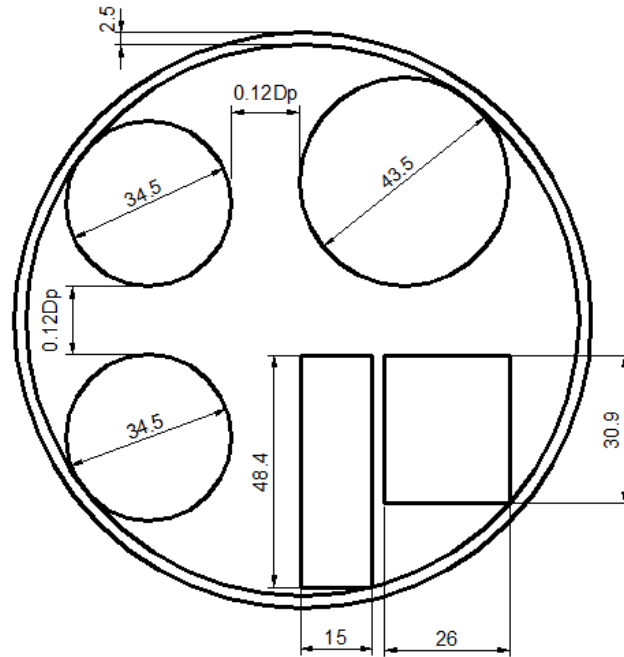
483 While power losses of HP open loop are significant, the power losses of LP open
 484 loop are not significant, 140 W in the case of maximal recuperated power. The long time
 485 period to move the air during the low pressure loop compared with the high pressure one
 486 produces that significant reduction on power loss.



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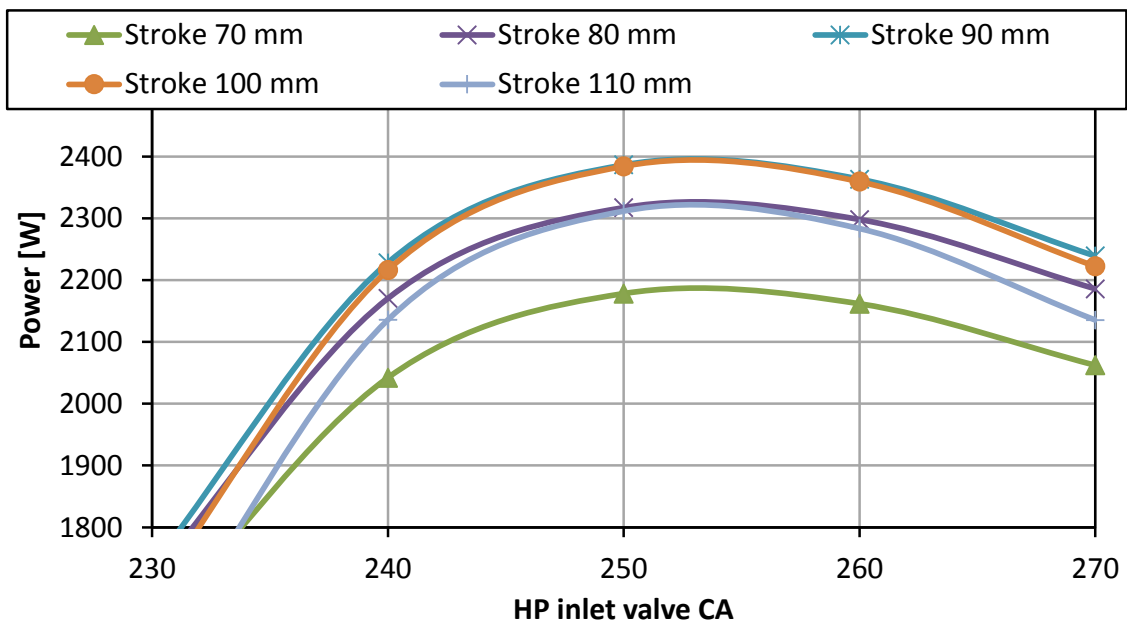
Figure 12. pV diagram comparison for different HP valve timing

489 In order to reduce the HP loop negative work and to increase the adaptability of
 490 the system, the HP outlet poppet valve has been replaced with a reed valve in the next
 491 study. A reed valve model was used to substitute the poppet HP outlet valve model. Two
 492 reed petals were placed in the place of substituted poppet valve. The distance between the
 493 reed valve and other valves was the same as it was for all poppet valves, when
 494 recommendations were used. Figure 13 shows the dimensions and placement of the reed
 495 valves in the cylinder head. It was decided to use two reed valves in order to use the entire
 496 surface previously occupied by the poppet valve. Timing of the LP valves and HP inlet
 497 valve OA were kept the same as for poppet valve. As reed valve opening and closing is
 498 automatic and related with the reed valve pressure difference that leaves only 1 parameter
 499 (the HP inlet CA) for valve timing optimisation. This parameter was varied in the range
 500 240-280 degrees with the 10 degrees step. Piston stroke was used as a second variable to
 501 include the effect of ratio of air and gas mass flows (AirGasRatio). Stroke was varied in
 502 the range of 70-100 mm with the 10 mm step. Results are presented in Figure 14. The
 503 maximum recuperated power was 2386 W for HP inlet valve CA 250 degrees and a piston
 504 stroke of 90 mm that corresponds to an AirGasRatio of 0.77. For the case when the
 505 recuperated power was maximal (2386 W), positive work generated 3560 W while HP
 506 pumping losses consumed 1032 W and LP pumping losses consumed 142 W. HP
 507 pumping losses are significant as they consume 28.99% of the energy generated by
 508 positive work loop (3560 W). The maximum recuperated power for the reed valve model
 509 was higher than the one that was obtained with HP outlet poppet valve (2157 W).



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Figure 13. Placement of reed valves

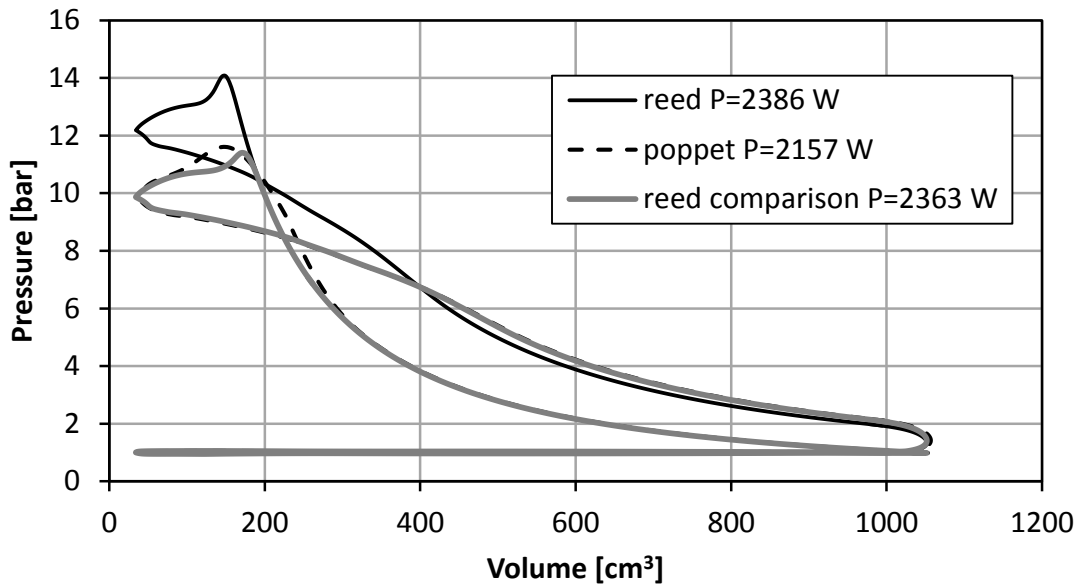


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Figure 14. Recuperated power as a function of HP inlet valve CA and stroke

514 Figure 15 shows the comparison of pV diagrams for the two cases of HP outlet
 515 valve as a reed valve and as a poppet valve. The values of HP inlet valve timing and piston
 516 stroke that provided best recuperated power were different for each valve type. Curve
 517 named “reed” represents the pV diagram of the reed valve model for the values of HP
 518 inlet valve CA of 250 degrees and stroke of 90 mm that provided the maximum
 519 recuperated power. Likewise, the curve “poppet” refers to pV diagram of the poppet valve
 520 for HP inlet valve CA 260 degrees and stroke of 80 mm that provided the maximum
 521 recuperated power. Because of earlier HP inlet valve closing the pressure of the reed valve
 522 is higher and because of the longer stroke the volume is also higher. This makes it difficult

523 to compare directly two valve types in the pV diagram. The curve named “reed
 524 comparison” was added in order to compare reed and poppet valve in similar conditions.
 525 For this curve the same HP inlet valve timing and stroke was used as for poppet valve.
 526 Clearly, the HP negative work of the reed valve is less than the poppet valve.



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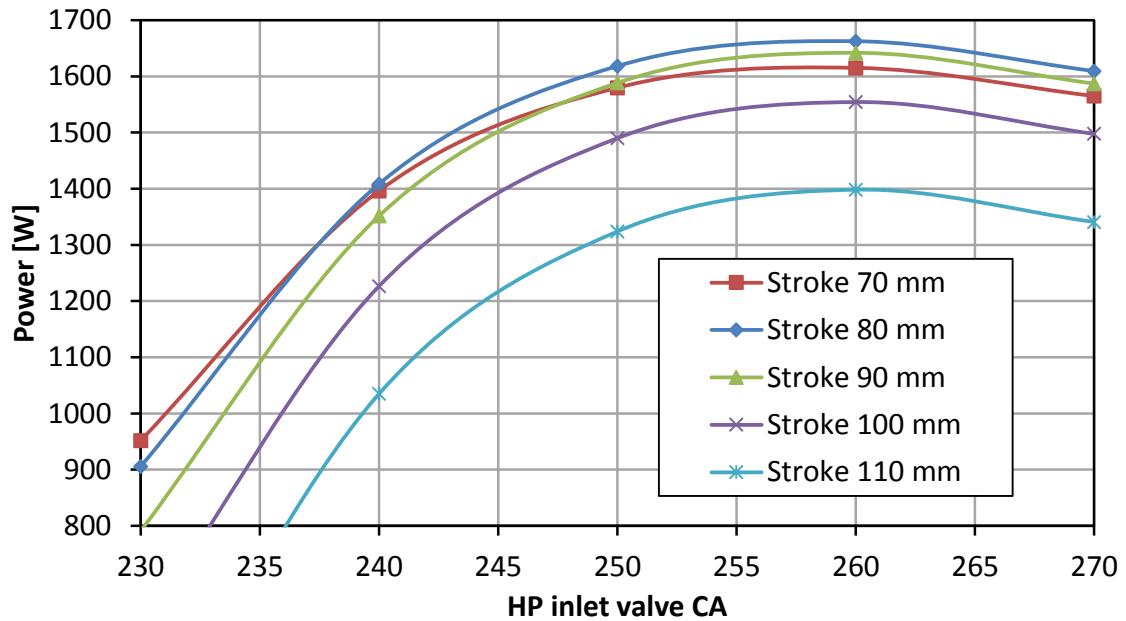
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Figure 15. Reed valve pV diagram

529 Using the reed valve as outlet valve represents an improvement over the poppet
 530 valve in both simplicity and recuperated power. For the inlet valve, the reed valve cannot
 531 be used or any other valve that opens with the difference of pressures on each valve side.
 532 This is because heat exchanger and connecting pipes must be pressurized and automatic
 533 valve would depressurize them during the admission and exhaust stroke.

534 3.2 Heat transfer

535 In order to improve the machine model, the heat transfer model described in
 536 previous point was applied to the 0D compression-expansion machine model where reed
 537 valve was used as a HP outlet valve and poppet valve as HP inlet valve. As in previous
 538 studies, variables were piston stroke and HP inlet valve closing angle (CA). Piston stroke
 539 was varied in the range 70-110 mm and HP inlet valve CA in the range 230-270 degrees.
 540 Figure 16 shows the results of recuperated power with the heat transfer model included.
 541 A maximum recuperated power of 1662 W was obtained with HP inlet valve CA of 260
 542 degrees and piston stroke of 80 mm that provided the AirGasRatio of 0.68. Maximum
 543 recuperated power was 724 W lower than it was for the model without the heat transfer
 544 (2386 W). This power represents 20.34% of the energy generated by positive work loop
 545 for the reference model (3560 W for the model with reed valve and without heat transfer).
 546 Due to this effect of heat transfer during the compression and expansion strokes,
 547 AirGasRatio that provided the maximum recuperated power was lower than for the model
 548 without the heat transfer. Consequently, the piston stroke that provided the maximum
 549 power was 10 mm shorter.



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Figure 16. Recuperated power with the heat transfer model

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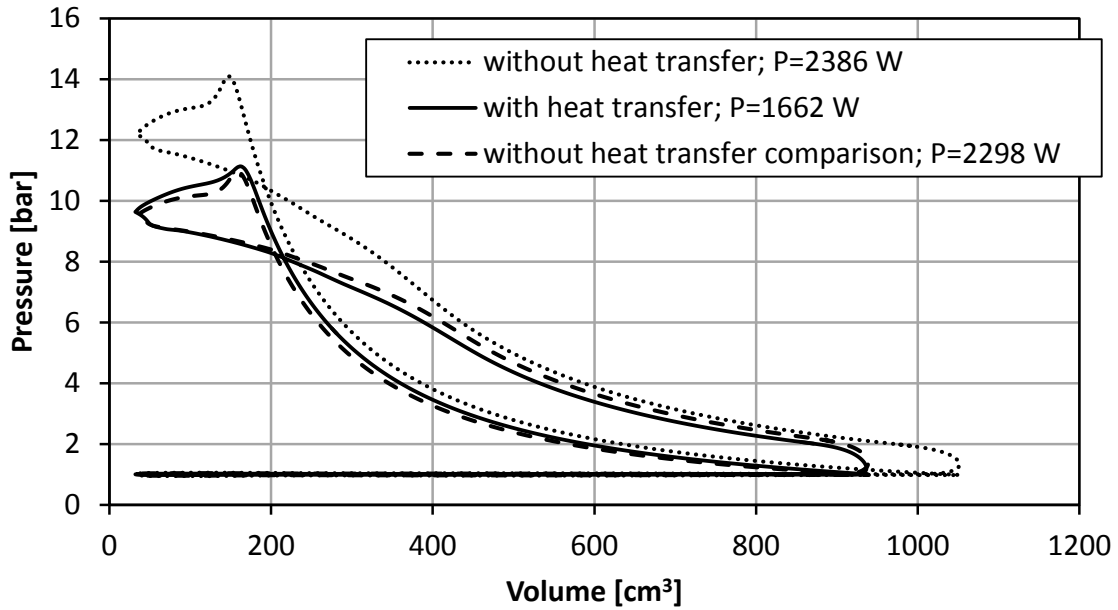
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Pressure-volume diagram of the configuration that gave the maximum power is represented in Figure 17 (plot “with heat transfer”) along with the same plot for the cycle without the heat transfer. Again, the areas of pressure-volume diagrams cannot be easily compared if HP inlet valve CA and stroke are not the same for both plots. For that reason additional plot is added for the model without the heat transfer. For this plot the same parameters were used that provided the maximum recuperated power for the model with heat transfer (HP inlet valve CA 260 degrees, stroke 80 mm). This plot is called “without heat transfer comparison”. For this curve, HP inlet valve CA and stroke were not the ones that gave the highest recuperated power. The plot of the model without the heat transfer that gave the maximum recuperated power (2386 W) is called “without heat transfer”. The main difference between the two cycles is that, with the heat transfer, the positive work area is narrower. Compression stroke presents higher pressure values because heat transfer from the warm cylinder wall rises the temperature and the pressure of the air. On the other hand, expansion stroke presents lower pressure values because heat is transferred from the air to the cylinder wall which decreases the air temperature and pressure. These heat transfers decrease significantly the cycle power.



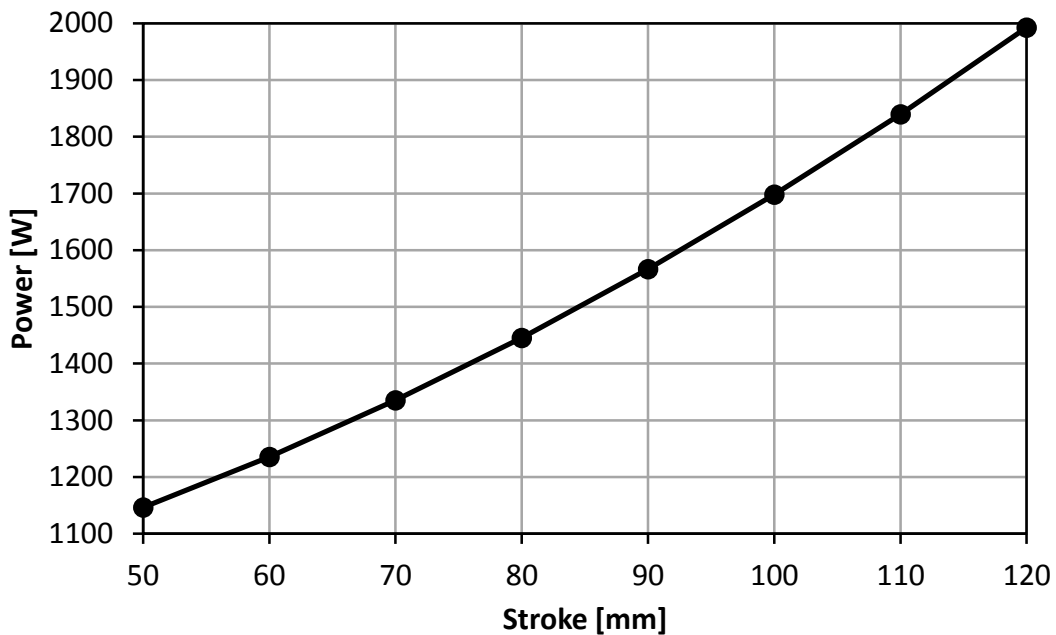
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Figure 17. pV diagram of the cycle with and without the heat transfer

570 *3.3 Mechanical losses*

571 For a warmed up machine, mechanical losses would mainly depend on machine
 572 speed and piston stroke. Machine rotary speed was fixed because it was supposed that
 573 machine is directly coupled to the IC engine and its speed was fixed for the selected
 574 operative point to 2623 rpm. Thereby, for all other parameters defined, mechanical losses
 575 would depend on piston stroke. Figure 18 shows this dependency and it can be seen that
 576 the power of mechanical losses is in the same order of magnitude than the recuperated
 577 power.



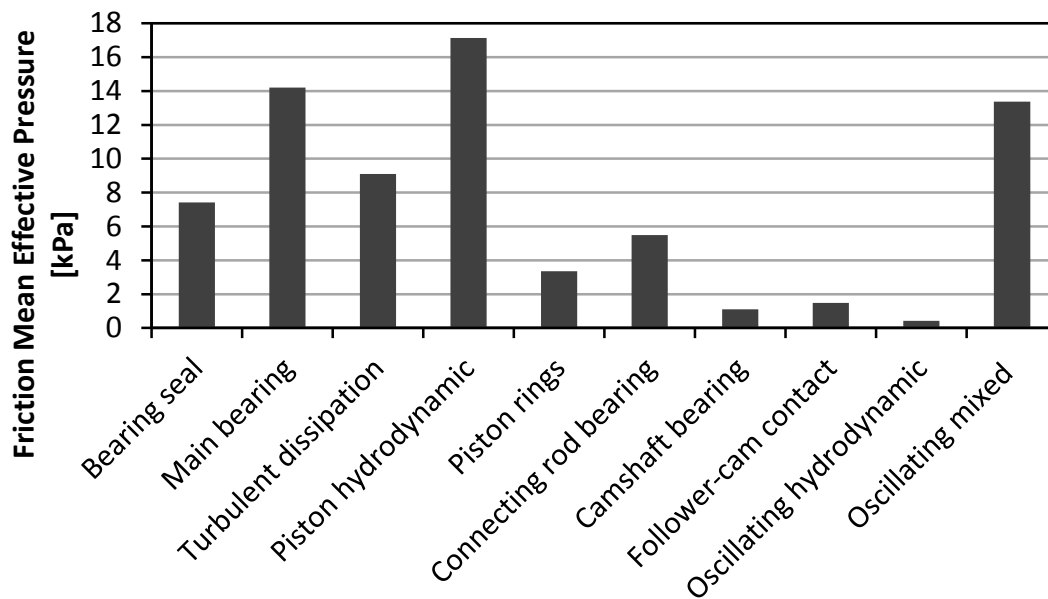
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Figure 18. Power of mechanical losses as a function of piston stroke

580 Figure 19 shows the calculated friction mean effective pressure (fmep) for each
 581 component from the equations for a piston stroke 80 mm. The equations for calculation
 582 of each component were taken from the literature [35]. Total calculated fmep was 68.67
 583 kPa. This friction mean effective pressure produces a calculated power of mechanical
 584 losses of 1445 W. This power represents 40.59% of the energy generated by positive work
 585 loop for the reference model (3560 W for the model with reed valve and without heat
 586 transfer). These high mechanical losses would waste almost all the power obtained by the
 587 indicated cycle (1662 W obtained by the model with heat transfer).

588 It can be seen that piston hydrodynamic friction, friction in main bearings and
 589 mixed friction in the valvetrain represent the most significant losses. These are the main
 590 losses that should be addressed in order to reduce the total mechanical losses.



591
 592 Figure 19. Friction mean effective pressure of each machine component; Stroke
 593 80 mm

594 *3.4 Indirect losses*

595 *Exhaust backpressure pumping losses*

596 By considering the heat transferred through the heat exchanger in the model,
 597 temperatures and pressures at the inlet and the outlet of heat exchanger in the gas side can
 598 be estimated. By using these values, mean gas density was then calculated to be $\rho=0.439$
 599 kg/m^3 and pressure drop $\Delta p=1.45$ kPa was calculated from the heat exchanger model.
 600 Power loss was calculated to be approximately 89 W.

601 *Additional weight*

602 Waste heat recovery system is composed of two main parts: heat exchanger and
 603 compression-expansion piston machine. Apart from these two main elements other
 604 possible components that could increase the vehicle weight could be: tubes that connect
 605 the heat exchanger and piston machine, control system, clutch to detach the machine from
 606 the engine when the machine cannot produce power, pulleys and belt or other system to

607 connect the machine with the engine etc. Nevertheless, probably the biggest part of the
 608 system weight goes on two main components. Heat exchanger prototype exists so it was
 609 possible to measure its weight. The heat exchanger that was used in this study weighted
 610 10 kg. It should be noted that this is a prototype of the heat exchanger and it is reasonable
 611 to believe that a production version would be lighter. As no prototype of the piston
 612 machine was made, its weight had to be estimated. The weight of several aluminium
 613 internal combustion engines with different displacement and cylinder number was used
 614 to estimate the weight per volume ratio of these engines. The engines that were used as a
 615 sample were: 1 cylinder 600 cm³ motorcycle engine, 10 cylinder 5000 cm³ car engine and
 616 4 cylinder 2000 cm³ car engine. They weight per displaced volume ratio was in the range
 617 45-48 kg/dm³. As displaced volume of the WHR machine is 0.936 dm³ for the 80 mm
 618 stroke, machine weight was estimated at 43 kg. As a first approximation, the total WHR
 619 system weight was estimated at 55 kg.

620 Ford Mondeo was used as an example of the vehicle. Parameters that are needed
 621 for calculation of additional engine power due to the weigh increment are given in Table
 622 5.

Parameter	Value
f	0.01
η_{TR}	0.9
v_{veh} [km/h]	120

623 Table 5. Parameters for calculation of engine power to compensate vehicle
 624 weight

625 It was estimated that engine has to make 200 W more to compensate the additional
 626 weight.

627 4 Results

628 The summary of the proposed system positive and negative contributions is
 629 represented in Application of the WHR in a passenger car is limited by available space,
 630 regulations that prevent use of certain fluids and cost. For these reasons, Brayton cycle
 631 seems as a promising solution because it offers compact and simple system with lower
 632 costs that uses air as a working fluid. Additionally, a volumetric compression-expansion
 633 machine has been considered for the cycle increasing the compactness and the simplicity
 634 of the proposed system. Although it seems as a promising solution it was not much studied
 635 in the scientific circles. This lack of publications and mentioned advantages of the system
 636 were the main motivation for this study. However, the results of this study show that
 637 practical realisation of the cycle is not very viable because the system would probably
 638 work only in the engine operating points with high exhaust gas energy, .such as highway
 639 driving, Even then the recuperated power would be too small to justify the complexity
 640 and additional cost of the system.

641 . It is evident that losses overcome the cycle positive work. As can be seen in this
 642 table, the power obtained from the positive work loop is totally cancelled by the power
 643 losses of the considered sources. In order to design a viable system, high pressure

644 pumping losses, mechanical losses and heat losses must be reduced as these phenomena
 645 are responsible for most of WHR system losses.

	Contribution	Power [W]	Percentage with respect to positive loop [%]	Percentage with respect to available heat power [%]
Positive	Positive work loop; 0D model without heat transfer with reed valve as HP outlet valve	+3560	+100	+18.4
Negative	HP negative work loop	-1032	-29	-5.3
	LP negative work loop	-142	-4	-0.7
	Heat transfer losses	-724	-20.3	-3.7
	Mechanical losses	-1445	-40.6	-7.5
Recovered Mechanical Power		217	+6.1	+1.1
Indirect losses	Additional back pressure	-89	-2.5	-0.5
	Additional weight	-200	-5.6	-1

646 Table 6. Cycle power summary

647 By considering the indicated power, 3560 W are recuperated in the ideal positive
 648 work loop. It means an 18% of the total heat power available in the exhaust gasses. This
 649 percentage is much related to the heat transfer efficiency of the heat exchanger. The heat
 650 exchanger model validation was done by tests performed at constant air mass flow while
 651 the air flow in the alternating piston machine is very pulsating. Pulsating flow could be
 652 important for the heat transfer. Many researchers investigated the effect of pulsation on
 653 heat transfer. Different studies [37–39] showed that, depending on conditions, pulsating
 654 flow could increase the heat transfer coefficient compared to constant flow. Heat
 655 exchanger efficiency directly affects the recuperated power so it is very important to have
 656 a good design of this element to improve its efficiency.

657 On the other hand, 1032 W (29% of the positive work loop power) are lost in the
 658 HP negative loop, 142 W (4% of the positive work loop power) are lost in the LP negative
 659 loop and 724 W (20.3% of the positive work loop power) are lost due to heat losses in the
 660 expander. It means that by considering positive and negative loops and expander heat
 661 losses, the power recuperated by the reed valve compression-expansion machine is
 662 estimated to 1662 W. Considering these values, the highest contribution to the expander
 663 power loss comes from the HP negative loop. In order to reduce this loss, other valve
 664 characteristics with higher effective areas should be considered in order to reduce the
 665 power loss produced during the breathing process of the machine.

666 The model of mechanical losses estimates that 1445 W of crankshaft power
 667 (40.6% of the positive work loop power) would be spent on friction. This amount of
 668 mechanical losses would effectively make the cycle non-viable, as it uses almost all the
 669 recuperated power that was left after applying the heat transfer model. The model of
 670 mechanical losses used empirical equations that were obtained from the measurements of
 671 mechanical losses in internal combustion engines. As in the Brayton cycle machine there

672 is no combustion, pressures are much lower than in the ICE. Thereby, stress on the
673 machine parts is much lower. Machine parts that would be less loaded are primarily
674 piston, piston rings, connecting rod, connecting rod bearings, crankshaft and crankshaft
675 bearings. A big part of mechanical losses comes exactly from those parts. Piston
676 hydrodynamic friction losses and friction losses in the main bearings make for almost
677 42% of all mechanical losses. If piston and main bearings are dimensioned lighter, it is
678 reasonable to believe that mechanical losses could be less than what was estimated by the
679 model that was fitted with the ICE experimental values. Considering all these
680 contributions, positive and negative loops, heat transfer losses and mechanical losses, the
681 total recovered mechanical power in the compression-expansion machine is reduced to
682 217 W. It means only 1.1% of the total heat power available in the exhaust gasses.

683 Finally, other indirect power losses, external to the volumetric machine, such as
684 the additional back pressure in the exhaust line introduced by the heat exchanger or the
685 additional weight of the Brayton cycle have been considered. They have a lower
686 contribution to the global power losses but they will produce an unviable system for the
687 waste heat recovery system, cancelling out all the power obtained from the volumetric
688 machine, as Table 6 shows.

689 **5 Conclusions**

690 Application of the WHR in a passenger car is limited by available space,
691 regulations that prevent use of certain fluids and cost. For these reasons, Brayton cycle
692 seems as a promising solution because it offers compact and simple system with lower
693 costs that uses air as a working fluid. Additionally, a volumetric compression-expansion
694 machine has been considered for the cycle increasing the compactness and the simplicity
695 of the proposed system. Although it seems as a promising solution it was not much studied
696 in the scientific circles. This lack of publications and mentioned advantages of the system
697 were the main motivation for this study. However, the results of this study show that
698 practical realisation of the cycle is not very viable because the system would probably
699 work only in the engine operating points with high exhaust gas energy, .such as highway
700 driving, Even then the recuperated power would be too small to justify the complexity
701 and additional cost of the system.

702 Considering the results summarized in Table 6, it seems hard to imagine that the
703 proposed cycle could be made viable. Nevertheless, some power losses sources of the
704 Brayton cycle system were identified as the most important losses sources and they
705 deserve further study. These power losses sources are the efficiency of the heat exchanger,
706 the HP negative loop and the mechanical losses of the compression-expansion machine.
707 Regarding the efficiency of the heat exchanger and also thermodynamic irreversibilities,
708 only 18% of the total heat power available in the exhaust gasses is recuperated in the
709 positive work loop of the machine. A redesign of this heat exchanger in order to improve
710 its efficiency is mandatory to increase this value. Regarding the HP negative loop power
711 losses, they represent 29% of the recovered power in the positive work loop of the
712 machine. They are produced due to the short time for the air movement between the
713 volumetric machine and the heat exchanger. To improve this value, a redesign of the valve
714 system should be considered in order to increase the effective area of these valves to
715 improve this process. Finally, the mechanical losses of the machine represent 40.6% of
716 the recovered power in the positive work loop of the machine. In order to reduce this

717 value, a redesign of the lubrication system should be considered to reduce the mechanical
718 losses of the machine.
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