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Additional Information

MPC for optimal dispatch of an AC-linked hybrid PV/wind/biomass/H₂ system incorporating demand response.

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Summary.

A Model Predictive Control (MPC) strategy based on the Evolutionary Algorithms (EA) is proposed for the optimal dispatch of renewable generation units and demand response in a grid-tied hybrid system. The generating system is based on the experimental setup installed in a Distributed Energy Resources Laboratory (LabDER), which includes an AC micro-grid with small scale PV/Wind/Biomass systems. Energy storage is by lead-acid batteries and an H₂ system (electrolyzer, H₂ cylinders and Fuel Cell). The energy demand is residential in nature, consisting of a base load plus others that can be disconnected or moved to other times of the day within a demand response program. Based on the experimental data from each of the LabDER renewable generation and storage systems, a micro-grid operating model was developed in MATLAB[®] to simulate energy flows and their interaction with the grid. The proposed optimization algorithm seeks the minimum hourly cost of the energy consumed by the demand and the maximum use of renewable resources, using the minimum computational resources. The simulation results of the experimental micro-grid are given with seasonal data and the benefits of using the algorithm are pointed out.

Keywords.

Model Predictive Control, Genetic Algorithm, Hybrid energy systems, Micro-grids

33 **1. Introduction.**

34 Increasing awareness of the impact of conventional energy generating systems on
35 sustainability, the frequent incorporation of public policies for integrating renewable
36 sources in the energy generation matrix, and the development of increasingly affordable
37 small-scale distributed generation technology [1] are all factors that have led to the growth
38 in the use of small hybrid generating systems for residential use. These systems use
39 renewable energies to reduce the local demand on the public grid and can stay connected
40 to act as a backup when renewable energy is generated. The grid can also be used to
41 maintain reference voltages and frequency and any power surplus produced by the micro-
42 grid can be sold off. The development of regulatory schemes in the small-scale consumer
43 market, which allow for hourly price differentiation, gives the option of a hybrid
44 generating system to small residential consumers and opens up the possibility of
45 importing or exporting energy from/to the grid according to hourly prices and the energy
46 resources available.

47 In this type of project, the capital, operating, maintenance and replacements costs, in
48 relation to the power consumed, should result in a lower price than the electrical energy
49 tariff of a final consumer. These benefits must be maintained throughout the lifetime of
50 the installation in order to recover the investment and to consume the lowest amount of
51 energy from the grid [2].

52 As neither solar nor wind energy are dispatchable resources, one or more storage systems
53 are necessary to provide a reliable energy system, and since a wide range of different
54 elements may be involved, these systems must be optimized in order to achieve technical
55 and economic feasibility.

56 Considering the small margin between the levelized cost of electricity – LCOE and the
57 hourly final consumer grid tariff, the energy supply and demand in the micro-grid must
58 be carefully managed. This margin is the factor which determines whether the power
59 supply is bought from the grid or consumed from the micro-grid's renewable resources.

60 A number of studies have been published recently on the optimization of micro-grid
61 systems [3] or hybrid energy generation systems. In [4], different analysis software tools
62 for hybrid systems are described. However, in the literature, optimization is usually
63 achieved by considering the dimensioning of the PV-Wind-Battery off-grid hybrid system
64 [5], dimensioning plus a hydrogen storage system [6], genetic algorithms [7,8] or
65 comparing the new algorithms with classical techniques [9,10]. The optimization
66 parameters do not always reduce costs, but may deal with the maximum allowable loss
67 of supply probability LPSP [11] or even social-environmental aspects as well as
68 technical-economic aspects [12]. In [13,14], genetic algorithms are used to dimension an
69 isolated system using hydrogen for energy storage.

70 However, genetic algorithms are not only used in isolated systems to optimize the design.
71 In [15] the Particle Swarm Optimization algorithm is used to dimension a tie-grid hybrid
72 system including different renewable energy sources (PV, Wind, Solar Heat, Biomass).

73 Apart from dimensioning, these algorithms have also been used to control energy flow in
74 tie-grid hybrid systems. In some cases these are simple hybrid systems composed of PV
75 and batteries [16], while others include wind energy and hydrogen [17] or simply demand
76 response [18]. The flexibility of genetic algorithms thus makes it possible to achieve a
77 number of different objectives, including economic and environmental, using a hybrid
78 algorithm in a tie-grid system consisting of photovoltaics, batteries and a fuel cell

79 powered by natural gas [19]. Daily operation is a simple tie-grid hybrid system (PV, wind,
80 batteries and diesel) that is cost optimized by the predictive control algorithms in [20] to
81 improve the system behavior when under the conventional “load following” strategy. The
82 improvements have been reported to reach 36%.

83 This paper proposes a supervisory control that schedules daily inputs to be implemented
84 in the system. When possible, the controller decides the power to be delivered from the
85 generation subsystems (i.e. biomass and fuel cell), while also programming how the loads
86 specified in the demand response program will be met.

87 In order to decide the inputs (power generation and demand response program loads), the
88 controller simulates the system to predict the consequences of these actions and measure
89 the system performance by an index including the overall cost. The best control action
90 will thus be the one that achieves the best score. This control method is known as the
91 model predictive control (MPC).

92 The MPC optimization procedure is closely related to the definition of the model to be
93 simulated [21]. Although conventional optimization techniques (linear programming) can
94 be used to optimize the controller, these methods are not effective on complex models. In
95 these cases [22], metaheuristic optimization can be used to search for the optimal solution.
96 In [23] a MPC approach is used to optimize the management of a hybrid PV-Wind-
97 Batteries system. The goal is to achieve high profitability by selling energy from
98 renewable sources to the grid. The MPC algorithm is used to forecast the price of the
99 energy hour by hour and to decide if the energy is stored or sold. In [24] a MPC algorithm
100 is used to optimize the hydrogen production via anaerobic fermentation of glucose in a
101 hybrid system PV-Wind-Hydrogen.

102 This study used a metaheuristic optimization procedure based on an Evolutionary
103 Algorithm (EA). EAs are algorithms that simulate the biological evolution of a species so
104 that each proposed solution evolves and improves on a previous set of possible solutions
105 [25]. Several modern EAs can be used to search for the best solution of the MPC problem
106 [26,27]. The particle swarm optimization (PSO) algorithm used in the present study has
107 been shown to perform well in identification applications [28].

108 The micro-grid is based on the Distributed Energy Resources Laboratory (LabDER,
109 IUIIE, *Universitat Politècnica de València*) generation and energy storage equipment.
110 The design of this existing generating system is not described here. The proposed tool
111 uses the forecast weather variables and hourly energy prices to the final consumer to
112 program the next day’s dispatchable generation and switchable loads.

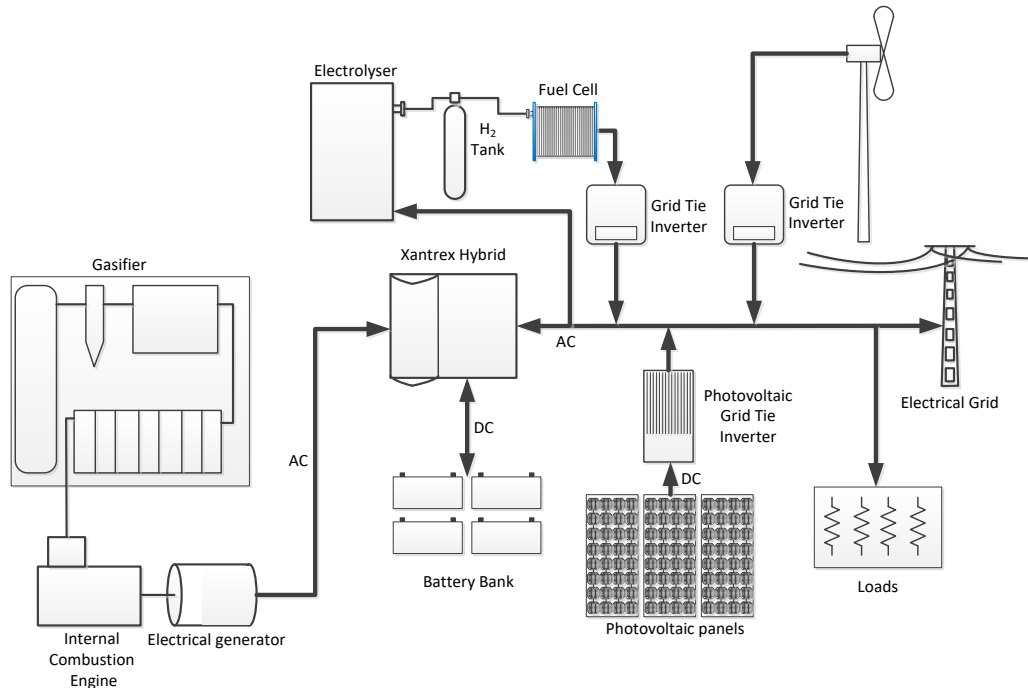
113 The paper is organized as follows: Section 2 describes the overall system and how the
114 mathematical model of each generating element was obtained. The energy management
115 system is described in Section 3. Section 4 explains the design of the genetic algorithm
116 and specifies the scenarios to be simulated. Section 5 gives the results obtained from the
117 different client configurations (3, 5 or 7 households), while our conclusions are given in
118 Section 6.

119

120 **2. System components, characteristics and models.**

121 The LabDER's experimental micro-grid has four solar, wind, biomass and hydrogen
122 renewable energy systems, in addition to batteries, hydrogen bottles and dry biomass fuel.
123 This hybrid generating system can operate in isolation, interconnected to feed a

124 programmable load or deliver power to the grid. It also has a Supervisory Control and
 125 Data Acquisition (SCADA) management and control system to monitor the available
 126 energy resources and generation mix, as well as directing energy in any direction from or
 127 to the storage systems, to the load or the public grid. Figure 1 shows a diagram of the
 128 LabDER system, with the current configuration in terms of components and connections.
 129 A more detailed description of this micro-grid can be found in [29,30].



130
 131 **FIGURE 1** Diagram of LabDER configuration.

132
 133 An operating model was developed to simulate the integrated energy balance of a real
 134 interconnected micro-grid for residential consumers. The components of the experimental
 135 micro-grid, its characteristics, modeling, simulation and operating data are described
 136 below.

137
 138 **2.1 Photovoltaic system.**

139 The PV System consists of 11 modules of three different specifications. All modules are
 140 connected in series for academic and experimental purposes. The PV array is composed
 141 of 4 Zhejiang Wanxiang Solar WSX180 modules of Si Monocrystalline (180 Wp), 5 Rec
 142 Solar 230AE Modules of Si Polycrystalline (230 Wp) and 2 USL Photovoltaics USP145
 143 Modules of Si Polycrystalline (145 Wp). Therefore, the total installed peak power is 2160
 144 W. This energy flows to a Xantrex GT 2.5-DE (2.5 kW) tie inverter connected to a
 145 common single-phase AC bus.

146 The mathematical model of each PV module was developed from its equivalent circuit,
 147 as shown in Figure 2. The model parameters from A. Bellini et al. [31] together with the
 148 modifications proposed by A. Hadj Arab et al. [32] and M. Villalba et al. [33] were used
 149 in (1) to establish the parameters of the equivalent circuit.

$$I_P = I_{SC} \left[1 - C_1 \left(e^{\left(\frac{V_P}{C_2 V_{OC}} \right)} - 1 \right) \right] \quad (1)$$

where

$$C_1 = \left(1 - \frac{I_{MPPS}}{I_{SCS}} \right) \cdot e^{\left(\frac{-V_{MPPS}}{C_2 V_{OCS}} \right)} \quad \text{and,} \quad C_2 = \frac{\left(\frac{V_{MPPS}}{V_{OCS}} - 1 \right)}{\ln \left(1 - \frac{I_{MPPS}}{I_{SCS}} \right)} \quad (2)$$

Coefficients C_1 and C_2 depend on parameters defined in standard conditions of irradiance and temperature ($G_S=1000\text{W/m}^2$ and $T_S=25^\circ\text{C}$) such as: short circuit current I_{SCS} , open circuit voltage V_{OCS} , maximum power point voltage V_{MPPS} and maximum power point current I_{MPPS} . Appendix 1 explains how the parameters were calculated in other operational conditions.

The equivalent circuits of each module were connected in series and the total voltage and current of the photovoltaic array V_{array} and I_{array} were determined. The power of the PV system is calculated by Eq.(3).

$$P_{PV} = V_{array} \cdot I_{array} \cdot \eta_{inv} \quad (3)$$

Figure 2 shows the equivalent circuit of a PV device and figure 3 compares the results obtained from the LabDER tests and those of the MATLAB[®] model. A root-mean-square error (RMSE) of 72.45W was obtained between the set of measurements and its corresponding result in the MATLAB[®] model.

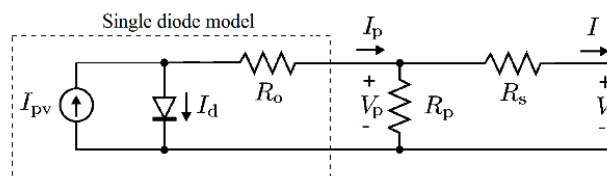


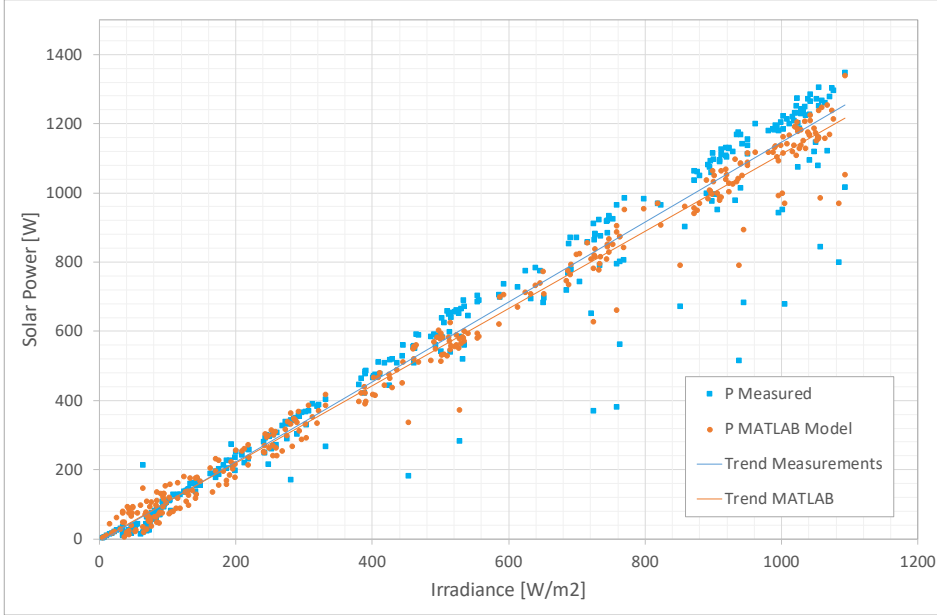
FIGURE 2 Single-diode model - Equivalent circuit of a practical PV device.

Table 1 shows the parameters in each of the three solar module specifications and the result of the coefficients C_1 and C_2 .

TABLE 1 Characteristics and parameters of the PV array modules.

	Zhejiang Wanxiang Solar	Rec Solar	USL Photovoltaics
Model	WSX180	230AE	USP 145
Number of Modules	4	5	2
Type	Monocrystalline	Polycrystalline	Polycrystalline
Maximum Power	180 W	230 W	145 W
Maximum Power Voltage	35.36 V	29.0 V	33.5 V
Maximum Power Current	4.79 A	8.0 A	4.57 A
Open Circuit Voltage	43.88 V	36.9 V	42.7 A
Short Circuit Current	5.18 A	8.6 A	5.03 A
C_1	1.64029×10^{-6}	1.83985×10^{-7}	1.50857×10^{-5}
C_2	0.07507	0.06448	0.09007

178
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FIGURE 3 Comparison between the Power from the PV Array obtained by MATLAB model and real data.

186 2.2 Wind system.

187 The wind system consists of an Anelion SW 3.5-GT 3-bladed wind turbine with a rotor
 188 diameter of 3.5 m and a nominal capacity of 4000 W and a tower height of 21 m. The AC
 189 voltage (up to 400 Vrms) is connected to a rectifier that delivers a DC signal to a Grid-
 190 tied SMA Windy Boy WB2500 inverter connected to the single-phase AC bus.

191 For modeling purposes, the power curve provided by the wind turbine manufacturer,
 192 applying Hellmann's exponential law, was used to correct the wind speed at the wind
 193 turbine hub as expressed in Eq.(4).

$$194 \quad v = v_0 \left(\frac{H}{H_0} \right)^\gamma \quad (4)$$

195

196 where v is the speed to the height H , v_0 is the speed to the height H_0 (frequently referred
 197 to as 10-m) and γ is the friction coefficient or Hellman exponent.

198 A curve adjustment was made using the “pchip” function (Piecewise Cubic Hermite
 199 Interpolating Polynomial) as proposed by Lydia et al. [34]. A power adjustment was also
 200 applied due to the effect of air density at different heights. The expression for output
 201 power of a wind turbine can be related to wind speed by Eq.(5).
 202

203

$$204 \quad P_w = \begin{cases} 0, & v < v_{ci} \text{ or } v \geq v_{co} \\ P_{w-adj} \cdot CF_{dens-temp} \cdot \eta_{inv}, & v_{ci} \leq v < v_{co} \end{cases} \quad (5)$$

205

206

207 where v_{ci} , v_{co} and v are cut-in, cut-off and wind speed adjusted for Hellmann’s law,
208 respectively. P_{W-adj} is the final wind power output in the common single-phase AC bus
209 obtained by the pchip MATLAB[®] function and adjusted to wind speed v , $C_{Fdens-temp}$ is a
210 correction factor for density and temperature effect and η_{inv} is the inverter efficiency.
211 Table 2 shows the wind system parameters.

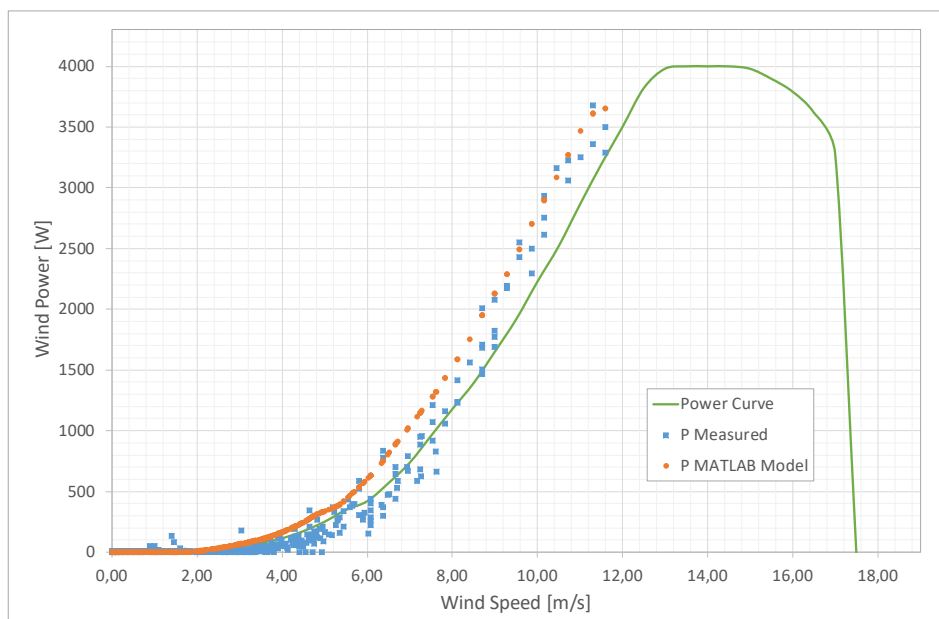
212 **TABLE 2** Wind Energy System – Turbine and grid-tie inverter features.

Anelion Wind Turbine	
Model	SW 3.5-GT
Rated Power Output	4 kW
Type	3 blades, horizontal axis
Generator	Direct Drive PMSG
Swept Area	9.62 m ²
Rated Wind Speed	12 m/s
Start-up Wind Speed	3.5 m/s
Survival Wind Speed	17,5 m/s
Voltage/Phase	400 Vrms
Current/Phase	20 Arms
SMA Grid-tie Inverter	
Model	Windy Boy WB2500
Input Voltage Range	224 – 600 V _{DC}
Maximum Input Power	2700 W
Maximum Input Current	12 A _{DC}
Nominal Output Peak Power	2500 W
Nominal Output Current	9.6 Arms
Operating Range Grid Voltage	180 – 265 V _{AC}
Operating Range Grid Frequency	45.5 – 54.5 Hz

213

214

215 Figure 4 compares the results obtained from the LabDER tests and the simulations of the
216 MATLAB[®] model. The real data was different from the manufacturer’s curve and our
217 model fitted the real behavior instead of the nominal behavior in the datasheet. The RMSE
218 obtained between the set of measurements and its corresponding result in the MATLAB[®]
219 model was 140.5W.



220

221 **FIGURE 4** Comparison of the power from the wind turbine obtained by MATLAB model and real
 222 operation (continuous line shows the manufacturer curve).

223 **2.3 Biomass system.**

224 This system consists of a gasification plant and a generator set connected to the common
 225 single-phase AC bus with a maximum power of 10 kW, producing a synthesis gas at a
 226 flow of 27 to 33 Nm³/h which is burned in an internal combustion engine. To optimize
 227 operations its daily generation schedule in a real application must be planned. The FG
 228 Wilson UG14P1 generating set consists of a 1.8 litre HM natural gas engine, adapted to
 229 burn syngas and a Leroy Somer LUA1014NX 10 kW synchronous generator. This
 230 adaptation changes the performance of the generating system to an electrical generating
 231 capacity of 8.7 kW. Table 3 summarizes the main parameters of the biomass generation
 232 system.

233 **TABLE 3** Gasification power plant features.

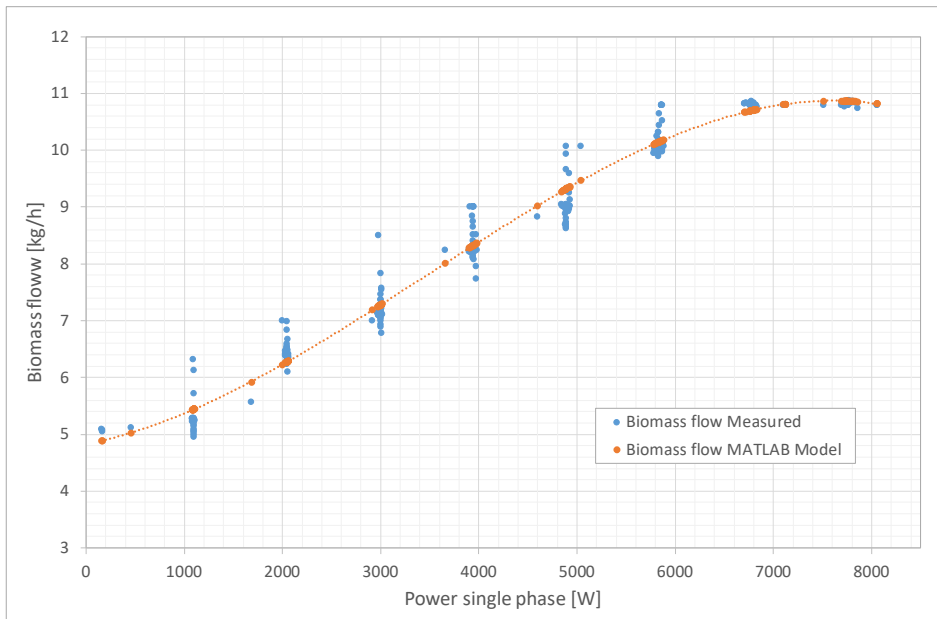
Biomass Gasification Reactor	
Type	Bubbling fluidized bed
Biomass reactor dimensions	Diameter: 106 mm, Height: 155 mm
Fuel type	Wood chips (10 - 15 mm maximum length) Pellets (diameter 6 mm, 15 - 25 mm length)
Biomass hopper capacity	237.1 (up to 166 kg of biomass)
Biomass input (@ 10%	6 – 13 kg/h 30 - 60 kWt (referred to higher heating value)
Syngas production	13 – 33 Nm ³ /h
Syngas higher heating value	5 – 5.8 MJ/Nm ³
Global efficiency	14 – 20%
FG Wilson Generator Set	
Model	UG14p1
Cylinder capacity	1.8 L
Engine velocity	1500 rpm
Compression ratio	8.5:1
Fuel Consumption	2475 m ³ /h (Gas Natural) 7.5 kg/h (Syngas)
Rated Electric Power	10 kW (Gas Natural) 8.7 kW (Syngas)
Voltage and Frequency	220/240 V _{AC} & 50 Hz

234
 235 The energy balance equations of the model can be entered in the MATLAB model based
 236 on Vargas's proposal [35] and applied to the economic analysis by Montouri [36] from
 237 efficiency curves. The curve fit was based on the experimental results (Eq. (6)).

238
 239
$$Q_{Bio} = -21.577 \times 10^{-12} P_{Gasif}^3 + 223.972 \times 10^{-9} P_{Gasif}^2 + 339.382 \times 10^{-6} P_{Gasif} + 4.8264 \quad (6)$$

240
 241 where Q_{Bio} is the biomass flow into the gasifier and P_{Gasif} is the active power in the
 242 common single-phase AC bus.

243 Since the gasifier produces dispatchable energy, the input argument for the function is in
 244 this case the power on the single-phase AC side. Figure 5 shows the comparison between
 245 the results obtained from the LabDER tests and the MATLAB[®] simulations. As expected,
 246 the simulated data fitted perfectly with the experimental data; in this case, the RMSE
 247 obtained between the set of measurements and its corresponding result in the MATLAB[®]
 248 model was 0.28 kg/h.



250

251 **FIGURE 5** Comparison between the Power from the Gasifier obtained by MATLAB model and real
 252 operation.

253

254 2.4 Hydrogen system

255 This system consists of an electrolyzer, a compressor, a bottle of H₂ and a PEM (Proton
 256 Exchange Membrane) fuel cell. Its main purpose is to absorb excess energy and then
 257 store it in the form of hydrogen.

258 An Erre Due G2.0 electrolyzer is used to produce H₂ with a maximum production capacity
 259 of 1.33 Nm³/h at a pressure of 4 bar. For its operation, it requires a three-phase power
 260 supply with a nominal electrical power of 7.2 kW. At present, the electrolyzer is
 261 connected to the grid, but for the purposes of the hydrogen system described above, a
 262 single-phase AC-DC-AC three-phase converter is proposed in the model to allow excess
 263 energy to be used in the common single-phase AC bus. Hydrogen is compressed to 200
 264 bar in the bottle. Table 4 shows the principal characteristics of the hydrogen energy
 265 system.

266

267

TABLE 4. Hydrogen Energy System – Electrolyzer and Fuel Cell Stack.

Erre Due Electrolyzer	
Model	ED-G2.0
Rated Power	7,2 kW
Electric Power Suply	3x400 V + N & 50 Hz
Hydrogen Production	1.33 Nm ³ /h
Oxygen Production	0.66 Nm ³ /h
Deionized Water Consumption	1.2 l/h
Hydrogen Purity	99.3 – 99.8%
Hydrogen Purity	98.5 – 99.5%
Ballard Fuel Cell Stack	
Model	Nexa 1200
Type	PEM
Rated Power	1200 W
Rated Current	52 A _{DC}

Output Voltage (unregulated)	20 – 36 V _{DC}
Operating Temperature	5 – 35°C
Hydrogen Quality	4.0 (99.99 % or better)
Hydrogen Consumption	15 Slpm (at rated output)
Air Consumption	335 m ³ /h (at rated output, 30 °C ambient temperature)

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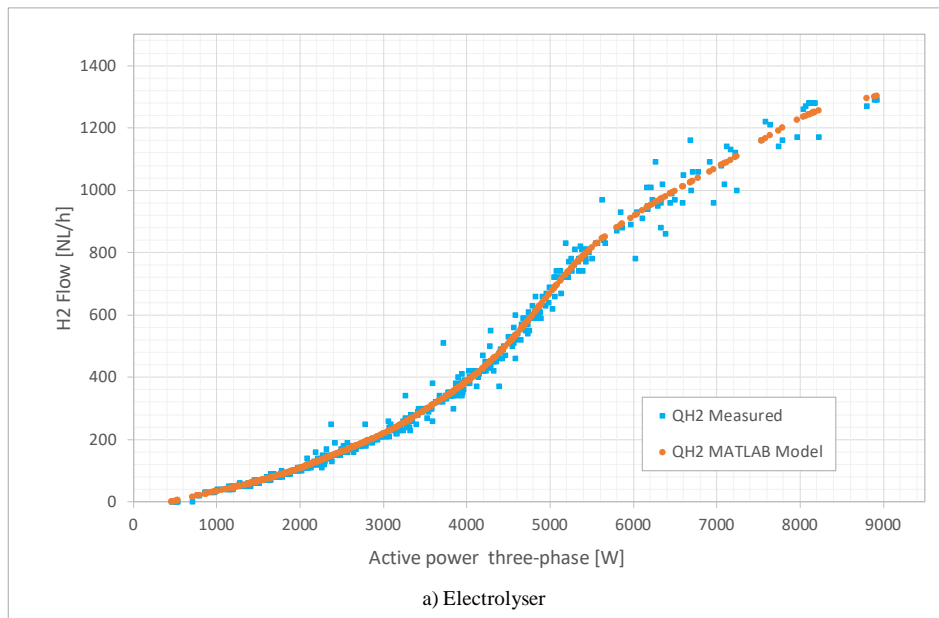
270 For the MATLAB[®] simulation a function was developed from the curve fit with
271 experimental data using Smoothing Spline, where $f(x)$ is a piecewise polynomial
272 computed from $p=4.7396674 \times 10^{-9}$ as a smoothing parameter. Figure 6 (a) shows the
273 hydrogen production obtained from the LabDER tests and the MATLAB[®] simulations.
274 The RMSE between the set of measurements and its corresponding result in the
275 MATLAB[®] model was 26.91 NL/h

276 The fuel cell system used in LabDER is a Ballard Nexa 1.2 kW commercial stack
277 producing up to 1200 W of unregulated DC power from a hydrogen and oxygen supply.
278 The fuel cell is electrically connected to the common single-phase AC bus via a 1200 W
279 pure sine wave inverter specifically designed for this application. For the MATLAB[®]
280 model a curve fit was performed with the experimental data (Eq. (7)).

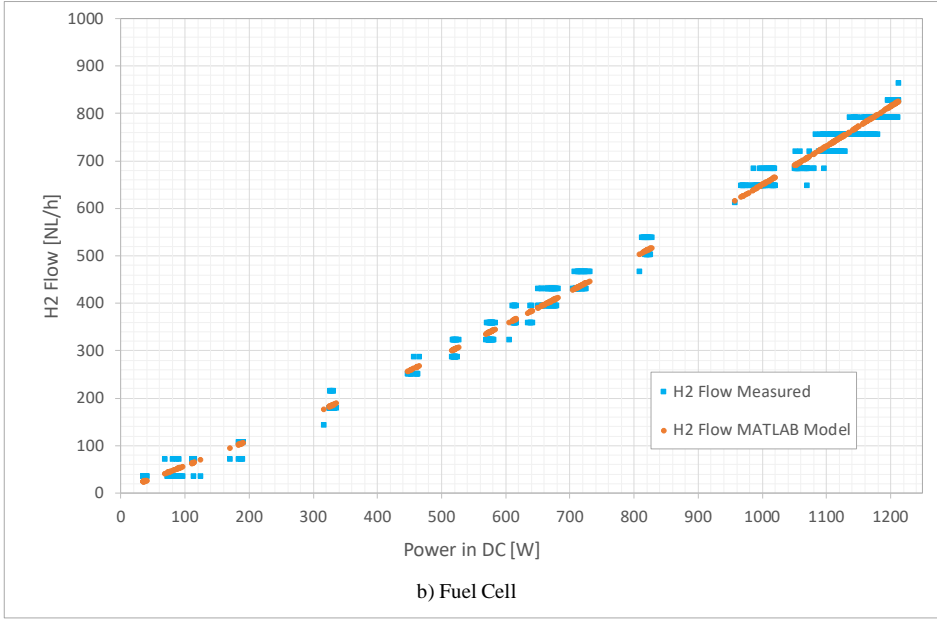
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283

$$QH2 = 42.199 \times 10^{-9} P_{FCdc}^2 + 136.454 \times 10^{-6} P_{FCdc} + 1.906 \times 10^{-3} \quad (7)$$

284 Where $QH2$ is the Hydrogen Flow from the bottle to the fuel cell and P_{FCdc} is the power
285 of the stack on the DC side. Figure 6 (b) compares the experimental results with the
286 MATLAB[®] model [37, 38]. The RMSE obtained between the set of measurements and
287 its corresponding result in the MATLAB[®] model was 18.47 NL/h.



288



289

290 **FIGURE 6** Comparison between the hydrogen production in the electrolyzer (a) and hydrogen consumed
 291 in the fuel cell (b) from real operational data and the MATLAB model.

292

293 **2.5 Batteries.**

294 The other storage system modeled was the battery bank, which is composed of four
 295 Saclima Power 250 12V 250 Ah C100 lead-acid Monoblock batteries connected in series,
 296 which supply a voltage of 48 VDC with a nominal capacity of 12000 Wh. The battery
 297 bank is connected to a XANTREX XW4548 inverter-charger and central micro grid
 298 controller, which allows maximum battery discharge of up to 40% of the nominal capacity
 299 to extend its service life.

300 The model developed in MATLAB[®] was based on the energy balance. To adjust the
 301 models, a test was carried out in which the batteries were charged by connecting them to
 302 the grid and discharged by controlled demand. Figure 7 shows the data from this
 303 experiment. The difference in the results is due to the data measurement: directly on the
 304 battery side in the real operation and in the common single-phase AC bus in the MATLAB
 305 model.

306 If the difference between the generated energy a demand is positive and the batteries have
 307 already been charged to 100% (State of Charge - SOC in the maximum value), this energy
 308 would be used to produce hydrogen in the electrolyzer, and any further excess is delivered
 309 to the electrical grid. If the difference is negative, the battery delivers its power to meet
 310 demand until its state of charge - SOC is the minimum set point; if the deficit persists,
 311 power will be imported from the grid. The equation (8) shows the above process,
 312 performing the power flow balance in the common single-phase AC bus.

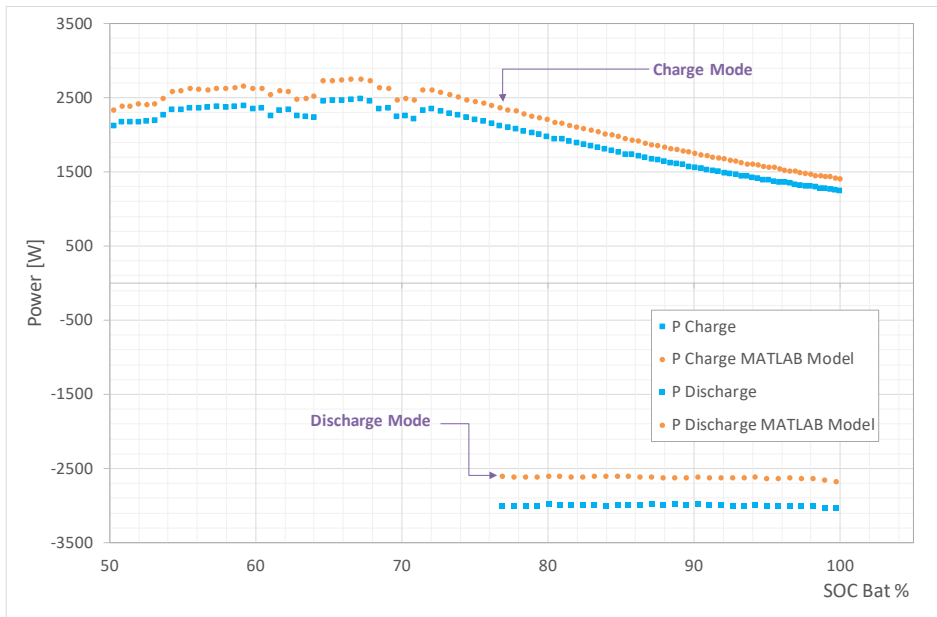
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314

$$315 P_{BAT} = \begin{cases} 0 & \text{if, } SOC = SOC_{MAX} \vee SOC < SOC_{MIN} \\ (P_{PV} + P_W + P_{Gasif}) - P_{LOAD} & \text{if, } SOC_{MIN} \leq SOC < SOC_{MAX} \end{cases} \quad (8)$$

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317



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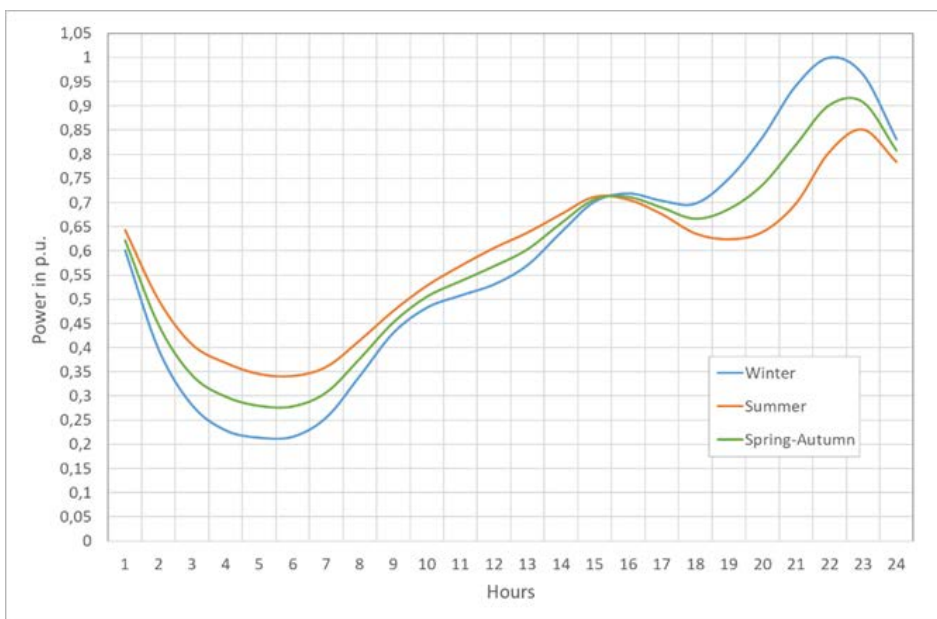
319 **FIGURE 7** Comparison of real battery operation and the MATLAB model.

320

321 **2.5 Loads.**

322 To model the load in the experimental micro-grid, a demand behavior was proposed as a
 323 function of a typical residential curve, which passes through 3 seasonal periods in the
 324 year: Winter, Summer and Spring-Autumn. Figure 8, shows the base demand curve of a
 325 household in "per unit" values (p.u.), from which it is possible to vary the maximum
 326 demand, add the number of households, consider randomness and take into account the
 327 effect of additional loads which are enrolled in a demand response program.

328



329

330 **FIGURE 8** Base load power (per unit)

331

332 The total power consumed by the demand can be expressed in Eq.(9) for each hour of the
 333 day.

$$334 \quad P_{LOAD} = (P_{pu} \cdot D_{MAX} \cdot N_H \cdot R) + P_{DR} = P_{BASE} + P_{DR} \quad (9)$$

337 P_{pu} is the hourly demand of one household in per unit, D_{MAX} is the maximum demand of
 338 one household, N_H is the number of households considered (from 1 to 20), R is a
 339 randomness factor calculated by Eq.(10) and P_{DR} is the sum of the power of the loads
 340 enrolled in the demand response program, which can be disconnected or moved to another
 341 time during the day.

$$342 \quad R = \frac{(100 + V_D) - ((100 + V_D) - (100 - V_D)) * rand}{100} \quad (10)$$

346 Where V_D is the percentage of the desired demand variation interval (usually between 0%
 347 and 15%) and $rand$ is a random number generated by the computer between 0 and 1.

348 Additional loads associated with a demand response program in 5 houses were
 349 considered. Loads were assumed to be part of the demand response program in 5 homes,
 350 plus a communal water pumping system to an overhead tank, whose power varies
 351 according to the number of homes (for 5 households the power is 2 HP for 2 hours of
 352 operation). Residential energy consumption habits of household users was taken into
 353 account to define the initial response demand program. One of the controller task is to
 354 locate these loads during the day in an optimal position under criteria of cost and energy
 355 availability. The loads registered for each household are shown in Table 5.

356

357 **TABLE 5** Characteristics of dispatchable loads.

Household/Load	Power [W]	Operating Time [h]	Initial Daily Timing [h]
1/Dishwasher	600	3	9:00 to 11:59
1/Charger electric vehicle	3375	3	22:00 to 24:59
2/ Pool treatment plant	2500	3	14:00 to 16:59
3/ Pool treatment plant	2000	3	15:00 to 17:59
3/Charger electric vehicle	1575	6	19:00 to 24:59
4/Dishwasher	800	3	10:00 to 12:59
5/Dishwasher	700	3	20:00 to 22:59
Water Pumping System	1755	2	10:00 to 11:00

358

359 The optimization process developed from the genetic algorithm will establish the best
 360 time for these loads to function, according to the minimum cost criterion given by hourly
 361 differentiated tariffs for these loads in the demand response program.

362

363 **3. Energy management modeling**

364 The micro-grid energy management problem has been addressed in recent publications.
 365 Nosratabi et al. [39] reviewed the concepts associated with the dispatch or generation
 366 programming and demand response in the micro-grid. Problems in programming the
 367 micro-grid resources are generally associated with factors such as the forecasting
 368 uncertainty of the input model variables, energy supply reliability, stability of the

369 electrical system (frequency control, voltage, reactive power, etc.), emissions and final
 370 user prices. The models proposed in [40-43] have the common characteristic of the
 371 hierarchical arrangement of the power flux addressed from the sources to the loads, the
 372 storage systems or the grid. The computational organization is divided into special
 373 modules for input information management, forecasting, operation, optimization and
 374 finally the response module. The sum of the power inputs for each hour of day is used at
 375 a common link point.

376 The individual models of the different LabDER systems were integrated in a MATLAB®
 377 operating model of the hybrid generation-storage-demand system. This model calculates
 378 the hourly balance of the power from every source (photovoltaic, wind, hydrogen and
 379 biomass and grid), considering the required storage or the energy available (battery state
 380 of charge and level of the hydrogen tank) to meet the demand. The model considers
 381 internal consumption (electrolyzer stand-by energy consumption and leakage) and grid
 382 exports. Energy management considers dispatchable power generation (gasifier and fuel
 383 cell) and the opportunity of load time shift or even load disconnection as demand
 384 response.

385 The reference of the hourly power balance of the integrated system is the common AC
 386 single-phase bus. Inputs are the power from: photovoltaic array P_{PV} ; wind turbine P_W ;
 387 gasifier generator P_{Gasif} ; fuel cell stack P_{FC} ; battery bank (when it discharges) $P_{BAT-disch}$;
 388 and grid power (when imported) $P_{Grid-in}$. The outputs include: electrolyzer consumption
 389 when producing hydrogen P_{ELY} ; power required to charge the batteries P_{BAT-ch} ; export
 390 energy to the grid $P_{Grid-out}$; power consumption due to the stand-by of the all systems,
 391 control systems and air compressor to manage the hydrogen booster $P_{Loss+SC}$; and finally,
 392 power required by the residential loads P_{LOAD} . This balance does not consider the power
 393 from the backup system, since it is only used in emergencies. The balance is shown in
 394 Eq.(11).

$$\begin{aligned}
 395 \quad & P_{PV} + P_W + P_{Gasif} + P_{FC} + P_{BAT-disch} + P_{Grid-in} = \\
 396 \quad & P_{ELY} + P_{BAT-ch} + P_{Grid-out} + P_{LOAD} + P_{LOSS+SC}
 \end{aligned} \tag{11}$$

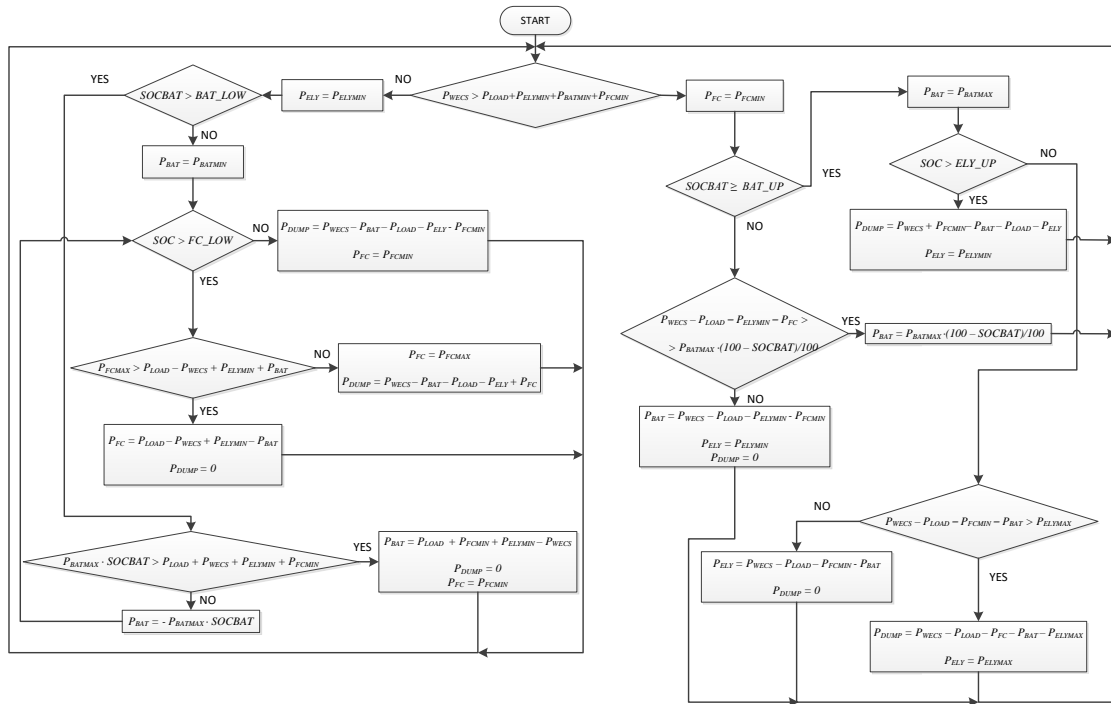
398 To achieve this balance, the MATLAB operational model reads three types of data from
 399 Excel tables: *i.* master control data, which comprises operation modes, equipment
 400 parameters and maximum and minimum operation; *ii.* hourly data on temperature,
 401 irradiance, wind speed, load demand and consumer prices of energy from the forecasting
 402 system; *iii.* generation schedule of gasifier and fuel cell, plus the loads that can be
 403 disconnected or shifted over time from the demand response program. In addition to
 404 applying (1), the model must take into account the priorities of the resources used and the
 405 destination of this energy. Figure 9 shows the energy management strategy of the pre-
 406 scheduled controller by the XANTREX XW4548 Hybrid Inverter and SCADA system.

407 The controller must first check whether the energy from the photovoltaics, wind turbine
 408 and gasifier generator P_{WECS} is enough to supply the load demand P_{LOAD} , the minimum
 409 power of the electrolyzer P_{ELYMIN} , the minimum power to charge the batteries P_{BATMIN} and
 410 the minimum energy to keep the fuel cell P_{FCMIN} operating, as shown in Eq. (12).

$$411 \quad P_{WECS} > P_{LOAD} + P_{ELYMIN} + P_{BATMIN} + P_{FCMIN} \tag{12}$$

412
 413 As pre-scheduled, surplus energy is distributed in the following order: first, all the energy
 414 is used to charge the batteries; if batteries are fully charged ($SOC_{BAT}=100\%$), energy
 415 surplus will be used to produce hydrogen if the tank is not full. Maximum and minimum

416 battery state of charge and hydrogen tank levels are strictly controlled. When all storage
 417 systems are full, the surplus energy is injected into the grid.
 418



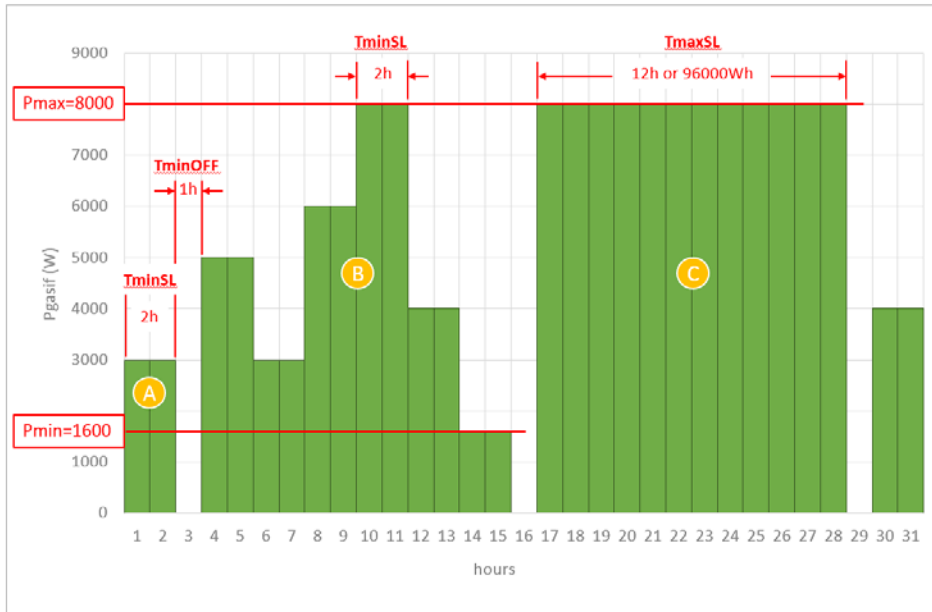
419
 420 **FIGURE 9** Energy management strategy of experimental micro-grid
 421

422 When the conditions in Eq. (12) are not met it will be necessary to use stored energy. In
 423 this case the order is in reverse, with a FIFO system (First In, First Out). When demand
 424 is greater than battery capacity or the batteries are low ($SOC_{BAT} = 40\%$), the fuel cell
 425 will supply the required energy from hydrogen. This situation will continue till maximum
 426 fuel cell power is achieved or the hydrogen tank is at minimum ($SOCH_2 = 10\%$). If
 427 batteries plus fuel cell cannot supply the load demand, energy will be taken from the grid.
 428 This hierarchy is based on the premise that batteries are considered a short-term storage
 429 element (due to the self-discharge coefficient) and hydrogen a long-term storage element
 430 (self-discharge coefficient zero).

431 There are two types of power generation in the proposed micro-grid operating model:
 432 non-dispatchable generation, depending on the availability of solar and wind resources,
 433 and dispatchable generation (FC and gasifier generator set), with the idea of satisfying
 434 the entire base load mainly from the gasifier. The nominal capacity of the gasifier is the
 435 largest of the LabDER's four generating systems.

436 As the gasifier system can reach maximum power (8000 W) from minimum (1600 W) in
 437 10 seconds, this time is not considered in the balance. The gasifier must be in continuous
 438 operation (at the same power output) for a minimum of 2 hours. The maximum capacity
 439 of the pellet hopper is 96000 Wh, so that when the hopper must be refilled, the gasifier
 440 stops for one hour. Figure 10 shows the restrictions of the gasifier system in terms of the
 441 electrical power delivered to the common single-phase AC bus.

442



443

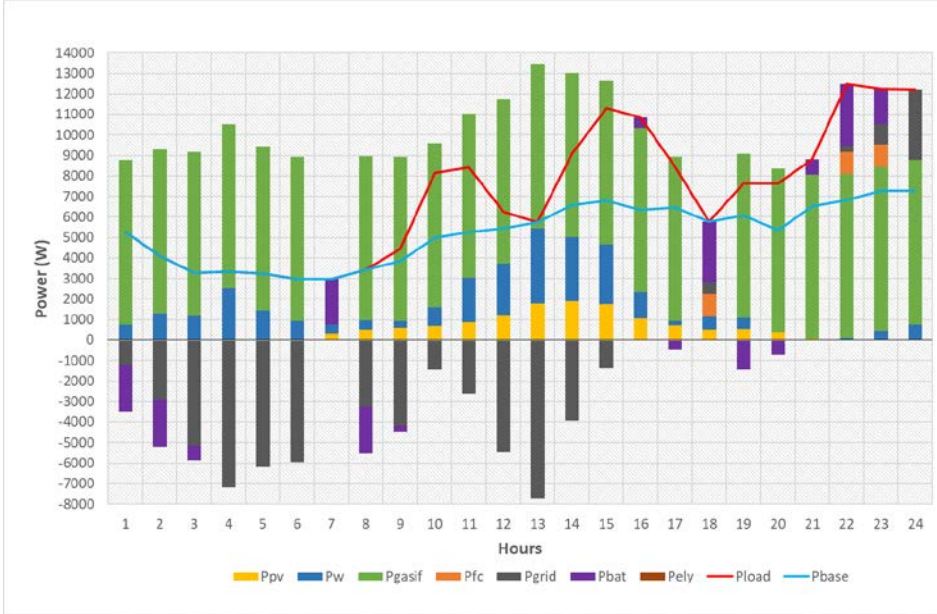
444 **FIGURE 10** Rules of gasifier system operation: A, minimum time of operation in stable load (2 hours); B,
 445 variation according to the demand (maximum 96000 Wh) and 1 hour to refuel; C, maximum time at stable
 446 load in maximum power.

447 The operating model does not perform any optimization process in terms of the dispatch
 448 of the generating systems, it simply performs the hourly energy balance according to the
 449 order and rules described in Figure 9, delivering excess energy to the grid or requesting
 450 energy from it in the event of a deficit. Likewise, the 24-hour timing of the loads subject
 451 to the demand response program is initially based on typical household loads.

452 The micro-grid operating model starts from an initial dispatch from the gasifier and fuel
 453 cell, as well as from the daily timing of the loads subject to the demand response program.
 454 In this sense, the gasification system's operating strategy is to deliver the maximum
 455 possible power (8000 W) while complying with the maximum stable load operating time
 456 ($T_{maxSL}=12$ hours) and the rules given in Figure 10, since the gasification system is
 457 assumed to be at maximum efficiency.

458 In the case of the FC, the initial dispatch delivers 1100 W during 4 hours because of
 459 limitations of hydrogen production and storage. Initially, the FC starts its operation when
 460 the gasifier is out (T_{minoff}) and when there is a maximum demand during 2 consecutive
 461 hours. Table 5 shows the initial operation of the loads included in the demand response
 462 program. Figure 11 shows the energy balance on the common single-phase AC bus for 5
 463 households on a summer day. The micro-grid operating model used was tested with
 464 hourly data of weather variables and hourly energy prices to the final consumer and base
 465 demand for the whole of 2016 in the city of Valencia (Spain). However, for purposes of
 466 analysis, only a portion of the data from the tests performed for the period from 13 to 27
 467 June 2016 will be given here. This balance is specifically that of the ninth day (June 20),
 468 and it can be seen how each of the energy resources (bars in the figure) are used to cover
 469 the total demand (P_{load}) of five households, represented by the continuous red line. The
 470 initial location of the loads registered in the demand response program can be observed
 471 by means of the difference with the base demand (continuous blue line).

472



473

474 **FIGURE 11** Results of the energy balance in the micro-grid operating model for the 5 households in a
 475 summer day case. Blue continuous line, base demand; red continuous line, dispatchable demand.

476

477 **4. Algorithm description.**

478 Sections 2 and 3 showed how the LabDER can be simulated to effectively represent its
 479 actual behavior. This simulator can be used as if it were a real micro-grid power generator
 480 connected to any system in order to test different high-level control strategies to optimize
 481 different indicators.

482 This study modeled a micro-grid supplying a residential unit composed of a series of
 483 houses with a configurable demand. The residential load can be configured with n houses
 484 whose base demand in per unit is shown in Figure 8.

485 Some of the loads can be scheduled to optimize grid performance. As the user knows the
 486 schedule a day in advance, he can take advantage of lower prices if he follows the
 487 proposed scheduling. The loads to be scheduled are: 600 W to 800 W for dishwashers, 2
 488 kW to 2.5kW for swimming pool pumps, 1755W for the community water pump, or 1575
 489 W to 3375 W to charge electric cars. Each load must be scheduled for a number of
 490 consecutive hours: 3 hours for dishwashers and pools, 2 hours for the community pump,
 491 and 4 to 6 for the chargers.

492 The micro-grid operator has to define a timetable for each of the detachable loads and
 493 send it to the consumers. Even though the controller can change the hourly inputs, the
 494 consumer should know the detachable loads at least a day in advance. The biomass power
 495 to be dispatched and the energy supplied to the electrolyzer to generate H_2 must also be
 496 defined. The controller plans a whole day and puts 24 values (for each input) into the
 497 system.

498 As the controller's main goal is to minimize operational cost of the system, its
 499 computation is a key issue. The total cost over the period analyzed for each of the energy
 500 sources is given by Eq.(13).

501

$$C_{SOURCE} = \sum_{h=1}^t P_{S_h} \cdot LCOEs \quad (13)$$

502

503 Where, C_{SOURCE} is the total cost for t hours of the period analyzed, P_{sh} is the power of
 504 source s at time h , and $LCOEs$ is the Levelized Cost of Electricity of source s . Table 2
 505 shows the references used to define the LCOE of each energy source.

506

507 **TABLE 2** LCOE Renewable sources value and reference

Source	LCOEs [€/kWh]	Reference
Photovoltaic	0.1578	Lazard's Levelized Cost of Energy Analysis [44] - Minimum value for residential roof top: 187 \$/MWh; 0,844 €\$)
Wind	0.08	Predescu, Economic Evaluation of Small Wind Turbines and Hybrid Systems For Residential Use [45]
Biomass	0.0962	Lazard's Levelized Cost of Energy Analysis [44] – Maximum value for biomass direct: 114 \$/MWh; 0,844 €\$)
Fuel Cell	0.0895	Lazard's Levelized Cost of Energy Analysis [44] - Minimum value for FC: 106 \$/MWh; 0,844 €\$)
Energy storage - Batteries	0.505	Lazard's Levelized Cost of Energy Analysis [44] - Minimum value for residential lead acid batteries: 598 \$/MWh; 0,844 €\$)

508

509 It is important to underline that the use of LCOE obtained in other works could be
 510 incorrect. The reason is that LCOE depends on the technology (affecting investment
 511 costs) and on its utilization in the site (affecting energy generation and operating costs).
 512 This work uses the reference values available in Lazard's annual report [44] (with the
 513 exception of wind energy, since this report does not consider small-scale generation) in
 514 order to facilitate the comparison of results in subsequent works. This fact becomes a
 515 limitation to the operational model that could be solved with a LCOE calculation for each
 516 technology in each iteration of the controller, since the amount of energy generated by
 517 each technology is known at that moment. However, in the case of this work, the
 518 information of the Investment and Operation Costs is not available. Likewise, special
 519 care must be taken with the LCOE calculation of the batteries, since it depends
 520 significantly on the technology, number of duty cycles and other aspects of the working
 521 conditions associated with the location.

522 When calculating the total production cost of hydrogen C_{ELY} , and the cost of battery
 523 storage (in charge mode C_{BAT-ch} for i hours), it should be remembered that these are fed
 524 from the photovoltaic, wind and gasifier systems. Likewise, when the batteries are
 525 discharged, the cost ($C_{BAT-disch}$ for j hours) is calculated from the battery $LCOE$, as in the
 526 equations (14)-(17).

527

$$528 \quad C_{ELY} = \sum_{h=1}^t P_{ELY,h} \cdot LCOE_{WECS} \quad (14)$$

$$529 \quad C_{BAT-ch} = -\sum_{i=1}^t P_{BAT,i} \cdot LCOE_{WECS} \quad (15)$$

$$530 \quad C_{BAT-disch} = \sum_{j=1}^t P_{BAT,j} \cdot LCOE_{BAT} \quad (16)$$

$$531 \quad LCOE_{WECS} = \frac{C_{FV} + C_W + C_{Gasif}}{\sum_{h=1}^t P_{PV,h} + \sum_{h=1}^t P_{W,h} + \sum_{h=1}^t P_{Gasif,h}} \quad (17)$$

532

533

534

535

536

537 Where P_{ELY} is the power consumed by the electrolyzer, P_{BAT} is the power from or to
538 batteries, and $LCOE_{WECS}$ is the weighted average levelized cost of electricity from the
539 renewable energy sources. Note that in battery charging a minus sign appears, since P_{BAT}
540 is positive when the battery is delivering power. The Total Cost ($TCmg$) of meeting the
541 demand from the experimental micro-grid is defined in Eq.(18) and the equivalent LCOE
542 is as shown in Eq.(19).

543

544

545

$$TCmg = C_{PV} + C_W + C_{Gasif} + C_{FC} + C_{BAT-disch} + C_{Grid} - (C_{ELY} + C_{BAT-ch} + I_{Grid}) \quad (18)$$

546

547

$$LCOE_{EQ} = \frac{TCmg}{\sum_{h=1}^t P_{LOAD,h}} \quad (19)$$

548

549

550 Where C_{PV} , C_W , C_{Gasif} , C_{FC} are the total costs of all sources, C_{Grid} is the total cost of
551 purchasing power from the grid and I_{Grid} is the total income from power sales to the grid.
552 In the former case, the energy purchase tariff T_P is used, which is defined hourly, while
553 in the latter, income is calculated by means of a single agreed sales tariff T_S to the network,
554 as in Eq.(20).

555

556

557

$$C_{Grid} = \sum_{h=1}^t P_{Grid-in,h} \cdot T_{P,h} \quad and, \quad I_{Grid} = \sum_{h=1}^t P_{Grid-out,h} \cdot T_S \quad (20)$$

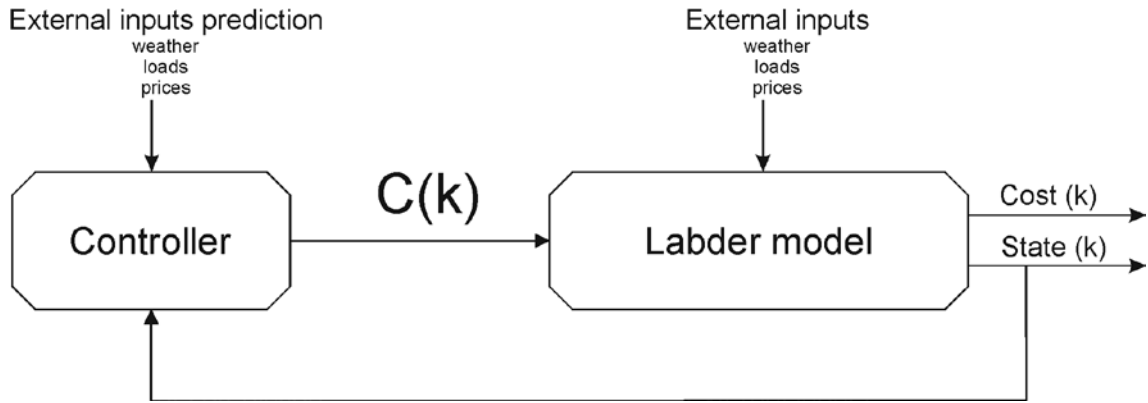
558

559 Labder model simulates the operation of a full day (day k) and it needs to be fed with one
560 hour sampled inputs. On one hand, the model needs prices, weather conditions and the
561 base demand curve at each hour for the day to be simulated. On the other hand, the model
562 needs to be fed with the hourly decisions on the fuel cell power and the biomass power
563 to be dispatched and the scheduling of the disconnectable loads as they are defined on
564 sections 2 and 3. Because of the simulation, the model generates two outputs: the global
565 cost of the operation and the state of the storage systems (hydrogen and batteries).

566

567 In order to achieve the lowest cost, this paper proposes the use of a Model Predictive
568 Controller (MPC) based on Evolutionary Algorithms (EA) to improve the overall cost of
569 the operation. This controller is an optimizer that looks for the minimum cost controller
570 to be implemented over a finite horizon. The control horizon is set to 7 days (one week).
571 Figure 12 shows the control scheme.

572



573
574

575 Figure 12. Control closed loop scheme.

576

577 The controller uses predictions on weather, prices and base demand curves, and the
578 previous state of the system to compute the optimal distribution of power dispatching and
579 disconnectable load configurations for the next day.

580

581 The optimal control command for day k is a $(a+2) \times 24$ matrix: $C_k = \{B_k, H_k, \overline{DL}_k\}$, where
582 B_k (1×24) and H_k (1×24) are array including the 24 power dispatching values of biomass
583 and hydrogen power, respectively. \overline{DL}_k ($a \times 24$) is the matrix containing 24 hourly values
584 of each of the n detachable load. This controller has to satisfy the restrictions stated in
585 section 3 for each one of the power sources and the detachable loads.

586 In order to compute the optimal control command matrix, the controller searches for the
587 set of seven consecutive control commands (for seven days) that achieve the minimum
588 cumulative cost during this period. Therefore, controller does not look for the best control
589 command matrix for the next day but the best for the whole horizon of seven days. Then,
590 the first day of the optimal control command matrix is selected as the control command
591 for the next day. This kind of control is called MPC in the literature [21].

592 Therefore, the controller has to solve an optimization problem with restrictions. Because
593 the model is very complex, this paper has chosen a heuristic optimization method based
594 on evolutionary algorithms. This kind of optimization has been widely used to solve
595 complex problems with restrictions [25]. The optimization methodology defines a set of
596 candidates and tests each one to find the best under certain criteria. Once the best
597 candidate has been found, the EA generates a new set of candidates based on the previous
598 result. This new set is also tested so it is expected to improve the result of the previous
599 generation. Some EA such as Particle Swarm Optimization (PSO) [22] have proven to
600 converge to optimal solutions.

601

602 The EA implemented in this paper is based on the movement of a swarm known as PSO,
603 which generates candidates in the population for testing. The algorithm creates variations
604 in each control command to search for better solutions (lower cost solutions). Each of
605 these control commands (including the best candidate of the last day) are simulated to
606 find the best control strategy (P_{best}) in the population and the associated minimum cost.
607 Figure 13 shows the flowchart of the optimization process.

608 The control computation starts by defining the first control command $C_{0,0} =$
609 $\{B_{0,0}, H_{0,0}, \overline{DL}_{0,0}\}$, where $B_{0,0}$ stands for biomass power, $H_{0,0}$ is hydrogen power, and
610 $\overline{DL}_{0,0}$ is the matrix containing the values of each detachable load. Each of these

611 components includes 168 (7 days x 24 hours) hourly values to be simulated. This
 612 controller has to be simulated in Labbder and it is set as the best-computed solution. The
 613 first day of the simulation, this controller has to be defined externally. For the next day,
 614 the controller will use as the first control command the optimal controller of the previous
 615 day.

616 The next step (step 1) is performed by PSO, which generates a population (P_1) of m
 617 different controls $P_1 = \{C_{1,1}, \dots, C_{1,m}\}$

618 Each one of the controllers has the form:

$$619 \quad C_{1,k} = \begin{bmatrix} 620 \quad cc_{1,1}^{\square} & \cdots & cc_{1,a+2}^{\square} \\ 621 \quad \vdots & \ddots & \vdots \\ 622 \quad cc_{1,168}^{\square} & \cdots & cc_{168,a+2}^{\square} \end{bmatrix} \quad (21)$$

623
 624 Where $k \in [1, m]$, $[cc_{1,1} \dots cc_{1,168}]$ is the array including all biomass power values for the next
 625 week, $[cc_{2,1} \dots cc_{2,168}]$ is the array including all hydrogen power values for the next week
 626 and $[cc_{l,1} \dots cc_{l,168}]$ ($l \in [3, a+2]$) are the arrays including the next week power values of each
 627 detachable load. For the shake of generality, equation (21) uses a as the number of
 628 detachable loads.

629
 630 Each one of the values is created from the best previous controller (the controller
 631 achieving the minimum cost). In the case of the first iteration, $C_{0,0}$ is used as the best
 632 controller because there is no previous result. So, each one of the values in equation (21)
 633 is computed as:

$$634 \quad cc_{l,p}^{\square} = cc_{l,p}^{j-1} \cdot z \cdot q + cc_{l,p}^{j-1} \quad (22)$$

635
 636
 637 Where $l \in [1, 168]$, $p \in [1, a+2]$, $cc_{l,p}^{j-1}$ is a corresponding value on the best previous
 638 controller, z) is a random number ($z \in [-1, 1]$) and q is a perturbation (see [28]) that can be
 639 activated for some of the candidates in order to include perturbations in the swarm. In this
 640 work, half of the population is perturbed each 10 iterations with perturbations between [-
 641 2, 2] thus kicking the candidates double far as the optimal solution. This strategy can avoid
 642 local minima [28].

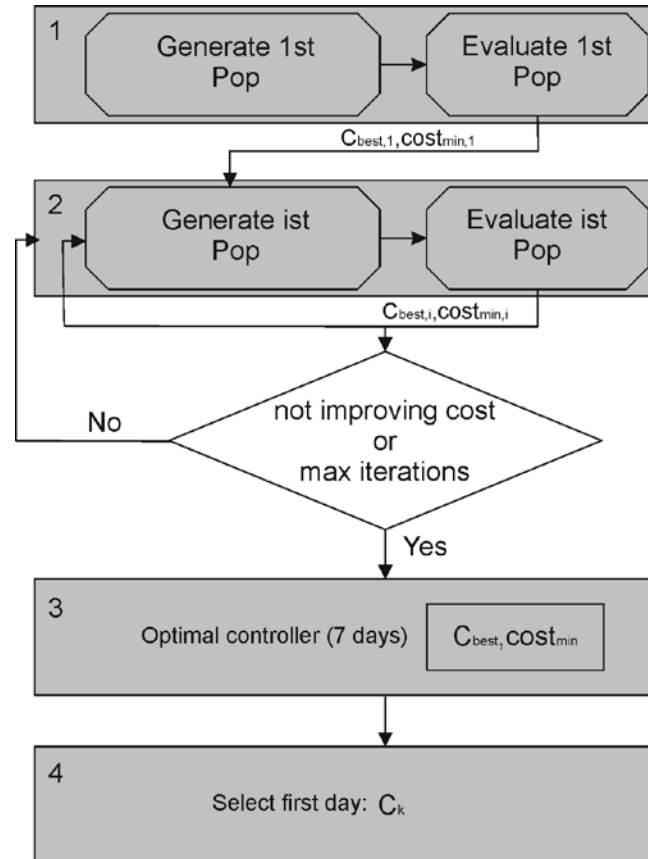
643
 644 Each candidate value is tested in order to find if they satisfy the restrictions. If not, values
 645 are adjusted to satisfy them. Then, each candidate in the population is tested so the
 646 controller ($C_{best,1}$) achieving the minimum cost ($cost_{min,1}$) is found.

647
 648 The next step (step 2) is using a loop to look for the minimum. PSO generates a new
 649 population (P_2) from the $C_{best,1}$ obtained in the previous iteration with equation (22) and
 650 each candidate is modified (if necessary) to fulfill the restrictions. Then, the whole
 651 population is tested in the Labder simulator, so the best controller in the population is
 652 found (the local best). If the cost of this controller ($C_{best,2}$) is lower than the previous
 653 better cost ($cost_{min,1}$), then the new overall best controller is set to $C_{best,2}$. Else, no
 654 candidate improves the result of the previous generation, so the best controller is kept to
 655 be $C_{best,1}$.

656 The next step consists of deciding if the algorithm continues testing new populations or
 657 if it has to stop. This paper implements two policies that can be activated or not if

658 necessary as final conditions. The algorithm can be stopped if the number of iterations
 659 overpass certain value or if the improve in cost does not reaches a limit value (2%
 660 improve).

661 If the final condition is not met, then PSO generates a new population thus closing the
 662 loop (see Figure 13).



663

664 **FIGURE 13** Controller computing diagram.

665 At the end of the optimization process (step 3), the controller has computed the values of
 666 the control commands that achieve the minimum cumulative cost ($cost_{min}$) for the next
 667 seven days (C_{best}).

668 The final controller command to be implemented (C_k) are the values corresponding to the
 669 first day (step 4).

670

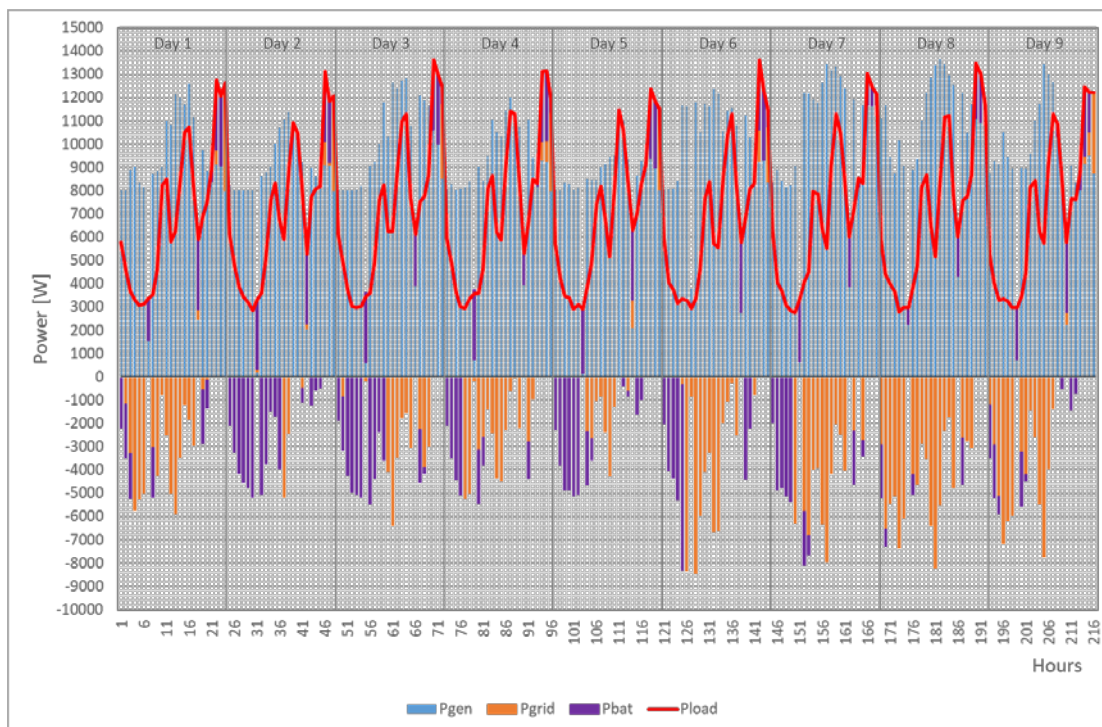
671 **5. Results and control performance.**

672 The system was simulated with several configurations of the residential units in order to
 673 test the MPC controller. In the first scenario a residential unit of 3, 5, and 7 houses was
 674 tested with a pre-scheduled (non-optimized) controller (see Section 3). Figure 11 shows
 675 the initial energy balance for 5 households on a summer day, resulting in a mean total
 676 cost $TCmg$ of 24.834 €/day and $LCOE_{EQ}$ of 0.147 €/kWh.

677 The same residential units were then controlled by the MPC controller to see whether it
 678 could improve on the pre-scheduled controller's results. The optimization EA was
 679 configured to generate 200 controllers in each iteration and a maximum of 100 iterations
 680 for each day. The system was tested for 15 days with 50 simulations for each scenario.

681 Figures 14 and 15 show how the MPC algorithm evolves the controller in order to reduce
 682 the cost. Figure 14 shows the initial situation with the pre-scheduled controller for the
 683 first 9 days. Since the control strategy remains constant, each detachable load is scheduled
 684 at the same time each day, so that P_{load} shows minor variations due to oscillations in
 685 P_{base} . The renewable power generation P_{gen} remains stable each day, showing
 686 variations due to different weather conditions at constant biomass and fuel cell
 687 production. The system balances the overall energy, so that grid P_{grid} and batteries P_{bat}
 688 absorb the surplus. Figure 15 shows the system controller under the MPC strategy. On
 689 the first day the system is controlled by the pre-scheduled controller. This controller is
 690 included as one of the candidates for the next day, together with the mutations proposed
 691 by the EA. The second day's system is controlled by the best controller achieved by the
 692 optimization process, which will also be one of the controllers to be tested for the third
 693 day. In a stable price and load scenario, the MPC algorithm therefore “polishes” the best
 694 candidate from the previous day in order to reduce the overall cost of the system.

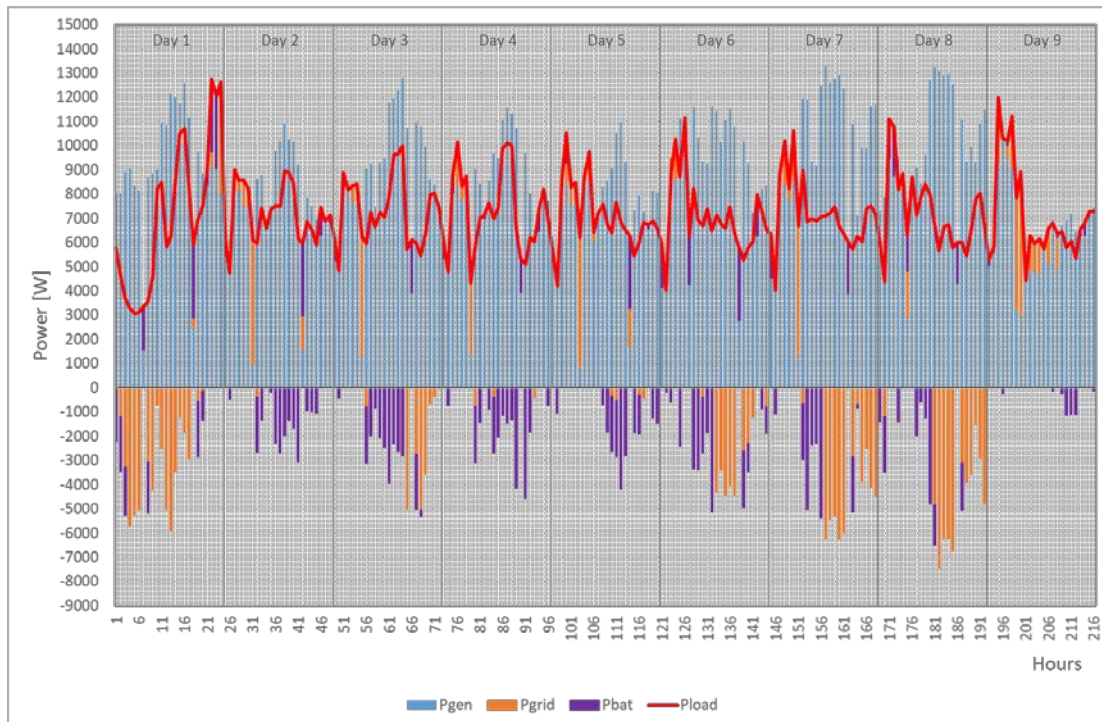
695



696

697 **FIGURE 14** Hourly results in a week from a pre-scheduled controller for 5 households in summer days.

698

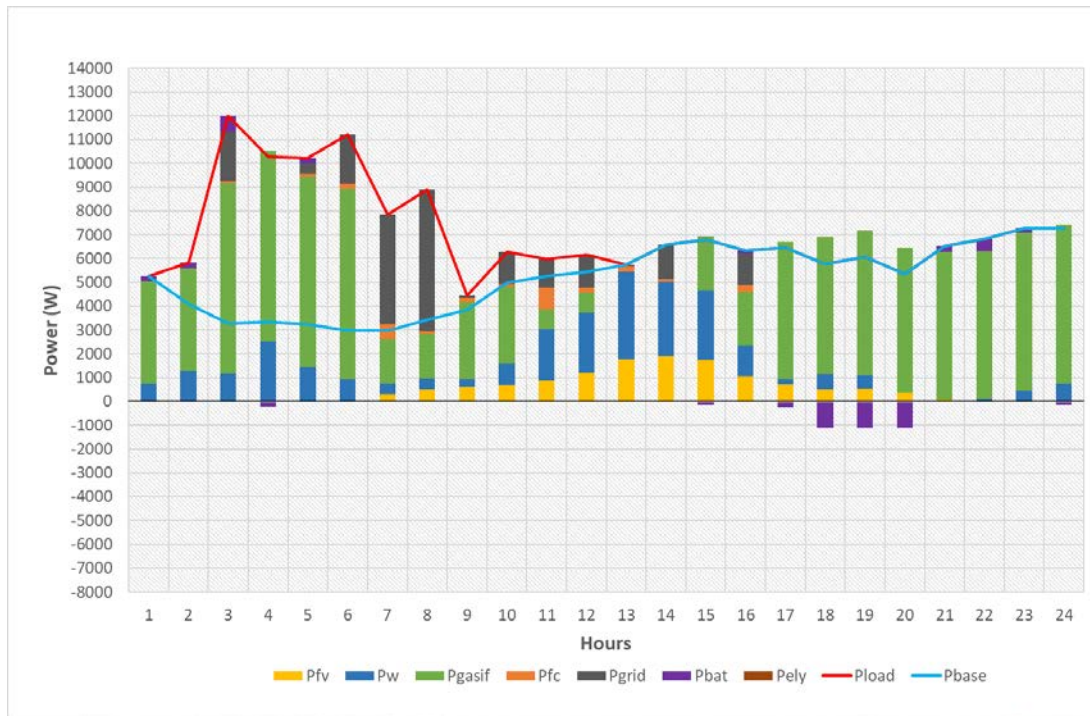


699

700 **FIGURE 15** Weekly results from MPC controller for 5 households in summer days.

701 It can be seen that the demand curve P_{load} changes its shape by gradually moving the
 702 detachable loads to the cheapest hours of the day (also the hours with the lowest base
 703 demand) thus reducing the cost. The most refined controller (day 9) forces each
 704 detachable load to the first day times and optimizes biomass use. Figure 16 shows in detail
 705 the hourly behavior of the generation dispatch, the relocation of the transferable loads in
 706 the demand response program and the energy balance with the grid to satisfy the demand
 707 on day 9 (see Figure 11). Note that no hydrogen energy is used. There are two reasons for
 708 this behavior: firstly, the total energy generated is optimized and less energy needs to be
 709 stored. Secondly, the cost of storing energy as internal energy of hydrogen molecules is
 710 much higher than the cost of storing energy in batteries, due to the low power installed
 711 and the fact that the electrolyzer mostly works at partial load, reducing its efficiency, so
 712 that the algorithm discards hydrogen storage. Dispatchable demand is placed where the
 713 base demand is lowest and energy from the grid is cheapest.

714



715

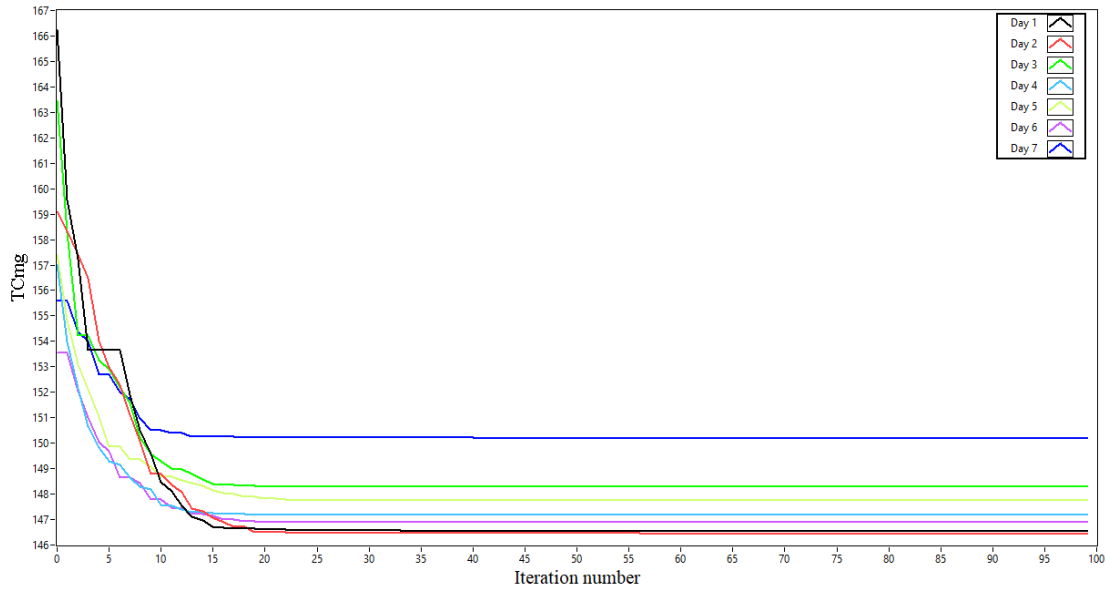
716 **FIGURE 16** MPC results for 5 households on optimal summer day. Blue continuous line - base demand;
 717 red continuous line - dispatchable demand

718

719 Mean $TCmg$ drops to 21.161 €/day and $LCOE_{EQ}$ to 0.123 €/kWh, with a 14.790% mean
 720 improvement in $TCmg$ and 16.211% in the LCOE. $TCmg$ and $LCOE$ are improved in the
 721 8% to 17% range, according to the number of houses involved. The standard deviation of
 722 the data remains at low values, indicating that there is no improvement on specific days,
 723 but over the whole period.

724 The EA performance in Figure 17 shows the evolution of $TCmg$ for the best daily
 725 controller found during the optimization process (forcing 100 iterations for each day).
 726 The $TCmg$ values are the sum of the seven best cost wise days. It can be seen that the
 727 optimizer sharply reduced the cost during the first 10 iterations, with a slight improvement
 728 up to iteration 20, after which the performance remained constant. When the controller
 729 checks a threshold in cost improvement (1%) in order to stop the process, the number of
 730 iterations oscillates between 8 and 10, thus reducing the computational cost. The average
 731 computing time of the MPC is 21.9 seconds, with an SD of 5.69 seconds (Windows® x64
 732 Intel® Core® i5, 3GHz, 8GB RAM). This means it is suitable for computing a daily
 733 schedule without problems, while the short computation time shows that this system
 734 could also be used to configure hourly system outputs.

735



736

737 **FIGURE 17** Total costs of micro-grid TC_{mg} evolution during the optimization process.

738

739 **6. Conclusions.**

740 A control system was designed to optimize energy supply to a residential load from a
741 hybrid renewable energy system connected to the public grid. The energy sources and
742 storage systems studied were those installed in the LabDER experimental laboratory of
743 the *Universitat Politècnica de València*. In order to check the controller's performance, a
744 mathematical model was built from the experimental data collected in the laboratory from
745 residential loads following a response demand program. The objective was for the
746 controller to guarantee the supply of energy to the loads at the minimum cost according
747 to the defined cost equations.

748 A Model Predictive Control Strategy based on Evolutionary Algorithms was developed,
749 which searches for the minimum cost controller to be implemented over a finite horizon.

750 The simulation results obtained indicate that the MPC searches for a stable and smooth
751 control strategy that improves the total cost of the system by defining the best time and
752 power level to be generated by the biomass system and the PEM in relation to the
753 expected values of the external inputs.

754 To demonstrate the improvements created by the MPC strategy actions, the initial control
755 strategy (pre-scheduled controller) is set to operate the gasifier at maximum efficiency
756 and use it the only dispatchable renewable source. The proposed controller achieved
757 a 14.790% mean improvement in total micro-grid costs and 16.211% in LCOE, or even
758 up to 17% in LCOE, according to the number of residential units considered.

759 Future studies are planned to deal with non-stable scenarios, including price changes due
760 to international conditions, load changes, failures and other variations.

761

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- 868

869 **APPENDIX**

870

871 Currents and Voltages in the photovoltaic model can be calculated as follows:

872

873

$$874 \quad I_{SC} = I_{SCS} \frac{G}{G_s} [1 + \alpha(T - T_s)] \quad (24)$$

875

$$876 \quad V_{OC} = V_{SCS} + \beta(T - T_s) - \Delta V \quad (25)$$

877

$$878 \quad I_{MPP} = I_{MPPS} \frac{G}{G_s} [1 + \alpha(T - T_s)] \quad (26)$$

879

$$880 \quad V_{MPP} = V_{MPPS} + \beta(T - T_s) - \Delta V \quad (27)$$

881

882 Where α and β are respectively the current and the voltage temperature coefficient. To improve the
883 accuracy of the model, in the expressions (25) and (26) inserting a correction term, ΔV , taking into account
884 voltage variation as a function of solar irradiance, which is calculated from the equation (28).

885

$$886 \quad \Delta V = C_2 \cdot V_t \cdot m \cdot \ln\left(\frac{G}{G_s}\right) \quad (28)$$

887

888 Where V_t is the thermal voltage depending on the Boltzmann constant K_B , the temperature of the cell T and
889 the electron charge q . Additionally, m is the diode quality factor.

890

$$891 \quad V_t = \frac{K_B}{qT} \quad (29)$$

892

$$893 \quad m = \frac{V_{MPP} + I_{MPP} \cdot R_0 - V_{OC}}{V_t \left[\ln\left(I_{SC} - \frac{V_{MPP}}{R_0} - I_{MPP}\right) - \ln\left(I_{SC} - \frac{V_{OC}}{R_0}\right) + \left(\frac{I_{MPP}}{I_{SC} \frac{V_{OC}}{R_0}}\right) \right]} \quad (30)$$

896 The internal resistance R_0 in the single diode model is calculated from the equation (31).

897

$$898 \quad R_0 = \left(C_2 \frac{V_{OC}}{I_{SC}(1 + C_1)} \right) \quad (31)$$

899 Generating values for V_P from 0 to V_{OC} , at a given temperature and irradiance, the I_P current is obtained.
900 The resistances R_S and R_P are then calculated from the reciprocal of the slope near to the open circuit point
901 and that of the slope near to the short circuit point, respectively.

902

903

$$904 \quad \left(\frac{dV}{dI}\right)_{V=V_{OC}} = -R_S \quad \left(\frac{dV}{dI}\right)_{I=I_{SC}} = -R_P \quad (32)$$

905