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Additional Information

Technical considerations on phase mapping for identification of atrial reentrant activity in direct and inverse-computed electrograms

Rodrigo - Phase Mapping of Atrial Reentrant Activity

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30 **ABSTRACT**

Background: Phase mapping has become a broadly used technique to identify atrial reentrant circuits for ablative therapy guidance. This work studies the phase mapping process and how the signal nature and its filtering affect the reentrant pattern characterization in EGM, Body Surface Potential Mapping (BSPM) and
35 Electrocardiographic Imaging (ECGI) signals.

Methods and Results: EGM, BSPM and ECGI phase maps were obtained from 17 simulations of atrial fibrillation (AF), atrial flutter (AFL) and focal atrial tachycardia (AT). Reentrant activity was identified by singularity point recognition in raw signals and in signals after narrow band-pass filtering at the Highest Dominant Frequency
40 (HDF). Reentrant activity was dominantly present in the EGM recordings only for AF and some AFL propagations patterns, and HDF filtering allowed increasing the reentrant activity detection from 60% to 70% of time in AF in unipolar recordings and from 0% to 62% in bipolar. In BSPM maps, HDF filtering increased from 10% to 90% the sensitivity, although provoked a residual false reentrant activity ~30% of time. In
45 ECGI, HDF filtering allowed to increase up to 100% the time with detected rotors, although provoked the apparition of false rotors during 100% of time. Nevertheless, raw ECGI phase maps presented reentrant activity just in AF recordings accounting for ~80% of time.

Conclusions: Rotor identification is accurate and sensitive and does not require
50 additional signal processing in measured or noninvasively computed unipolar EGMs. Bipolar EGMs and BSPM do require HDF filtering in order to detect rotors at the expense of a decreased specificity.

Key terms: reentrant activity; atrial rotors; electrocardiographic imaging; body surface potential mapping; electrogram; phase mapping.

55 **INTRODUCTION**

Reentrant propagation of electrical activity plays a decisive role in the perpetuation of atrial tachy-arrhythmias. While atrial flutter (AFL) is caused by a macroreentrant circuit around anatomical and/or functional obstacles that can be terminated ablating the critical isthmus¹, the nature of the waves' mechanisms that maintain atrial fibrillation (AF) is still controversial². Fibrillatory electrograms analyzed using rules developed for organized rhythms, such as activation mapping², are unreliable due to inconsistencies in the estimated activation times in relation to the presence of far-field intra-chamber crosstalk, noise or multicomponent EGMs³. On the other hand, the value of sequential mapping during AF is limited due to the dynamic changes in activation sequence during AF. Despite these limitations, there is substantial experimental and clinical evidence, based on activation phase and frequency analyses, demonstrating that AF is maintained by functional reentries, or rotors, and that localized ablation of the atrial regions harboring such rotors can terminate AF episodes⁴⁻⁵.

70 Recent progress in ablative therapies for AF has been paired with increased understanding of the wave mechanisms responsible for AF as a direct consequence of the development of novel mapping systems to characterize spatiotemporal patterns of AF electrical activity. These mapping systems include experimental optical systems based on the use of potentiometric dyes⁶, or clinical electrical recording systems using multipolar catheters⁵. Phase analysis of optical mapping signals has become the most reliable method to identify reentrant patterns, since pivoting activity naturally renders singularity points (SPs) in the phase maps that can be clearly identified⁷. However, optical mapping dyes are toxic in the clinical setting and the extrapolation from experimental optical mapping to clinical electrode-based

80 mapping lacks validation and raises the possibility of false association of phase SPs
with AF reentries, since non-reentrant electrical activity may also cause the
appearance of SPs under certain circumstances. On the other hand, multi-electrode
mapping catheters have difficulties to consistently map global biatrial activation with
uniform accuracy. Moreover, activation time mapping that has been used to map
85 AF⁵, can be ambiguous because of multicomponent EGMs and result in
inconsistencies in the estimated activation times and wave descriptions². To
overcome the ambiguity in marking the activation time, the phase analysis is
considering the whole cardiac activation cycle indiscriminately⁶. However phase
mapping techniques, as other techniques as well, make use of temporal signal
90 filtering for improving the interpretation of propagation and reentrant pattern
identification⁸⁻⁹, adding another possible uncertainty into wave propagation studies in
AF.

More recently, noninvasive systems have emerged as a panoramic mapping
approach for simultaneous body surface recordings of biatrial activation during AF.
95 Body Surface Potential Mapping (BSPM)^{8,10}, uses tens of electrodes for the analysis
of surface ECG signals, while the electrocardiographic imaging (ECGI)¹¹
computationally reconstructs the epicardial electrical activity from the BSPM
recordings. However, the accuracy of those technologies on determination of the
driving role of observed rotors in human AF has not been established. Therefore, in
100 this study we utilize mathematical models of different atrial reentrant arrhythmias to
provide a robust characterization of invasive and non-invasive mapping approach for
localization of reentrant activation patterns in AF. The objective of the present study
is to analyze the phase mapping processes in EGM, BSPM and ECGI, including the
effects of signals nature, temporal filtering and an automatic detection of SPs in

105 phase maps, to outline the validity and potential clinical use of those AF mapping approaches.

MATERIALS AND METHODS

Atrial mathematical models

110 A realistic 3D model of the atrial anatomy composed by 284,578 nodes and 1,353,783 tetrahedrons ($673.4 \pm 130.3 \mu\text{m}$ between nodes) was used to simulate the atrial electrical activity¹². A gradient on the electrophysiological properties of the atrial myocardium, specifically on $I_{k,ACH}$, I_{K1} , I_{Na} and I_{CaL} , was introduced into the atrial cell formulation¹³ to obtain propagation patterns maintained by rotors. Fibrotic tissue was
115 modeled by disconnecting a percentage of nodes between 20% and 60%, and scar tissue by disconnecting 100% of nodes in the scar region. The system of differential equations was solved by using Runge-Kutta integration based on a graphic processors unit (NVIDIA Tesla C2075 6G)¹⁴.

An ensemble of 17 different arrhythmic electrical patterns was simulated, divided into
120 4 groups according to the nature of their activation patterns. Group I was composed by one AF pattern driven by multiple rotational sources and 4 AF patterns driven by a single rotor at varying locations of the LA: Pulmonary Veins (PV), Posterior Wall of the Left Atrium (PLAW) and Right Atrial Appendage (RAA). Group II was composed by 4 AFL patterns: a typical AFL, a clockwise atypical AFL, an Inferior Vena Cava
125 (IVC) atypical AFL and an atypical AFL turning around the Pulmonary Veins (PV) due to the existence of inactive scar tissue in the PLAW. Group III was composed by 4 focal Atrial Tachycardia (AT) models repeatedly stimulated at different locations of the atria (IVC, LSPV, RIPV and RAA). Group IV was composed by the same AT simulations of Group III in which scar regions were added in order to create more

130 complex propagation patterns.

Electrical signals generation

For each simulation, a uniform mesh of 2048 unipolar EGMs was calculated surrounding the epicardial surface (1 mm distance) under the assumption of a
135 homogenous, unbounded and quasi-static conducting medium by summing up all effective dipole contributions over the entire model¹⁵. Computed electrograms were stored for processing at a sampling frequency of 500 Hz. Bipolar electrograms were obtained as the potential difference between each node and the nearest neighbor.

The BSPM potentials on the torso model were calculated by solving the Forward
140 Problem with the Boundary Element Method¹⁶ in a mesh formed by 771 nodes and 1538 triangular patches (**Figure 1**). White Gaussian noise was added to the BSPM signals with a signal-to-noise ratio of 60 dB and all signals were then referenced to the Wilson Central Terminal.

Inverse-computed EGMs (ECGI signals) were obtained by solving the inverse
145 problem with zero-order Tikhonov's regularization method and election of the regularization parameter based on the L-curve¹⁶⁻¹⁷.

To evaluate the performance of an automatic rotor identification technique, epicardial EGMs of atrial scenarios with real reentrant activity were randomly re-assigned to different nodes¹⁸. This random epicardial EGM maps were processed as described
150 above to obtain the BSPM and then the corresponding ECGI signals for the rotor analysis.

Signal filtering

Baseline EGM, BSPM and ECGI signals were estimated by decimation to 12.5 Hz

155 and filtering with a Butterworth 10th-order low-pass filter with a cut-off frequency of 2 Hz. Signals were interpolated to 500 Hz and subtracted from the original signals. EGM, BSPM and ECGI signals were then low-pass filtered with a 10th-order Butterworth filter with a cut-off frequency of 30 Hz. Processing procedures here were similar to clinical procedures elsewhere¹⁰.

160 For DF analysis, EGM, BSPM and ECGI signals were baseline-removed as previously reported¹⁰ and were then low-pass filtered with a 10th-order Butterworth filter with a cut-off frequency of 10 Hz. Power spectral density of all signals was computed using Welch periodogram (65536 point FFT and 80% overlap) to determine the local Dominant Frequency (DF) with a spectral resolution of 0.01Hz¹⁰.

165 We also tested the effect of narrow band-pass filtering of EGM, BSPM and ECGI centered at the Highest DF (HDF) found on the atrial surface by using a cascade of high-pass elliptic filters with a cut-off frequency equal to HDF - 1 Hz and a low-pass elliptic filter with a cut-off frequency equal to HDF + 1 Hz⁸.

170 **Reentrant activity identification**

Reentrant wave localization was carried out by identification of singularity points (SP) in the phase signal map obtained with the Hilbert Transform¹⁹. As shown in **Figure 2**, the phase transformation assigns a phase value between $-\pi$ and π for each sample of the signal, and thus each phase corresponds to a given state of the action potential (π for resting, $\pi/2$ for depolarization, 0 for plateau and $-\pi$ for repolarization). A phase map snapshot, therefore, allows inferring the propagation patterns and specifically the center of a pivoting rotor appears as a point in which phase is not defined (hence the term singularity point; SP) surrounded by phases ranging monotonically from $-\pi$ to π .

180 In order to identify SPs, phase values were evaluated along 3 different circles surrounding each tested point with increasing radii. Six to twelve points per circle were used for the phase analysis in which the EGM, BSPM and ECGI signals were interpolated by a weighted average of the neighboring nodes, being d^{-2} the weight for each node and d the distance between nodes.

185 A tested point was assigned to be an SP only when the phases of at least two of these three circles was gradually increasing or decreasing for a total of $2\pi^{\circ}$, and if the mean phase error with respect to a straight line was lower than a threshold: 0.4 radians for EGM, 0.2 radians for BSPM and no threshold for ECGI.

Testing with circles of various radii (**Figure S1**), radii of 0.5, 1 and 1.5 cm were found
190 to maximize sensitivity of SP identification in AF models, for both raw and HDF filtered signals, and therefore selected for the study.

An SP reflects the instantaneous condition of phase reentry. Thus, a pivoting excitation pattern was considered to constitute a propagating wave when maintaining a sequential connection between its SPs across time. The distance between SPs at
195 consecutive time instants should be less than 1 cm (EGM and ECGI) or 5 cm (BSPM) to be considered related and maintain a continuity of the wave rotation. In **Figure S2** we show the effect of this spatial threshold on true/spurious rotor identification. Finally, only long lasting SP describing waves that complete at least two rotations were considered as rotors and other SPs were discarded.

200

Sensitivity and specificity calculation

The different filtering strategies were evaluated in their ability to identify stable reentrant patterns (>2 rotations) in our models of AF as functional reentries (rotors) and in AFL patterns as anatomical reentries. Different criteria for considering a

205 detected SP as true or false were applied for the atrial EGM and ECGI maps versus
the BSPM. In EGM and ECGI maps, the sensitivity and specificity measures were
based on SP location criterion, due to the implication in the ablation guidance of the
SP location while in the BSPM the location of the detected SP have no direct
implication and therefore sensitivity and specificity measures considered only a
210 presence or absence criterion.

Accordingly, when the EGM and ECGI maps were analyzed on the atrial wall,
excluding valves and veins, only AF rotors detected less than 1.5 cm from the actual
rotor core were considered as true-location positives (named as true rotors in
Figures 4, 5 and 7), whereas AF rotors detected >1.5 cm from the actual rotor core
215 were considered as false-location positives. We chose 1.5 cm as a threshold
distance based on the rotor precession distance in our database, which was below
this value (see **Figure S3**).

In our AFL simulations a reentry was present around the TV, LPVs or IVC and its
counter rotating wave was in the IVC or PV orifices, or at the septum. Therefore, in
220 our AFL simulations the electric re-entrant pattern should generate phase
singularities only inside the orifices or the septal areas. As the EGM and ECGI time-
series signals in the sensitivity and specificity analysis were not calculated at the
orifices and the septal areas, all SPs detected during AFL are necessarily
considered as false-location positives.

225 When the electrical activity was analyzed on the torso surface (BSPM) the sensitivity
and specificity measures were based on an SP presence criterion. In this case, the
re-entrant electrical patterns generated by AF and AFL simulations can generate a
rotor anywhere accross the surface⁸, so only their presence or absence were
considered and not their location as in EGM or ECGI maps. Therefore, all surface

230 reentries detected during AF and AFL patterns were considered as true-presence positives.

Additionally, reference sensitivity and specificity analyses of SP detections were as follows: (i) all SP detections (>2 rotations) during random distributions of the EGMs were considered as false positives, and (ii) all SP detections during AT and AT+scar
235 rhythms which were simulated to be maintained by periodic focal stimulation were considered false positives.

Statistical analysis

All measures of continuous variables are reported as average \pm standard deviation,
240 and displayed as bars with a height equal to the average and whiskers length equal to the standard deviation. Statistical significance of differences between normally distributed continuous variables was estimated using the student's t-test. Linear fitting for phase measurements was carried out by using the least squares method; R-square were calculated as the coefficient of determination and phase errors were
245 calculated as the square difference between phase measurements and their linear best-fitting. A $p < 0.05$ was considered to be significant.

RESULTS

Restrictions in rotor identification

250 We found that we were able to identify more SPs in random EGM activity than in rotor-driven AF models (**Figure 3.D**), and phase transitions around SPs that arise from non-rotating activity were less gradual than those arising from rotational activity. In **Figure 3.A-B** the phase transitions in three concentric circles around detected SPs are shown for a rotational and a wave break pattern from an AF simulation. In

255 this example, deviation from a linearly gradual change transition was largest in the
outermost circle (1.5 cm radius) for the wave break pattern since phase was not
monotonically increasing. Overall, this deviation was larger in the random patterns
than in rotor-driven AF (1.00 ± 0.04 vs 0.47 ± 0.20 rad, $p < 0.01$). In order to reject
spurious SP detections a linearity threshold (0.4 rad) was applied to SP detections,
260 resulting in a reduction in the amount of detected SPs, as it can be observed in
Figure 3.D.

Transient SPs can also be found in our phase maps that arise from U turns around
scars from an AT+scar simulation instead of from actual functional rotations. In
Figure 4 one of such examples is depicted. Overall, if a duration of 0.5 turns is
265 required to SPs to be considered as rotors, all false detections in random
propagation patterns are rejected (**Figure 4.D**), while most true rotation patterns are
detected ($66.5 \pm 47.2\%$ of time for AF models). However several false positives are
detected ($6.5 \pm 14.1\%$ of time for AF patterns, $32.9 \pm 24.5\%$ for AFL patterns or
 $57.9 \pm 43.6\%$ for AT+scars). Since SPs that do not arise from an actual rotation
270 transiently disappear from the phase maps without completing a rotating cycle
(**Figure 4.C**), imposing a duration threshold of 2 turns reduces considerably the
amount of false detections (to 0% for AF, 0% for AFL and $15.9 \pm 28.8\%$ for AT+scar)
while keeping almost unaltered the detection of true rotors ($60.0 \pm 54.7\%$). **Figure S4**
from Supplemental Material shows rotor detection sensitivity when considering 0.25
275 to 4 rotations, were the incidence of spurious rotors detected in patterns other than
AF decreases with the number of required rotations.

The reported detection ratio for AF models can be increased by preprocessing the
EGMs before performing the phase transformation. Hilbert's transform is particularly
well suited for smooth or sinusoidal signals and therefore, a band-pass filter, centred

280 at the activation rate allows increasing the detection ratio (from $60.0\pm 54.7\%$ to $70.9\pm 39.9\%$) for AF models while the false positive rate detection in AF models is only $2.6\pm 5.1\%$ (**Figure 5**). This band-pass filtering was required for detecting rotors by using EGMs with multiple deflections, as found in bipolar EGMs. In bipolar EGMs, rotors were detected with the same detection rate than in unipolar EGMs but only
285 after band-pass filtering (**Figure 5.C-D** and **Figure 5.F**).

However, the increased sensitivity for AF rotors detection after band-pass filtering takes place at the expense of increasing the detection ratio in AFL models, with up to $47.9\pm 55.3\%$ of time with detected rotors. **Figure S5** shows an example of a stable macro-reentry around the inferior vena cava. Here, the upward propagation in the
290 RA is followed by propagation through the Bachman's Bundle and subsequent downward depolarization of the posterior wall of the LA. This pattern was not reflected into a stable SP in the EGMs, but got smoothed and stabilized after HDF filtering and a SP appeared. Therefore, HDF filtering may increase the false positive detections that arise from actual rotating patterns -but not rotors- in the tail of the
295 propagating wavefront.

Reentrant activity in BSPM and ECGI

We have previously proposed to apply HDF filtering to BSPM during AF in order to increase the sensitivity of rotor detection⁸ but were unable to quantify the specificity
300 of the method and whether it could be applied for computation of the ECGI maps. As shown in surface BSPMs for different mathematical models with and without HDF filtering (**Figure 6**), stable rotors can be observed after HDF filtering but not on the raw signals. However, HDF filtering also stabilized the patterns generated by random EGMs. Overall, HDF filtering allowed an increased detection of rotors in AF patterns,

305 from $10.8\pm 18.2\%$ to $92.9\pm 11.9\%$ (**Figure 7.A**) and in AFL, from $10.8\pm 18.2\%$ to $92.9\pm 11.9\%$. However, it also resulted in false detections in complex AT patterns, from 0% to $15.9\pm 31.8\%$ and even in random AF patterns, from 0% to $32.4\pm 28.4\%$.

When solving the inverse problem of electrocardiography for AF patterns, rotors can be accurately detected even without applying HDF filtering, as it is depicted in

310 **Figure 6**. Overall, true rotors during AF could be detected during $72.5\pm 42.0\%$ of time in AF patterns, with only $4.7\pm 10.7\%$ of time with false detections for AF, $13.2\pm 18.0\%$ for random EGMs and $25.0\pm 50.0\%$ for AFL and no false detections in the other situations (**Figure 7.B**). HDF filtering applied after inverse problem solution, increased the detection of true rotors during AF up to $80.0\pm 44.7\%$, but also

315 increased the amount of false detections in all models: i.e. $99.2\pm 1.8\%$ for random AF EGMs, $85.7\pm 5.2\%$ or random AFL EGMs or $81.9\pm 3.1\%$ for complex ATs.

DISCUSSION

Main findings

320 In this in-silico study, we have found that rotor identification based on phase singularities detection is accurate and sensitive and does not require additional signal processing in smooth signals such as unipolar EGMs, either measured or computed non-invasively. Bipolar EGMs and surface BSPM do require HDF filtering in order to detect rotors as phase singularities at the expense of a decreased

325 specificity. HDF filtering is not recommended in the solution of the inverse problem of electrocardiography because of an increased susceptibility to detect artefactual phase singularities (see Table 1).

Phase mapping of human AF

330 The mechanisms of AF are still unclear because the available mapping techniques
yield diverse maps ranging from organized sources to highly disordered
waves^{2,5,7,11,18,20}. Although phase analysis of signals has provided experimental
evidence that localized re-entrant sources or rotors drive AF^{7,9}, it has shown
conflicting results when applied to endocardial signals or body surface
335 electrocardiographic recordings in patients. On one hand, phased-analyzed
multipolar endocardial recordings showed stable and long-lasting rotors, while short-
lasting rotors that tend to recur to the same anatomic location were the hallmark of
inverse-computed body surface maps^{5,11}. On the other hand, AF activation patterns
reported using various noninvasive systems (i.e. BSMP, ECGI) using different signal
340 processing methods appear to be simpler than epicardial maps recorded in other
studies which do not report stable rotors^{2,8,11}. To clarify the effect of the filtering and
validate phase processing on intra-cardiac AF activity and body surface recordings,
we reproduced the mapping processing in computer simulations.

345 **Rotors and phase singularities**

The phase transform has been widely used for the identification of electrical patterns
in transmembrane potentials^{6,19}. However, the sole detection of a phase singularity
does not imply the presence of an underlying rotor, since singularities may arise from
wavebreaks or fibrillatory conduction^{2,9}. Nevertheless, SPs arising from wavebreaks
350 are more unstable and do not consistently present monotonical increases in phase.
In this context, other authors have already proposed to search for phase singularities
in two concentric rings around the SP¹⁸ and impose a restriction of a temporal span
of at least 1 turn in order to increase specificity. In the same direction, in the present
study we found that application of time and space restrictions to detected SPs allows

355 increasing the specificity in the detection of rotors. In particular, we propose the
requirement of a good fit to a monotonical increase of phase in the 3 concentric
rings. The use of 3 rings increases sensitivity as compared to a single ring, since
rotors occupying a small region are detected by the inner circles while rotors with a
large precession are detected by the outer rings. At the same time, the use of three
360 rings reduces the chance for randomly distributed phases to be considered as SPs.

Phase transformation and signal morphology

We have shown that the equivalence between propagation patterns and phase maps
depends on signal morphology. While the Hilbert transform results in an
365 unambiguous phase assignment for signals with simple morphologies, for complex
morphologies there is no relationship between the assigned phase values and the
phase in the action potential of the tissue. Hilbert transform is mathematically defined
for properly identifying the instantaneous phase value of a sinusoidal wave,
assigning the whole range values from $-\pi$ to π to the interval between signal peaks.
370 However, the Hilbert transformation of complex signals with several deflections
assigns the whole range of phase values from $-\pi$ to π between two consecutive
deflections and thus this assignment does not convey any useful information for
pattern identification. We have shown that phase singularities can be detected after
the phase transformation of unipolar, noise-free EGMs. However, raw EGMs with
375 multiple deflections, such as bipolar EGMs, are not suitable for SP detection and
require a pre-processing step before applying Hilbert's transform.

HDF filtering and BSPM phase mapping

We have previously proposed the use of a narrow band-pass filter prior to the

380 computation of the phase transformation in order to stabilize phase singularities in
BSPM recordings⁸. We showed that HDF filtering allows selecting the contribution of
areas that activate at the HDF while reduces the contribution on the body surface
from regions that activate at a slower rate and are not harboring rotors⁸. In the
present work we investigated the effect of HDF filtering on propagation patterns not
385 maintained by rotors in order to quantify the proportion of artefactual detections
introduced by our signal processing. According to our results, narrow bandpass
filtering does induce false detections that can be as high as 30% in randomly
distributed EGMs from AF models. For this reason, isolated SPs on BSPM maps
obtained after HDF filtering, even if they last for longer than 2 turns should be
390 interpreted with care since they are not an unequivocal demonstration of the
presence of a rotational activity. However, we have shown that a high incidence of
long-lasting SPs is indicative for rotational activity, since rotors were more than two-
fold detected during underlying rotational patterns than for non-rotational ones.

HDF filtering of BSPM results in a particularly high incidence of detected rotational
395 patterns in AFL models. This was to be expected because raw BSPM data already
shows rotational patterns that gets stabilized by the HDF filtering. This resemblance
between AF and AFL patterns can be explained by the fact that electrical potential
recordings contain far-field components and, as such, the electrical sources at the
vicinity of the anatomical obstacle may generate rotational electrical fields elsewhere
400 even without an actual functional reentry source. Thus, the BSPM detection of SPs
does not allow, in principle, discriminating between rotational patterns around an
obstacle and functional rotors. However, here we studied the sensitivity and
specificity of the BSPM to discriminate between rotational and non-rotational
patterns, which is feasible and clinically relevant. Our simulations show that stable

405 rotational patterns on the BSPM phase maps should be considered as indicative of either AFL or AF and activation frequency should allow discriminating between these two rhythms.

HDF filtering and EGM phase mapping

410 A quite aggressive band-pass filtering strategy has been proposed for detecting rotational patterns in multipolar catheter baskets^{5,18}, similar to our HDF filtering⁸. Consistently, we have shown here that HDF filtering applied to EGMs increases the detection rate of rotors during AF at the expense of very few false detections (see Table 1). In addition, the smoothing effect of the HDF filtering appears to be
415 necessary when the EGMs present multiple deflections so that the phase assignment by the Hilbert Transform is related to a phase in the action potential.

However, HDF filtering of EGMs results in some artefactual detections that should be taken into consideration. In particular, when the underlying pattern presents a coincidental rotation and not a mother rotor, there is an increased chance of
420 detecting a rotor due to the smoothing effect of the HDF filtering. These coincidental rotational patterns were especially relevant in our AFL model population in which either the activation tail or anatomical obstacles give rise to non AF-driving rotations. While these coincidental rotational patterns may not fulfill the eligibility criteria for rotors because there is no single rotational center where all phases between $-\pi$ and
425 π converge, phase homogenization that results after HDF filtering may make these patterns as qualified for rotor detection. This effect has been also seen in both ECGI, EGM and BSPM phase maps.

HDF filtering and ECGI phase mapping

430 Narrow band-pass filtering has also been employed following inverse problem
solution in mapping rotors during AF^{9,11}. The filtering has been shown to stabilize
SPs, however, we demonstrate in this study that aggressive filtering strategies
applied to the inverse computed electrograms may also cause artefactual rotors.
This comes as no surprise if we consider the ECGI virtual EGMs to depend on the
435 BSPM recordings, which themselves are showing a limited sensitivity and specificity
for SP and rotors detection. It is of notice though that the HDF filtering increases the
detection of ECGI rotors generated by random EGMs more than for the BSPM
(**Figure 7**), probably because of the additional smoothing by the inverse solution
relative to the forward solution.

440

Limitations

The present work is based on the use of mathematical models instead of patient
data because current technology does not allow determining whether detected rotors
are artefactual or they are in fact AF drivers. Mathematical models, instead, allow
445 defining specific activation patterns in which the presence of mother rotors is known
a priori and thus enabled accurate classification. However, our mathematical AF
models may be too simplistic and may not fully represent the whole spectra of AF
patients.

Different thresholds for detection of reentrant activity had to be established, such as
450 phase linearity or the radii of the circles for the phase assessment. The threshold
election allowed increasing the specificity at the expense of decreasing the
sensitivity of the reentrant activity detection, and vice versa. These thresholds were
chosen to achieve a balance between specificity and sensitivity according to our
database. It should be further explored whether the proposed thresholds should be

455 adapted to other scenarios.

Finally, we used the random distribution of the EGMs in order to generate propagation patterns with no stable reentrant patterns. Nevertheless, some of them could still retain some reentrant-like activity, due to the casual alignment of the EGMs, although in this manuscript all reentries detected in randomly patterns have
460 been classified as false positives.

Clinical Implications

The results of the present study may have several clinical implications that should be taken into consideration during phase analysis of AF signals. First, time and space
465 restrictions should be applied to avoid false rotors detections. To this purpose, we suggest to only consider true rotors those rotational patterns lasting >2 turns. Secondly, differentiation between AFL and AF for correct classification of rotational patterns on the BSPM phase maps should be based on activation frequency. Thirdly, selection of signals preprocessing will depend on the recording type and method.
470 Unipolar EGMs, either recorded from the endocardium (FIRM) or those computed non-invasively (ECGI), do not require additional signal processing^{5,11,16}. In contrast, endocardial bipolar EGMs and surface BSPM require HDF filtering in order to be able to detect rotors^{8,18}. However, care must be taken to exclude falsely detected rotors due to the methodology. Finally, aggressive filtering strategies should be
475 avoided during ECGI because of an increased susceptibility to stabilization and detection of false rotors (Table 1).

Conclusions

Phase transformation and singularity point identification is a robust method to identify

480 reentrant activity in the atrium. Smooth signals such as inverse-computed unipolar
EGMs do not require additional signal processing for rotor identification. Rotor
identification in signals with complex morphology such as bipolar EGMs or BSPM
signals require HDF filtering to simplify the phase maps at the expense of a
decreased specificity.

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		Sensitivity	Specificity
Unipolar EGMs (location criterion)	RAW	59.97%	97.94%
	HDF	68.22%	93.39%
Bipolar EGMs (location criterion)	RAW	0%	100%
	HDF	61.95%	93.35%
BSPM (presence criterion)	RAW	15.21%	100%
	HDF	89.31%	90.97%
ECGI (location criterion)	RAW	72.50%	94.27%
	HDF	80.00%	49.01%

Table 1. Sensitivity and specificity for rotor detection measurements.

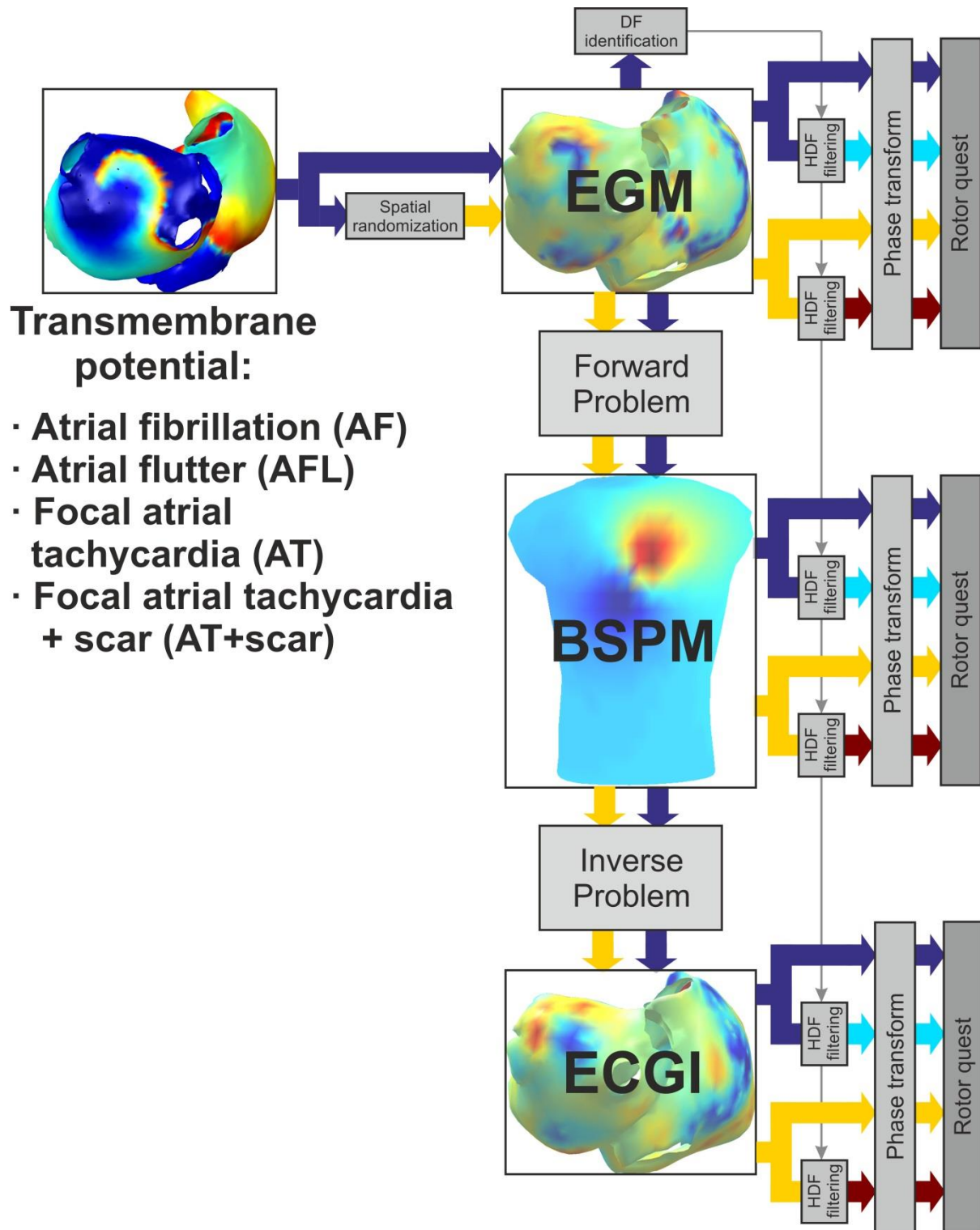


Figure 1. Workflow.

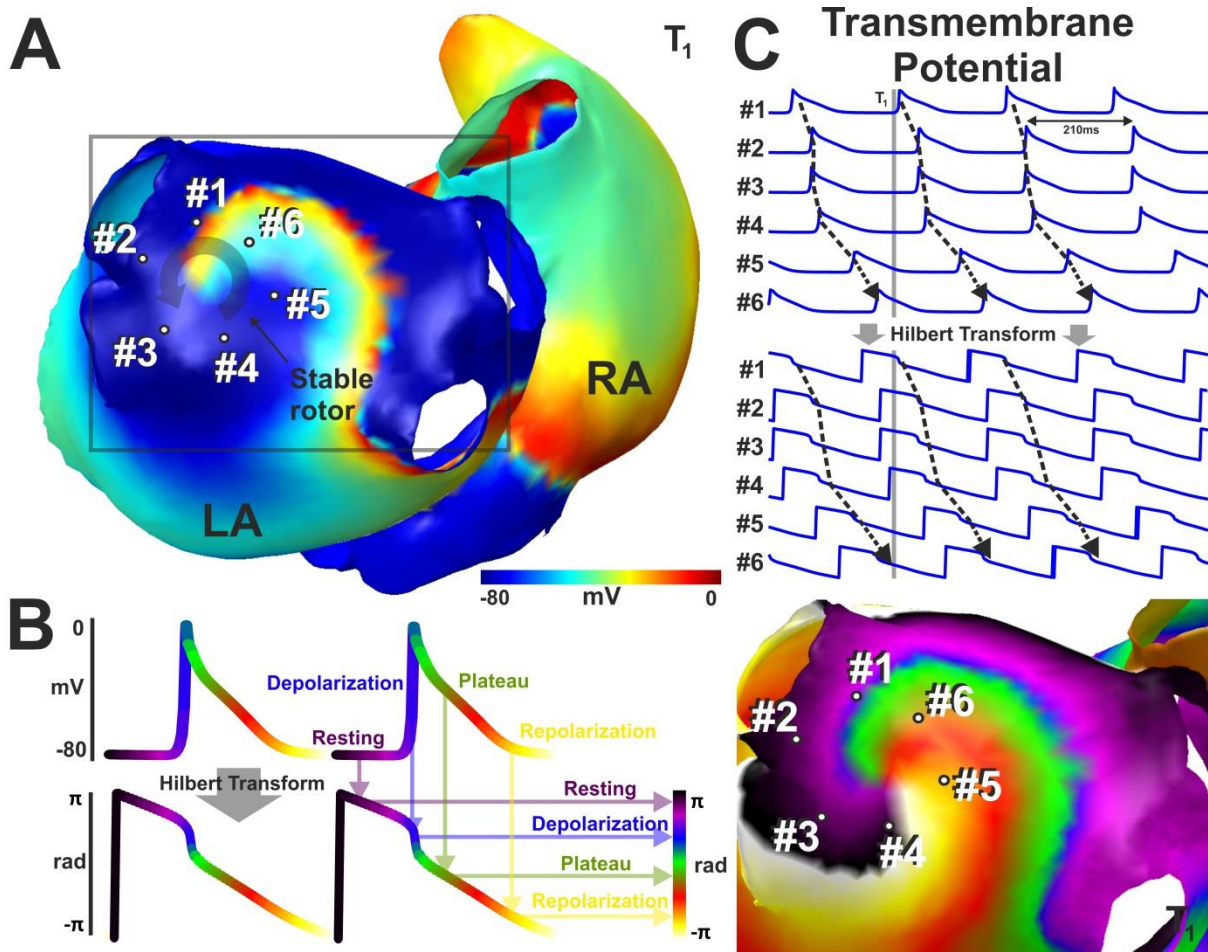


Figure 2. An example of a phase map of an atrial rotor. **(A)** Transmembrane potential map for an AF model maintained by a stable rotor in the posterior wall of the left atria. **(B)** Transmembrane potential signal (top) and its Hilbert Transform (bottom). **(C)** Transmembrane potential at 6 positions marked in (A) (top), its phase transforms (middle) and the corresponding phase map (bottom).

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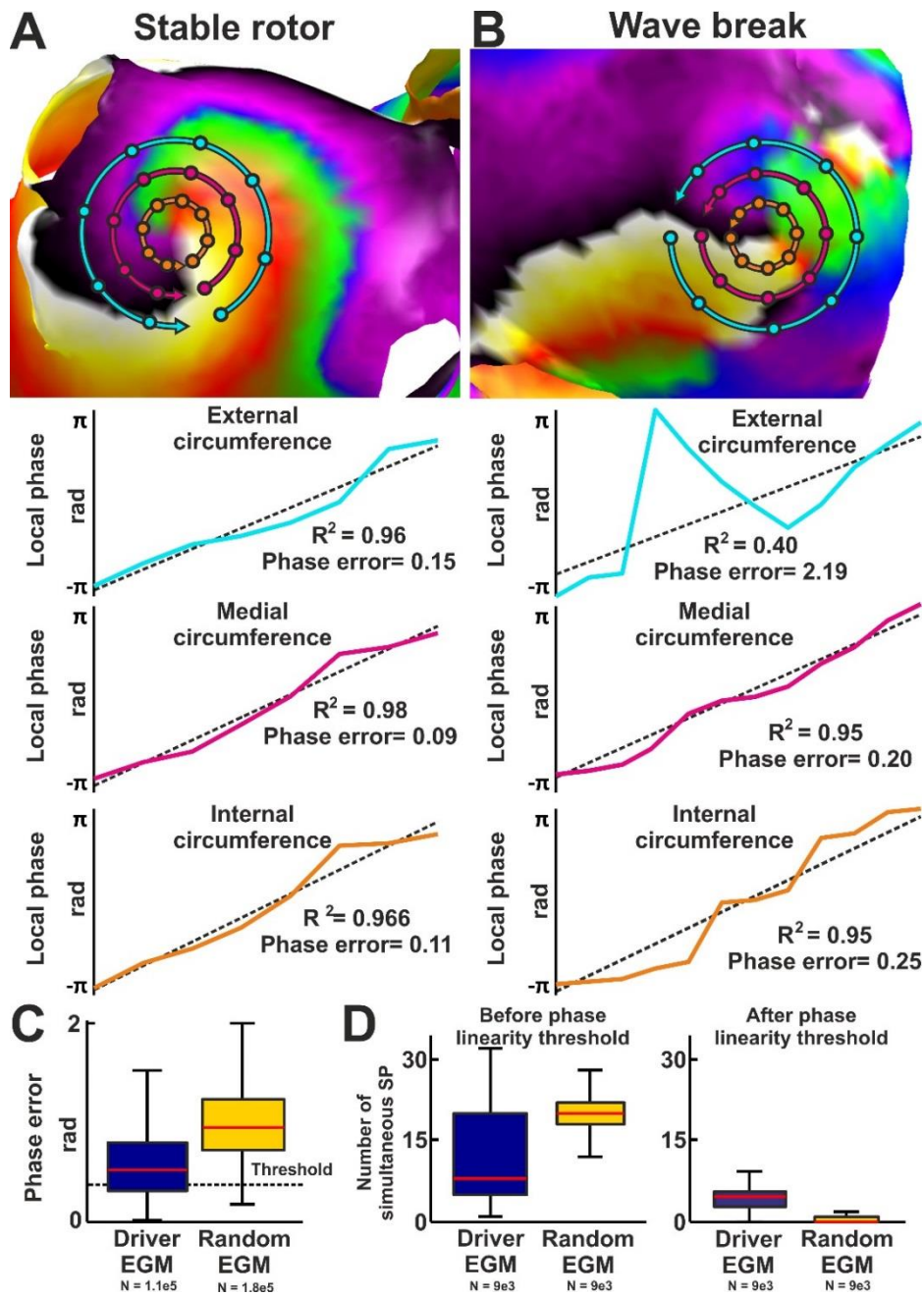
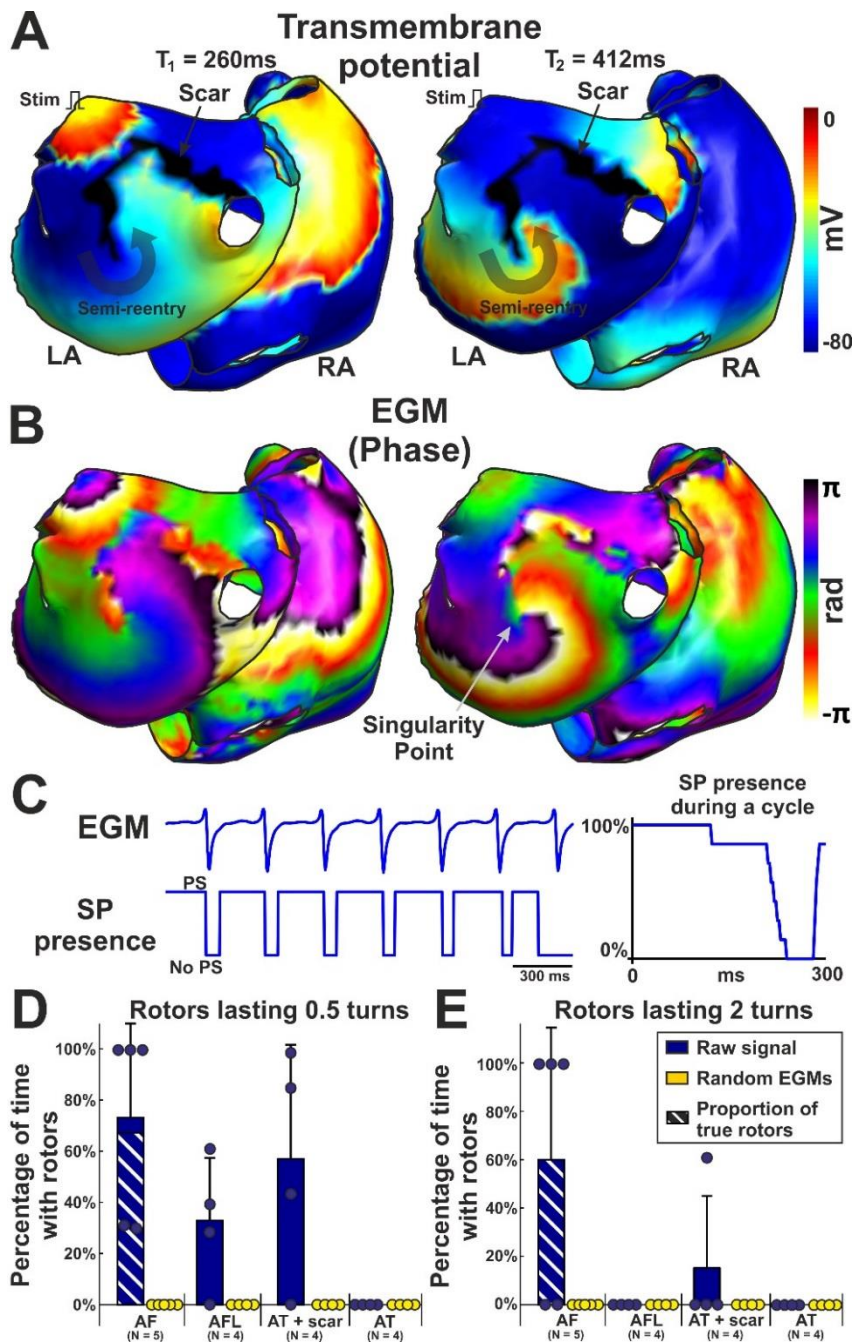


Figure 3. Phase evaluation at three concentric circles. **(A)** Phase map of transmembrane potentials from a stable rotor in the PLAW (top) and the phase values at the three concentric circles (bottom). **(B)** Phase map of transmembrane potential from a wave break (top) and the phase values at the three concentric circles (bottom). **(C)** Phase linearity error for 5 AF models. **(D)** Number of simultaneous SPs in the AF models before (left) and after (right) applying the linearity threshold.



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Figure 4. Temporal stability of phase singularities. **(A)** Transmembrane potential map of an AT simulation with a scar in the PLAW. **(B)** Phase map of EGM signals. **(C)** Left panel, EGM signal at the point marked with an arrow in **(B)**; right panel, SP presence at that point has been averaged for a single cycle. **(D)** Percentage of time with rotors lasting 0.5 turns and **(E)** lasting 2 turns for the complete cohort of atrial models. Color dots represent the individual measures.

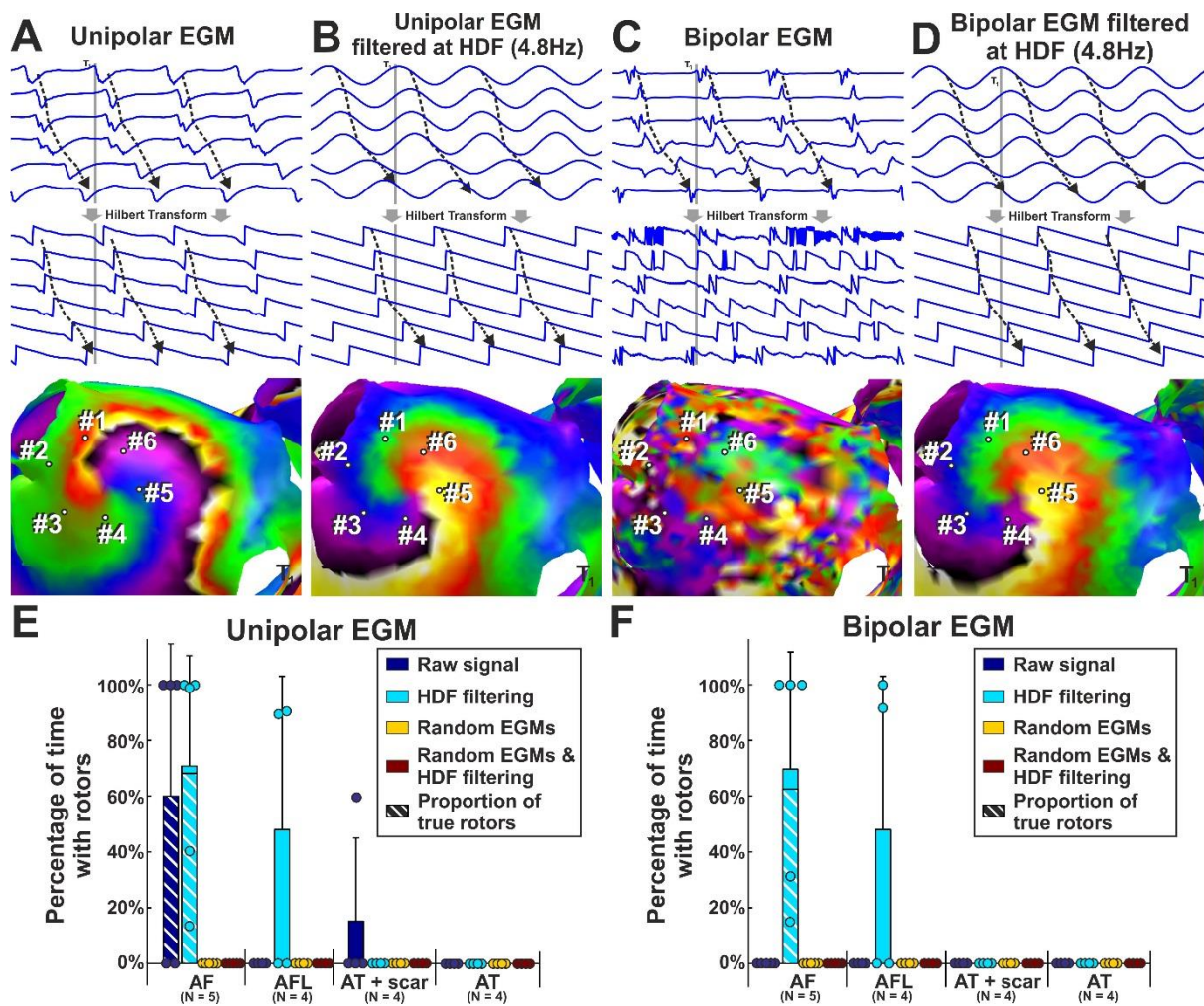


Figure 5. Phase singularity and rotor presence in EGM mapping. **(A)** Unipolar
610 EGMs, **(B)** Unipolar EGMs filtered at the HDF, **(C)** Bipolar EGMs and **(D)** Bipolar
EGMs filtered at the HDF at 6 positions (up), their phase transform (middle) and the
correspondent phase map (down). **(E)** Percentage of time with rotors lasting 2 turns
using unipolar signals. **(F)** Percentage of time with rotors lasting 2 turns using bipolar
signals. Color dots represent the individual measures.

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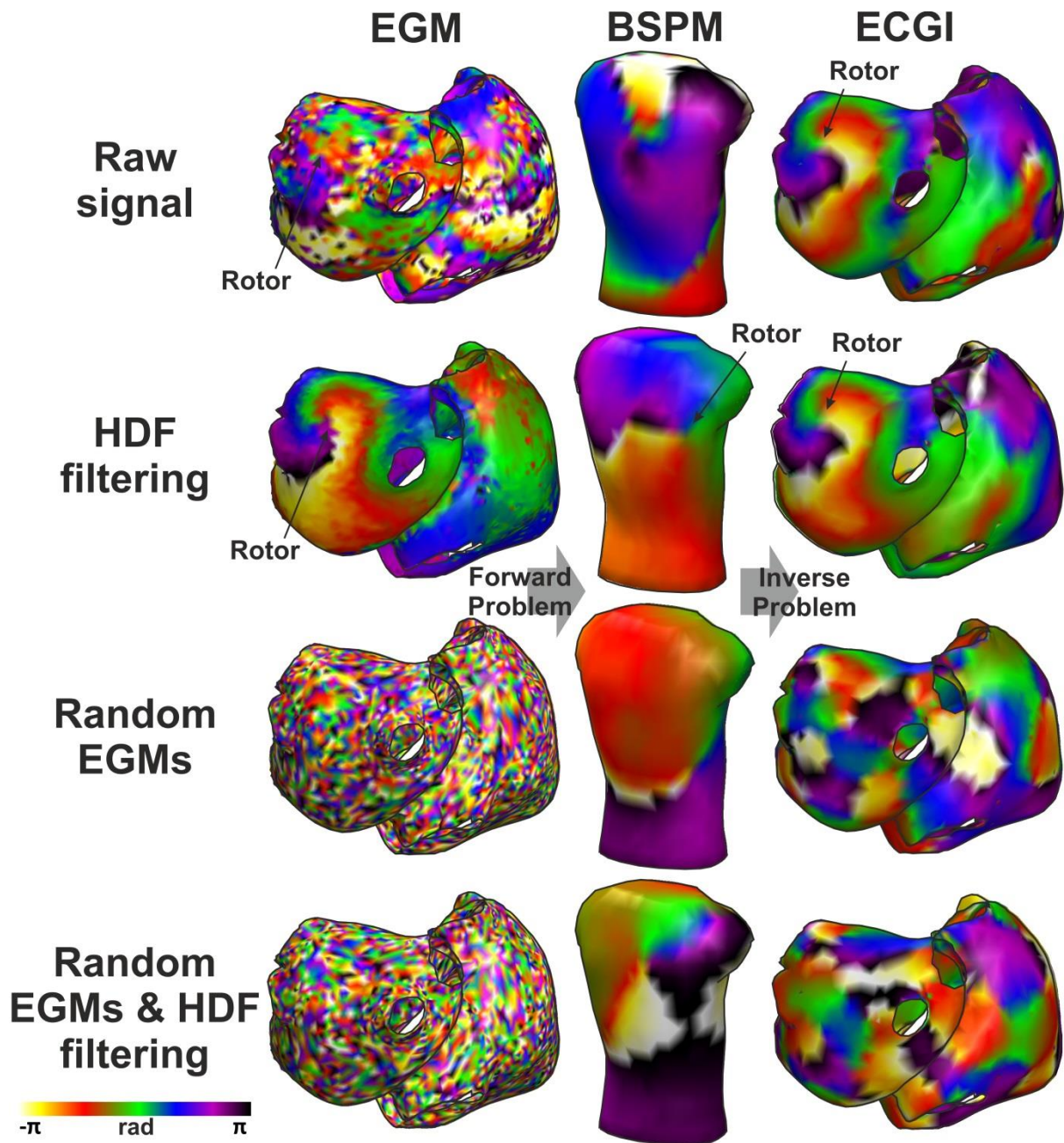


Figure 6. Example of noninvasive phase mapping and HDF filtering effect. Computed phase maps for an AF model maintained by a stable rotor in the PWLA (upper panels 1 & 2) and random EGMs (lower panels 3 & 4), together with their projection onto the torso and their backpropagation to the atrial surface (ECGi).

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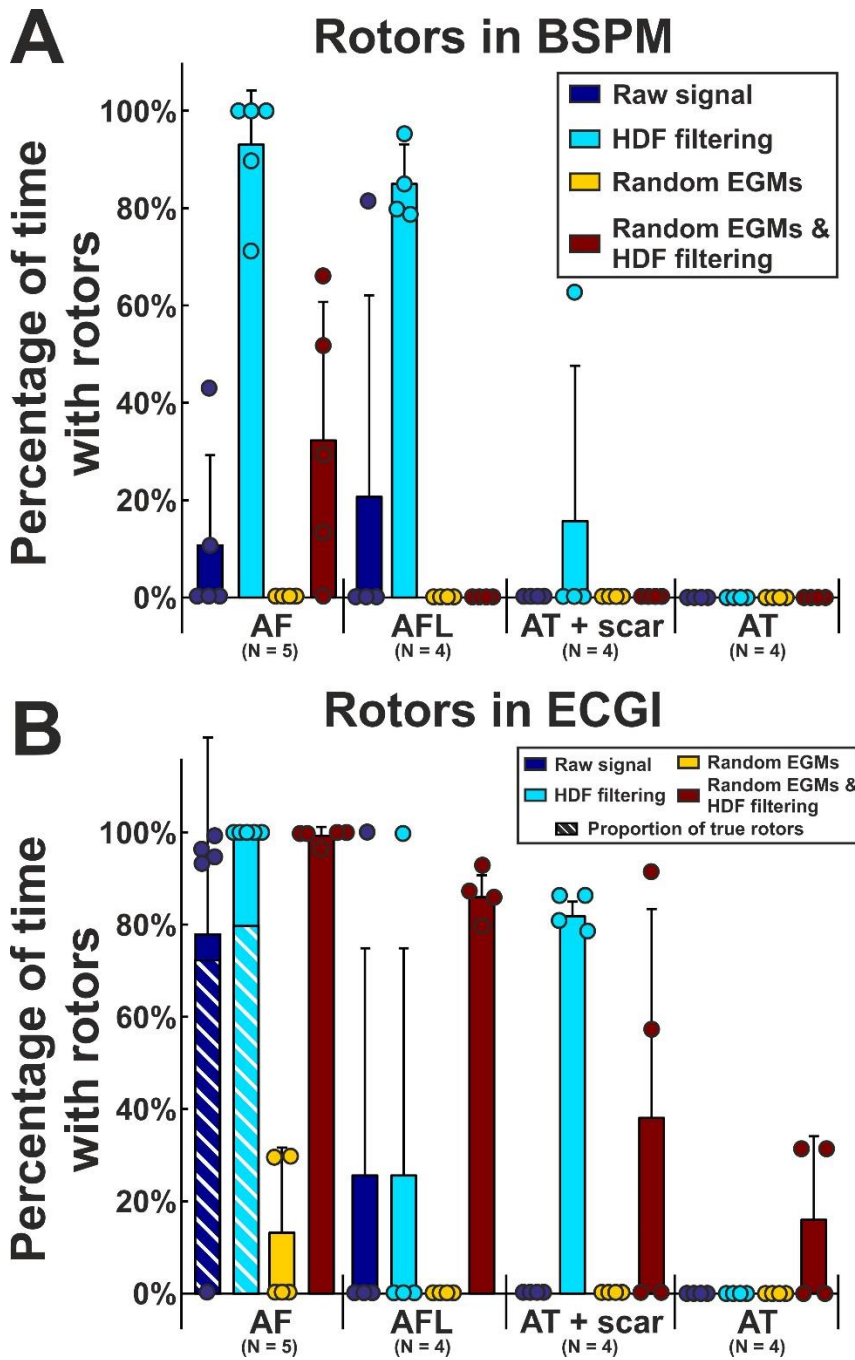


Figure 7. Rotor presence in **(A)** BSPM and **(B)** inverse-computed EGM mapping. Percentage of time with rotors lasting at least 2 turns. Color dots represent the individual measures.

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