Compact Combline Filter Embedded in a Bed of Nails

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Abstract—In this paper, we propose a compact topology for high frequency bandpass filters using coaxial cavities embedded in a bed of nails, including a complete design procedure combining equivalent circuit models and full-wave simulators. The resonance generated around a shortened cylindrical nail of the bed hosting structure is used as the basic element of the proposed filter, which is fed through Groove Gap Waveguides. For design purposes, an equivalent circuit model of the considered resonance is first obtained, and then the coupling levels between resonators are recovered with the distance between adjacent shortened nails. In order to validate the proposed structure and its design procedure, a filter prototype with a bandpass response (centered at 30 GHz and with relative bandwidth of 1.7%) has been designed, manufactured and measured. Good experimental results, in terms of insertion losses (with a minimum value of 1.6 dB) and return losses (greater than 16.6 dB in the whole pass-band), have been achieved.

Index Terms—Aggressive space mapping (ASM), band-pass filter, combline filter, groove gap waveguide, periodic structures, stopband response.

I. INTRODUCTION

I N recent years, periodic structures have regained considerable relevance in the design of passive microwave devices. The frequency selective properties of these periodic structures can be used for many different purposes, [1]. For instance, artificial magnetic conductor (AMC) is one of that non-physical concepts that can be physically realized thanks to periodic structures. The combination of two parallel plates, one being an AMC and the other a perfect electric conductor (PEC), was proposed as a platform providing a stopband response, in which different circuits can be embedded in a contactless fashion [2], [3]. The analysis and modeling of these structures, recently named gap waveguides, can be found in [4], [5].

The practical usage of this technology has been growing in the last years, as confirmed by the increasing number of designed transitions between gap waveguides and other classical

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technologies (see [6]–[11]), and their practical employment for implementing many other passive components. Among them, we can find power dividers, [11], antenna feeding network, [12], and different filter topologies for microwave and millimeter-wave applications, [13]–[19].

More recently, new topologies for slot array antennas with enhanced radiation properties, based on a resonance around a shortened nail of the gap waveguide structure, have been successfully proposed in [20]–[23]. As it was identified in [21], such resonance is very similar to the one of a coaxial resonant cavity, which are typically employed in combline waveguide filters [24], [25]. Therefore, this resonance could be used for implementing a compact version of combline filters in gap waveguide technology.

In this paper, we demonstrate the practical implementation of a combline filter seamlessly integrated in a supporting bed of nails, making use of coupled resonances due to shortened nails of the hosting structure. For designing these filters, an efficient procedure based on the aggressive space mapping technique, [26], used in combination with a classical method based on coupled-resonator circuits [27], has been proposed and illustrated with a practical case. For this purpose, a bandpass response centered at 30 GHz and with a bandwidth of 500 MHz (i.e., 1.7%), in-band return losses of 20 dB and ripple level of 0.0436 dB, has been considered.

The paper is organized as follows. In section II, we have studied the stopband behaviour of the periodic structure used for embedding the proposed filters. Section III includes a detailed analysis of the coaxial cavity resonance, providing an equivalent circuit for its accurate modeling. Then, Section IV details the complete design procedure of the proposed coaxial filter based on the ASM technique. Its practical realization, including experimental validation results, are shown in Section V. Finally, Section VI outlines the main conclusions of this work.

II. STOPBAND OF THE BED OF NAILS

A periodic structure provides a stopband frequency response that can be used for different purposes. Several studies of the stopband properties of gap waveguides have been already published, as can be seen in [28], [29]. Due to its simple machining, a square section nail (see Fig. 1) is frequently used as the unit cell of periodic structures, being able to provide a stopband response with an octave bandwidth. The relationship between the provided stopband response and the geometrical

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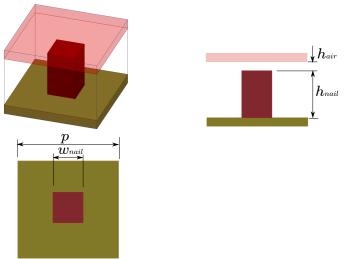


Fig. 1. Geometry of a square section nail used in periodic structures.

dimensions of the unit cell, i.e., w_{nail} , h_{nail} , h_{air} and p in Fig. 1, has been studied with detail in [2] and [29].

One of the main advantages of gap waveguide technology, lies in the fact that perfect shielding is not required to keep electromagnetic fields confined in the waveguide. Conventional gap waveguides leave a small air gap (less than $\lambda/4$) between the nails top and the lid. The high-impedance condition created by the bed of nails forces a stopband in the air gap. However it has been observed [30] that in fact the presence of the air gap is not strictly necessary and the lid can rest directly onto the nails. Therefore some nails may be in contact with the nails while others may not, due to machining imperfections, but the stopband condition is still retained or even increased in frequency range. Such arrangement has been named zero-gap and it provides certain practical advantages since assuring a thin air gap is not an easy task, particularly in the millimeter-wave band and above.

We have performed a parametric analysis in terms of the variable h_{air} , considering values for h_{air} between 0 and 100 microns, as well as keeping constant the sum of the nail height, h_{nail} , and the air gap, h_{air} , (i.e., $h_{air} + h_{nail} = 1.8$ mm). For the other dimensions of the unit cell shown in Fig. 1, we have chosen $w_{nail} = 0.9$ mm and p= 2.5 mm, which provides a stopband response of enough bandwidth, so that it will be possible to allocate the bandpass response of the coaxial filter to be designed.

In Fig. 2, we show results obtained with *HFSS* eigenmode solver (from *ANSYS*), where we can see that the minimum frequency of the stopband response tends to 0 GHz when the air gap value is progressively reduced up to be null. On the other hand, the maximum frequency of the stopband response is practically kept constant for different values of h_{air} , around 70 GHz.

From this study, it can be seen that the stopband bandwidth of these periodic structures tends to grow when the air gap decreases, and that the stopband response is preserved (in terms of bandwidth) even for a zero-gap case.

For hosting the bandpass coaxial filter proposed in this

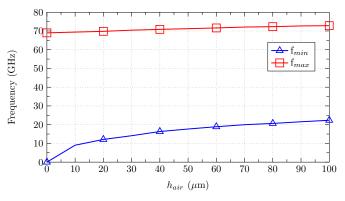


Fig. 2. Stopband behaviour versus h_{air} , with w_{nail} =0.9 mm, h_{nail} + h_{air} =1.8 mm and p=2.5 mm.

work, we will make use of zero-gap to alleviate fabrication burden.

III. SHORTENED NAIL RESONANCE MODELING

As can be seen in Fig. 3 (results from *ANSYS HFSS* eigenmode solver), a shortened nail embedded in a bed of square section nails has a clear resonant behaviour around it. It can be observed that the electric field is vertical at the air gap and radial near the base of the resonator. From these results (and the resonator topology), it can be concluded that this resonance is similar to the fundamental one of a coaxial resonant cavity used in more classical combline waveguide filters [24]. Compared with the resonators made in RGW and GGW presented in [16] the main advantage of the proposed combline resonator is related to its smaller size, that provides a cleaner out-of-band frequency spectrum response.

It can be noticed that the shortened nail has been chosen with cylindrical shape. This shape has been selected to avoid square corners, which can concentrate intense currents which normally imply higher losses. Other advantage of using cylindrical shapes is related to its meshing for modeling purposes, because with curved surfaces and using a curvilinear meshing, the number of requested tetrahedrons is lower and the computation effort is substantially reduced.

Additionally, as it also happens with an equivalent coaxial waveguide resonator, it has been checked that the resonance frequency of the proposed structure (Fig. 3) can be effectively controlled with the height of the cylindrical nail (or equivalently, with the value of the gap between the shortened nail and the top metal piece).

Therefore, in order to model the resonance around the shortened nail, it seems reasonable to choose the equivalent circuit shown in Fig. 4, which is composed of a length of shortcircuited coaxial transmission line (representing the cylindrical nail connected to the bed metallic base), loaded at its end with a capacitor (modeling the gap effect between the nail and the top metal plate)

As it is well known, the resonance condition of the proposed equivalent circuit (Fig. 4) is given by:

$$Y_L + Y_R = 0 \tag{1}$$

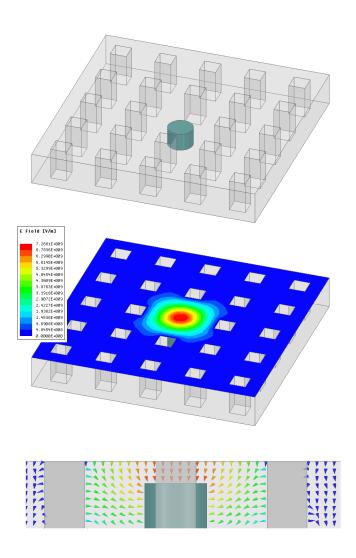


Fig. 3. Geometry of a cylindrical shortened nail within a bed of square nails, and electromagnetic field distribution at the corresponding resonant frequency.

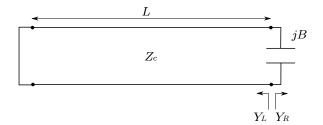


Fig. 4. Equivalent circuit model of the considered resonance around the shortened nail.

being:

$$Y_L = -jY_c \frac{1}{\tan\beta L}$$

$$Y_R = jB = j\omega C$$
(2)

where Y_c is the characteristic admittance of the transmission line representing the cylindrical nail. In order to compute Y_c , an equivalent square coaxial guide with circular center conductor is proposed. In Fig. 5 we can see all involved geometrical variables, as well as dashed red lines defining

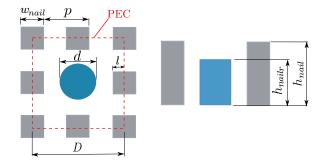


Fig. 5. Geometry and dimensions of the square coaxial guide with circular center conductor.

the outer conductor of the square coaxial guide. With regard to the length L of the equivalent transmission line, we have considered the reference plane location as indicated in [31], thus using $L = h_{nail}$.

In order to find the exact location of the square outer conductor (i.e., the value for l dimension in Fig. 5), we have followed the technique detailed in [5]. Basically, it consists on finding l to make equal the values of the two following input impedances: the one seen towards a lateral size of the real structure defined by the real periodic bed of nails, and the same impedance after replacing the bed of nails by a continuous metal wall (square dashed line). Then, using this value of l, the dimension of the external conductor of the square coaxial guide (i.e., D) is obtained through the following expression:

$$D = 2p - w_{nail} + 2l \tag{3}$$

In our case, considering again $w_{nail}=0.9$ mm, $h_{nail}=1.8$ mm and p=2.5 mm, we obtain (after applying the previously cited technique), a value of l = 0.181 mm, and therefore D=4.462mm. Choosing a diameter for the shortened cylindrical nail of d=1.4 mm, we compute the value for the characteristic impedance of the square coaxial guide as follows [32]:

$$Z_c = 60 \ln\left(\frac{1.0787D}{d}\right) = 74.09 \ \Omega \tag{4}$$

To calculate the value for the capacitor of the considered equivalent circuit, the following expression (proposed by Marcuvitz in [31] for modeling the termination of a coaxial line by a capacitive gap) can be used:

$$\frac{B}{Y_c} = \left(\frac{2d}{\lambda_0}\ln\frac{D}{d}\right) \left[\frac{\pi d}{8(h_{nail} - h_{nailr})} + \ln\left(\frac{D - d}{2(h_{nail} - h_{nailr})}\right)\right]$$
(5)

However, as explained in [31], the previous expression corresponds to the case of a cylindrical coaxial line (i.e., with a circular outer conductor), and it is only valid for a certain range of geometrical dimensions. Therefore, in order to obtain more accurate results for the normalized susceptance of the capacitor, it will be necessary to use full-wave electromagnetic (EM) simulators considering the real geometry of our equivalent coaxial line. For this purpose, we have again employed the commercial tool *ANSYS HFSS*.

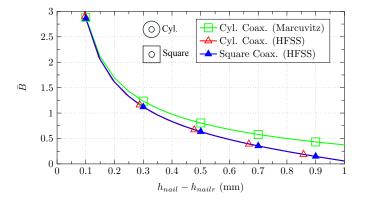


Fig. 6. Normalized equivalent susceptance (\bar{B}) versus the gap height (i.e., $h_{nail} - h_{nailr}$).

For the same shortened nail configuration studied before, we have computed the normalized susceptance values for different gap heights (or $h_{nail} - h_{nailr}$) at a frequency of 30 GHz, employing the Marcuvitz expression in (5) and ANSYS HFSS commercial software (considering both a circular and a square outer conductor for equivalent coaxial guide). All these results are compared in Fig. 6, where it can be concluded that ANSYS HFSS HFSS results are independent of the shape (circular or square) selected for the outer conductor of the equivalent coaxial guide, and that expression (5) provides valid results for small values of the gap height.

Once all the element values of the proposed equivalent circuit (see Fig. 4) have been computed, the resonance frequency of the considered resonator can be found solving the transcendental equation defined in (1)-(2), using any numerical method suitable for this purpose. This procedure has been applied to the very same resonator geometry under study, and the resonance frequencies obtained for different values of the shortened nail height (h_{nailr}) are shown in Fig. 7, where they are successfully compared with the results from ANSYS HFSS eigenmode solver.

From the results displayed in Fig. 7, two main conclusions can be outlined. The first one is that the proposed equivalent circuit is really modeling the resonant behaviour of the selected coaxial resonators very accurately, and, therefore, it can be effectively used for accelerating the design process of the corresponding shortened nail topology. Secondly, the curves relating the resonance frequency with the height of the shortened nail can be very well approximated (as can be seen in Fig. 7) by means of a linear equation, with a slope of m=-16.4 GHz/mm for the particular example considered in such figure. This linear behaviour will be also employed, as explained next, in the design procedure outlined for the proposed combline filters in gap waveguide technology.

IV. FILTER DESIGN PROCEDURE

In this section, we will present the physical topology of the proposed coaxial filters, based on the cascaded coupling of the resonances due to shortened nails that have just been properly modeled. The complete design procedure of these filters, based on a very efficient approach combining circuital and

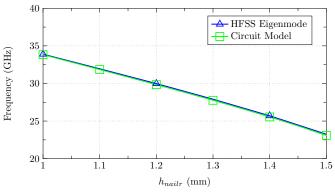


Fig. 7. Resonance frequency versus h_{nailr} (height of the cylindrical shorted nail), with w_{nail} =0.9 mm, h_{nail} =1.8 mm, p=2.5 mm, and d=1.4 mm.

electromagnetic simulation models, will be also thoroughly described next.

In order to illustrate the proposed filter topology, and its related design process, we will focus on recovering a bandpass response of 500 MHz centered at 30 GHz (i.e., with a relative bandwidth of 1.7%), with in-band return loss and equi-ripple levels of 20 dB and 0.0436 dB, respectively. Choosing a fourth-order filter, the normalized values for the corresponding low-pass prototype can be easily obtained from classical textbooks, [33]. Then, using well known expressions from [25], [27], we can compute the values of the coupling coefficients (k) and external quality factor (Q_e) of an equivalent circuit based on coupled resonators, which in our particular example are:

$$k_{12} = k_{34} = 0.0152$$

$$k_{23} = 0.0117$$

$$Q_e = 55.88$$
(6)

This equivalent circuit representation of the complete bandpass filter, based on coupled series resonators, is shown in Fig. 8, where all the input variables needed to compute its electrical response are included. In our particular filter example (of order 4 and considering a symmetrical implementation in two equal halves), the only involved variables are the cited Q_e , k_{12} , k_{23} , f_{01} and f_{02} , being f_{01} the resonance frequency of the first and fourth resonators, and f_{02} the one for the second and third resonators of our symmetric configuration.

Using the values for Q_e , k_{12} and k_{23} collected in (6), and choosing $f_{01} = f_{02} = 30$ GHz, we have obtained (using the commercial software *ADS*, from *Keysight*) the ideal bandpass response shown in Fig. 9, which is the objective to be recovered with the physical topology selected for implementing the combline filter.

In the proposed design procedure, we will obtain a first set of physical values for the filter geometrical variables following the well-known method described in [27]. The practical application of this method requires the previous design of the filter resonators, which in our case are the shortened nails discussed in Section III. Selecting the same hosting bed considered before (whose values are included in the caption of Fig. 7), and using the results of such figure, we have selected a value for

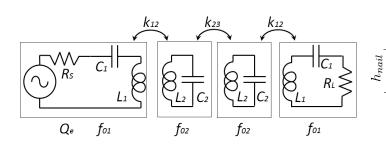


Fig. 8. Equivalent circuit representation of the filter based on series coupled resonators.

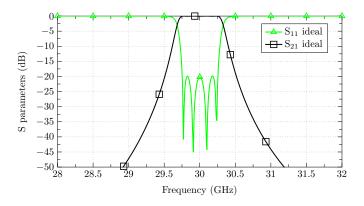


Fig. 9. Ideal band-pass response of the filter equivalent circuit.

 $h_{nailr} = 1.2 \text{ mm}$ (which provides, as requested, a resonance frequency equal to 30 GHz).

Next, we will explain how we can recover, with the appropriate physical structures, the requested values for the other electrical variables (i.e., Q_e , k_{12} and k_{23}) of our equivalent circuit representation.

A. External Quality Factor Implementation

The input and output cavities of the filter will be fed through two horizontally-polarized groove gap waveguides (GGWs), similar to the ones already employed in [21], that will be properly matched to standard rectangular waveguides WR28 ($a_{WR28} = 7.112$ mm, $b_{WR28} = 3.556$ mm) used for measurement purposes. Close to the metal base of the resonator the field is radial, thus presenting good matching with the fundamental mode of the GGW used for excitation. A side view of the considered input and output ports can be seen in Fig. 10, where all involved dimensions are included (the values for the hosting bed of square nails are the same ones used before).

As can be seen in Fig. 11, the feeding GGW is ended in a backshort, which is located at a distance, d_f , from the center of the first resonant shortened nail. This is the physical parameter to be optimized, in order to recover the ideal value for the Q_e electrical parameter found before (i.e., $Q_e = 55.88$).

According to [27], the Q_e value provided by an input coupling structure (in our case the one of Fig. 11) is evaluated as follows:

$$Q_e = \frac{\omega_0}{\Delta \omega_{\pm 90^o}} \tag{7}$$

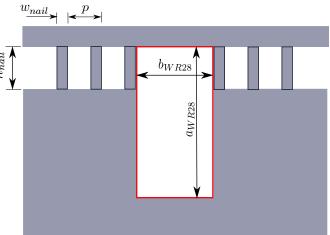


Fig. 10. Side view of an horizontally-polarized GGW feeding the proposed filter.

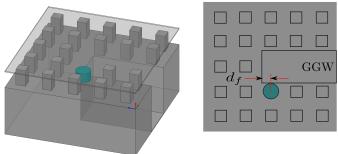


Fig. 11. 3D and 2D views of the input cavity, including the feeding GGW.

where ω_0 is the resonance frequency of the considered structure; and $\Delta \omega_{\pm 90^\circ}$ is the difference between the two angular frequencies where the phase of the S_{11} parameter is shifted, respectively, $\pm 90^\circ$ with respect to the phase value at ω_0 .

As recommended in [27], in order to obtain the exact value of ω_0 (due to potential loading effects in the structure of Fig. 11), we will compute the group delay of S_{11} through the expression:

$$\tau_{S_{11}}(\omega) = -\frac{\partial \phi_{S_{11}}}{\partial \omega} \tag{8}$$

being ω_0 the value of the angular frequency where the group delay is maximum.

For design purposes, we have first obtained (using ANSYS HFSS for the electromagnetic simulations) a curve relating the values of Q_e that can be achieved with the structure of Fig. 11 for different values of the distance d_f . From these results (displayed in Fig. 12), we select an initial value of d_f = 1.073 mm for recovering the requested value of Q_e = 55.88.

Additionally, in order to keep the resonance frequency of the loaded input cavity at 30 GHz (center frequency of the objective bandpass response), we have found a new value for the height of the first shortened nail (h_{nailr} =1.013 mm). For this purpose, a curve relating the resonant frequency of the considered structure (Fig. 11) in terms of $h_{nailr01}$ has been obtained. This new design curve resembles the one included

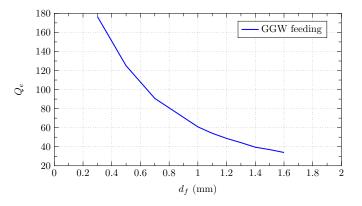


Fig. 12. Qe values versus the physical parameter d_f of the input cavity.

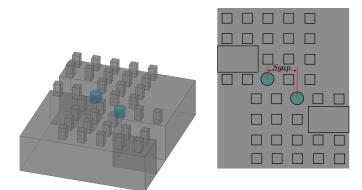


Fig. 13. 3D and 2D views of two coupled adjacent resonators, including weak excitation through GGWs.

in Fig. 7, but it can be now approximated by a linear equation with a slope m=-15.7 GHz/mm.

B. Coupling Implementation

In order to implement the coupling between adjacent resonant cavities, the geometrical configuration shown in Fig. 13 is proposed, where the distance, s_{gap} , between the two shortened nails of the resonators can be changed. This physical parameter will be optimized for realizing, in each case, the ideal value of the corresponding coupling coefficient previously computed (i.e., $k_{12} = 0.0152$ and $k_{23} = 0.0117$).

As can be observed in Fig. 13, and with the aim of preserving the density of the bed of square nails surrounding each resonant cylindrical post, the relative distance between consecutive rows of nails is kept constant. Proceeding in this way, the resonant behaviour of each shortened nail will be very practically equal to the one studied in Section III.

For computing the value of the coupling coefficient between the two coupled resonators, as explained in [27], we have weakly excited the structure (in our case with two GGWs as shown in Fig. 13). Then, the two frequencies, f_1 and f_2 , where the $|S_{21}|$ of the considered structure has two resonant peaks are identified, and used in the following expression for computing the value of k:

$$k = \frac{f_2^2 - f_1^2}{f_2^2 + f_1^2} \tag{9}$$

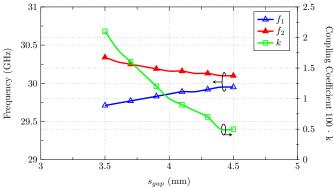


Fig. 14. Values for the frequencies f_1 and f_2 used in (9), and the corresponding k values, versus the physical distance s_{gap} between adjacent shortened nails.

TABLE I VALUES FOR ALL FILTER DESIGN VARIABLES

Elec. Par.	Opt. Value	Phys. Par.	Init. Value	Final Value
Q_e	55.88	$d_f(\text{mm})$	1.073	1.002
k_{12}	0.0152	$s_{gap12}(mm)$	3.715	3.743
k_{23}	0.0117	$s_{gap23}(mm)$	3.892	3.942
$f_{01}(\text{GHz})$	30	$h_{nailr01}(mm)$	1.012	0.989
$f_{02}(\text{GHz})$	30	$h_{nailr02}(mm)$	1.181	1.188

As we did before, a new design curve (using again AN-SYS HFSS for the full-wave electromagnetic analysis of the structure in Fig. 13) that relates the values of k that can be achieved with different separation (s_{gap}) between the coupled resonators was obtained. These results (included in Fig. 14) have been used to select initial values for s_{gap12} =3.715 mm and s_{gap23} =3.892 mm, which are able to provide, respectively, the requested ideal values for k_{12} and k_{23} of 0.0152 and 0.0117.

Again, due to the loading effect of the physical coupling on each adjacent cavity, their corresponding resonant frequencies are slightly detuned with regard to the center frequency of the bandpass response. In order to compensate this effect, a new value for the height of the shortened nails in the second and third cavities are obtained ($h_{nailr02} = 1.181$ mm). In order to find such value, a design curve relating the resonant frequency of the two coupled cavities (Fig. 13) with regard to $h_{nailr02}$ has been obtained. It is again very similar to the one included in Fig. 7, but its linear approximation has now a slope m=-21.0 GHz/mm.

C. Filter Optimization

A complete view of the proposed combline filter in gap waveguide technology can be seen in Fig. 15, and the initial values for all involved geometrical variables (obtained with the method just described before) are collected in Table I. The full-wave simulated results of the initially designed structure are shown in Fig. 16, where the ideal response of the equivalent circuit representation (with the optimum values of the electrical parameters summarized in Table I) is also included.

As can be seen in Fig. 16, the initial design of the proposed filter does not provide good enough results, so an optimization

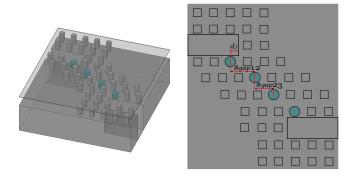


Fig. 15. 3D and 2D views of the proposed coaxial filter with shortened nails in gap waveguide technology.

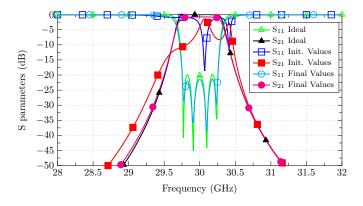


Fig. 16. Ideal and full-wave simulated responses (S-parameters) of the considered filter.

procedure of all involved geometrical variables should be performed in order to get results much closer to the ideal response. This optimization stage could be directly done using the employed full-wave electromagnetic simulator, but the involved computational effort (due to the intensive use of the employed accurate software tool) would be unaffordable.

In order to enhance this last optimization stage of the design procedure, we proposed in this work to use the Aggressive Space Mapping (ASM) technique, originally proposed by Prof. Bandler et al. in [26], and updated here (as detailed next) to make an efficient use of the equivalent circuit model based on coupled resonators (see Fig. 8). There are other alternative powerful approaches, that using model estimation and extraction methods, get the tuning of practical lossy microwave filters [34], [35] and [36].

Any ASM method makes use of two variable (or parameter) spaces, where two different tools (or models, known as "coarse" and "fine") are used for performing simulations of the component to be designed. In the coarse model space, an efficient simulation tool provides results without enough accuracy, whereas a more accurate analysis method (with a higher computational cost) is employed in the fine model space. Then, an iterative mapping between both simulation spaces is performed, thus finally providing an accurate optimal solution with a few number of fine model simulations.

In our particular case, the coarse space is defined with the five electrical parameters used as input variables in the equivalent circuit of the filter (see Fig. 8), i.e., $\mathbf{x}_c =$ $[Q_e \ k_{12} \ k_{23} \ f_{01} \ f_{02}]^T$, and the corresponding coarse model response, denoted as $\mathbf{R}_c(\mathbf{x}_c)$, will be obtained with the previously employed tool (i.e., *ADS* from *Keysight*). On the other hand, the fine space parameters are the physical dimensions of the proposed filter topology, i.e., $\mathbf{x}_f = [d_f \ s_{gap12} \ s_{gap23} \ h_{nailr01} \ h_{nailr02}]^T$, and *ANSYS HFSS* tool will provide the fine model response, i.e., $\mathbf{R}_f(\mathbf{x}_f)$. In order to start the ASM algorithm, we need to know an optimal solution in the coarse model space, called \mathbf{x}_c^* , whose values are the ones for the electrical parameters in Table I, and a first approximated solution in the fine model space, labelled as $\mathbf{x}_f^{(1)}$, which is obtained as indicated in Sections IV-A and IV-B (i.e., the initial values for the physical dimensions collected in Table I).

Then, an accurate mapping between the fine and coarse spaces, defined as $\mathbf{x}_c = \mathbf{P}_{fc}(\mathbf{x}_f)$, must be established. For this purpose, the *HFSS* fine model response, $\mathbf{R}_f(\mathbf{x}_f)$, will be fully recovered through an optimization process performed with the *ADS* software tool, which provides the values of the electrical parameters of the equivalent circuit, i.e., the corresponding \mathbf{x}_c .

Making use of the cited mapping procedure, we can easily obtain the first set of electrical parameters, i.e., $\mathbf{x}_c^{(1)}$, that provides the *HFSS* response shown in Fig. 16 for the initial values of the physical variables; and then compute the deviation between this solution and the optimal one in the coarse space, i.e., $\Delta \mathbf{x}_c^{(1)} = \mathbf{P}_{fc}(\mathbf{x}_f^{(1)}) - \mathbf{x}_c^*$.

Now, the iterative part of the ASM algorithm can be applied, thus solving the next equation for the *j*-th iteration (with j=1,2,...):

$$\mathbf{B}^{(j)}\Delta\mathbf{x}_f^{(j)} = -\Delta\mathbf{x}_c^{(j)} \tag{10}$$

and evaluating the new solution in the fine space as follows:

$$\mathbf{x}_f^{(j+1)} = \mathbf{x}_f^{(j)} + \Delta \mathbf{x}_f^{(j)} \tag{11}$$

In (10), $\mathbf{B}^{(j)}$ represents the approximation to the Jacobian (or mapping) matrix of the ASM algorithm at iteration j; that is updated by the classical Broyden formula, [37]:

$$\mathbf{B}^{(j+1)} = \mathbf{B}^{(j)} + \frac{\Delta \mathbf{x}_c^{(j+1)} \Delta \mathbf{x}_f^{(j)T}}{\Delta \mathbf{x}_f^{(j)T} \Delta \mathbf{x}_f^{(j)}}$$
(12)

Obviously, the mapping matrix must be initialized in the first iteration, i.e., $\mathbf{B}^{(1)}$, and this choice is key for the fastest and robust evolution of the ASM algorithm. In this work, we have used for $\mathbf{B}^{(1)}$ a diagonal matrix, whose meaningful elements are obtained as the derivatives of the corresponding design curves generated before (i.e., the ones included in Figs. 12 and 14), or taking directly the values of the slopes indicated in Sections IV-A and IV-B for the linear approximations of design curves similar to the one in Fig. 7.

The previous iterative process is ended when the fine model response at *j*-th iteration, $\mathbf{R}_f(\mathbf{x}_f^{(j)})$, is close enough to the ideal one, i.e., $\mathbf{R}_c(\mathbf{x}_c^*)$. Thanks to the proposed initialization of the mapping matrix, in our filter example, we have just needed five iterations to reach the optimal solution in the fine model space (see final values in Table I). The full-wave simulated

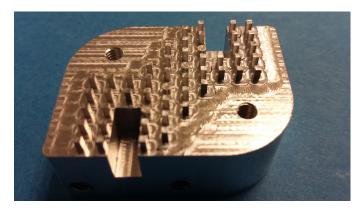


Fig. 17. Filter base piece, with periodic bed of nails, shortened cylindrical resonant nails, and input/output groove gap waveguides.

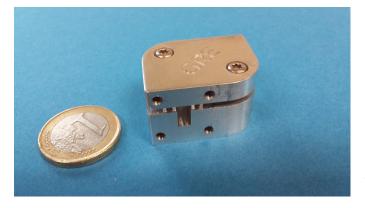


Fig. 18. Top metal cover of the filter fixed on top of the main body (base piece).

results of the designed combline filter, using *ANSYS HFSS*, is successfully compared to the ideal filter response in Fig. 16.

It is worth recalling that at each iteration of the ASM algorithm, the main computational cost is related to the corresponding full-wave *HFSS* simulation, being practically negligible the time effort requested by the optimization of the filter equivalent circuit performed with *ADS*. If the optimization process had been directly performed with the electromagnetic simulator, the number of requested iterations (and, therefore, of accurate simulations) would have been much larger than five, thus making the design process of the proposed filter rather inefficient and less robust.

V. EXPERIMENTAL RESULTS

The designed combline filter has been manufactured in gap waveguide technology, using a standard milling process with aluminum as base material. As it can be seen in Fig. 17, the supporting bed of nails, together with the excitation groove gap waveguides (GGWs) and the shortened resonant nails, are included in the same base piece (or main body of the filter). Then, a metal cover is fixed on top of the previous structure (see Fig. 18), ideally providing a perfect contact with the periodic bed of nails.

In Fig. 19 we show the measured results of the manufactured prototype, where it can be noticed a frequency shift of 210 MHz with regard to the simulated filter response,

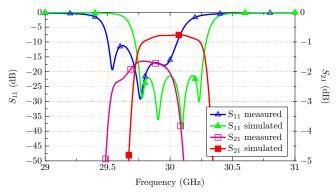


Fig. 19. Measured and simulated responses (S-parameters) of the manufactured filter prototype.

and in-band return losses below the ideal requirement of 20 dB. After performing an inspection of the main filter body with a metrology equipment, we detected an increment of 15 μ m in the height of the shortened nails with regard to the final design values, which explains the observed frequency shift. Furthermore, the corners of the input/output GGWs were not finished well enough, thus changing the value of the achieved external quality factor (affecting the measured in-band return loss level). In order to verify this, a new simulation taking into account the manufacturing errors has been done. Fig. 20 shows the new simulation results compared with measurements. It can be noted the agreement between the two responses of Fig. 20. These manufacturing errors could be taken into account in the filter design stage, thus alleviating its undesired effects with a second fabrication round. However, in order to avoid the manufacturing of a new filter prototype, we have tried to enhance the previous results for the in-band return losses by adding input/output matching networks. Taking advantage of available sections of standard WR28 waveguide of 3 cm fixed length, each matching network is composed of one piece of this waveguide length located between two reactive irises, which have been properly designed for matching purposes. A view of the manufactured pieces for the designed irises, as well as of the final test set-up (including the filter with the input/output matching networks), can be seen in Figs. 21 and 22, respectively. In order to avoid the use of these input/output matching networks, embedded screws located on top of the coaxial cavities and coupling apertures of the filter could have been used too. After properly fixing all these tuning screws, the measured response can be shifted in frequency to the desired nominal value, and the related return loss response substantially enhanced.

The measured results of the manufactured filter prototype, including now the designed input/output matching networks, is shown in Fig. 23, where it can be appreciated that in-band results have been improved (with regard to the experimental data of Fig. 19). In particular, a return loss level higher than 16.6 dB has been recovered in the frequency range between 29.535 GHz and 30.015 GHz, thus providing a useful bandwidth of 480 MHz (rather close to the 500 MHz specification of the ideal filter response). A minimum value of 1.607 dB has been measured for the in-band insertion losses

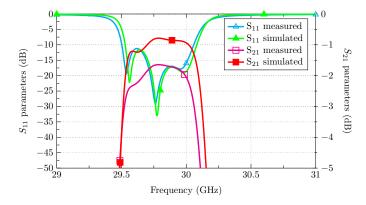


Fig. 20. Measured and simulated with manufactured errors responses (Sparameters) of the filter prototype.



Fig. 21. View of the manufactured irises of the designed matching networks.

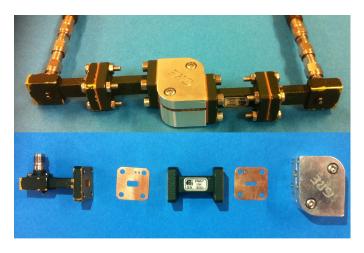


Fig. 22. Complete view of the test set-up for measuring the manufactured filter with input/output matching networks.

of the filter (including the matching networks), whereas the simulated value with *ANSYS HFSS* for the designed filter (without matching networks and considering aluminum as material) was just 0.76 dB.

VI. CONCLUSION

A compact topology for implementing combline filters in gap waveguide technology, providing bandpass responses at high frequencies, has been successfully proposed. For this purpose, we have employed shortened cylindrical nails as resonators, which are fully integrated in a periodic structure (bed of square nails) with a stopband behaviour. The resonance behaviour of the considered resonators has been studied and properly modeled with an equivalent circuit. Effective coupling mechanisms between adjacent resonators, as well as for the

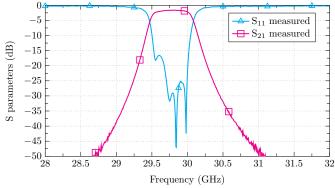


Fig. 23. Measured results (S-parameters) of the manufactured filter prototype including the input/output matching networks.

input and output excitation of the filter with GGWs, have been detailed; including design curves relating the physical parameters of the filter topology with electrical parameters of an equivalent circuit representation. A more efficient procedure for optimizing the physical dimensions of the proposed filter topology, making use of an updated version of the ASM technique, has been also derived and illustrated with a practical design example. For validation purposes, a prototype of a designed combline filter (with a bandpass response of 1.7% relative bandwidth at 30 GHz) has been manufactured and measured. The proposed filters can be easily embedded, together with other components, within a hosting structure based on a bed of nails, thus making feasible the practical realization of integrated subsystems in gap waveguide technology.

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