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Additional Information

1 **NUMERICAL OPTIMIZATION OF AN EJECTOR FOR WASTE HEAT**
2 **RECOVERY USED TO COOL DOWN THE INTAKE AIR IN AN IC**
3 **ENGINE**

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6 **Abstract**

7 In the present paper, a numerical investigation of a jet-ejector is carried out using a real gas
8 model of R1234yf. The prototype under investigation works with specific operating conditions
9 of a jet-ejector refrigeration system intended for waste heat recovery in an internal combustion
10 engine. In the first instance, the geometry optimization involving nozzle exit diameter, mixing
11 chamber diameter and nozzle exit position is performed. Once the optimum geometry has been
12 obtained, the jet-ejector prototype is tested with different operating pressure ratios to
13 determine its off-design performance. The flow structure in relevant cases has been examined
14 with an emphasis on critical and subcritical modes. The flow phenomena occurring during
15 expansion, entrainment and mixing processes are discussed so performance degradation can be
16 directly related to physical processes. The analysis has been completed fitting simulated points
17 to critical and subcritical planar surfaces. The results in terms of goodness of fit are satisfactory
18 so the jet-ejector performance in off-design operating conditions can be reflected through
19 simple mathematic models. When the overall cycle is assessed by using previous CFD maps it is
20 observed that the achievable cooling drops significantly when an ambient temperature of 31 °C
21 is exceeded.

22 **Keywords**

23 Waste heat recovery, jet-ejector cycle, adiabatic engine, jet-ejector optimization, engine
24 efficiency, R1234yf

25 **Nomenclature**

26 **Acronyms**

ICE	Internal Combustion Engine
CFD	Computational Fluid Dynamics
COP	Coefficient Of Performance
GWP	Global Warming Potential

27

28 **Notation**

29 **Latin**

A	Area (m ²)
c	Specific Heat Capacity (J/kg·K)
D	Diameter (mm)
h	Specific enthalpy (J/kg)
k	Pump pressure ratio (-)
L	Length (mm)
\dot{m}	Mass flow rate (kg/s)
P	Pressure (bar)
\dot{Q}	Heat exchanger power (W)
\dot{W}	Mechanical power (W)
Z	Mesh zone

30 Greek letters

α	Angle (°)
β	Curve fit coefficient (-)
κ	Fraction of the available heat power at the exhaust line (-)
λ	Jet-ejector scaling factor (-)
π	Jet-ejector pressure ratio (-)
ω	Entrainment ratio (-)

31 Subscripts

1 – 8	Cycle state points
I – VI	Generic index
<i>amb</i>	Ambient conditions
<i>crit</i>	Jet-ejector critical operational mode
<i>e</i>	Jet-Ejector
<i>ev</i>	Ejection cycle evaporator
<i>ex</i>	Engine exhaust
<i>ft</i>	Curve fitting
<i>ge</i>	Ejection cycle generator
<i>i</i>	Inlet flow
<i>in</i>	Engine intake
<i>max</i>	Maximum
<i>o</i>	Outlet flow
<i>OD</i>	Off-design conditions
<i>p</i>	Primary flow

<i>pm</i>	Ejection cycle pump
<i>ref</i>	Reference conditions
<i>s</i>	Secondary flow
<i>scrit</i>	Ejector subcritical operational mode
<i>sm</i>	Simulated
<i>sup</i>	Superheating temperature
<i>v</i>	Expansion valve

32

33 1. INTRODUCTION

34

35 Over the past decades, many research projects have focused on the improvement of ejection
 36 cycles in search of a refrigeration technology with lower environmental impact. Ejection cycles
 37 seem to be a promising way of taking advantage of low-grade waste heat coming from industrial
 38 processes, vehicle exhaust or solar energy reducing significantly the electric power consumed
 39 by conventional refrigeration systems.

40 In comparison with traditional vapor-compression refrigeration systems, they present lower
 41 mechanical complexity as well as improved reliability and lifespan (Varga et al., 2009; Yan et al.,
 42 2012). However, poor performance when operating in off-design conditions has been reported.
 43 This well-known factor together with their low COP is responsible for the limited market
 44 penetration up to now (He et al., 2009).

45 On ejection cycles, a secondary flow characterized by low temperature and pressure generates
 46 a cooling capacity at the evaporator, absorbing heat from the medium to be cooled. The primary
 47 flow, which has received energy at the generator from a low-grade heat source, expands within
 48 a nozzle at the jet-ejector inlet thereby enabling the suction of secondary flow inside the jet-
 49 ejector. Both flows mix completely, leave the jet-ejector and condense at an intermediate

50 pressure. As a result of the condensation, heat is rejected to ambient. Downstream the
51 condenser the liquid splits: a fraction of total mass flow passes through a liquid pump and the
52 resulting high-pressure fluid is recirculated to the generator thus completing the power loop.
53 The rest of the available mass flow expands at an expansion valve and evaporates closing the
54 refrigeration loop and producing the desired cooling capacity.

55 Jet-ejector improvement is a key factor to maximize the performance of ejection cycles. The
56 geometric configuration and the operating conditions dramatically affect the entrainment
57 process so a deep understanding of flow evolution inside the jet-ejector is essential. Specific
58 design for a certain application and operating conditions is needed. Both experimental,
59 numerical and analytical studies comprise the main development methodologies. Studies
60 concerning the jet-ejector design (Dong et al., 2016; Jia and Wenjian, 2012; Ruangtrakoon et al.,
61 2013; Wang et al., 2017; Yan et al., 2012; Zhu et al., 2009) and modeling (Soroureddin et al.,
62 2013) are quite common in the literature. Many research papers have been focused on studying
63 fundamental phenomena occurring inside the jet-ejector since it is the basis for improving the
64 entrainment process (Ruangtrakoon et al., 2013; Sargolzaei et al., 2010; Zhu and Jiang, 2014a,
65 2014b).

66 When applied to a vehicle this energy-efficient cycle is developed within the framework of
67 different strategies of waste heat recovery (WHR) dedicated to reusing the exhaust waste heat.
68 In the last few years, the need for cleaner vehicles with lower environmental impact is leading
69 to a growing interest in these technologies. On an internal combustion engine (ICE) for
70 automotive applications, approximately one-third of available fuel energy is lost as exhaust
71 waste heat and an additional one third is rejected to ambient at the cooling water system.
72 Several approaches have been under investigation to unlock this potential (Armstead and Miers,
73 2013) with special emphasis on: Intake charge heating, applied specifically during warm-up
74 process (Luján et al., 2016), turbocompounding systems (Aghaali and Ångström, 2015),

75 thermoelectric generators (Hsiao et al., 2010; In and Lee, 2016), Rankine cycles (Aly, 1988; Dolz
76 et al., 2012; J. Galindo et al., 2015; Glover et al., 2014), ejection or absorption cycles (Galindo et
77 al., 2019; Novella et al., 2017; Zegenhagen and Ziegler, 2015a) and Brayton, Stirling or Ericsson
78 cycles (J Galindo et al., 2015).

79 The feasibility of cooling down the engine intake by using a jet-ejector cycle with R134a as
80 working fluid has been studied before by Zegenhagen and Ziegler (Zegenhagen and Ziegler,
81 2015a), (Zegenhagen and Ziegler, 2015b) following an experimental approach. The attained
82 cooling capacities ranged between 2.3 kW and 5.3 kW with charge air temperatures ranging
83 between 270.8 K and 284.8 K depending on boundary conditions. Recently, Galindo et al.
84 (Galindo et al., 2019) have evaluated and optimized numerically the performance of a jet-ejector
85 refrigeration cycle intended for charge air cooling in an ICE. Special emphasis is put on
86 performance degradation away from design conditions, that is, different engine operating
87 points. They showed that ICE charge air temperature can be reduced from $\sim 40^{\circ}\text{C}$ to $\sim 0^{\circ}\text{C}$ if the
88 jet-ejector size is given as a design variable. Otherwise, the achievable cooling capacity is
89 seriously reduced.

90 Beyond these experimental and analytical approaches, none numerical studies have been found
91 for this particular application. Numerous numerical studies focused on jet-ejector modeling can
92 be found in the literature with a general approach, however, almost all of them focus on ideal
93 gas models, (Bartosiewicz et al., 2005; Chen et al., 2013; Mazzelli et al., 2015; Ruangtrakoon et
94 al., 2013; Sriveerakul et al., 2007) or algebraic equations of state (Mazzelli and Milazzo, 2015)
95 since the convergence for real gas models is more complex. Some of these studies have set low
96 operating pressures so the differences between real gas models and the aforementioned
97 approaches might not be significant. Croquer et al. (Croquer et al., 2016), carried out simulations
98 with real gas models (R134a) and their operating pressures are similar to those of the present
99 paper, however, their research work is not dealing with a jet-ejector optimization and off-design

100 performance evaluation.

101 The main innovative aspect of the present paper is the geometric design and characterization of
102 a jet-ejector implemented in a jet-ejector refrigeration system intended for intake air cooling in
103 an ICE. As a novelty, R1234yf is used as working fluid and the performance of the optimized jet-
104 ejector design is assessed from the perspective of the overall refrigeration system operating in
105 off-design ambient conditions.

106 The main objective of this study is the numerical optimization of a jet-ejector working under
107 specific conditions of an ICE in terms of exhaust energy and required cooling capacities. This
108 application (ICE intake cooling) gives the work its main originality. All calculations have been
109 performed using real gas models of a new generation refrigerant (R1234yf). As a result, a non-
110 dimensional expression which collects information related to the geometry and off-design
111 operating conditions is presented. The secondary objective of the present paper is to evaluate
112 the performance degradation of the overall ejection cycle when the ambient temperature
113 increases. For that purpose, the jet-ejector maps computed with CFD play a major role.

114 This methodology could be applied to introduce the jet-ejector behavior in theoretical models
115 of the overall cycle including heat exchangers, expansion valve and pump.

116

117 2. EJECTION CYCLE INTEGRATION AND EVALUATION PROCESS

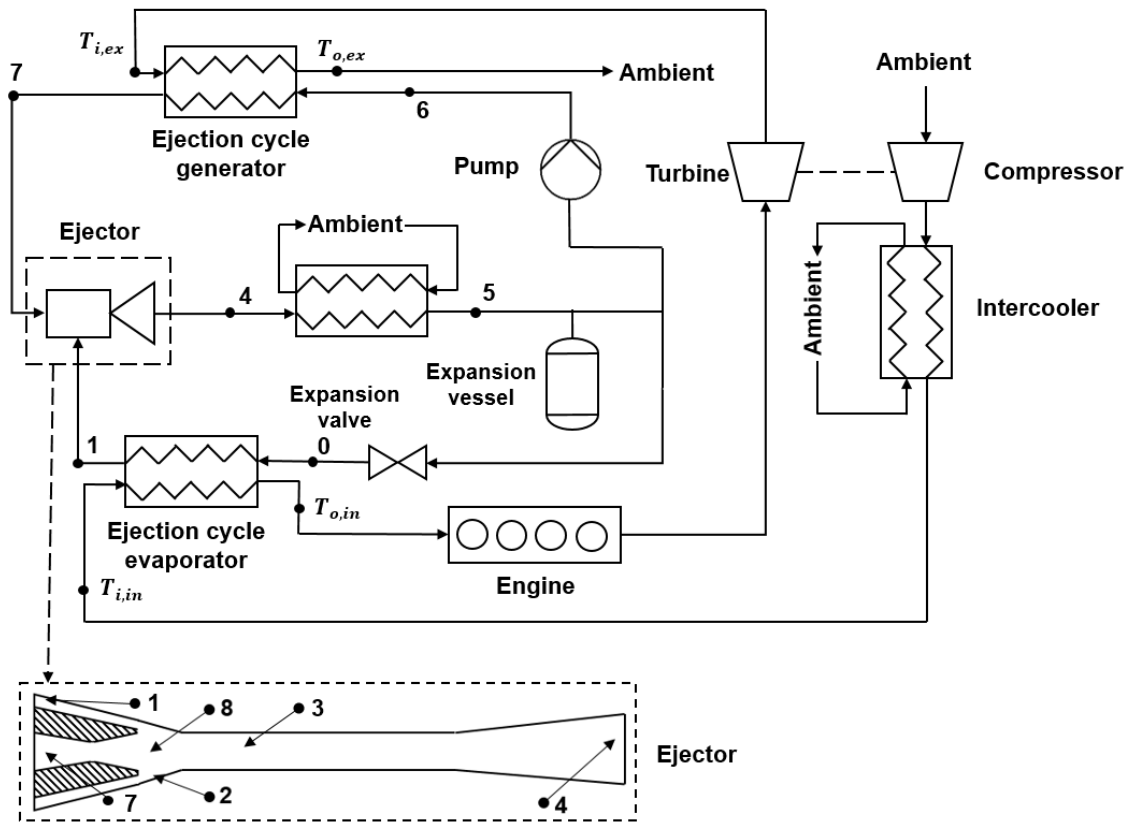
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119 In Figure 1 a jet-ejector refrigeration system equipped in an automotive ICE is schematically
120 illustrated. The jet-ejector refrigeration system is coupled in the ICE downstream of the
121 intercooler and at the exhaust line downstream of the turbine. The heat exchanger placed at
122 the engine intake is intended to produce the cooling effect at the engine intake while the
123 generator transfers heat from the exhaust line to the refrigerant to drive the primary flow. The
124 jet-ejector is the key element of the cycle and its limitations when adapting to off-design

125 operating conditions dramatically affect cycle performance. Therefore, this component plays a
126 major role in a jet-ejector refrigeration system coupled in an ICE and its dimensions must be
127 carefully designed for a particular cooling capacity requirement, ambient temperature and
128 exhaust thermal level.

129 The logic flow chart of the steps followed in the jet-ejector characterization stage and overall
130 cycle evaluation are schematically illustrated in Figure 2. The paper is structured in four parts.
131 In Section 3, the jet-ejector geometry is described and the numerical setup is presented with
132 special emphasis on boundary conditions, thermodynamic model and validation of the CFD
133 approach. Also in Section 3, the jet-ejector dimensions involved in parametric optimization are
134 presented. In Section 4, the theoretical model used to describe the overall system performance
135 is presented.

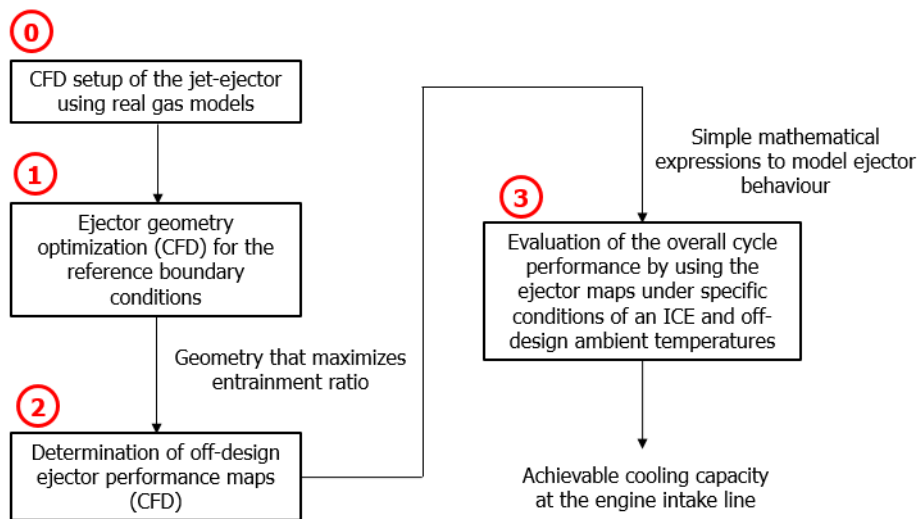
136 In Section 5, the main results are presented. Firstly, the geometry that maximizes the
137 entrainment ratio is found. Special attention is paid to the flow pattern in optimized and non-
138 optimized geometries. Then, the optimum jet-ejector design is evaluated against different
139 evaporating and condensing pressures to find the jet-ejector characteristic maps. Subsequently,
140 the aforementioned maps are used to feed a 1D model overall cycle to assess the performance
141 degradation that occurs when the ambient temperature is increased with a fixed jet-ejector size.
142 Finally, in Section 6, the most relevant findings are summarized.



143

144

Figure 1. Jet-ejector refrigeration system coupled in an ICE



145

146

Figure 2. Calculation sequence of the jet-ejector and the overall cycle, respectively

147

3. JET-EJECTOR MODELING

148

149

150 In this section, the geometry of the jet-ejector prototype is presented as well as the setup in the
151 Computational Fluid Dynamics (CFD) code including the descriptions of the mesh, turbulence
152 model, thermodynamic model and boundary conditions. Subsequently, the CFD approach used
153 to model the jet-ejector behavior is validated using experimental data.

154 3.1 Working fluid selection

155

156 R1234yf has been used as the working fluid in the present study due to its reduced
157 environmental impact (GWP = 4) as well as its widespread use in modern automotive air
158 conditioning systems. It is an energy-efficient replacement for R134a and its implementation
159 requires minor modifications in actual automotive equipment (Lee and Jung, 2012), (Vaghela,
160 2017). This new generation refrigerant exhibits low toxicity, however, it is flammable so safety
161 measures must be adopted to cope with leaks during service.

162

163 3.2 Jet-ejector flow phenomena and geometry description

164

165 In the present jet-ejector design, the high-pressure primary flow (7) is expanded in a converging-
166 diverging nozzle reaching sonic conditions at the nozzle throat with a subsequent increase in
167 supersonic level owing to expansion at the diverging section. The subsequent pressure reduction
168 downstream nozzle exit region (8) favors secondary flow entrainment at the suction chamber
169 (2). Only a little fraction of both flows mix in the first instance but the primary flow boundary is
170 clearly delimited creating an apparent converging duct with the wall where secondary flow
171 expands. Once the secondary flow is expanded a mixing process characterized by momentum
172 transference from primary to secondary flow occurs (3). Due to the higher outlet backpressure,
173 additional shockwave pattern appears along the constant area zone. Therefore, the mixed flow
174 returns to subsonic conditions and the static pressure of the mixed flow increases. Mixed flow
175 leaves the ejector with an additional pressure recovery induced by the subsonic diffuser (4).

176 The entrainment ratio, i.e, the ratio between secondary and primary mass flow ($\omega = \dot{m}_s/\dot{m}_p$)
177 has been selected as the reference performance parameter. From the performance perspective,
178 high entrainment ratio values have a positive impact on the cooling capacity and COP. According
179 to Figure 1, cooling capacity and COP of the ejection cycle under investigation are defined as
180 follows:

$$\dot{Q}_{ev} = \dot{m}_s \cdot (h_1 - h_0) \quad (1)$$

181

$$COP = \frac{\dot{Q}_{ev}}{\dot{Q}_{ge} + \dot{W}_{pm}} \approx \frac{\dot{m}_s}{\dot{m}_p} \cdot \frac{(h_1 - h_0)}{(h_7 - h_6)} = \omega \cdot \frac{(h_1 - h_0)}{(h_7 - h_6)} \quad (2)$$

182 It must be noted that the input power to drive the pump has been neglected in the COP
183 definition because it is much lower than the incoming heat power.

184 Figure 3 depicts a schematic view of the axisymmetric jet-ejector prototype under investigation
185 with all the relevant dimensions. The geometric optimization has been carried out for different
186 nozzle exit diameters ($D_{e,3}$), constant mixing diameters ($D_{e,4}$) and nozzle exit positions ($L_{e,2}$)
187 for a fixed nozzle throat diameter ($D_{e,2}$). The primary nozzle throat has remained constant in all
188 simulations, thus fixing the critical mass flow when primary pressure and temperature are
189 maintained.

190

191 The diffuser length and the mixing chamber length have been assigned to ensure negligible
192 gradients of both pressure and Mach number on the radial direction at the jet-ejector outlet.
193 Several preliminary studies concerning the jet-ejector geometry have been conducted to fix
194 some geometric values that do not have a strong influence over the jet-ejector performance. All
195 the dimensions involved in the geometrical design of the jet-ejector are presented in Table 1.

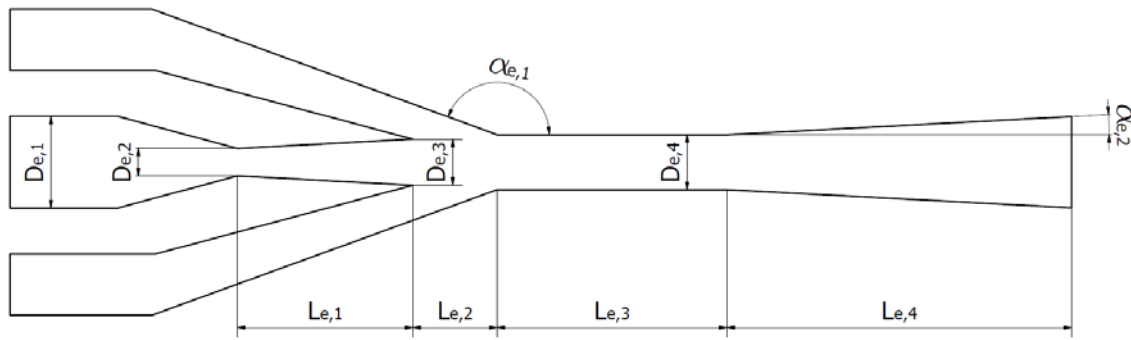


Figure 3. Jet-ejector axisymmetric design

Dimension		Value	Dimension		Value
$\alpha_{e,1} [^\circ]$	Constant	150	$D_{e,4} [mm]$	Variable	[3.2, 3.8]
$\alpha_{e,2} [^\circ]$	Constant	3	$L_{e,1} [mm]$	Constant	11.5
$D_{e,1} [mm]$	Constant	6	$L_{e,2} [mm]$	Variable	[4,7]
$D_{e,2} [mm]$	Constant	1.8	$L_{e,3} [mm]$	Constant	30
$D_{e,3} [mm]$	Variable	[2.6, 3.2]	$L_{e,4} [mm]$	Constant	45

Table 1. Dimensions of the jet-ejector model

The jet-ejector area ratio, that is, the ratio between the mixing chamber area and the primary nozzle throat area, has proven to be one of the most sensitive parameters on ejector performance and its influence over the mixing process has been widely studied in the literature (Varga et al., 2009; Wang et al., 2018). For this reason, it has been treated as a design variable. Additionally, the nozzle exit area determines the expansion level of the primary flow, i.e., Mach number of primary flow leaving the nozzle. The influence over the jet-ejector internal phenomena has proven to be decisive (Ruangtrakoon et al., 2013) so it has been considered as the second geometric variable under investigation. The nozzle exit position (NXP) is also crucial in the jet-ejector operation (Chen et al., 2015) and it must be optimized together with the primary nozzle exit diameter and mixing chamber diameter to maximize the jet-ejector

215 performance. It must be noted that for a fixed nozzle throat, the mixing chamber diameter
216 ($D_{e,4}$), the primary nozzle exit diameter ($D_{e,3}$) and the nozzle exit position ($L_{e,2}$) govern primary
217 flow expansion as well as the suction and mixing processes of the secondary flow.

218 A parametric factorial study has been conducted with $D_{e,3}$, $D_{e,4}$ and $L_{e,2}$ to find the best
219 combination in terms of entrainment ratio maximization. The range of these geometric variables
220 is specified in Table 1. The mesh of the computational domain has been adapted for each case
221 according to changes in geometry.

222 Concerning the weight of the jet-ejector and the hypothetical penalty over the vehicle,
223 Zegenhagen and Ziegler (Zegenhagen and Ziegler, 2015a) reported a gravimetric power density
224 of 0.6-1.3 kW (of cooling capacity)/kg for the jet-ejector considering real equipment. This
225 reference is useful to provide an estimation of the jet-ejector expected mass but it would
226 depend on each particular design. The present jet-ejector is intended to be implemented in a
227 refrigeration system with a cooling capacity of approximately 2kW. Assuming the
228 aforementioned gravimetric power density, a mass of 1.5 kg could be a reasonable
229 approximation.

230

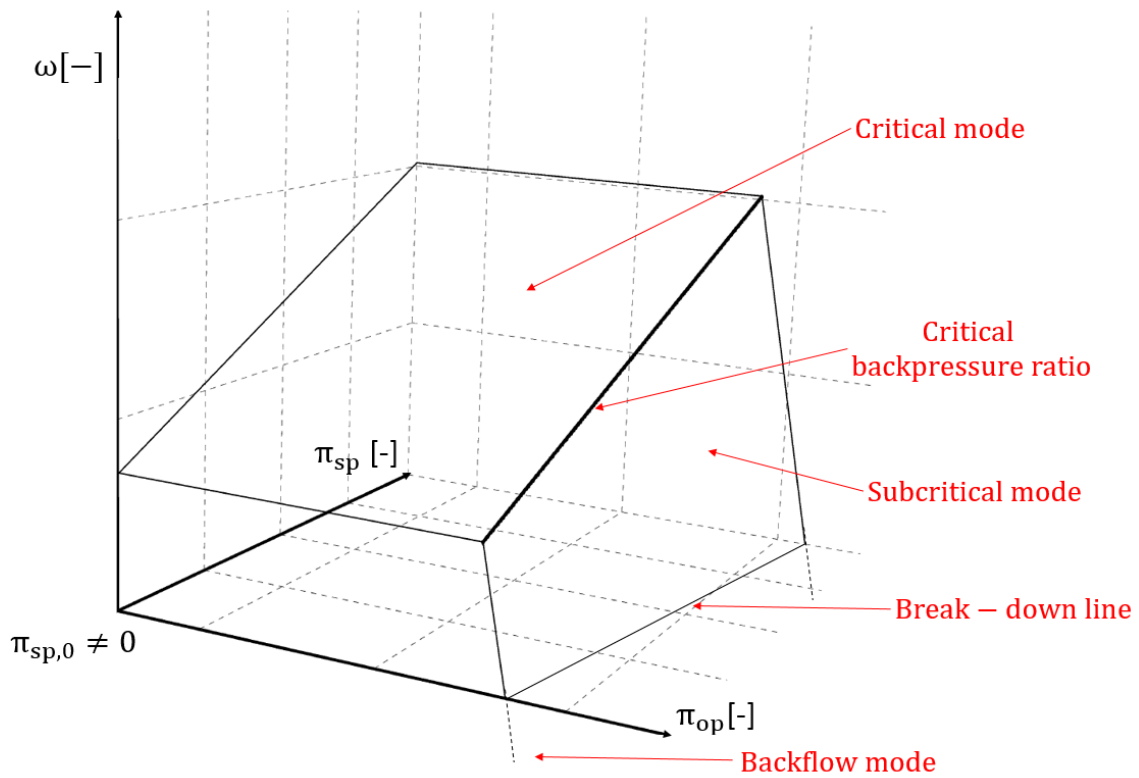
231 3.3 Jet-ejector off-design performance maps

232

233 In this subsection, the jet-ejector performance maps representing the entrainment ratio against
234 the operating pressure ratios are introduced. The operating conditions of an ejection cycle
235 intended for ICE intake cooling can change significantly depending on cooling requirements or
236 the ambient conditions. Hence, for this particular application, the ejection cycle operation would
237 be far from being steady and off-design evaluation has a special significance.

238 Off-design jet-ejector performance is usually evaluated by means of a characteristic surface
239 (Zegenhagen and Ziegler, 2015a, 2015b) which represents the operating pressures expressed as
240 pressure ratios ($\pi_{sp} = P_s/P_p$ and $\pi_{op} = P_o/P_p$) together with entrainment ratio ($\omega = \dot{m}_s/\dot{m}_p$).

241 Resulting operating modes are depicted in Figure 4 keeping constant the primary pressure (P_p)
 242 in order to simplify the analysis.
 243



244

245

Figure 4. Jet-ejector characteristic surfaces

246

247 According to jet-ejector maps of Figure 4, three different modes can be distinguished: double-
 248 choking mode also known as critical mode, single-choking mode, known as subcritical mode and
 249 backflow mode. In the double-choking mode, both primary and secondary flows reach
 250 supersonic conditions and the entrainment ratio does not depend on the jet-ejector
 251 backpressure (outlet pressure) until a certain critical value if the primary pressure is fixed. The
 252 primary flow reaches sonic conditions during the expansion on the converging-diverging nozzle
 253 and the secondary flow is accelerated to sonic conditions as it passes through a converging duct
 254 created by the shockwave structure downstream the primary nozzle. This 'effective area' is

255 produced at the mixing chamber and its position depends on operating conditions and
256 geometry. Double-choking operating mode corresponds to the desired ejector operating mode.

257 In single-choking mode, the critical backpressure is exceeded and only the primary flow is
258 choked. In this case, the relatively high backpressure shifts oblique shockwaves induced
259 upstream the diffuser (called second shockwave pattern) toward the primary nozzle, thus
260 affecting the mixing process. Therefore, the entrainment process of the secondary flow is
261 altered and the jet-ejector entrainment ratio is not independent of jet-ejector backpressure.
262 Once the jet-ejector critical backpressure is exceeded secondary mass flow is reduced with the
263 increase of the jet-ejector backpressure. A further increase can lead to the break-down line
264 where no secondary mass flow is entrained. This operating mode should be avoided because
265 slight variations in jet-ejector backpressure can lead to significant performance degradation.

266 In backflow mode, the break-down pressure (Figure 4) is exceeded and the second shockwave
267 moves upstream affecting primary expanded flow. With the disturbance of primary flow
268 expansion, it tends to penetrate into the secondary duct flowing upstream. It is considered as a
269 malfunctioning mode because the jet-ejector is unable to entrain secondary flow.

270 When the critical pressure is exceeded the entrainment ratio drops dramatically with the
271 subsequent reduction in cooling capacity and COP. Thus, critical, subcritical and backflow modes
272 are directly dependent on operating conditions and off-design operation can lead to severe
273 performance degradation.

274 Both critical and subcritical performance maps are expressed in Equations 3-7. The aim of the
275 off-design study is obtaining the fitting coefficients β_{I-VI} . For that purpose, the response of the
276 optimum geometry has been evaluated over different pressure ratios, $\pi_{sp} \in [0.103, 0.152]$ and
277 $\pi_{op} \in [0.300, 0.376]$.

$$\omega(\pi_{sp}, \pi_{op}) = \frac{\dot{m}_s}{\dot{m}_p} \quad (3)$$

$$\omega_{crit}(\pi_{sp}, \pi_{op}) = \beta_I + \beta_{II} \cdot \pi_{sp} + \beta_{III} \cdot \pi_{op} \quad (4)$$

$$\omega_{scrit}(\pi_{sp}, \pi_{op}) = \beta_{IV} + \beta_V \cdot \pi_{sp} + \beta_{VI} \cdot \pi_{op} \quad (5)$$

$$\omega(\pi_{sp}, \pi_{op}) = \omega_{crit}(\pi_{sp}, \pi_{op}) \quad \text{if} \quad \omega_{crit}(\pi_{sp}, \pi_{op}) \leq \omega_{scrit}(\pi_{sp}, \pi_{op}) \quad (6)$$

$$\omega(\pi_{sp}, \pi_{op}) = \omega_{scrit}(\pi_{sp}, \pi_{op}) \quad \text{if} \quad \omega_{crit}(\pi_{sp}, \pi_{op}) > \omega_{scrit}(\pi_{sp}, \pi_{op}) \quad (7)$$

278

279 3.4 Computational characterization

280 3.4.1 Numerical simulation setup

281

282 Numerical simulations of the jet-ejector internal flow over different geometries and boundary
 283 conditions have been accomplished. All the cases under investigation have been simulated using
 284 a computational fluid dynamics (CFD) code based on the finite volume method. The governing
 285 equations are based on mass, momentum and energy conservation. The three-dimensional
 286 geometry of this particular problem has been taken into account by considering a 2D domain
 287 with axisymmetry. Steady-state conditions and compressible turbulent flow are assumed since
 288 the flow inside the jet-ejector is thought to be supersonic according to the operating pressures.
 289 The computational code assumes that the fluid behaves as superheated vapor, supercritical
 290 fluid, or liquid. Two-phase subcritical flow conditions, where vapor coexists with liquid, are not
 291 supported. In the event of two-phase flow during primary nozzle expansion, the calculation is
 292 automatically stopped.

293 As the working fluid used in the jet-ejector is R1234yf and the operating pressures are relatively
 294 high, the perfect gas assumption may not be an accurate approach (Zegenhagen and Ziegler,
 295 2015c). Instead, libraries containing thermodynamic properties of R1234yf are dynamically

296 loaded into the solver when real gas models are activated. This causes certain difficulties to start
297 and stabilize the calculations. First-order upwind spatial discretization schemes for turbulence
298 and conservation equations are used in the first instance and then switched to a second-order
299 scheme when stability is attained. At the early stages of calculation, the SIMPLE pressure-
300 velocity coupling scheme is considered and then switched to a Coupled scheme after reaching
301 final boundary conditions and stabilization. Least Square Cell-Based is selected as gradient
302 scheme and diffusion terms are discretized following a second-order central difference form.
303 The pressure-based coupling model has been employed because current implementations of
304 this approach have been reformulated in order to work successfully with high Mach number
305 compressible flow. Furthermore, satisfactory results implementing this approach when
306 simulating jet-ejector internal flow have been reported in the literature (Croquer et al., 2016).
307 Density-based formulations have been also tested but offered poor performance in terms of
308 stability.

309 The Reynolds Averaged Navier Stokes (RANS) approach has been employed in all simulations,
310 and the standard $k - \epsilon$ has been selected as the turbulence model. Despite it is not the most
311 recommended turbulence model while simulating supersonic flow in jet-ejectors it has proved
312 to do an accurate description of phenomena occurring inside the jet-ejector as well as accurate
313 predictions of global flow parameters like entrainment ratio (Besagni et al., 2015; Croquer et al.,
314 2016; Gagan et al., 2014; Hakkaki-Fard et al., 2015). Standard wall functions have been
315 considered as the near-wall formulation scheme in accordance with the turbulence model and
316 y^+ values (Besagni and Inzoli, 2017).

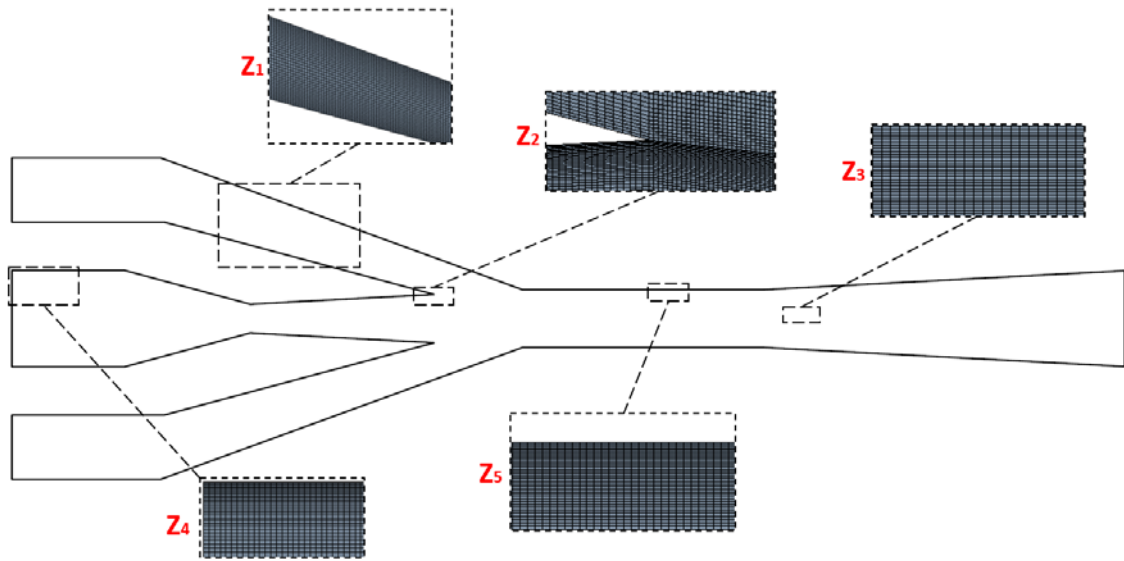
317 A quadrilateral structured mesh with wall refinement (Figure 5) is selected due to the prevalence
318 of axial flow. Global skewness, orthogonal quality and aspect ratio are checked as quality
319 indicators. The number of cells of the computational domain is around 55,000 in all simulations
320 with slight variations due to the different dimensions of each geometry in the parametric study.

321 The influence of the number of elements is evaluated by comparing the Mach number along the
322 jet-ejector axis and the entrainment ratio of three cases with different mesh refinement (Figure
323 6). There are small discrepancies in the position and magnitude of strong shockwaves, however,
324 differences in entrainment ratio are lower than 1% with respect to the case with the highest
325 number of cells.

326 The discrepancies found in Mach number distribution in some axial positions can be attributed
327 to the strong gradients occurring due to the shockwave pattern. It is common in the literature
328 to carry out a detailed mesh refinement in these particular zones to capture the shockwave
329 structure. In the present paper, priority was given to the computational economy due to the
330 high number of simulations that were required to perform an exhaustive optimization of the jet-
331 ejector internal geometry. These minor differences are considered as admissible so the mesh
332 with the lower number of elements (54,600) is selected according to the following criteria:

- 333 • The flow phenomena occurring inside the jet-ejector is described only from a qualitative
334 point of view. Therefore, the main trends described on the flow pattern when the jet-
335 ejector internal geometry is modified would remain valid, regardless of the slight
336 discrepancies in the position and magnitude of strong shockwaves.
- 337 • The global performance of the jet-ejector is computed from a quantitative point of view
338 by using the jet-ejector entrainment ratio. The validation process as well as the low
339 discrepancies between the three meshes under consideration (less than <1%) guarantee
340 that this global parameter is correctly predicted.

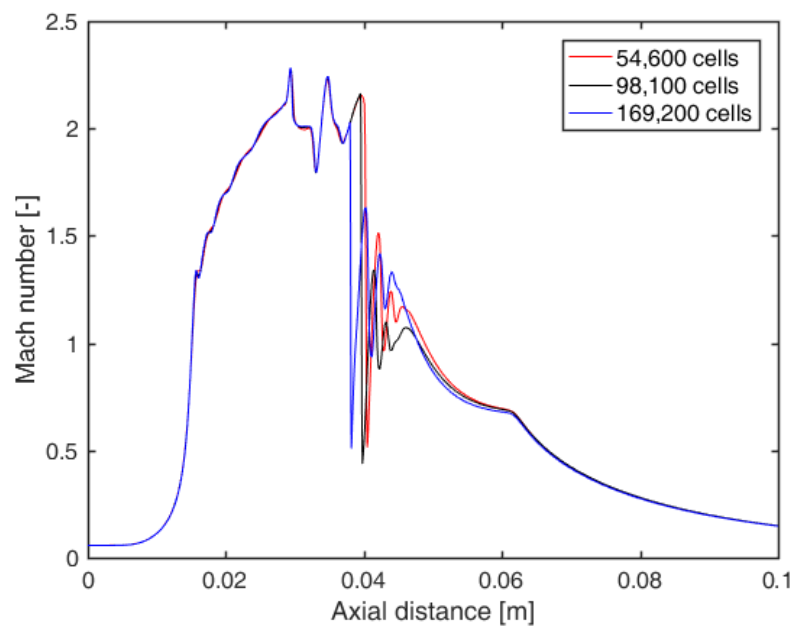
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342

343 *Figure 5. Details of the mesh grid. The element size in the radial direction in each zone corresponds to $1.3e-4$ m (Z_1),*

344 *$5e-5$ m (Z_2), $4e-5$ m (Z_3 near the axis), $1e-4$ m (Z_4), $2e-5$ m (Z_5 near the wall).*



345

346 *Figure 6. Mach number along the jet-ejector axis for cases with different mesh refinement*

347

348 **3.4.2 Boundary conditions**

349

350 The jet-ejector operating pressures/temperatures have been selected depending on cooling
 351 requirements and ambient conditions. Table 2 summarizes the reference operating conditions
 352 (expressed as saturation conditions) considered to perform the computational calculations.

Working Fluid: R1234yf	Value	Units	State number in Figure 1
Condensing pressure (mixed flow)	10.7	[bar]	(4)
Condensing temperature (mixed flow)	42	[°C]	(4)
Evaporating pressure (secondary flow)	3.2	[bar]	(1)
Evaporating temperature (secondary flow)	0	[°C]	(1)
Generating pressure (primary flow)	30.6	[bar]	(7)
Generating temperature (primary flow)	89.7	[°C]	(7)

353

354 *Table 2. Reference boundary conditions considered in the CFD simulations*

355 The values shown in Table 2 predetermine the maximum achievable performance of the
 356 designed jet-ejector and they have been selected according to the following criteria:

- 357 • To determine the condensing temperature (42 °C) an ambient temperature of 30 °C has
 358 been considered as well as a pinch point of approximately 10 °C at the heat exchanger
 359 and some degree of liquid subcooling. This is a reasonable outdoor temperature during
 360 summer periods in warm climates.
- 361 • To determine the evaporating temperature (0 °C) a pinch point of 10 °C at the heat
 362 exchanger has been assumed. Therefore, the jet-ejector is designed to cool the intake
 363 line temperature down to 10 °C.
- 364 • A priori, there is no constraint to select the generating temperature because the exhaust
 365 line shows a high thermal level. A relatively high primary pressure has been chosen in
 366 order to reduce the outlet-primary flow pressure ratio ($\pi_{op} = 0.35$) and subsequently
 367 to prevent the jet-ejector from operating in subcritical mode. However, this value is not

368 necessarily the optimum one. It has been fixed just to reduce the number of degrees of
369 freedom involved in the optimization process. If another generating pressure was
370 selected the optimum jet-ejector geometry might differ from the one found in the
371 present paper. Concerning the off-design analysis, the primary pressure could be
372 affected if there was a change in heat power availability in the exhaust line. This event
373 often happens in a standard driving behavior because the ICE operating point is
374 constantly changing. In such a case the maximum primary pressure might be limited and
375 a severe performance degradation might occur if the jet-ejector operates within the
376 subcritical or the backflow modes. Nevertheless, the ICE transient conditions play a
377 major role when assessing the evolution of the exhaust line temperature and this
378 analysis exceeds the aim of the present paper.

379 Primary and secondary inlets are set to static pressure boundary condition and the outlet zone
380 of the jet-ejector is set to total pressure (see Figure 7). Total and static values in both inlets are
381 supposed to be essentially the same because the inlet velocity is neglected as a common
382 approximation (Croquer et al., 2016). Hence, the mass flow rates passing through the jet-ejector
383 are a result of the three pressure boundary conditions.

384 Total temperature is also imposed on both inlets and it is equal to static temperature following
385 the previous criteria. A superheating temperature of $10\text{ }^{\circ}\text{C}$ has been assumed in the primary and
386 secondary flows to avoid condensation in the expansion process occurring downstream.

387 In order to reduce the calculation time and to take into account the 3D geometry domain, the
388 axisymmetric condition is assigned at the jet-ejector mid-line since 3D effects can be neglected
389 (Pianthong et al., 2007).

390 The walls are defined as adiabatic, impermeable and smooth surfaces in which the no-slip
391 condition is satisfied. A schematic representation of the wall domain is represented in Figure 7.

392 To sum up, the following boundary conditions are assigned in the CFD cases to solve the
393 governing equations:

- 394 - Domain with axisymmetry.
- 395 - Two pressure inlet assignments (primary flow and secondary flow). Static pressure and
396 static temperature are imposed in these pressure inlets.
- 397 - One pressure outlet assignment (mixed flow).
- 398 - Wall to bound fluid and solid regions.

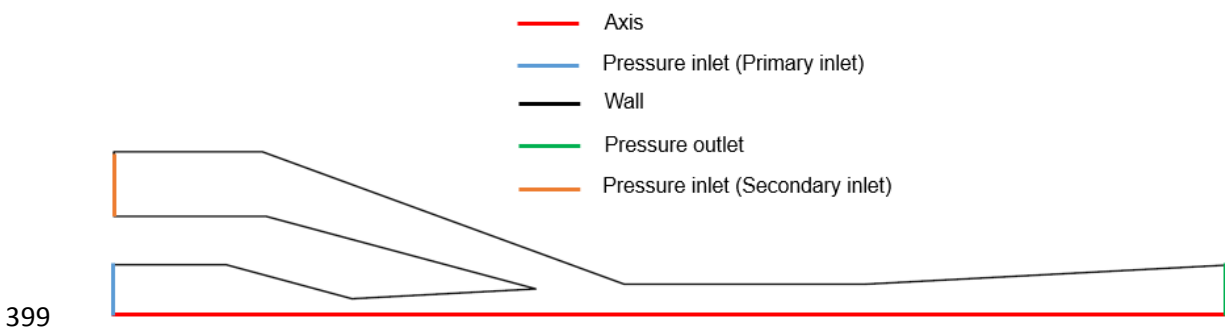


Figure 7. Boundary condition assignment on geometry

401

402 3.4.3 Thermodynamic model and convergence criteria

403

404 The thermodynamic properties of R1234yf stored at CFD code are based on the formulation of
405 Richter et al. (Richter et al., 2011). A real gas model has been considered instead of an ideal gas
406 assumption since absolute pressure inside the jet-ejector is assumed to be relatively high and in
407 this situation, the behavior of both models might not be similar. The fluid thermodynamic
408 variables can be determined accurately in the temperature range between $-53\text{ }^{\circ}\text{C}$ and $137\text{ }^{\circ}\text{C}$
409 and pressure values up to 300 bar. The properties of the refrigerant are implemented in the CFD
410 code by means of NIST libraries. Due to the NIST real gas model approach, the solution converges
411 at a slower rate than when running an ideal gas flow. The converging process of the calculation
412 is also more unstable. The solution diverges if flow properties exceed the bounded range even
413 though the state is physically valid. In order to avoid an aggressive convergence strategy the

414 boundary conditions are changed dynamically. Different transitions have been performed in
415 order to progressively achieve the desired pressure boundary conditions in both inlets and the
416 outlet. Gradual pressure increments in the primary inlet are the best strategy especially in the
417 early stages of calculation since the solution oscillates. Five criteria are examined to consider
418 each case as converged:

419

- 420 - Inlet and outlet mass flow rates do not vary with iterations, i.e., values are constant.
- 421 - The balance between the inlet and outlet mass flow rates is at least three orders of
422 magnitude lower than the minimum inlet mass flow.
- 423 - Calculation residuals are stable.
- 424 - Mach number at the converging-diverging nozzle throat is constant.
- 425 - The values of prescribed pressure and temperature boundary conditions do not vary
426 with iterations.

427 Around 20,000 iterations are required in order to satisfy previous conditions but strong
428 dependence with the jet-ejector operating mode has been found. The mass flow rate balance
429 and secondary mass flow rate stabilization are the limiting factors. Those cases in which the jet-
430 ejector operates in critical mode exhibit secondary mass flow stabilization in fewer iterations.
431 However, those cases in which boundary conditions lead to the subcritical operating mode
432 usually require more iterations.

433

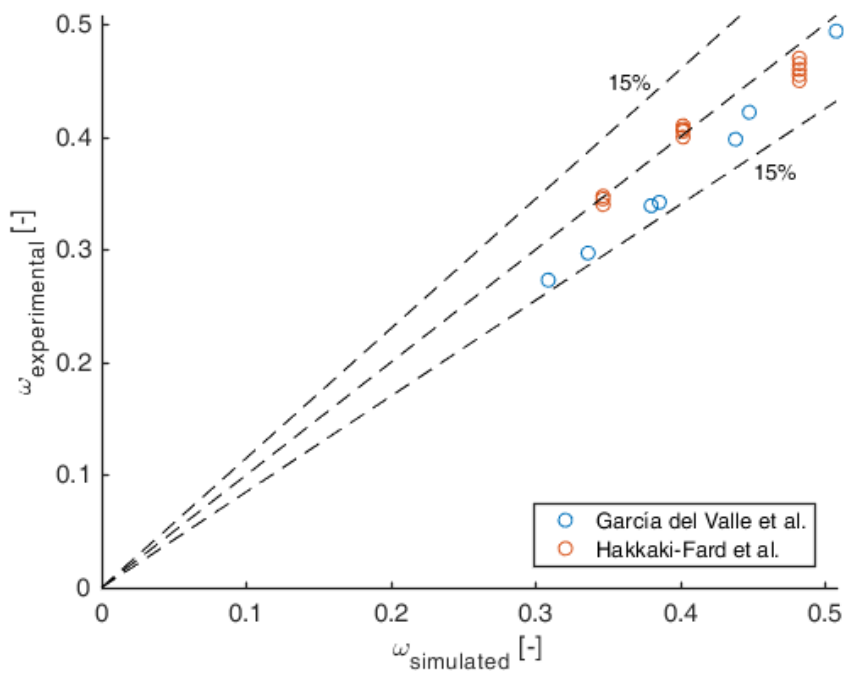
434 3.4.4 Computational model validation

435

436 The previous numerical approach has been validated with two experimental datasets available
437 in the literature (García Del Valle et al., 2014; Hakkaki-Fard et al., 2015). Discrepancies in
438 entrainment ratio have been evaluated between the present CFD approach and the three jet-
439 ejector prototypes presented in the research work of Hakkaki-Fard et al. (Hakkaki-Fard et al.,
440 2015) and the geometry “A” of the results reported by García del Valle et al (García Del Valle et

441 al., 2014). The relative deviation in the entrainment ratio between the simulated points and the
442 former experimental study does not exceed 7.2%. When the deviations are compared with the
443 latter research work the discrepancies do not exceed 13.2% but the CFD simulations tend to
444 slightly overestimate the jet-ejector entrainment ratio. Regardless of the small discrepancies,
445 these results demonstrate that the CFD setup is providing reliable results.

446 The geometry and operating pressures of the jet-ejector under investigation in the present study
447 are comparable to those of the research works used for validation. The working fluid used in the
448 present paper (R1234yf) and the refrigerant used to validate the simulations (R134a) show
449 comparable thermodynamic properties. In fact, R1234yf is the environmentally-friendly
450 replacement of R134a in many applications.



451

452 *Figure 8. Deviations of the present CFD approach and experimental data from the literature*

453 4. JET-EJECTOR REFRIGERATION SYSTEM MODELING

454

455 In this section, the theoretical model used to determine the maximum achievable cooling
456 capacity when the jet-ejector cycle operates against a high ambient temperature is presented.

457 The influence of ambient conditions in the overall cycle performance has been tested by using
458 the 1D thermodynamic model and the optimization procedure investigated by Galindo et al.
459 (Galindo et al., 2019) as well as the non-dimensional jet-ejector maps of the present paper.

460 The refrigeration system aims to reduce the intake air temperature downstream of the
461 intercooler of the ICE from $\sim 40\text{ }^{\circ}\text{C}$ to $\sim 0\text{ }^{\circ}\text{C}$ with a resulting cooling capacity of approximately
462 1.7 kW for the operating point of 2000 rpm and 50% load.

463 The cycle layout corresponds to the scheme depicted in Figure 1. The ambient conditions
464 sensitivity analysis has been carried out for a frequent engine operating point (2000 rpm, 50%
465 load) taking as boundary conditions in the engine side experimental measurements of the
466 temperature and mass flow at the intake and exhaust lines (see Table 3). The engine data come
467 from an experimental campaign carried out on an engine test bench in order to characterize the
468 ICE performance operating under several engine loads and speeds.

469 The inputs required to solve the cycle are shown in Table 4 and are varied dynamically by the
470 algorithm MOGA-II (Multi-Objective Genetic Algorithm) to find those feasible operating points
471 that minimize charge air temperature. The MOGA-II is widely used in engineering applications
472 and other areas as an optimization tool (Poles et al., 2007). The solution constraints, as well as
473 the general solving procedure, are available in the research paper referenced before (Galindo et
474 al., 2019). The aforementioned inputs (thermodynamic variables and degrees of freedom) are
475 shown in Table 4 and correspond to the expansion valve pressure drop (ΔP_v), the liquid pump
476 pressure ratio (k), the fraction of available heat at the exhaust line (κ), the superheating
477 temperature of the evaporator in the ejection cycle side ($T_{sup,1}$) and the jet-ejector scaling
478 factor (λ).

479 An ambient temperature of $30\text{ }^{\circ}\text{C}$ has been set as the reference condition, that is, the optimum
480 size of the jet-ejector in all the simulations corresponds to the ejection cycle coupled to the ICE
481 working with the mentioned ambient temperature. Then, the overall cycle performance is

482 reassessed when the ambient temperature varies from 31°C to 38°C maintaining a fixed jet-
 483 ejector size. This off-design modeling approach has been presented in detail by Galindo et al.
 484 (Galindo et al., 2019).

485

Parameter	Description	Value
$\dot{m}_{in}[kg \cdot s^{-1}]$	Engine intake mass flow	0.042
$\dot{m}_{ex}[kg \cdot s^{-1}]$	Engine exhaust mass flow	0.044
$T_{i,in}[^{\circ}C]$	Evaporator inlet temperature at the engine side	40.5
$T_{i,ex}[^{\circ}C]$	Generator inlet temperature at the engine side	417

486

487 *Table 3. Engine data used as boundary conditions. The operating point corresponds to 2000 rpm, 50% load*

488

Parameter	Lower limit	Upper limit
$\Delta P_v[bar]$	7	14
$k[-]$	2.5	4.5
$\kappa[-]$	0	1
$T_{sup,1}[^{\circ}C]$	0	60
$\lambda[-]$ (*)	0.5	2

489

490 *Table 4. Cycle variables modified by the genetic algorithm MOGA-II. (*) This variable is a degree of freedom only*
 491 *when the reference ambient condition is considered.*

492

493 5. RESULTS

494

5.1 Determination of the jet-ejector optimum geometry

495

496

497 Three key dimensions are involved simultaneously in the optimization process as described in

498 Section 3: nozzle exit diameter, $D_{e,3} \in [2.6 \text{ mm}, 3.2 \text{ mm}]$, mixing chamber diameter, $D_{e,4} \in$

499 $[3.2 \text{ mm}, 3.7 \text{ mm}]$, and nozzle exit position, $L_{e,2} \in [4 \text{ mm}, 7 \text{ mm}]$. The influence of $D_{e,3}$ and

500 $D_{e,4}$ over the entrainment ratio is presented in Figure 9 by means of interpolation of scattered

501 data which passes through the simulated points for the optimum nozzle exit position ($L_{e,2} =$

502 5.5 mm). Figure 10 depicts the sensitivity analysis of entrainment ratio with the variation of

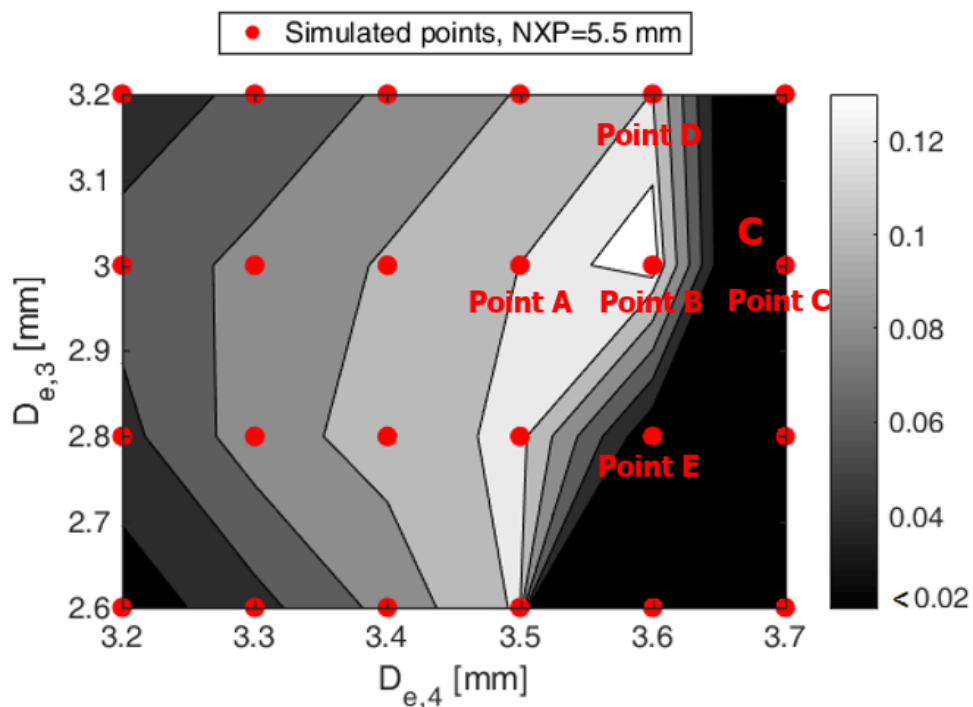
503 nozzle exit position ($L_{e,2}$) after finding for each case the optimum combination of nozzle exit

504 diameter ($D_{e,3}$) and mixing chamber diameter ($D_{e,4}$).

505 The relatively low value of optimum entrainment ratio ($\omega_{max} = 0.139$) in comparison with

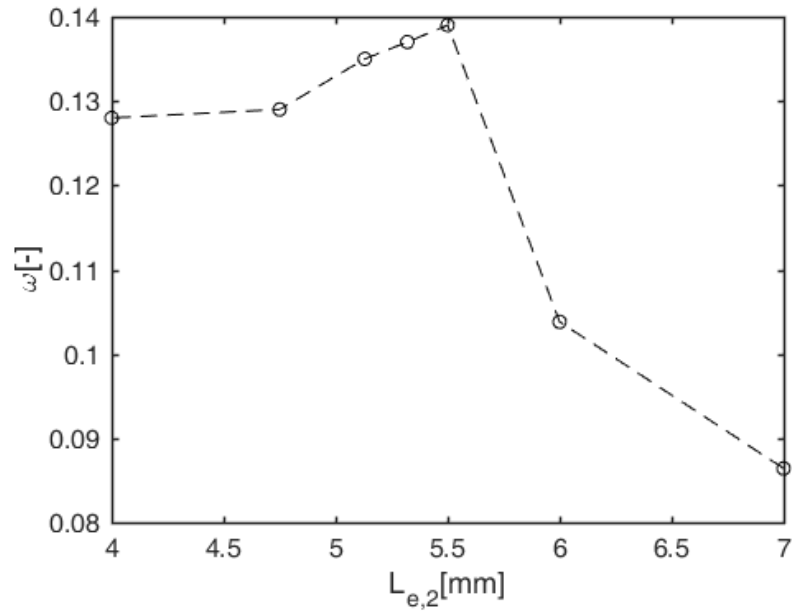
506 other studies can be attributed to the low secondary-primary pressure ratio and the relatively

507 high outlet-primary pressure ratio.



508

509 Figure 9. Entrainment ratio contours over nozzle exit diameter and mixing area diameter. A) $D_{e,3} = 3 \text{ mm}$, $D_{e,4} =$
 510 3.5 mm , B) $D_{e,3} = 3 \text{ mm}$, $D_{e,4} = 3.6 \text{ mm}$, C) $D_{e,3} = 3 \text{ mm}$, $D_{e,4} = 3.7 \text{ mm}$, D) $D_{e,3} = 3.2 \text{ mm}$, $D_{e,4} = 3.6 \text{ mm}$, E)
 511 $D_{e,3} = 2.8 \text{ mm}$, $D_{e,4} = 3.6 \text{ mm}$



512

513 Figure 10. Optimum entrainment ratio for each nozzle exit position ($L_{e,2}$) submitted to study

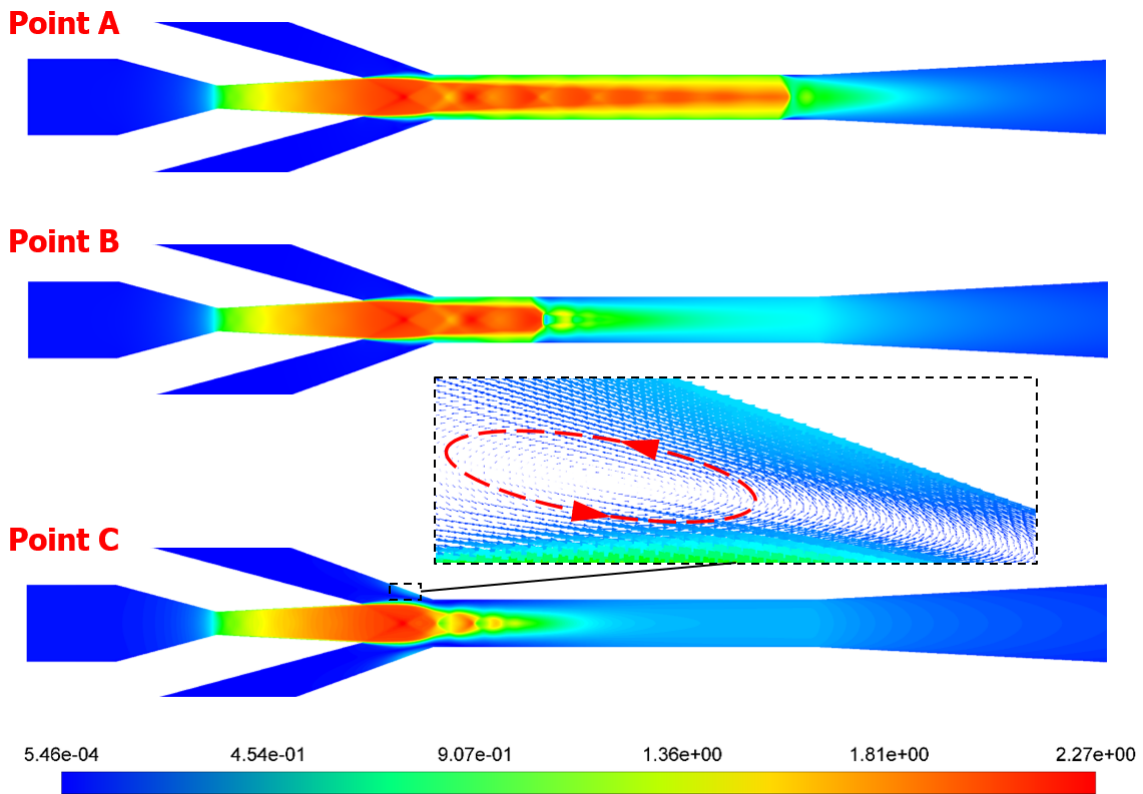
514

515 Flow pattern in non-optimized geometries

516

517 Mach contours are depicted in Figure 11 for mixing chamber diameters ($D_{e,4}$) of 3.5 mm, 3.6
 518 mm (case with optimum entrainment ratio) and 3.7 mm with a constant nozzle exit diameter of
 519 3 mm and constant nozzle exit position ($L_{e,2} = 5.5 \text{ mm}$). These cases correspond with the Points
 520 A, B, and C points of Figure 9. The case with a mixing chamber diameter of 3.5 mm (Figure 11)
 521 produces an interaction between jet core and the jet-ejector wall, reducing effective area and
 522 preventing secondary flow from being entrained. The reduction of entrainment ratio, in this
 523 case, has been quantified in 13.3 % with respect to the reference (optimum). On the opposite,
 524 the jet-ejector with mixing chamber diameter higher than optimum (3.7 mm), inhibits the
 525 entrainment of secondary flow by means of a recirculation bubble placed in a section
 526 downstream of the primary nozzle exit plane (see Figure 11). As a result effective area between

527 the jet-ejector wall and the jet core is also reduced and the secondary flow cannot be entrained
 528 (negative values of entrainment ratio are found). Point B (Figure 11) shows the highest
 529 entrainment ratio and it corresponds to a trade-off between the flow phenomena exposed
 530 before. It demonstrates that for this particular operating conditions and converging-diverging
 531 nozzle area ratio an optimum mixing chamber diameter exists.



532

533 *Figure 11. Mach contours over different mixing diameters with $D_{e,3} = 3 \text{ mm}$. A) $D_{e,4} = 3.5 \text{ mm}$, B) $D_{e,4} = 3.6 \text{ mm}$,*
 534 *C) $D_{e,4} = 3.7 \text{ mm}$*

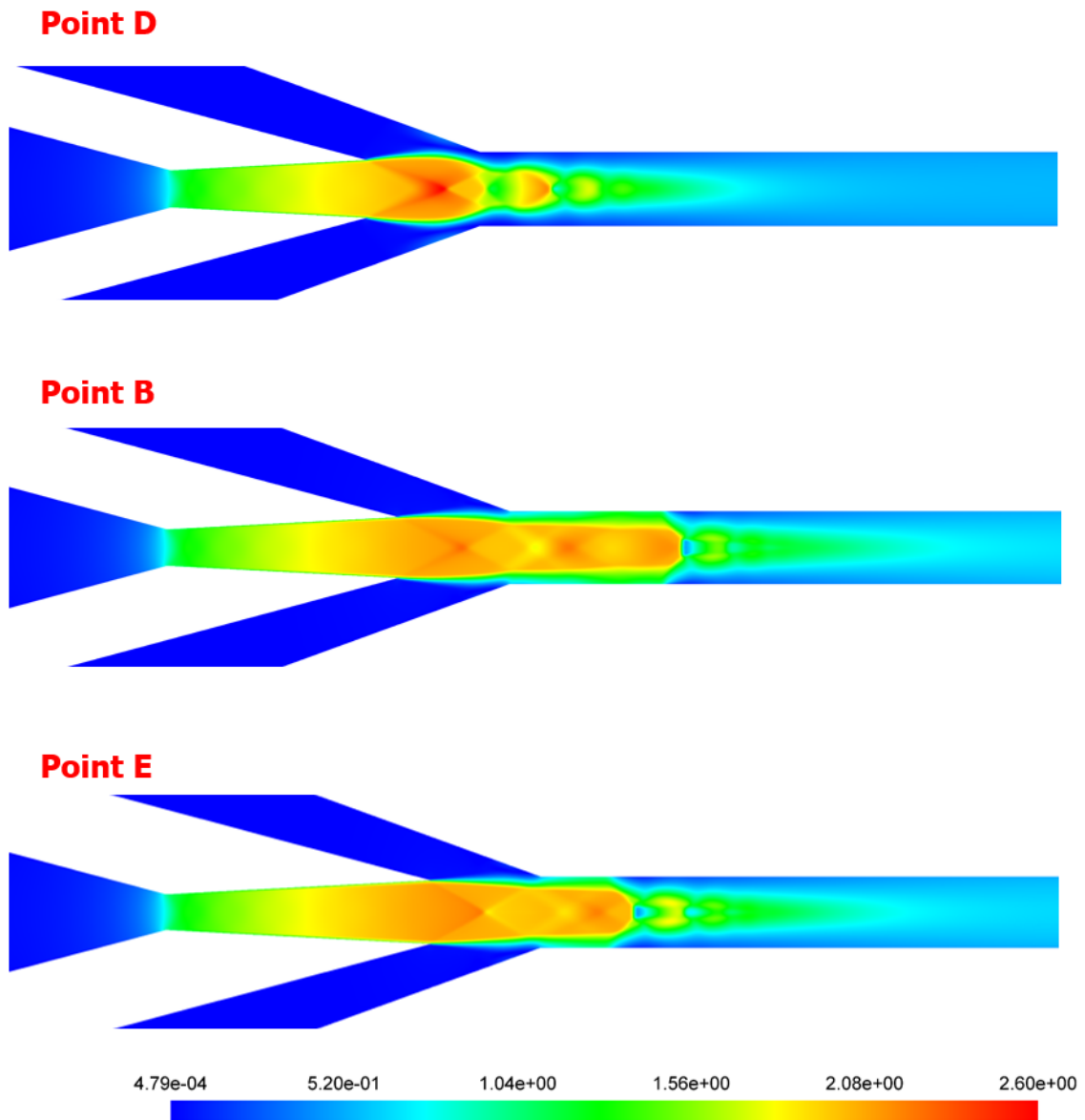
535

536 Figure 12 shows Mach contours for nozzle exit diameter ($D_{e,3}$) of 2.8 mm, 3 mm and 3.2 mm
 537 with constant nozzle throat diameter ($D_{e,2}$) of 1.8 mm, fixed mixing diameter ($D_{e,4}$) of 3.6 mm
 538 and fixed nozzle exit position ($L_{e,2} = 5.5 \text{ mm}$). These cases correspond with the Points D, B and
 539 E of Figure 9. The first geometry represented in Figure 12 (Point D) shows a divergence in
 540 expansion angle which is indicative of under-expanded flow. The divergence angle depends on

541 the pressure difference between the flow leaving nozzle and the flow conditions downstream.
542 As a consequence, additional expansion is produced downstream the exit plane of the nozzle
543 with the subsequent increase of Mach number. Unlike the under-expanded nozzle geometry,
544 the flow pattern of the Point E (Figure 12) reveals that the flow leaves the nozzle with a
545 convergence angle, thus over-expansion occurs. Furthermore, the supersonic level attained at
546 oblique shock pattern downstream the nozzle is not as strong as the case with an under-
547 expanded wave which is a feature of over-expanded waves.

548 Increased momentum at the jet core owing to the higher exit Mach number results in
549 improvement of critical pressure, however, the expansion of jet core affects the secondary flow
550 and produces a partial blockage of the secondary duct limiting the entrainment ratio. The
551 optimum geometry in terms of entrainment ratio corresponds to Point B in Figure 12, that is, an
552 intermediate case between Point D and Point E. In percentage terms, the reduction of
553 entrainment ratio with respect to optimum geometry (B) in cases D and E corresponds to 13.2%
554 and 85.1%, respectively.

555 From the parametric study already mentioned it can be inferred that a great dependence on jet-
556 ejector dimensions exists and precision during the manufacturing process is essential.
557 Manufacturing deviations of only 0.1 mm (<10%) can lead to significant variations in the
558 entrainment ratio.



559

560 *Figure 12. Mach contours over different nozzle exit diameters with $D_{e,4} = 3.6$ mm. D) $D_{e,3} = 2.8$ mm, B) $D_{e,3} =$*

561

3 mm, E) $D_{e,3} = 3.2$ mm

562

563 5.2 Jet-ejector off-design performance

564

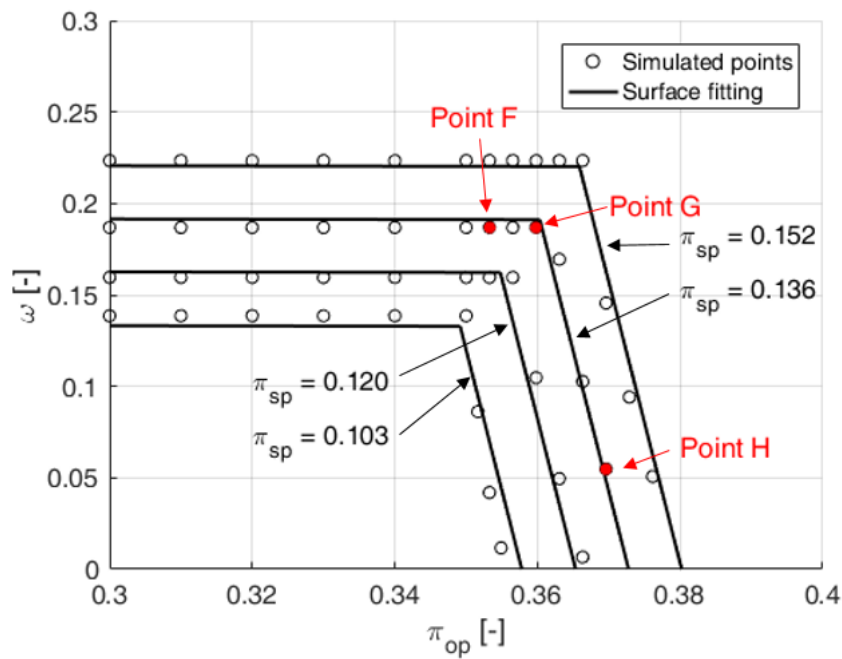
565 To carry out the off-design performance evaluation, the primary flow pressure (P_p) has been set

566 to 30.6 bar in all the simulations in order to facilitate the analysis of the results. The secondary

567 flow pressure (P_s) has ranged from 3.15 bar to 4.65 bar keeping a constant value for each set of

568 data. Therefore, for a fixed secondary-primary pressure ratio (π_{sp}), the outlet-primary pressure

569 ratio (π_{op}) has been varied by changing the jet-ejector backpressure. At least three points at
 570 critical and subcritical modes have been simulated for each set of data and the results have been
 571 represented in Figure 13. Resulting fitting coefficients are presented in Table 5. It should be
 572 noted that as π_{sp} increases critical backpressure is expected to appear at higher π_{op} values
 573 since mixed flow momentum increases. Because of this, the jet-ejector with $\pi_{op} = 0.36$
 574 operates in critical mode if $\pi_{sp} = 0.152$ but otherwise operates in subcritical mode if $\pi_{sp} =$
 575 0.12.



576

577 *Figure 13. Off-design pressure results with corresponding fitted critical and subcritical surfaces.*

β_I	-0.0476	β_{IV}	4.771
β_{II}	1.773	β_V	6.976
β_{III}	-0.0063	β_{VI}	-15.34

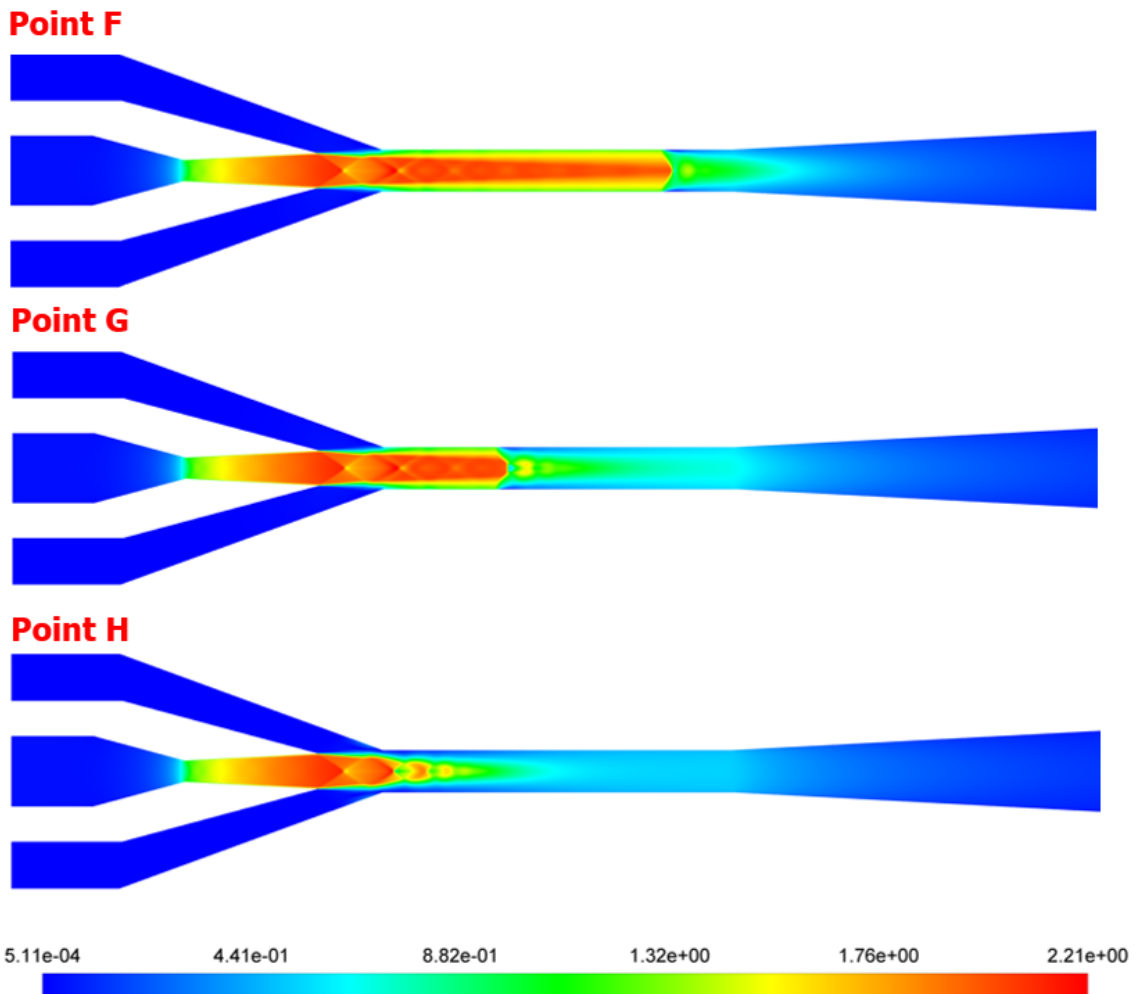
578

579 *Table 5. Fitting coefficients for critical and subcritical characteristic surfaces*

580 The root mean squared error (RSME) has been used as a quality indicator for fitting both critical
581 and subcritical surfaces. Obtained values ($RSME_{crit} = 0.0041$, $RSME_{scrit} = 0.020$) prove the
582 accuracy of the present approach.

583 The results of Figure 14 show Mach number contours representing the effect of backpressure
584 keeping constant primary and secondary inlet pressure, with 30.6 bar and 4.15 bar ($\pi_{sp} =$
585 0.136), respectively. Thus, the flow behavior over characteristic cases is analyzed. It should be
586 noted that two cases represented in Figure 14 (Point F and Point G) are operating in critical
587 mode, i.e, double-choking mode with constant entrainment ratio. As backpressure increases the
588 second series of oblique shocks, that is, shockwave pattern that appears at the constant mixing
589 area region moves upstream without having an influence on the mixing process as can be seen
590 in Figure 14 (Point F and Point G). When the critical backpressure is exceeded and the second
591 series of shockwaves interact with the mixing process, the secondary flow is no longer choked
592 and the secondary mass flow is dramatically reduced (Point H of Figure 14).

593 Comparing the Points F and G working on critical mode with reference operating pressures ($P_p =$
594 30.6 bar, $P_s = 3.15$ bar, $P_o = 10.7$ bar) an improvement of entrainment ratio of 34.8% is
595 observed which is consistent with critical mode representation since $\pi_{sp} > \pi_{sp,ref}$. In contrast,
596 Point H working on subcritical mode suffers a significant deterioration in the entrainment ratio.



597

598 *Figure 14. Mach contours over different backpressure with fixed primary flow inlet pressure $P_p = 30.6$ bar, and*

599 *secondary inlet flow pressure $P_s = 4.15$ bar. G) $P_o = 10.81$ bar, H) $P_o = 11.01$ bar, I) $P_o = 11.31$ bar*

600

601 5.3 Overall cycle evaluation with off-design ambient temperatures

602

603 The minimum achievable charge air temperature in each ambient condition is schematically

604 depicted in Figure 15 and Figure 16. When the ambient temperature ranges between 30°C and

605 31°C the jet-ejector works in critical operating mode and the desired cooling demand can be

606 attained. Indeed, an engine charge air temperature of 4.6°C ($COP = 0.113$) can be achieved if

607 the ambient temperature is lower than 31°C . On the contrary, when an ambient temperature

608 of 31°C is exceeded a significant performance degradation is observed since the jet-ejector

609 works in subcritical mode. In this situation, the critical backpressure is exceeded and the jet-

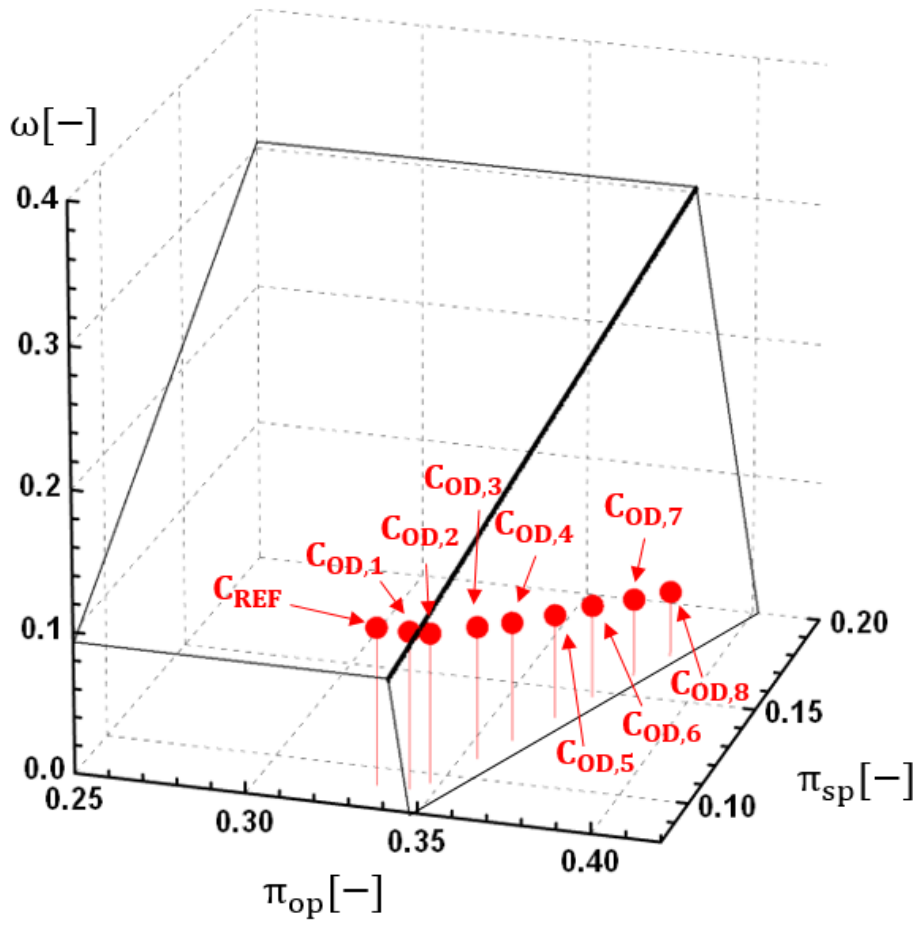
610 ejector entrainment ratio decreases steeply (see Figure 15 and Figure 16). In this case, the
611 minimum achievable temperatures range between 6.3°C and 26.3°C . When the ambient
612 temperature (and therefore the condensing pressure) is increased it is observed that the genetic
613 algorithm tends to increase secondary flow evaporating pressure in order to improve the
614 entrainment ratio by avoiding the break-down line of the jet-ejector subcritical map.

615 In view of the above, a high dependence with ambient temperature exists and the jet-ejector
616 must be designed carefully to prevent the ejection cycle from operating in the subcritical mode.
617 Otherwise, the cooling load can drop dramatically.

618 It is complicated to carry out a reliable comparison between the present paper and existing
619 research works in the literature because the real improvement potential of the jet-ejector itself
620 and the jet-ejector refrigeration system strongly depends on the design operating conditions
621 and the working fluid. Furthermore, the research papers relative to application of the recovered
622 ICE waste heat to drive a jet-ejector refrigeration system are scarce. Galindo et al. (Galindo et
623 al., 2019) and Zegenhagen and Ziegler (Zegenhagen and Ziegler, 2015a) studied the feasibility of
624 a jet-ejector refrigeration system coupled to an ICE using R134a as working fluid with a numerical
625 approach in a Diesel engine and an experimental approach in a gasoline engine, respectively.

626
627 Despite the relatively low COP values reported (maximum of 0.113 in the present paper,
628 maximum of 0.151 in the first research work (Galindo et al., 2019) and 0.26 in the second one
629 (Zegenhagen and Ziegler, 2015a), these studies demonstrate the feasibility of cooling the ICE
630 intake line down to a temperature close to 0°C by using a jet-ejector refrigeration cycle because
631 the exhaust waste heat is abundant in comparison with the required cooling capacity. This paper
632 provides a supplementary point of view: A quantification of the performance degradation that
633 occurs with an optimized jet-ejector design when the outdoor temperature increases.

634

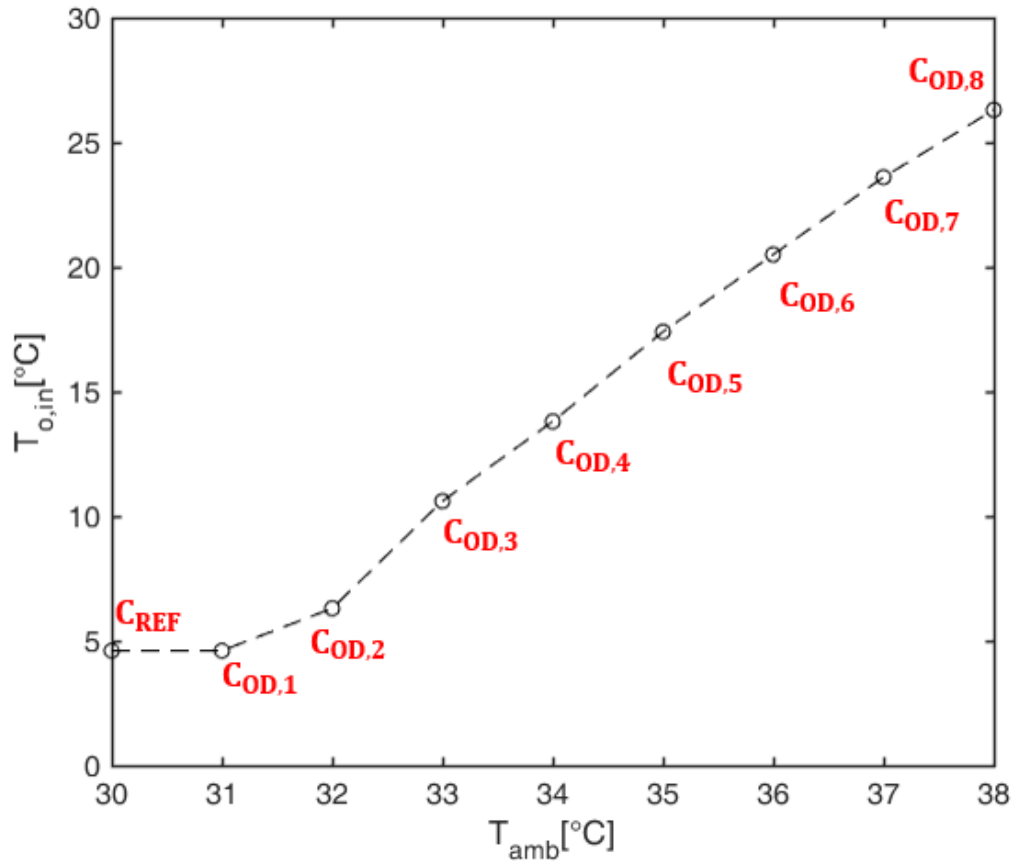


$C_{REF} \rightarrow T_{amb} = 30^{\circ}\text{C}; T_{o,in} = 4.6^{\circ}\text{C}$	$C_{OD,5} \rightarrow T_{amb} = 35^{\circ}\text{C}; T_{o,in} = 17.4^{\circ}\text{C}$
$C_{OD,1} \rightarrow T_{amb} = 31^{\circ}\text{C}; T_{o,in} = 4.6^{\circ}\text{C}$	$C_{OD,6} \rightarrow T_{amb} = 36^{\circ}\text{C}; T_{o,in} = 20.5^{\circ}\text{C}$
$C_{OD,2} \rightarrow T_{amb} = 32^{\circ}\text{C}; T_{o,in} = 6.3^{\circ}\text{C}$	$C_{OD,7} \rightarrow T_{amb} = 37^{\circ}\text{C}; T_{o,in} = 23.6^{\circ}\text{C}$
$C_{OD,3} \rightarrow T_{amb} = 33^{\circ}\text{C}; T_{o,in} = 10.6^{\circ}\text{C}$	$C_{OD,8} \rightarrow T_{amb} = 38^{\circ}\text{C}; T_{o,in} = 26.3^{\circ}\text{C}$
$C_{OD,4} \rightarrow T_{amb} = 34^{\circ}\text{C}; T_{o,in} = 13.8^{\circ}\text{C}$	

636

637 *Figure 15. Ejection cycle operating points with different ambient temperature represented over the jet-ejector maps*

638



639

640

Figure 16. The cooling effect of the ejection cycle over different ambient temperatures

641

6. CONCLUSIONS

642

643

In the present paper, a jet-ejector prototype intended for cooling down an ICE intake for an

644

automotive application has been designed and characterized. In the first instance, a geometric

645

optimization has been performed under specific operating conditions of a passenger vehicle ICE,

646

in terms of thermal power availability and cooling requirements. Subsequently, the optimum

647

geometry has been submitted to off-design operating pressures to obtain the critical and

648

subcritical characteristic surfaces. To conclude, the performance of the overall system has been

649

evaluated against off-design ambient temperatures using the previous jet-ejector design. The

650

main conclusions are outlined below:

651

- An optimum entrainment ratio of $\omega_{max} = 0.139$ has been obtained for a nozzle exit

652

diameter ($D_{e,3}$), mixing chamber diameter ($D_{e,4}$) and nozzle exit position ($L_{e,2}$) values of

653 3 mm, 3.6 mm and 5.5 mm, respectively. The relatively low entrainment ratio values can
654 be attributed to the adverse operating pressures. In the non-optimized geometries, the
655 mixing chamber diameter ($D_{e,4}$) is a key factor affecting jet core and wall interaction and
656 consequently entrainment process. Likewise, the nozzle exit diameter ($D_{e,3}$) determines
657 primary flow expansion level and flow structure downstream the nozzle. Hence, the
658 optimum values of previous dimensions are strongly influenced by operating pressures
659 so boundary conditions coming from the ejection cycle must be accurately predicted to
660 maximize performance. Furthermore, the short total length of the jet-ejector (<110 mm)
661 would facilitate a compact-sized system easier to package in a vehicle.

662 - Simple expressions of both critical and subcritical modes have been demonstrated to be
663 a feasible approach to model the jet-ejector behavior in off-design operating conditions.

664 This non-dimensional two planar model contains information about the jet-ejector
665 geometry as well as performance and they would remain valid if the jet-ejector scale is
666 modified.

667 - When the ability of the overall ejection refrigeration system to cool down the intake of
668 an ICE operating at 2000 rpm and 50% load is assessed, it is observed that temperatures
669 near zero Celsius degrees ($4.6^{\circ}C$) can be attained at the reference ambient temperature
670 ($30^{\circ}C$). However, if the ambient temperature exceeds $31^{\circ}C$ then the jet-ejector
671 operates in subcritical mode and the system performance drops dramatically. Despite
672 this, if the system operates with $38^{\circ}C$ of ambient temperature it is still possible to
673 generate some cooling capacity. In such a case $26.3^{\circ}C$ can be attained at the engine
674 intake line.

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