RESEARCH Open Access



A case study of 2019-nCOV cases in Argentina with the real data based on daily cases from March 03, 2020 to March 29, 2021 using classical and fractional derivatives

Pushpendra Kumar¹, Vedat Suat Erturk², Marina Murillo-Arcila^{3*}, Ramashis Banerjee⁴ and A. Manickam⁵

*Correspondence: mamuar1@upv.es

³Instituto Universitario de Matematica Pura y Aplicada, Universitat Politècnica de València, 46022 Valencia, Spain Full list of author information is available at the end of the article

Abstract

In this study, our aim is to explore the dynamics of COVID-19 or 2019-nCOV in Argentina considering the parameter values based on the real data of this virus from *March* 03, 2020 to *March* 29, 2021 which is a data range of more than one complete year. We propose a Atangana–Baleanu type fractional-order model and simulate it by using predictor–corrector (P-C) method. First we introduce the biological nature of this virus in theoretical way and then formulate a mathematical model to define its dynamics. We use a well-known effective optimization scheme based on the renowned trust-region-reflective (TRR) method to perform the model calibration. We have plotted the real cases of COVID-19 and compared our integer-order model with the simulated data along with the calculation of basic reproductive number. Concerning fractional-order simulations, first we prove the existence and uniqueness of solution and then write the solution along with the stability of the given P-C method. A number of graphs at various fractional-order values are simulated to predict the future dynamics of the virus in Argentina which is the main contribution of this paper.

MSC: 34D20; 26A33; 47H10; 92D30

Keywords: COVID-19; Argentina; Mathematical models; TRR algorithm;

Atangana-Baleanu non-classical derivative

1 Introduction

The coronavirus disease 2019 (COVID-19) is considered as the most dangerous epidemic disease of this decade, which appeared for the first time in Wuhan (China) in the last month of 2019. It has been observed that coronavirus disease 2019 (COVID-19) is a vital health concern as it can be fatal specially in old-aged people. SARS-CoV-2 virus causes COVID-19 disease. Researchers and medical practitioners have much information about the death due to the clinical disease but they do not know much about its pathobiology. It has been seen that the characteristics of cellular responses to COVID-19 are not clearly known and understood, but based on the previous studies on SARS-CoV, a predictable



© The Author(s) 2021. This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit http://creativecommons.org/licenses/by/4.0/.

sequence of events can be hypothesized. According to the cells that SARS-CoV infects, COVID-19 can be separated into three periods that coincide with the clinical parts of the disease [1].

The structure of SARS-CoV-2 needs to be understood. It has been found that SARS-CoV-2 is part of the family of beta-coronavirus, some of which caused two other epidemics named as MERS-CoV and SARS-CoV as can be found in Ref. [2]. In [3] Hui et al. analyzed the structure of such coronaviruses. According to the World Health Organisation (WHO), the rate of death due to SARS-CoV-2 is lower than the one due to SARS-CoV though the rate of transmission is higher in the case of SARS-CoV-2 than SARS-CoV. The RNA structure of different coronaviruses has been stated in [4]. It has been observed that SARS-CoV-2 has distinctive spike proteins and presents a specific peptide, namely PrrA, which allows one to divide the spike protein using cellular protease enzymes in order to disseminate the virus from the cell of the host easily [5, 6]. So, the rate of transmission of SARS CoV-2 is much higher and this is the prime cause of its spreading throughout the globe in a very short period of time.

It has been observed that as soon as SARS-CoV-2 makes its entrance into the epithelial cell of alveoli of the respiratory tract of human being, the virus activates the immune response of human being due to the fast multiplication rate of SARS-CoV-2 cells. After that, the pulmonary tissue from the respiratory tract of human being is damaged causing the stimulation of more and more white blood cells. This process is known as the cytokine release syndrome [7], which can cause a multiple organ failure [8].

There are a number of stages included in the infection of COVID-19. The initial stage is asymptomatic and covers 1 to 2 days after getting infected. It has been noticed that after inhaling the virus it attaches to epithelial cells from the nasal cavity of human being and the virus starts the process of replication [9]. In this initial stage, infected people are able to spread the infection. During the second stage the virus is able to spread and move quickly down to the respiratory tract along with the conducting passage of air [10]. It has been observed that for 80% of the infected individuals the COVID-19 illness will be lenient and it is restricted to upper as well as conducting passages of air. The third stage of the disease involves hypoxia and ground glass infiltrates along with the growth of acute respiratory distress syndrome (ARDS). It has been seen that 20% of the infected individuals will move to third stage of the disease and they will develop pulmonary invasions which will lead to severe disease. From the initial estimation the rate of severity is about 2% but it varies with age [1]. In this stage SARS-Cov-2 virus is able to reach the units of the lung which are responsible for exchange of gas and infect the type II cells of alveoli. SARS-CoV is able to spread within type II cells and huge viral particles are liberated [11]. Old-aged people are at high risk since they have a low immune response, which can lead to severe consequences [12].

Mathematical models are the best way to describe the dynamics of the disease. Many mathematical models have been provided to illustrate the behavior of COVID-19 by using integer- and fractional-order derivatives [13–18]. A fractional-order COVID-19 model with delay has been proposed in [19]. *Atangana et al.* in [20] have discussed a mathematical model of COVID-19 with deterministic and stochastic approaches. The authors in [21–23] have also simulated the dynamics of 2019-nCOV by using effective mathematical models. A study of a fractional-order model of HIV is given in [24]. The au-

thors in [25] proposed a research on the dynamics of a population model. In [26], a COVID-19 model along with necessary awareness programs has been explored. The roles of isolation and quarantine measures for COVID-19 outbreaks are given in [27]. The authors in [28] have solved a model of huanglongbing transmission with an effective numerical algorithm. A psychological model in fractional-order sense has been introduced in [29]. *Kumar et al.* in [30] have described a time-delay fractional-order mathematical model of oncolytic virotherapy. Many other epidemics have been described by using fractional mathematical models [31, 32]. Recently, the authors in [33] studied the structure of rabies, and canine distemper virus epidemics by using generalised Caputo non-classical derivative. Two fractional-order mathematical models for describing mosaic disease have been given in [34]. A environmental study in the fractional-order sense is given in [35].

This paper is formulated to trace the dynamics of COVID-19 cases in Argentina by using Atangana—Baleanu type fractional mathematical model. The study is organized as follows: In Sect. 2, we describe the integer-order model dynamics. In Sect. 3, we plot the real-data cases of COVID-19 in Argentina and calculate the parameter values for our simulations. Section 4 is organized in a number of sub-sections where we simulate the fractional-order model and perform all theoretical and graphical simulations. Finally in Sect. 5, we present our conclusions about the study.

2 Model description

In this paper, we consider a compartmental mathematical model [36]. Natural births and death rates have not been considered in the model as those have no impact on the short-term outbreaks of COVID-19. The mentioned model focuses on two distinct groups of susceptible individuals: susceptible individuals given by S(t) and confined individuals who follow lockdown or confinement intervention partially as the confinement is not perfect. We symbolize the class of confined individuals as C(t). The rest of the population is compartmentalized as follows: exposed individuals E(t) at time t, asymptomatic (having no clinical symptoms or mild symptoms) individuals A(t), quarantined symptomatic infectious individuals Q(t), hospitalized or isolated individuals H(t) and recovered individuals R(t).

In the given model, p is the transmission rate from confined susceptible humans to rejoined unconfined susceptible humans, $q\gamma$ is the exposure rate of the asymptomatic humans, $r_4\sigma_2$ is the progression rate from severely infected to hospitalization and quarantine rate is given by $(1-q)\gamma$. $r_1\sigma_1$ denotes the transmission rate of the asymptomatic humans to become severely infectious. $r_2\sigma_1$ shows the transmission rate of confinement or hospitalization to isolation of the asymptomatic group. The natural recovery of soft symptomatic humans is represented by the rate $(1-r_1-r_2)\sigma_1$, whereas $(1-r_3-r_4)\sigma_2$ is the recovery rate for Q classes. In the model, δ_h , δ_q , and δ_a are stood for the COVID-19 death rates in the given model classes, respectively. The structure of the non-linear model based on the

given parameters explanation is provided as follows:

$$\begin{cases} \frac{dS}{dt}(t) = pC(t) - cS(t) - \left[\frac{\beta(A(t) + \eta Q(t))}{N(t)}\right] S(t), \\ \frac{dC}{dt}(t) = cS(t) - pC(t) - (1 - \epsilon) \left[\frac{\beta(A(t) + \eta Q(t))}{N(t)}\right] C(t), \\ \frac{dE}{dt}(t) = \left[\frac{\beta(A(t) + \eta Q(t))}{N(t)}\right] \left[S(t) + (1 - \epsilon)C(t)\right] - \gamma E(t), \\ \frac{dA}{dt}(t) = q\gamma E(t) + r_3\sigma_2 Q(t) - (\sigma_1 + \delta_a)A(t), \\ \frac{dQ}{dt}(t) = (1 - q)\gamma E(t) + r_1\sigma_1 A(t) - (\sigma_2 + \delta_q)Q(t), \\ \frac{dH}{dt}(t) = r_2\sigma_1 A(t) + r_4\sigma_2 Q(t) - (\sigma_3 + \delta_h)H(t), \\ \frac{dR}{dt}(t) = (1 - r_1 - r_2)\sigma_1 A(t) + (1 - r_3 - r_4)\sigma_2 Q(t) + \sigma_3 H(t). \end{cases}$$

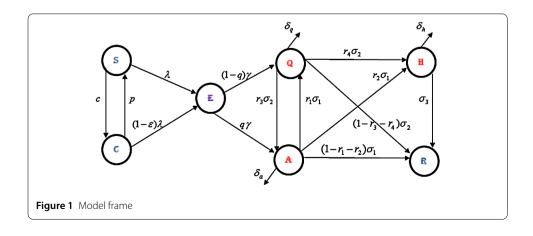
$$(1)$$

The parameters are given in Table 1 and the model structure is provided in Fig. 1. A brief discussion on the model characteristics like boundedness and positivity of solutions is given in reference [36]. The authors in [36] calculated the greatest disease-free equilibrium point, which is defined by

$$x_0 = (S_0, C_0, 0, 0, 0, 0, 0)' = \left(\frac{pN_0}{p+c}, \frac{cN_0}{p+c}, 0, 0, 0, 0, 0\right)'.$$

Table 1 Model parameters and their description

Parameter	Description		
β	Contact rate		
η	Relative transmissibility of quarantined infected carrier		
р	Rate of transition from C(t) to S(t)		
C	Confinement rate		
ϵ	Confinement efficacy		
γ	Rate of transition from E(t) to Q(t)		
9	Rate of exposed individuals becoming quarantined		
σ_1	Rate of transition from A(t) to Q(t)		
σ_2	Transition rate from Q(t) to A(t)		
σ_3	Rate of transition from hospitalized to recovered group		
r_1	Fraction of A(t) becoming quarantined humans		
r_2	Rate of unquarantined infected humans going to be hospitalized		
r_3	Rate of quarantined infected humans moving to unquarantined infected humans		
r ₄	Rate of quarantined infected humans going to be hospitalized		
$oldsymbol{\delta}_{a}$	Rate of 2019-nCOV deaths in unquarantined infected humans		
$oldsymbol{\delta}_q$	Rate of 2019-nCOV deaths in quarantined infected humans		
δ_h	Rate of 2019-nCOV deaths in hospitalized		



Using the procedure given in [37], the matrices F and V for calculating the basic reproductive number are given by

$$F = \begin{pmatrix} 0 & \beta \frac{S_0 + (1 - \epsilon)C_0}{N_0} & \eta \beta \frac{S_0 + (1 - \epsilon)C_0}{N_0} \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix},$$

$$V = \begin{pmatrix} \gamma & 0 & 0 \\ -q\gamma & (\sigma_1 + \delta_a) & -r_3\sigma_2 \\ -(1 - q)\gamma & -r_1\sigma_1 & (\sigma_2 + \delta_q) \end{pmatrix}.$$
(2)

As a consequence, they obtained the basic reproductive number as the spectral-radius of the generation matrix, FV^{-1} :

$$\mathcal{R}_{c} = \rho \left(FV^{-1} \right)$$

$$= \beta \frac{S_{0} + (1 - \epsilon)C_{0}}{N_{0}} \frac{(r_{1}\sigma_{1}\eta + (\sigma_{2} + \delta_{q}))q + ((\sigma_{1} + \delta_{a})\eta + \sigma_{2}r_{3})(1 - q)}{(\sigma_{1} + \delta_{a})(\sigma_{2} + \delta_{q}) - r_{1}r_{3}\sigma_{1}\sigma_{2}}.$$
(3)

Here $\rho(\cdot)$ denotes the spectral-radius operator.

Lemma 1 If $\mathcal{R}_c < 1$, the epidemic-free equilibrium x_0 is locally asymptotically stable and unstable if $\mathcal{R}_c > 1$.

Proof First, we observe that the last two equations of (1) are not coupled to the rest of equations of the model. As the total population size, N_0 , is constant, we get $S + C = N_0 - (E + A + Q + H + R)$. Then the local stability of the given system (1) can be analyzed via remaining model of variables (E, A, Q). As a consequence, we establish that the Jacobian matrix related to these variables is written by

$$\mathcal{J} = \begin{pmatrix} -\gamma & \beta \frac{(S_0 + (1 - \epsilon)C_0)}{N_0} & \beta \eta \frac{(S_0 + (1 - \epsilon)C_0)}{N_0} \\ q\gamma & -(\sigma_1 + \delta_a) & r_3\sigma_2 \\ (1 - q)\gamma & r_1\sigma_1 & -(\sigma_2 + \delta_q) \end{pmatrix}.$$

The roots of the next characteristic polynomial correspond to the eigenvalues of \mathcal{J} :

$$P_{\mathcal{T}}(x) = x^3 + a_2 x^2 + a_1 x + a_0$$

where

$$\begin{aligned} a_2 &= \gamma + k_2 + k_1, \\ a_2 &= (k_1 k_2 - \sigma_1 \sigma_2 r_1 r_3) \\ &\times \left[\frac{N_0 k_2 + N_0 k_1}{N_0 (k_1 k_2 - \sigma_1 \sigma_2 r_1 r_3)} \gamma + 1 - \gamma \frac{(\eta (1 - q) + q)}{q (k_2 + r_1 \sigma_1 \eta) + (1 - q)(\eta k_1 + r_3 \sigma_2)} \mathcal{R}_c \right] \end{aligned}$$

and $a_0 = \gamma(k_1k_2 - r_1r_3\sigma_1\sigma_2)(1 - R_c)$. Note that a_2 is always positive. a_0 and a_1 are positive as long as $\mathcal{R}_c < 1$. Therefore, all eigenvalues of \mathcal{J} have negative real parts. Consequently, the epidemic-free equilibrium x_0 , is locally asymptotically stable if $\mathcal{R}_c < 1$.

Excluding confinement measures, i.e. if $\epsilon = 0$, \mathcal{R}_c is convergent to the basic reproductive number, \mathcal{R}_0 , written by

$$\mathcal{R}_{0} = \beta \frac{(r_{1}\sigma_{1}\eta + (\sigma_{2} + \delta_{q}))q + ((\sigma_{1} + \delta_{a})\eta + \sigma_{2}r_{3})(1 - q)}{(\sigma_{1} + \delta_{a})(\sigma_{2} + \delta_{q}) - r_{1}r_{3}\sigma_{1}\sigma_{2}}.$$
(4)

Using (3), it follows that

$$\mathcal{R}_c = \mathcal{R}_0 \left(\frac{S_0 + (1 - \epsilon)C_0}{N_0} \right) = \mathcal{R}_0 \left(\frac{p + (1 - \epsilon)c}{p + c} \right). \tag{5}$$

3 Model calibration and forecasting

A recently proposed optimization scheme, which is an evolution of Levenberg–Marquardt one [36, 38] and depends on trust-region-reflective (TRR) scheme, is employed to perform the model (1) calibration. This robust optimization method can be applied for simulating non-linear least-squares problems. The implementation of the scheme is done with the help of *lsqcurvefit* function, which is included in Optimization Toolbox from MATLAB. Possible parameter values are calculated by this function. The real data of daily collected cases in Argentina are collected from the trusted data website which can be verified in [39]. We used 7-day running average of the given reported COVID-19 cases analyzed in the calibration of model because of changeable structure of real data as can be seen in Fig. 2. The daily testing in Argentina is really inconsistent as in all nations. By the early updates, the total population size of Argentina is around 45,481,402 [39]. As initial population amount, we get S(0) = 45,481,396, C(0) = 0, E(0) = 0

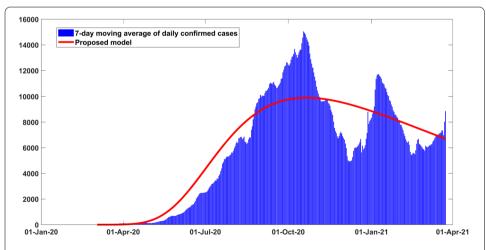


Figure 2 Output of the model performance fitting for daily cases of infection in Argentina from March 03, 2020 to March 29, 2021

Parameters	Probable range	Base value	TRR output	Reference
β	0.5-1.5	0.5	1.2757	Fitted
σ_1	0.001-0.1	0.03	0.01	Fitted
σ_2	0.1-0.9	0.3	0.3488	Fitted
σ_3	0.1-0.9	0.3	0.6917	Fitted
r_1	0.1-0.9	0.5	0.302	Estimated
r_2	0.1-0.9	0.5	0.302	Estimated
r_3	0.1-0.9	0.5	0.2227	Estimated
r_4	0.1-0.9	0.5	0.3172	Estimated
δ_a	0.001-0.1	0.01	0.1	Fitted
$\boldsymbol{\delta}_q$	0.001-0.1	0.01	0.09	Fitted
δ_h	0.001-0.1	0.01	0.0998	Fitted
р	0.0005-0.1	0.05	0.00051	Estimated
η	0.4-0.6	0.5	0.5077	Fitted
С	0.001-0.1	0.005	0.0155	Estimated
γ	1/14–1/3	1/5.1	0.1673	Fitted

0.7

0.2

0.8417

0.1181

Estimated

Estimated

Table 2 Model parameters calibration by using the mentioned scheme

0.1-0.99

0.001-0.5

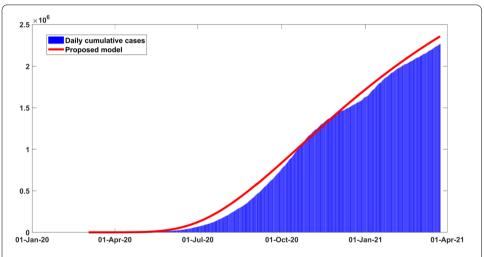


Figure 3 Output of the model performance fitting for cumulative cases of infection in Argentina from March 03, 2020 to March 29, 2021

equation:

$$\min_{\psi} \| \left(NPC_{predict}(t), NRC_{predict}(t) \right) - \left(NPC_{data}, NRC_{data} \right) \|, \tag{6}$$

where $\psi = \{\beta, \sigma_1, \sigma_2, \sigma_3, r_1, r_2, r_3, r_4, \delta_a, \delta_q, \delta_h, \eta, p, c, \epsilon, \gamma, q\}$ is shown in Table 2.

In Figs. 2 and 3 it is shown that our model fits really well to the given real data of Argentina. The estimated value of the basic reproductive number \mathcal{R}_0 is about ~ 1.41 (95% CI: 1.2–1.6) as of March 10, 2021. This value could change (increase or decrease) in future cause of the new wave of Covid-19 which will totally depend on our health care measures. The disease could fade out at the end of December 2021. All necessary parameter values aspects applied to justify this scenario are mentioned in Table 2. In Fig. 4 the new daily and reported cases projected in Argentina from March 2020 to late May 2021 are given. In Fig. 5 cumulative infected cases and projected in the same dates are provided.

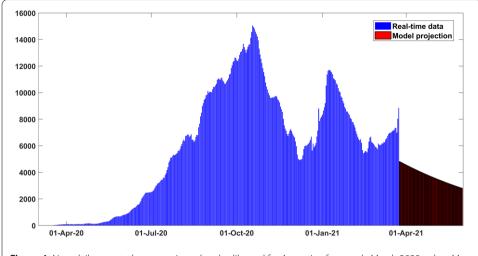
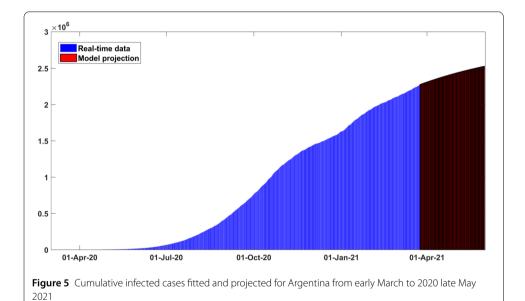


Figure 4 New daily reported cases projected and calibrated for Argentina from early March 2020 to late May 2021



4 Atangana-Baleanu fractional-order model

From the above integer-order simulations, we can see that the given model is working good to project real data for future. However, the integer-order model is not giving us much varieties in our predictions. In such cases, fractional-order derivatives always provide us a chance to obtain better predictions under the given real-data range. Motivated by this fact, we replace the above classical model into Atangana–Baleanu type fractional-order model which is defined under the Mittag-Leffler kernel.

4.1 Preliminaries

Some important definitions are recalled here.

Definition 1 ([40]) Given $S \in \mathcal{H}^1(u, v)$, where v > u and $0 \le \Phi \le 1$, the non-classical type Atangana–Baleanu (AB) derivative is stated as

$${}_{u}^{ABC}D_{t}^{\Phi}\left(\mathcal{S}(t)\right) = \frac{\mathrm{ABC}[\Phi]}{1-\Phi} \int_{u}^{t} \mathcal{S}'(\eta) E_{\Phi} \left[\Phi \frac{\left(t-\eta\right)^{\Phi}}{\Phi-1}\right] d\eta, \tag{7}$$

where ABC[Φ] verifying ABC[0] = ABC[1] = 1 designates the normalization function and $E_{\Phi}(\cdot)$ is the Mittag-Leffler function with one-parameter.

Definition 2 ([40]) The non-classical type AB integral for normalization function $ABC[\Phi]$ is set as

$${}_{u}^{ABC}I_{t}^{\Phi}\left(\mathcal{S}(t)\right) = \frac{1-\Phi}{\mathrm{ABC}[\Phi]}\mathcal{S}(t) + \frac{\Phi}{\Gamma(\Phi)\mathrm{ABC}[\Phi]}\int_{u}^{t}\mathcal{S}(\eta)(t-\eta)^{\Phi-1}\,d\eta. \tag{8}$$

Lemma 2 ([40]) *The solution of the given system for* $0 < \Phi < 1$

$$^{\mathcal{ABC}}\mathbf{D}_{0}^{\Phi}x(t)=z(t), \quad t\in[0,T],$$
 $x(0)=x_{0},$

is stated as

$$x(t) = x_0 + \frac{(1-\Phi)}{\text{ABC}(\Phi)}z(t) + \frac{\Phi}{\text{ABC}(\Phi)\Gamma(r)} \int_0^t (t-\omega)^{\Phi-1}z(\omega) d\omega.$$

Lemma 3 ([41]) If $0 < \Phi < 1$ and a_1 is a non-negative integer, then there exist constants $C_{\Phi,1} > 0$ and $C_{\Phi,2} > 0$ only dependent on Φ , such that

$$(a_1+1)^{\Phi}-a_1^{\Phi}\leq C_{\Phi,1}(a_1+1)^{\Phi-1}$$

and

$$(a_1+2)^{\phi+1}-2(a_1+1)^{\phi+1}+a_1^{\phi+1}\leq C_{\phi,2}(a_1+1)^{\phi-1}.$$

Lemma 4 ([41]) Let us suppose $v_{p,n} = (n-p)^{\Phi-1}$ (p = 1, 2, ..., n-1) and $v_{p,n} = 0$ for $p \ge n$, $\Phi, M, h, T > 0$, $a_1h \le T$ and a_1 is a positive integer. Let $\sum_{p=a_1}^{p=n} v_{p,n} |e_p| = 0$ for $k > n \ge 1$. If

$$|e_n| \le Mh^{\phi} \sum_{n=1}^{n-1} v_{p,n} |e_p| + |\eta_0|, \quad n = 1, 2, \dots, a_1,$$

then

$$|e_{a_1}| \le C|\eta_0|$$
, $a_1 = 1, 2, ...,$

where C is a positive constant independent of a_1 and h.

4.2 Unique solution existence for fractional-order model

Let consider the Banach space $\mathbf{Z} = \mathbf{X} \times \mathbf{X} \times \mathbf{X} \times \mathbf{X} \times \mathbf{X} \times \mathbf{X} \times \mathbf{X}$, where $\mathbf{X} = C[0, T]$ endowed with the norm-function $||A|| = ||(S, C, E, A, Q, H, R)|| = \max_{t \in [0, T]} [|S(t)| + |C(t)| + |E(t)| + |A(t)| + |Q(t)| + |H(t)| + |R(t)|].$

Theorem 1 ([42]) Consider **B** to be a convex subset of **Z** and let **F**, **G** depict couple operators satisfying

- 1. $\mathbf{F}u + \mathbf{G}u \in \mathbf{B} \ \forall u \in \mathbf{B}$;
- 2. **F** is a contraction;
- 3. **G** is compact and continuous.

Then $\mathbf{F}u + \mathbf{G}u = u$ possesses at least one solution."

Now the generalization of the classical model (1) in the Atangana–Baleanu fractional derivative sense reads as follows:

$$\begin{cases} {}^{ABC}D_{t}^{\Phi}S(t) = pC(t) - cS(t) - \left[\frac{\beta(A(t) + \eta Q(t))}{N(t)}\right]S(t), \\ {}^{ABC}D_{t}^{\Phi}C(t) = cS(t) - pC(t) - (1 - \epsilon)\left[\frac{\beta(A(t) + \eta Q(t))}{N(t)}\right]C(t), \\ {}^{ABC}D_{t}^{\Phi}E(t) = \left[\frac{\beta(A(t) + \eta Q(t))}{N(t)}\right]\left[S(t) + (1 - \epsilon)C(t)\right] - \gamma E(t), \\ {}^{ABC}D_{t}^{\Phi}A(t) = q\gamma E(t) + r_{3}\sigma_{2}Q(t) - (\sigma_{1} + \delta_{a})A(t), \\ {}^{ABC}D_{t}^{\Phi}Q(t) = (1 - q)\gamma E(t) + r_{1}\sigma_{1}A(t) - (\sigma_{2} + \delta_{q})Q(t), \\ {}^{ABC}D_{t}^{\Phi}H(t) = r_{2}\sigma_{1}A(t) + r_{4}\sigma_{2}Q(t) - (\sigma_{3} + \delta_{h})H(t), \\ {}^{ABC}D_{t}^{\Phi}R(t) = (1 - r_{1} - r_{2})\sigma_{1}A(t) + (1 - r_{3} - r_{4})\sigma_{2}Q(t) + \sigma_{3}H(t), \end{cases}$$

where ${}^{ABC}D_t^{\Phi}$ is the Atangana–Baleanu operator of fractional order Φ . Now we rewrite the right-hand side of model (9) as follows:

$$\begin{cases} f_{1}(t,S,...,R) = pC(t) - cS(t) - \left[\frac{\beta(A(t) + \eta Q(t))}{N(t)}\right] S(t), \\ f_{2}(t,S,...,R) = cS(t) - pC(t) - (1 - \epsilon) \left[\frac{\beta(A(t) + \eta Q(t))}{N(t)}\right] C(t), \\ f_{3}(t,S,...,R) = \left[\frac{\beta(A(t) + \eta Q(t))}{N(t)}\right] \left[S(t) + (1 - \epsilon)C(t)\right] - \gamma E(t), \\ f_{4}(t,S,...,R) = q\gamma E(t) + r_{3}\sigma_{2}Q(t) - (\sigma_{1} + \delta_{a})A(t), \\ f_{5}(t,S,...,R) = (1 - q)\gamma E(t) + r_{1}\sigma_{1}A(t) - (\sigma_{2} + \delta_{q})Q(t), \\ f_{6}(t,S,...,R) = r_{2}\sigma_{1}A(t) + r_{4}\sigma_{2}Q(t) - (\sigma_{3} + \delta_{h})H(t), \\ f_{7}(t,S,...,R) = (1 - r_{1} - r_{2})\sigma_{1}A(t) + (1 - r_{3} - r_{4})\sigma_{2}Q(t) + \sigma_{3}H(t). \end{cases}$$

$$(10)$$

By using (10), we have

$$\mathcal{ABC}\mathbf{D}_{t}^{\Phi}\mathcal{A}(t) = \Phi(t, \mathcal{A}(t)), \quad t \in [0, \tau], 0 < \Phi \le 1,$$

$$\mathcal{A}(0) = \mathcal{A}_{0}. \tag{11}$$

According to Lemma 2, (11) yields

$$\mathcal{A}(t) = \mathcal{A}_0(t) + \left[\Phi(t, \mathcal{A}(t)) - \Phi_0(t)\right] \frac{(1 - \Phi)}{\text{ABC}(\Phi)} + \frac{\Phi}{\Gamma(\Phi) \text{ABC}(\Phi)} \int_0^t (t - \omega)^{\Phi - 1} \Phi(\omega, \mathcal{A}(\omega)) d\omega, \tag{12}$$

where

$$A(t) = \begin{cases} S(t), & S_0, \\ C(t), & S_0, \\ E(t), & S_0, \\ A(t), & A_0(t) = \\ A(t), & A_0(t)$$

Applying (12) and (13), the two operators F, G are defined as

$$\mathbf{F}(\mathcal{A}) = \mathcal{A}_0(t) + \left[\Phi(t, \mathcal{A}(t)) - \Phi_0(t)\right] \frac{(1 - \Phi)}{\mathrm{ABC}(\Phi)},$$

$$\mathbf{G}(\mathcal{A}) = \frac{\Phi}{\Gamma(\Phi)\mathrm{ABC}(\Phi)} \int_0^t (t - \omega)^{\theta - 1} \Phi(\omega, \mathcal{A}(\omega)) d\omega. \tag{14}$$

We now state some basic axioms and the Lipschitzian hypothesis for showing the existence and uniqueness of a solution:

(H1) There are C_{Φ} , $D_{\Phi} > 0$ such that

$$|\Phi(t,\mathcal{A}(t))| \leq C_{\Phi}|\mathcal{A}| + D_{\Phi}.$$

(H2) There is $L_{\Phi} > 0$ such that $\forall \mathcal{A}, \bar{\mathcal{A}} \in \mathbf{Z}$ and it follows that

$$|\Phi(t,\mathcal{A}) - \Phi(t,\bar{\mathcal{A}})| < L_{\Phi}[|\mathcal{A} - \bar{\mathcal{A}}|].$$

Theorem 2 Under the hypotheses (H1), (H2), Eq. (12) possesses at least one solution, which implies that fractional model (9) possesses an equal number of solutions only if $\frac{(1-\Phi)}{ABC(\Phi)}L_{\Phi} < 1$.

Proof The proof is given in two parts.

Step I: Consider $\bar{A} \in \mathbf{B}$, where $\mathbf{B} = \{A \in \mathbf{Z} : ||A|| \le \rho, \rho > 0\}$ is closed and convex. The operator **F** provided in (14) gives

$$\|\mathbf{F}(\mathcal{A}) - \mathbf{F}(\bar{\mathcal{A}})\| = \frac{(1-\Phi)}{\mathrm{ABC}(\Phi)} \max_{t \in [0,\tau]} |\Phi(t,\mathcal{A}(t)) - \Phi(t,\bar{\mathcal{A}}(t))|,$$

$$\leq \frac{(1-\Phi)}{ABC(\Phi)} L_{\Phi} \| \mathcal{A} - \bar{\mathcal{A}} \|. \tag{15}$$

Thus, **F** is a contraction.

Step-II: We want **G** to be relatively compact. Clearly, it is sufficient if **G** is equicontinuous and bounded. Indeed, **G** is continuous as Φ is continuous and for all $A \in \mathbf{B}$, one has

$$\|\mathbf{G}(\mathcal{A})\| = \max_{t \in [0,\tau]} \|\frac{\Phi}{\Gamma(\Phi) ABC(\Phi)} \int_{0}^{t} (t - \omega)^{\Phi - 1} \Phi(\omega, \mathcal{A}(\omega)) d\omega|,$$

$$\leq \frac{\Phi}{\Gamma(\Phi) ABC(\Phi)} \int_{0}^{\tau} (\tau - \omega)^{\Phi - 1} |\Phi(\omega, \mathcal{A}(\omega))| d\omega,$$

$$\leq \frac{\tau^{\Phi}}{ABC(\Phi) \Gamma(\Phi)} [C_{\Phi} \rho + D_{\Phi}]. \tag{16}$$

Hence (16) shows the boundedness of **G**. For equicontinuity we assume $t_1 > t_2 \in [0, \tau]$, so that

$$\begin{aligned} \left| \mathbf{G}(\mathcal{A}(t_{1}) - \mathbf{G}(\mathcal{A}(t_{1})) \right| \\ &= \frac{\Phi}{\mathrm{ABC}(\Phi)\Gamma(\Phi)} \left| \int_{0}^{t_{1}} (t_{1} - \omega)^{\Phi - 1} \Phi(\omega, \mathcal{A}(\omega)) d\omega - \int_{0}^{t_{1}} (t_{1} - \omega)^{\Phi - 1} \Phi(\omega, \mathcal{A}(\omega)) d\omega \right|, \\ &\leq \frac{\left[C_{\Phi} \rho + D_{\Phi} \right]}{\mathrm{ABC}(\Phi)\Gamma(\Phi)} \left[t_{1}^{\Phi} - t_{2}^{\Phi} \right]. \end{aligned} \tag{17}$$

The right-hand side in (17) goes to zero as $t_1 \rightarrow t_2$ and then

$$|\mathbf{G}(\mathcal{A}(t_1) - \mathbf{G}(\mathcal{A}(t_1))| \to 0$$
, as $t_1 \to t_2$

since G is continuous. Because of the boundedness and continuity of G, then G is uniformly continuous and bounded. According to the Arzelá–Ascoli theorem, G is thus relatively compact and therefore entirely continuous. Consequently, the integral equation (12) and also the method have at least one solution.

We now proceed to show the uniqueness of the solution.

Theorem 3 Assuming (H_2) , Eq. (12) has a unique solution and this implies that model (9) has a unique solution only if $\left[\frac{(1-\Phi)L_{\Phi}}{ABC(\Phi)} + \frac{\tau^{\Phi}L_{\Phi}}{ABC(\Phi)\Gamma(\Phi)}\right] < 1$.

Proof Consider $T: \mathbb{Z} \to \mathbb{Z}$ defined as

$$T\mathcal{A}(t) = \mathcal{A}_{0}(t) + \left[\Phi(t, \mathcal{A}(t)) - \Phi_{0}(t)\right] \frac{(1 - \Phi)}{ABC(\Phi)} + \frac{\Phi}{ABC(\Phi)\Gamma(\Phi)} \int_{0}^{t} (t - \omega)^{\Phi - 1} \Phi(\omega, \mathcal{A}(\omega)) d\omega, \quad t \in [0, \tau].$$
(18)

Given $A, \bar{A} \in \mathbf{Z}$, then one can take

$$\|\mathbf{T}\mathcal{A} - \mathbf{T}\bar{\mathcal{A}}\| \leq \frac{(1-\Phi)}{\mathrm{ABC}(\Phi)} \max_{t \in [0,\tau]} |\Phi(t,\mathcal{A}(t)) - \Phi(t,\bar{\mathcal{A}}(t))|,$$

$$+ \frac{\Phi}{\Gamma(\Phi) ABC(\Phi)} \times \max_{t \in [0,\tau]} \left| \int_{0}^{t} (t - \omega)^{\Phi - 1} \Phi(\omega, A(\omega)) d\omega - \int_{0}^{t} (t - \omega)^{\Phi - 1} \Phi(\omega, \bar{A}(\omega)) d\omega \right|,$$

$$\leq \Xi \| A - \bar{A} \|, \tag{19}$$

where

$$\Xi = \left[\frac{(1 - \Phi)L_{\Phi}}{ABC(\Phi)} + \frac{\tau^{\Phi}L_{\Phi}}{\Gamma(\Phi)ABC(\Phi)} \right]. \tag{20}$$

Thus, **T** is a contraction. Therefore, Eq. (12) possesses a unique solution and so does model (9).

4.3 Derivation of solution

To date, number of numerical approximation algorithms have been proposed to solve the various kind of models describing the real world problems. When we apply such algorithms the analysis of convergence and stability are two important aspects of the effectiveness of the method. For solving our model, we are going to use predictor–corrector method, which has been defined probably for all fractional-order operators. Here we implement this algorithm in the sense of Atangana–Baleanu operator for writing the solution of the proposed COVID-19 model. For more information about this technique see Ref. [43]. We first recall Eq. (11) and consider

$$\mathcal{ABC}\mathbf{D}_{t}^{\Phi}\mathcal{A}(t) = \Phi(t, \mathcal{A}(t)), \quad t \in [0, \tau], 0 < \Phi \le 1,$$

$$\mathcal{A}(0) = \mathcal{A}_{0}. \tag{21}$$

The fractional Volterra integral equation is stated as

$$\mathcal{A}_{i+1} = \mathcal{A}_0 + (1 - \Phi)\Phi(t_{i+1}, \mathcal{A}_{i+1}) + \frac{\Phi}{\Gamma(\Phi)} \int_0^{t_{i+1}} (t_{i+1} - s)^{\Phi - 1} \Phi(s, \mathcal{A}(s)) ds.$$
 (22)

According to the method proposed in [43] for $\Phi \in [0,1]$, $0 \le t \le T$ and considering h = T/N and $t_n = nh$, for $n = 0, 1, 2, ..., N \in \mathbb{Z}^+$, the corrector formula for the given system is

$$\mathcal{A}_{i+1} = \mathcal{A}_0 + \frac{\Phi h^{\varsigma}}{\Gamma(\Phi + 2)} \left(a_{i+1,i+1} \Phi(t_{i+1}, \mathcal{A}_{i+1}^P) + \sum_{j=0}^i a_{i+1,j} \Phi(t_j, \mathcal{A}_j) \right), \tag{23}$$

where

$$a_{i+1,j} = \begin{cases} i^{\Phi+1} - (i-\Phi)(i+1)^{\Phi} & \text{if } j = 0, \\ (i-j+2)^{\Phi+1} + (i-j)^{\Phi+1} - 2(i-j+1)^{\Phi+1} & \text{if } 1 \le j \le i, \\ 1, \quad j = i+1, \end{cases}$$
(24)

and

$$a_{i+1,i+1} = 1 + \frac{(1-\Phi)\Gamma(\Phi+2)}{\Phi h^{\Phi}}.$$

The predictor formula is attained as

$$\mathcal{A}_{i+1}^{P} = \mathcal{A}_{0} + \frac{h^{\Phi}}{\Gamma(\Phi)} \sum_{j=0}^{i} b_{i+1,j} \Phi(t_{j}, \mathcal{A}_{j}), \tag{25}$$

where

$$b_{i+1,j} = \begin{cases} -(i-j)^{\phi} + (i-j+1)^{\phi}, & j = 0, \dots, i-1, \\ 1 + \frac{(1-\phi)\Gamma(\phi)}{h^{\phi}}, & j = i. \end{cases}$$
 (26)

Hence the corrector formulas for the given model (9) are stated as

$$\begin{split} S_{i+1} &= S_0 + \frac{\Phi h^{\Phi}}{\Gamma(\Phi + 2)} \left((a_{i+1,i+1}) f_1(t_{i+1}, S_{i+1}^P, C_{i+1}^P, E_{i+1}^P, A_{i+1}^P, Q_{i+1}^P, H_{i+1}^P, R_{i+1}^P) \right. \\ &+ \sum_{j=0}^i (a_{i+1,j}) f_1(t_i, S_j, C_j, E_j, A_j, Q_j, H_j, R_j) \right), \\ C_{i+1} &= C_0 + \frac{\Phi h^{\Phi}}{\Gamma(\Phi + 2)} \left((a_{i+1,i+1}) f_2(t_{i+1}, S_{i+1}^P, C_{i+1}^P, E_{i+1}^P, A_{i+1}^P, Q_{i+1}^P, H_{i+1}^P, R_{i+1}^P) \right. \\ &+ \sum_{j=0}^i (a_{i+1,j}) f_2(t_i, S_j, C_j, E_j, A_j, Q_j, H_j, R_j) \right), \\ E_{i+1} &= E_0 + \frac{\Phi h^{\Phi}}{\Gamma(\Phi + 2)} \left((a_{i+1,i+1}) f_3(t_{i+1}, S_{i+1}^P, C_{i+1}^P, E_{i+1}^P, A_{i+1}^P, Q_{i+1}^P, H_{i+1}^P, R_{i+1}^P) \right. \\ &+ \sum_{j=0}^i (a_{i+1,j}) f_3(t_i, S_j, C_j, E_j, A_j, Q_j, H_j, R_j) \right), \\ A_{i+1} &= A_0 + \frac{\Phi h^{\Phi}}{\Gamma(\Phi + 2)} \left((a_{i+1,i+1}) f_4(t_{i+1}, S_{i+1}^P, C_{i+1}^P, E_{i+1}^P, A_{i+1}^P, Q_{i+1}^P, H_{i+1}^P, R_{i+1}^P) \right. \\ &+ \sum_{j=0}^i (a_{i+1,j}) f_3(t_i, S_j, C_j, E_j, A_j, Q_j, H_j, R_j) \right), \\ Q_{i+1} &= Q_0 + \frac{\Phi h^{\Phi}}{\Gamma(\Phi + 2)} \left((a_{i+1,i+1}) f_5(t_{i+1}, S_{i+1}^P, C_{i+1}^P, E_{i+1}^P, A_{i+1}^P, Q_{i+1}^P, H_{i+1}^P, R_{i+1}^P) \right. \\ &+ \sum_{j=0}^i (a_{i+1,j}) f_5(t_i, S_j, C_j, E_j, A_j, Q_j, H_j, R_j) \right), \\ H_{i+1} &= H_0 + \frac{\Phi h^{\Phi}}{\Gamma(\Phi + 2)} \left((a_{i+1,i+1}) f_6(t_{i+1}, S_{i+1}^P, C_{i+1}^P, E_{i+1}^P, A_{i+1}^P, Q_{i+1}^P, H_{i+1}^P, R_{i+1}^P) \right. \\ &+ \sum_{j=0}^i (a_{i+1,j}) f_6(t_i, S_j, C_j, E_j, A_j, Q_j, H_j, R_j) \right), \\ R_{i+1} &= R_0 + \frac{\Phi h^{\Phi}}{\Gamma(\Phi + 2)} \left((a_{i+1,i+1}) f_7(t_{i+1}, S_{i+1}^P, C_{i+1}^P, E_{i+1}^P, A_{i+1}^P, Q_{i+1}^P, H_{i+1}^P, R_{i+1}^P) \right. \\ &+ \sum_{j=0}^i (a_{i+1,j}) f_6(t_i, S_j, C_j, E_j, A_j, Q_j, H_j, R_j) \right), \\ R_{i+1} &= R_0 + \frac{\Phi h^{\Phi}}{\Gamma(\Phi + 2)} \left((a_{i+1,i+1}) f_7(t_{i+1}, S_{i+1}^P, C_{i+1}^P, E_{i+1}^P, A_{i+1}^P, Q_{i+1}^P, H_{i+1}^P, R_{i+1}^P) \right. \\ &+ \sum_{j=0}^i (a_{i+1,j}) f_6(t_i, S_j, C_j, E_j, A_j, Q_j, H_j, R_j) \right), \\ R_{i+1} &= R_0 + \frac{\Phi h^{\Phi}}{\Gamma(\Phi + 2)} \left((a_{i+1,i+1}) f_7(t_{i+1}, S_{i+1}^P, C_{i+1}^P, E_{i+1}^P, A_{i+1}^P, Q_{i+1}^P, H_{i+1}^P, R_{i+1}^P) \right. \\ &+ \sum_{j=0}^i (a_{i+1,j}) f_7(t_{i+1}, S_{i+1}^P, C_{i+1}^P, C_{i+1}^P, E_{i+1}^P, A_{i+1}^P,$$

+
$$\sum_{j=0}^{i} (a_{i+1,j}) f_7(t_i, S_j, C_j, E_j, A_j, Q_j, H_j, R_j)$$

where

$$S_{i+1}^{P} = S_{0} + \frac{h^{\Phi}}{\Gamma(\Phi)} \sum_{j=0}^{i} b_{i+1,j} f_{1}(t_{j}, S_{j}, C_{j}, E_{j}, A_{j}, Q_{j}, H_{j}, R_{j}),$$

$$C_{i+1}^{P} = C_{0} + \frac{h^{\Phi}}{\Gamma(\Phi)} \sum_{j=0}^{i} b_{i+1,j} f_{2}(t_{j}, S_{j}, C_{j}, E_{j}, A_{j}, Q_{j}, H_{j}, R_{j}),$$

$$E_{i+1}^{P} = E_{0} + \frac{h^{\Phi}}{\Gamma(\Phi)} \sum_{j=0}^{i} b_{i+1,j} f_{3}(t_{j}, S_{j}, C_{j}, E_{j}, A_{j}, Q_{j}, H_{j}, R_{j}),$$

$$A_{i+1}^{P} = A_{0} + \frac{h^{\Phi}}{\Gamma(\Phi)} \sum_{j=0}^{i} b_{i+1,j} f_{4}(t_{j}, S_{j}, C_{j}, E_{j}, A_{j}, Q_{j}, H_{j}, R_{j}),$$

$$Q_{i+1}^{P} = Q_{0} + \frac{h^{\Phi}}{\Gamma(\Phi)} \sum_{j=0}^{i} b_{i+1,j} f_{5}(t_{j}, S_{j}, C_{j}, E_{j}, A_{j}, Q_{j}, H_{j}, R_{j}),$$

$$H_{i+1}^{P} = H_{0} + \frac{h^{\Phi}}{\Gamma(\Phi)} \sum_{j=0}^{i} b_{i+1,j} f_{6}(t_{j}, S_{j}, C_{j}, E_{j}, A_{j}, Q_{j}, H_{j}, R_{j}),$$

$$R_{i+1}^{P} = R_{0} + \frac{h^{\Phi}}{\Gamma(\Phi)} \sum_{i=0}^{i} b_{i+1,j} f_{7}(t_{j}, S_{j}, C_{j}, E_{j}, A_{j}, Q_{j}, H_{j}, R_{j}).$$

4.3.1 Stability of the method

Theorem 4 The given algorithm (27)–(28) is conditionally stable.

Proof Let $\tilde{\mathcal{A}}_0$, $\tilde{\mathcal{A}}_j$ ($j=0,\ldots,i+1$) and $\tilde{\mathcal{A}}_{i+1}^P$ ($i=0,\ldots,N-1$) be perturbations of \mathcal{A}_0 , \mathcal{A}_j and \mathcal{A}_{i+1}^P , respectively. Then the perturbation equations derived by using Eqs. (27) and (28) are given by

$$\tilde{\mathcal{A}}_{i+1}^{P} = \tilde{\mathcal{A}}_{0} + \frac{h^{\Phi}}{\Gamma(\Phi)} \sum_{j=0}^{i} b_{i+1,j} \left(\Phi(t_{j}, \mathcal{A}_{j} + \tilde{\mathcal{A}}_{j}) - \Phi(t_{j}, \mathcal{A}_{j}) \right), \tag{29}$$

$$\tilde{\mathcal{A}}_{i+1} = \tilde{\mathcal{A}}_{0} + \frac{\Phi h^{\Phi}}{\Gamma(\Phi + 2)} \left(a_{i+1,i+1} \left(\Phi \left(t_{i+1}, \mathcal{A}_{i+1}^{P} + \tilde{\mathcal{A}}_{i+1}^{P} \right) - \Phi \left(t_{i+1}, \mathcal{A}_{i+1}^{P} \right) \right) + \sum_{j=0}^{i} a_{i+1,j} \left(\Phi \left(t_{j}, \mathcal{A}_{j} + \tilde{\mathcal{A}}_{j} \right) - \Phi \left(t_{j}, \mathcal{A}_{j} \right) \right) \right).$$
(30)

According to the Lipschitz condition, we get

$$|\tilde{\mathcal{A}}_{i+1}| \le \Phi_0 + \frac{\Phi h^{\Phi} M}{\Gamma(\Phi + 2)} \left(a_{i+1,i+1} |\tilde{\mathcal{A}}_{i+1}^P| + \sum_{j=1}^i a_{j,i+1} |\tilde{\mathcal{A}}_j| \right),$$
 (31)

where $\Phi_0 = \max_{0 \le i \le N} \{ |\tilde{\mathcal{A}}_0| + \frac{\Phi h^\Phi M a_{i,0}}{\Gamma(\Phi+2)} |\tilde{\mathcal{A}}_0| \}$. Also, from Eq. (3.18) in [41] we write

$$\left|\tilde{\mathcal{A}}_{i+1}^{P}\right| \leq \eta_0 + \frac{h^{\Phi}M}{\Gamma(\Phi)} \sum_{j=1}^{i} b_{j,i+1} |\tilde{\mathcal{A}}_j|,\tag{32}$$

where $\eta_0 = \max_{0 \le i \le N} \{ |\tilde{\mathcal{A}}_0| + \frac{h^{\Phi}Mb_{n,0}}{\Gamma(\Phi)} |\tilde{\mathcal{A}}_0| \}$. Substituting $|\tilde{\mathcal{A}}_{i+1}^P|$ from Eq. (32) into Eq. (31) we find

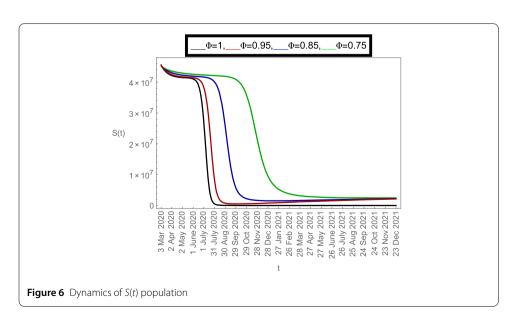
$$|\tilde{\mathcal{A}}_{i+1}| \leq \gamma_0 + \frac{\Phi h^{\Phi} M}{\Gamma(\Phi + 2)} \sum_{j=1}^{i} \left(a_{i+1,j} + \frac{h^{\Phi} M a_{i+1,i+1} b_{i+1,j}}{\Gamma(\Phi)} \right) |\tilde{\mathcal{A}}_{j}|$$

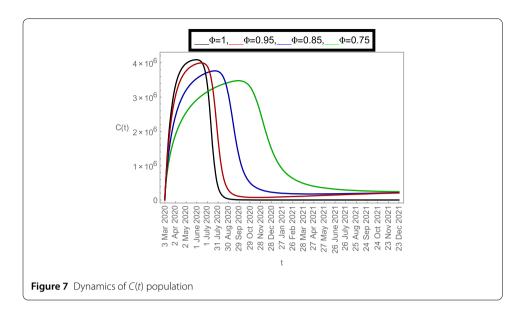
$$\leq \gamma_0 + \frac{\Phi h^{\Phi} M C_{\Phi,2}}{\Gamma(\Phi + 2)} \sum_{j=1}^{i} (i+1-j)^{\Phi-1} |\tilde{\mathcal{A}}_{j}|,$$
(33)

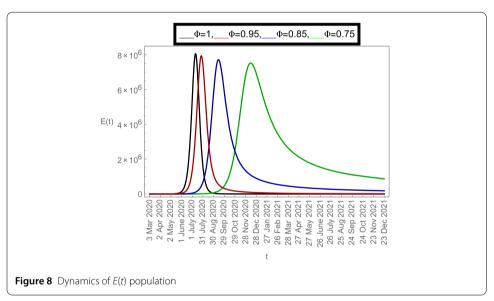
where $\gamma_0 = \max\{\Phi_0 + \frac{\Phi h^\Phi M a_{i+1,i+1}}{\Gamma(\Phi+2)}\eta_0\}$. $C_{\Phi,2} > 0$ is constant and only depends on Φ (see Lemma 3) and h is surmised to be small enough. From Lemma 4 we get $|\tilde{\mathcal{A}}_{i+1}| \leq C\gamma_0$, which finishes the requirement.

4.4 Graphical justifications

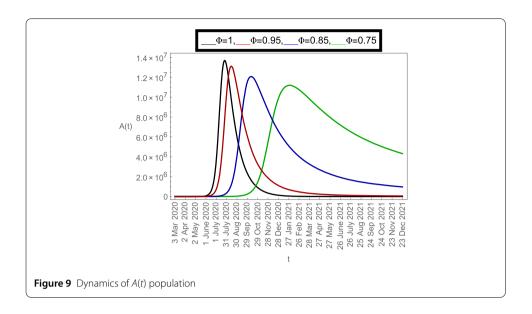
Now we plot the fractional-order solution by considering the parameter values simulated in Table 2. This time we used *Mathematica* software. In Fig. 6, we plotted the susceptible population S(t) and in Fig. 7, the plot of confined individuals C(t) is given. We can observe that when time increases then the population of susceptible individuals is decreasing which is a good indication for Argentina. In Fig. 8, we plotted the nature of exposed individuals E(t). We notice that when the fractional-order values decreases then the peak of E(t) shifts to the next month. At fractional order $\Phi = 1$, a peak occurs at near around 1 *July* 2020 and when we shifted to lower values of fractional order then we receive the peak near around 31 *July* 2020, at $\Phi = 0.95$, near around 29 *Sep* 2020, at $\Phi = 0.85$, and near around

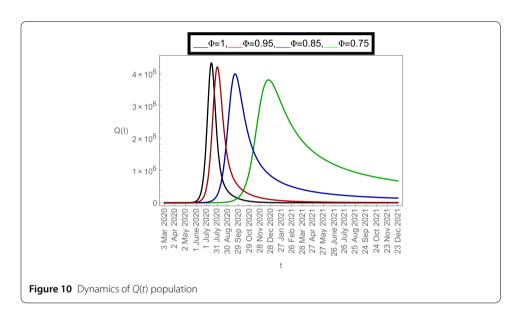






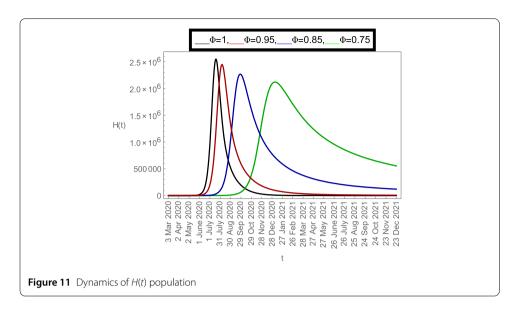
28 Dec 2020 when $\Phi=0.75$. This shows how the fractional-order derivatives give us more varieties to predict the real-data structure for the future. Similarly, in Fig. 9, we plotted the nature of asymptomatic individuals A(t) where we can see that at fractional-order $\Phi=1$, peak occurs at near around 31 July 2020 and when we shift to lower values of fractional order then we receive the peak near around 15 Aug 2020 at $\Phi=0.95$, near around 15 Oct 2020 at $\Phi=0.85$, and near around 27 Jan 2021 when $\Phi=0.75$. In this series, Fig. 10 plotted the nature of quarantined individuals Q(t) where different peaks can be seen. Here at fractional order $\Phi=1$, peak occurs at near around 15 July 2020 and when we shifted to lower values of fractional order then we obtain the peak around 31 July 2020 at $\Phi=0.95$, around 29 Sep 2020 at $\Phi=0.85$, and around 28 Dec 2020 at $\Phi=0.75$. Figure 11 described the behavior of hospitalized individuals H(t) for the given time range. Here at fractional order $\Phi=1$, a peak occurs around 15 July 2020 and when we shifted to lower values of fractional order then we receive the peak around 31 July 2020 at $\Phi=0.95$, around 29 Sep

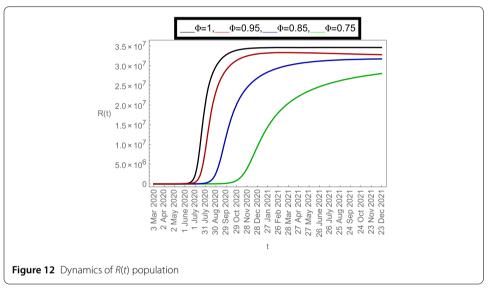




2020 at Φ = 0.85, and around 30 *Dec* 2020 at Φ = 0.75. Finally, Fig. 12 shows the nature of recovered individuals R(t) versus given time range.

All above given graphs confirm that the COVID-19 disease is under control in Argentina at this time stage (based on the given data simulations). However, it is well known that if the population does not follow all health care measures then the situation may change in the future. The given fractional-order model under Mittag-Leffler kernel gives very well outputs to predict the dynamics of COVID-19 in Argentina. We used different fractional-order values for the comparisons because an integer-order model can provide a single peak prediction which does not show the varieties in the predictions. Different fractional-order values give various predictions which may in the future be more accurate. This is the ultimate advantage of using fractional derivatives.





5 Conclusion

In our observations, we have explored the dynamics of the most deathly disease of this decade, COVID-19 in Argentina by considering parameter values based on real data. Firstly, we considered the reported cases of this virus from *March* 03, 2020 to *March* 29, 2021 and projected it for the future time period by using our models. We proposed a Atangana–Baleanu type fractional-order model and solved it employing predictor–corrector (P-C) algorithm. After analyzing the biological nature of this virus, we formulated a mathematical structure to define its dynamics. We used a well-known effective optimization method based on the renowned trust-region-reflective (TRR) scheme to perform the model calibration. We plotted the real cases of COVID-19 and fitted our integer-order model with the data along with the calculation of basic reproductive number. In the simulations of fractional-order analysis, first we proved the existence of unique solution and then wrote the solution of the model along with the stability of the given P-C method. We performed separate graphs for every model class at different fractional-order values to

predict the future dynamics of the virus in Argentina. Finally, we conclude that this virus is under control in Argentina for future under the given data range and all health care measures. In the future, the given estimated parameter values and models can be used to provide further predictions on the transmission of this virus. The proposed mathematical model is effective and trustable for future use. Not only from a mathematical point of view but also from a medical perspective, this research study may become very useful for the medical authorities to simulate the outbreaks of COVID-19 in Argentina for a future time period. Still, all the peak predictions which have been simulated in this paper, do not claim with 100% certainty that the dynamics of COVID-19 will be as it is. It may differ because of many health care measures (like isolation strategies, hospital facilities, and vaccine availability) which have been mentioned in this study.

Acknowledgements

Not applicable.

Funding

The third author is supported by MICINN and FEDER, Project PID2019-105011GB-I00.

Availability of data and materials

All the data is included in the paper.

Competing interests

This research does not have any conflict of interest. There is funding available to support this study.

Authors' contributions

PK: Conceptualization, Data curation, Investigation, Methodology, Formal analysis, Visualization, Resources, Project administration, Writing-original draft. VSE: Supervision, Software, Investigation, Validation, Visualization, Writing-review & editing. MM-A: Conceptualization, Investigation, Formal analysis, Supervision, Writing-review & editing. RB:Conceptualization, Investigation, Writing-review & editing. AM: Conceptualization, Investigation, Writing-review & editing. All authors read and approved the final manuscript.

Author details

¹Department of Mathematics and Statistics, School of Basic and Applied Sciences, Central University of Punjab, Bathinda, Punjab 151001, India. ²Department of Mathematics, Faculty of Arts and Sciences, Ondokuz Mayis University, Atakum, 55200, Samsun, Turkey. ³Instituto Universitario de Matematica Pura y Aplicada, Universitat Politècnica de València, 46022 Valencia, Spain. ⁴Department of Electrical Engineering, National Institute of Technology, Silchar, India. ⁵School of Advanced Sciences & Languages, Department of Mathematics, VIT Bhopal University, Kottri Kalan (Village), 466 114, Sehore (District), Madhya Pradesh, India.

Publisher's Note

Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Received: 16 May 2021 Accepted: 7 July 2021 Published online: 20 July 2021

References

- 1. Wu, Z., McGoogan, J.M.: Characteristics of and important lessons from the coronavirus disease 2019 (Covid-19) outbreak in China: summary of a report of 72 314 cases from the Chinese center for disease control and prevention. JAMA 323(13), 1239–1242 (2020)
- Zhang, C., Zheng, W., Huang, X., Bell, E.W., Zhou, X., Zhang, Y.: Protein structure and sequence reanalysis of 2019-ncov genome refutes snakes as its intermediate host and the unique similarity between its spike protein insertions and hiv-1. J. Proteome Res. 19(4), 1351–1360 (2020)
- 3. Hui, D.S., Azhar, E.I., Madani, T.A., Ntoumi, F., Kock, R., Dar, O., Ippolito, G., Mchugh, T.D., Memish, Z.A., Drosten, C., et al.: The continuing 2019-ncov epidemic threat of novel coronaviruses to global health—the latest 2019 novel coronavirus outbreak in Wuhan, China. Int. J. Infect. Dis. 91, 264–266 (2020)
- 4. Elfiky, A.A., Mahdy, S.M., Elshemey, W.M.: Quantitative structure-activity relationship and molecular docking revealed a potency of anti-hepatitis C virus drugs against human corona viruses. J. Med. Virol. 89(6), 1040–1047 (2017)
- 5. Li, X., Zai, J., Zhao, Q., Nie, Q., Li, Y., Foley, B.T., Chaillon, A.: Evolutionary history, potential intermediate animal host, and cross-species analyses of Sars-Cov-2. J. Med. Virol. 92(6), 602–611 (2020)
- Wrapp, D., Wang, N., Corbett, K.S., Goldsmith, J.A., Hsieh, C.-L., Abiona, O., Graham, B.S., McLellan, J.S.: Cryo-em structure of the 2019-ncov spike in the prefusion conformation. Science 367(6483), 1260–1263 (2020)
- 7. Villar, J., Zhang, H., Slutsky, A.S.: Lung repair and regeneration in ards: role of pecam1 and wnt signaling. Chest 155(3), 587–594 (2019)
- 8. Wang, H., Ma, S.: The cytokine storm and factors determining the sequence and severity of organ dysfunction in multiple organ dysfunction syndrome. Am. J. Emerg. Med. 26(6), 711–715 (2008)

- 9. Wan, Y., Shang, J., Graham, R., Baric, R.S., Li, F.: Receptor recognition by the novel coronavirus from Wuhan: an analysis based on decade-long structural studies of Sars coronavirus. J. Virol. 94(7), e00127-20 (2020)
- 10. Tang, N.L.-S., Chan, P.K.-S., Wong, C.-K., To, K.-F., Wu, A.K.-L., Sung, Y.-M., Hui, D.S.-C., Sung, J.J.-Y., Lam, C.W.-K.: Early enhanced expression of interferon-inducible protein-10 (cxcl-10) and other chemokines predicts adverse outcome in severe acute respiratory syndrome. Clin. Chem. **51**(12), 2333–2340 (2005)
- Gu, J., Korteweg, C.: Pathology and pathogenesis of severe acute respiratory syndrome. Am. J. Pathol. 170(4), 1136–1147 (2007)
- 12. Ho, J.C., Chan, K.N., Hu, W.H., Lam, W.K., Zheng, L., Tipoe, G.L., Sun, J., Leung, R., Tsang, K.W.: The effect of aging on nasal mucociliary clearance, beat frequency, and ultrastructure of respiratory cilia. Am. J. Respir. Crit. Care Med. 163(4), 983–988 (2001)
- 13. Kumar, P., Erturk, V.S., Murillo-Arcila, M.: A new fractional mathematical modelling of Covid-19 with the availability of vaccine. Results Phys. 24, 104213 (2021)
- 14. Kumar, P., Erturk, V.S.: A case study of Covid-19 epidemic in india via new generalised Caputo type fractional derivatives. Math. Methods Appl. Sci., 1–14 (2021)
- 15. Kumar, P., Erturk, V.S., Abboubakar, H., Nisar, K.S.: Prediction studies of the epidemic peak of coronavirus disease in Brazil via new generalised Caputo type fractional derivatives. Alex. Eng. J. **60**(3), 3189–3204 (2021)
- Nabi, K.N., Kumar, P., Erturk, V.S.: Projections and fractional dynamics of Covid-19 with optimal control strategies. Chaos Solitons Fractals 145, 110689 (2021)
- 17. Erturk, V.S., Kumar, P.: Solution of a Covid-19 model via new generalized Caputo-type fractional derivatives. Chaos Solitons Fractals 139, 110280 (2020)
- 18. Gao, W., Veeresha, P., Baskonus, H.M., Prakasha, D., Kumar, P.: A new study of unreported cases of 2019-ncov epidemic outbreaks. Chaos Solitons Fractals 138, 109929 (2020)
- Kumar, P., Suat Erturk, V.: The analysis of a time delay fractional Covid-19 model via Caputo type fractional derivative. Math. Methods Appl. Sci., 1–14 (2020)
- Atangana, A., Araz, S.İ.: Modeling and forecasting the spread of Covid-19 with stochastic and deterministic approaches: Africa and Europe. Adv. Differ. Equ. 2021(1), 1 (2021)
- 21. Atangana, A.: Modelling the spread of Covid-19 with new fractal-fractional operators: can the lockdown save mankind before vaccination? Chaos Solitons Fractals 136, 109860 (2020)
- 22. Atangana, A., Araz, S.İ.: Mathematical model of Covid-19 spread in Turkey and South Africa: theory, methods, and applications. Adv. Differ. Equ. 2020(1), 1 (2020)
- 23. Atangana, A., et al.: A novel Covid-19 model with fractional differential operators with singular and non-singular kernels: analysis and numerical scheme based on Newton polynomial. Alex. Eng. J. 60(4), 3781–3806 (2021)
- 24. Bulut, H., Kumar, D., Singh, J., Swroop, R., Baskonus, H.M.: Analytic study for a fractional model of hiv infection of cd4+ t lymphocyte cells. Math. Nat. Sci. 2(1), 33–43 (2018)
- 25. Zhoua, Y.-H., Yang, Y., Zhang, H.: Stability of non-monotone critical waves in a population dynamics model with spatio-temporal delay. Math. Nat. Sci. 2, 8–23 (2018)
- 26. Musa, S.S., Qureshi, S., Zhao, S., Yusuf, A., Mustapha, U.T., He, D.: Mathematical modeling of Covid-19 epidemic with effect of awareness programs. Infect. Dis. Model. 6, 448–460 (2021)
- Memon, Z., Qureshi, S., Memon, B.R.: Assessing the role of quarantine and isolation as control strategies for Covid-19 outbreak: a case study. Chaos Solitons Fractals 144, 110655 (2021)
- 28. Kumar, P., Suat Ertürk, V., Nisar, K.S.: Fractional dynamics of huanglongbing transmission within a citrus tree. Math. Methods Appl. Sci. (2021)
- 29. Kumar, P., Erturk, V.S., Murillo-Arcila, M.: A complex fractional mathematical modeling for the love story of layla and mainun. Chaos Solitons Fractals **150**, 111091 (2021)
- Kumar, P., Erturk, V.S., Yusuf, A., Kumar, S.: Fractional time-delay mathematical modeling of oncolytic virotherapy. Chaos Solitons Fractals 150, 111123 (2021)
- 31. Abboubakar, H., Kumar, P., Erturk, V.S., Kumar, A.: A mathematical study of a tuberculosis model with fractional derivatives. Int. J. Model. Simul. Sci. Comput. (2021)
- 32. Kumar, P., Rangaig, N.A., Abboubakar, H., Kumar, S.: A malaria model with Caputo–Fabrizio and Atangana–Baleanu derivatives. Int. J. Model. Simul. Sci. Comput. 12(2), 2150013 (2020)
- 33. Kumar, P., Erturk, V.S., Yusuf, A., Nisar, K.S., Abdelwahab, S.F.: A study on canine distemper virus (cdv) and rabies epidemics in the red fox population via fractional derivatives. Results Phys. 25, 104281 (2021)
- 34. Kumar, P., Erturk, V.S., Almusawa, H.: Mathematical structure of mosaic disease using microbial biostimulants via Caputo and Atangana–Baleanu derivatives. Results Phys. 24, 104186 (2021)
- 35. Kumar, P., Erturk, V.S.: Environmental persistence influences infection dynamics for a butterfly pathogen via new generalised Caputo type fractional derivative. Chaos Solitons Fractals 144, 110672 (2021)
- 36. Nabi, K.N., Abboubakar, H., Kumar, P.: Forecasting of Covid-19 pandemic: from integer derivatives to fractional derivatives. Chaos Solitons Fractals 141, 110283 (2020)
- 37. Van den Driessche, P., Watmough, J.: Reproduction numbers and sub-threshold endemic equilibria for compartmental models of disease transmission. Math. Biosci. **180**(1–2), 29–48 (2002)
- 38. Nabi, K.N.: Forecasting Covid-19 pandemic: a data-driven analysis. Chaos Solitons Fractals 139, 110046 (2020)
- 39. Politologue.com: Coronavirus (Covid19), https://coronavirus.politologue.com/coronavirus-cameroun.CM. Accessed 10 Jul 2020
- 40. Atangana, A., Baleanu, D.: New fractional derivatives with nonlocal and non-singular kernel: theory and application to heat transfer model (2016) arXiv:1602.03408
- 41. Li, C., Zeng, F.: The finite difference methods for fractional ordinary differential equations. Numer. Funct. Anal. Optim. 34(2), 149–179 (2013)
- Ahmed, E., El-Sayed, A., El-Saka, H., Ashry, G.A.: On applications of ulam-hyers stability in biology and economics (2010) arXiv:1004.1354
- 43. Baleanu, D., Jajarmi, A., Hajipour, M.: On the nonlinear dynamical systems within the generalized fractional derivatives with Mittag-Leffler kernel. Nonlinear Dyn. **94**(1), 397–414 (2018)