

## AMMONIA SLIP ESTIMATION BASED ON ASC CONTROL-ORIENTED MODELLING AND OBD NOX SENSOR CROSS-SENSITIVITY ANALYSIS

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### ABSTRACT

*The incoming emission regulations for internal combustion engines are gradually introducing new pollutant species, which requires greater complexity of the exhaust gas aftertreatment systems concerning layout, control and diagnostics. This is the case of ammonia, which is already regulated in heavy-duty vehicles and to be included in the emissions standards applied to passenger cars. The ammonia is injected into the exhaust gas through urea injections for NO<sub>x</sub> abatement in selective catalytic reduction (SCR) systems and can be also generated in other aftertreatment systems as three-way catalysts. However, ammonia slip may require removal on a dedicated catalyst called ammonia slip catalyst (ASC). The set consisting of the urea injection system, SCR and ASC requires control and on-board diagnostic tools to ensure high NO<sub>x</sub> conversion efficiency and minimization of the ammonia slip under real driving conditions. These tasks are based on the use of NO<sub>x</sub> sensors ZrO<sub>2</sub> pumping cell-based, which present as a drawback high cross-sensitivity to ammonia. Consequently, the presence of this species can affect the measurement of NO<sub>x</sub> and compromise SCR-ASC control strategies. In the present work, a methodology to predict ammonia and NO<sub>x</sub> tailpipe emissions is proposed. For this purpose, a control-oriented ASC model was developed to use its ammonia slip prediction to determine the cross-sensitivity correction of the NO<sub>x</sub> sensor placed downstream of the ASC. The model is based on a simplified solution of the transport equations of the species involved in the main ASC reactions. The ammonia slip model was calibrated using steady- and quasi-steady-state tests performed in a Euro 6c diesel engine. Finally, the performance of the proposed methodology to predict NO<sub>x</sub> and ammonia emissions was evaluated against experimental data corresponding to Worldwide harmonized Light vehicles Test Cycles (WLTC) applying different urea dosing strategies.*

Keywords: Exhaust aftertreatment, Ammonia slip catalyst, NO<sub>x</sub> sensor, OBD.

### NOMENCLATURE

#### ACRONIMS

ASC	Ammonia slip catalyst
ATS	Exhaust Aftertreatment Systems
DOC	Diesel oxidation catalyst
HP-EGR	High Pressure-Exhaust Gas Recirculation
OBD	On-board diagnostics
PGM	Platinum group metal
SCR	Selective catalytic reduction
SCRf	Selective catalytic reduction filter
WLTC	Worldwide harmonized Light vehicles Test Cycle
VGT	Variable geometry turbine

#### LATIN LETTERS

$A_{n,r}$	Preexponential factor
$E_{n,r}$	Activation energy
$k_{cell}$	Constant for cross-sensitivity
$K_{CS}$	Cross-sensitivity
$k_{n,r}$	Kinetic constant
$k_T$	Constant for temperature model
$\dot{m}$	Mass flow
$M_n$	Molecular weight
$R_r$	Reaction rate
$T$	Temperature
$u$	Gas velocity
$x$	Axial coordinate
$X_n$	Molar fraction

#### GREEK LETTERS

$\varepsilon$	Error
$\theta$	Coverage
$V_{n,r}$	Stoichiometric constant
$\sigma$	Standard deviation
$\psi$	Maximum capacity

## SUBSCRIPTS

cell	Sensor cell
in	Inlet
out	Outlet
sensor	Sensor

## SUPERSCRIPTS

t	Time
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## 1. INTRODUCTION

The regulation of pollutant emissions in internal combustion engines has progressively restricted the emissions of nitrogen oxides (NO<sub>x</sub>) [1], which are harmful to human health and environment [2]. Despite the evolution of combustion strategies to reduce the NO<sub>x</sub> formation [3], the use of exhaust gas after-treatment systems (ATS) is required to meet the emission standards limits [4]. Among the available alternatives, the most widespread catalyst for NO<sub>x</sub> emission control in Compression Ignition engines is the selective catalytic reduction (SCR) system [5]. SCR systems are based on the reduction of NO<sub>x</sub> to N<sub>2</sub> by means of ammonia (NH<sub>3</sub>) injected into the catalyst in the form of urea [6]. The SCR conversion efficiency depends on the amount of NH<sub>3</sub> loaded in the catalyst, which means that more ammonia is injected than necessary to reduce NO<sub>x</sub> [7], leading to a high NO<sub>x</sub> conversion efficiency, but consequently, more ammonia slip after the SCR catalyst. [8]. Moreover, the use of three-way catalysts in spark-ignition engines can lead to the formation of NH<sub>3</sub> [9]. To prevent tailpipe NH<sub>3</sub> emissions, ammonia slip catalysts (ASCs) are employed [10].

ASCs promote the oxidation of NH<sub>3</sub> in presence of O<sub>2</sub> to N<sub>2</sub> and water [11]. Currently, these systems combine an NH<sub>3</sub> oxidation catalyst component, commonly based on Platinum Group Metals (PGM), with an SCR catalyst since NO<sub>x</sub> species can be produced during the NH<sub>3</sub> oxidation [12]. There are several ways to combine these components. The most usual is to apply the SCR catalyst as a separate layer over the PGM one, thus creating a dual-layer washcoat structure. Nevertheless, the use of these two components together in a mono-layer structure can be also found in practical applications [13]. The reason for using two different substances is to achieve high NH<sub>3</sub> conversion efficiency increasing the selectivity of the oxidation to N<sub>2</sub> [14]. PGM particles are very active in the oxidation of NH<sub>3</sub> at the cost of low selectivity. This causes that at temperatures above 200 °C the oxidation of NH<sub>3</sub> on Platinum produces significant amounts of NO<sub>x</sub> [13]. To improve the N<sub>2</sub> selectivity of the system, SCR catalyst impregnation is used, usually Cu or Fe zeolites [13], as a way to promote the final conversion of the NO<sub>x</sub> produced by the NH<sub>3</sub> oxidation mechanism with the entering NH<sub>3</sub> [15].

For the understanding, optimization and control strategies development of this type of systems, the use of computational models is of great interest. The mathematical solvers of such systems involve axial flow advection in the monolithic channels, as well as coupled reaction / diffusion processes in the catalytic

layers [16]. In ASCs, the consideration of the NH<sub>3</sub> oxidation and NO<sub>x</sub> abatement reaction mechanism previously described is required [17].

The mathematical models that more accurately represent the real operation of this type of catalytic systems consist of non-linear partial differential equations in four independent variables, namely time and spatial coordinates. In this sense, it is possible to find models with different levels of complexity adapted to the particular application, from detailed design and analysis to on-board control. A simplification of this type of model is the one proposed by Torp *et al.* [13], based on a two-phase 1D-1D (pseudo 2D) single channel steady-state scheme for monolithic ASCs, distinguishing bulk gas from washcoat transport with up to two layers. Proposals of lower computational cost based on the use of reduced order models applied to two phase concepts are also available in the literature, such as the solution presented by Ratnakar *et al.* [18], based on multi-scale averaging method, or the Bisset's model [16], which provides an asymptotic solution of the reaction-diffusion problem. Finally, a step further in simplification consists of the use of pseudo-homogeneous models, which neglect the mass transfer from the bulk gas to the washcoat layers reducing the computational effort as compared to two-phase models [18].

In parallel, current and future regulations require the use of on-board diagnostics (OBD) to monitor the ATS performance and prevent its malfunction along lifetime [19]. Consequently, the control and diagnostics tasks of the SCR and ASC ideally require the use of NO<sub>x</sub> and also NH<sub>3</sub> sensors [20], the last still uncommon, combined to mathematical algorithms [21]. From the point of view of on-board measuring of both NO<sub>x</sub> and NH<sub>3</sub>, the most common approach is the use of amperometric sensors based on ZrO<sub>2</sub> pumping cell [22]. This type of sensor presents NH<sub>3</sub> cross-sensitivity as main drawback, what means that the actual NO<sub>x</sub> emission may not correspond to the sensor signal due to the presence of NH<sub>3</sub> [23]. This correction of the cross-sensitivity may require the use of NH<sub>3</sub> sensors or multiple NO<sub>x</sub> sensors with different degrees of sensitivity to NH<sub>3</sub> [23] at the expense of higher cost.

In this context, the present work proposes a methodology to predict NH<sub>3</sub> and NO<sub>x</sub> exhaust tailpipe emissions. As a first step, a control-oriented ASC model was developed to provide a prediction of the NH<sub>3</sub> slip at the ASC outlet using as input NO<sub>x</sub> and NH<sub>3</sub> emissions downstream the SCR system. This NH<sub>3</sub> prediction was used to determine the cross-sensitivity correction of the NO<sub>x</sub> sensor placed downstream of the ASC. The ASC model is based on a simplified solution of the transport equations of the reactants governing the main paths of the ASC reaction mechanism. The quasi-steady one-dimensional species conservation equation is explicitly solved under the assumption of negligible diffusion limitations, i.e. pseudo-homogeneous approach [18], and non-competitive reactions. It keeps the fundamental physical and chemical nature of the actual process while providing low complexity and computational effort

required for efficient OBD. The combined prediction of tailpipe  $\text{NH}_3$  and  $\text{NO}_x$  emissions was evaluated on a Euro 6 diesel engine installed on a fully instrumented test bench, a gas analyzer was also placed in the exhaust tailpipe to measure the actual emission of  $\text{NH}_3$  and  $\text{NO}_x$  separately. The performance of the proposed methodology was evaluated against experimental data corresponding to Worldwide harmonized Light vehicles Test Cycles (WLTC) tests in which different urea dosing strategies were imposed. As a result, the accuracy of the prediction of  $\text{NH}_3$  and  $\text{NO}_x$  tailpipe emissions is discussed, demonstrating the potential of modeling approaches to avoid the use of dedicated sensors for the  $\text{NH}_3$  slip prediction, while improving the  $\text{NO}_x$  measurement in the exhaust pipe.

## 2. MATERIALS AND METHODS

### 2.1 Experimental setup and test campaign

The engine used in this work was a serial production Euro 6c diesel engine for passenger car applications equipped with variable geometry turbine (VGT) and high-pressure exhaust gas recirculation (HP-EGR). Table 1 lists the main engine specifications.

**TABLE 1: MAIN CHARACTERISTICS OF THE ENGINE.**

Displaced volume	[cm <sup>3</sup> ]	1499
Bore	[mm]	75
Stroke	[mm]	84.8
Number of cylinders	[-]	4
Compression ratio	[-]	16.4:1
Maximum torque	[Nm@rpm]	300@1750
Maximum power	[kW@rpm]	96@3750
Emission standard	[-]	Euro 6c
EATS	[-]	DOC+SCRf+ASC

This engine was installed on an engine test bench equipped with a Horiba DYNAS3 asynchronous dynamometer, allowing dynamic and steady-state tests. Moreover, to ensure that the model was capable to be used in a real-time application, it was implemented into Simulink environment, compiled by the dSpace system, and connect via an ETK-ECU interface to an open ECU as a way to imposed the urea injection rate. The engine aftertreatment system (EATS) consisted of a close-coupled DOC, SCRf and ASC. In particular, the ASC was a dual-layer washcoat flow-through monolithic catalyst whose main geometrical characteristics are shown in Table 2.

The exhaust line was instrumented with K-type thermocouples at the inlet and outlet of every ATS monolith and an Horiba FTIR MEXA-ONE-FT engine exhaust gas analyzer sampling pollutant emissions upstream and downstream of the ASC. Finally, a  $\text{ZrO}_2$  pumping cell  $\text{NO}_x$  sensor was placed at the ASC outlet.

This experimental setup was applied to perform a series of tests driven to provide controlled ASC boundaries for model calibration and validation. A series of steady-state operating conditions, quasi-steady mapping tests and WLTC were performed including variations in the urea dosing strategy to feed the ASC with different  $\text{NH}_3$  concentration for the same fluid-dynamic conditions. To understand the application of each test, they are described in Sections 3.1 and 3.2, where the model performance is evaluated.

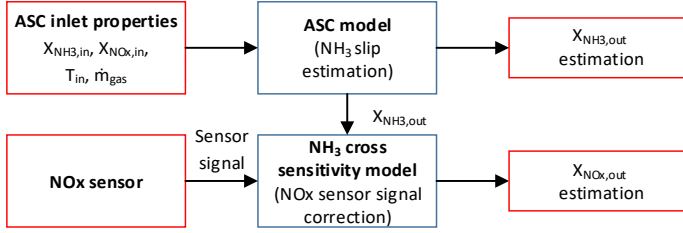
**TABLE 2: ASC GEOMETRIC PARAMETERS.**

Lenght	[m]	0.10
Diameter	[m]	0.14
Monolith Volume	[dm <sup>3</sup> ]	1.65
Channel cross-section	[-]	Square
Cell size	[mm]	0.9607
Wall thickness	[mm]	0.0762
Cell density	[cps]	600
Number of channels	[-]	15096
GSA (geometric specific area)	[1/m]	3574
CA (Catalytic area)	[m <sup>2</sup> ]	5.89

### 2.2 $\text{NO}_x$ & $\text{NH}_3$ estimation methodology

The proposed methodology to predict the  $\text{NH}_3$  and  $\text{NO}_x$  emissions downstream of the ASC is outlined in Figure 1. The  $\text{NH}_3$  and  $\text{NO}_x$  concentration, temperature and mass flow at the ASC inlet and a single  $\text{NO}_x$  sensor located downstream of the ASC are considered as boundary conditions.

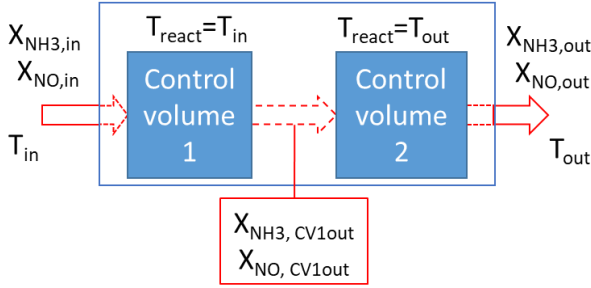
The use of two computational models is considered. The first model is a simplified ASC model that allows considering the  $\text{NH}_3$  accumulation reactions, as well as the elimination of accumulated  $\text{NH}_3$  through oxidation with  $\text{O}_2$  in the PGM layer and with  $\text{NO}_x$  in the SCR layer. The  $\text{NH}_3$  oxidation mechanism using  $\text{NO}_x$  is a simplified version of the complete SCR reactivity mechanism, considering that the set of reactions can be represented using the standard reaction of the SCR. Although it is assumed that this simplification allows a correct estimation of the  $\text{NH}_3$  oxidation rate, it is considered that the lack of detail of the model makes it not suitable for the prediction of the  $\text{NO}_x$  slip. For this reason, the focus of the ASC model is placed on the estimation of the  $\text{NH}_3$  emission, being necessary the use of a  $\text{NO}_x$  sensor to obtain the  $\text{NO}_x$  emissions at the ASC outlet. To correct the effect of  $\text{NH}_3$  emissions on the  $\text{NO}_x$  sensor signal, a second model is used, which allows the cross-sensitivity estimation. This model makes it possible to use the  $\text{NH}_3$  emissions estimated by the ASC model to reduce the error in the  $\text{NO}_x$  emission measurement.



**FIGURE 1:** FLOW-CHART OF THE PROPOSED METHODOLOGY FOR ASC NH<sub>3</sub> AND NO<sub>x</sub> SLIP PREDICTION.

### 2.3 ASC model

The ASC model is based on a lumped approach solving the chemical species transport in discrete control volumes explicitly. In this work, the monolith was divided into two volumes, as sketched in Figure 2, which were governed by different characteristic reaction temperature.



**FIGURE 2:** DISCRETIZATION OF THE ASC MODEL INTO CONTROL VOLUMES.

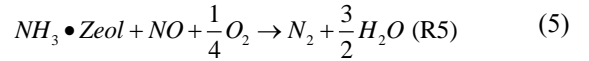
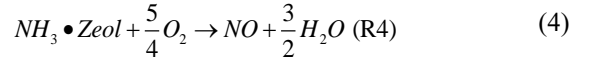
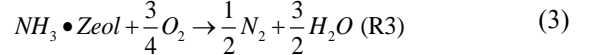
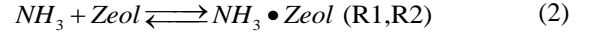
The temperature controlling the kinetics of the reaction mechanism in the first volume was assumed equal to the gas temperature provided by a sensor placed at the ASC inlet. The second control volume was aimed to represent the reactivity at the outlet region, so that the temperature of the gas at the ASC outlet was assumed. Since the engine did not account for an on-board temperature sensor at the ASC outlet, this temperature was calibrated from test bench temperature measurements correlating with the ASC gas inlet temperature on-board measurement according to Equation 1 [24].

$$T_{out}^t = k_{T,1} T_{out}^{t-1} + (1 - k_{T,1}) T_{in}^t + k_{T,2} \quad (1)$$

Due to the low amount of energy released by the reactions that take place in the ASC [25], this heat transfer model was decoupled from the chemical reactivity model. Nevertheless, its calibration, which was based on engine tests with urea injection, accounts implicitly for the energy released by the reactions.

In each control volume, the ASC model computed the variation in NH<sub>3</sub> and NO<sub>x</sub> along every control volume caused by the physisorption of NH<sub>3</sub> on the zeolites composing the SCR layer, the NO<sub>x</sub> reduction as well as the NH<sub>3</sub> oxidation to N<sub>2</sub> and NO. Equations 2-5 show the specific reactions considered in the model. This set of reactions is a reduced proposal of the global

mechanism of an ASC [15], highlighting the fact that only the standard reaction of the SCR was considered. On the one hand, this assumption responds to the need of NH<sub>3</sub> slip estimation with low computational effort. On the other hand, the NO<sub>2</sub> concentration at the ASC inlet is several orders of magnitude lower than that of NO [23]. The NO<sub>2</sub> estimation would require additional model features concerning combustion conditions as well as the transport of NO<sub>2</sub> along the catalyst, unbalancing the computational effort to accuracy trade-off negatively.



The NO and NH<sub>3</sub> conversion efficiency were determined solving the one-dimensional chemical species transport [26] assuming quasi-steady flow and neglecting the mass transfer from the bulk gas and the washcoat according to the pseudo-homogeneous approach, so that:

$$u \frac{dX_n}{dx} = \sum v_{n,r} R_{n,r} \quad (6)$$

In Equation (6),  $R_{n,r}$  and  $v_{n,r}$  are the reaction rate and the stoichiometric coefficient of species  $n$  in reaction  $r$ . The reaction rate for every reaction was depending on the kinetic constant, which was modelled according to the Arrhenius equation, and the composition. The adsorption and desorption processes involving NH<sub>3</sub> and zeolite sites on the washcoat were modelled taking into the NH<sub>3</sub> gas concentration and the cumulative amount as a function of the surface coverage ( $\theta_{NH_3}$ ) and the specific storage capacity of the washcoat ( $\psi_{NH_3}$ ):

$$R_{R1} = k_{NH_3,R1} \psi_{NH_3} (1 - \theta_{NH_3}) X_{NH_3} \quad (7)$$

$$R_{R2} = k_{NH_3,R2} \psi_{NH_3} \theta_{NH_3} \quad (8)$$

The reaction rate of every NH<sub>3</sub> oxidation reaction (NO<sub>x</sub> reduction, NH<sub>3</sub> oxidation to N<sub>2</sub> and NH<sub>3</sub> oxidation to NO) was modelled as:

$$R_{R3} = k_{O_2,R3} \psi_{NH_3} \theta_{NH_3} \quad (9)$$

$$R_{R4} = k_{O_2,R4} \psi_{NH_3} \theta_{NH_3} \quad (10)$$

$$R_{R5} = k_{NOx,R5} \psi_{NH_3} \theta_{NH_3} X_{NOx,in} \quad (11)$$

Therefore, assuming no competitiveness between reactions, the integration of Equation 6 yields the molar variation of the species  $n$  caused by the reaction  $r$  as:

$$u \frac{dX_{n,r}}{dx} = v_{n,r} R_{n,r} \rightarrow \int_{X_{n,in}}^{X_{n,in} + \Delta X_{n,r}} \frac{dX_{n,r}}{v_{n,r} R_{n,r}} = \int_0^L \frac{1}{u} dx \quad (12)$$

The concentration of NH<sub>3</sub> at the outlet of every control volume was calculated from the molar variation caused by the reactions involving NH<sub>3</sub> sorption in the washcoat as:

$$X_{NH_3, CVout} = X_{NH_3, CVin} + \Delta X_{NH_3, R1} + \Delta X_{NH_3, R2} \quad (13)$$

In a similar way, the cumulation of NH<sub>3</sub> in every control volume of the ASC was computed by means of the surface coverage as

$$\theta_{NH_3}^{t+1} = \frac{M_{NH_3}}{M} \sum \Delta X_{NH_3^s} \frac{\dot{m}}{\psi_{NH_3}} + \theta_{NH_3}^t, \quad (14)$$

where the variation in cumulated NH<sub>3</sub> was calculated from the transport of every reactant and the reaction mechanism stoichiometry as presented below:

$$\begin{aligned} \sum \Delta X_{NH_3^s} &= \frac{V_{NH_3^s, R1}}{V_{NH_3, R1}} \Delta X_{NH_3, R1} + \frac{V_{NH_3^s, R2}}{V_{NH_3, R2}} \Delta X_{NH_3, R2} + \\ &\frac{V_{NH_3^s, R3}}{V_{O_2, R3}} \Delta X_{O_2, R3} + \frac{V_{NH_3^s, R4}}{V_{O_2, R4}} \Delta X_{O_2, R4} + \frac{V_{NH_3^s, R5}}{V_{NOx, R5}} \Delta X_{NOx, R5} \\ &= -\Delta X_{NH_3, R1} - \Delta X_{NH_3, R2} + \frac{4}{3} \Delta X_{O_2, R3} + \frac{2}{5} \Delta X_{O_2, R4} + \Delta X_{NOx, R5} \end{aligned} \quad (15)$$

## 2.4 NH<sub>3</sub> cross-sensitivity for NOx sensor correction

The NH<sub>3</sub> cross-sensitivity model for the correction of the NOx sensor signal is described in detail by Pla *et al.* [23]. This model is based on the estimation of the oxidation rate of NH<sub>3</sub> to NOx within the sensor cell. This oxidation is highly dependent on the sensor cell temperature. Since this temperature cannot be measured, the energy balance in the sensor cell was solved assuming negligible cell volume, no heat transfer between the cell and the environment, constant electric heating rate and exothermics proportional to NH<sub>3</sub> molar fraction [23]. According to these hypotheses and rearranging the energy balance, the sensor cell temperature was finally expressed as

$$T_{cell}^{t+1} = T_{cell}^t + k_{cell,1} (T_{gas}^t - T_{cell}^t) + k_{cell,2} X_{NH_3} + k_{cell,3}, \quad (16)$$

where  $k_{cell,i}$  are physically-based constants experimentally determined.

Once the cell temperature was determined an empirical correlation, based on error function (erf), was proposed to estimate de cross-sensitivity factor as [23]

$$K_{CS}^t = 1 + k_{cell,4} \operatorname{erf} \left( \frac{T_{cell}^t - k_{cell,5}}{k_{cell,6}} \right), \quad (17)$$

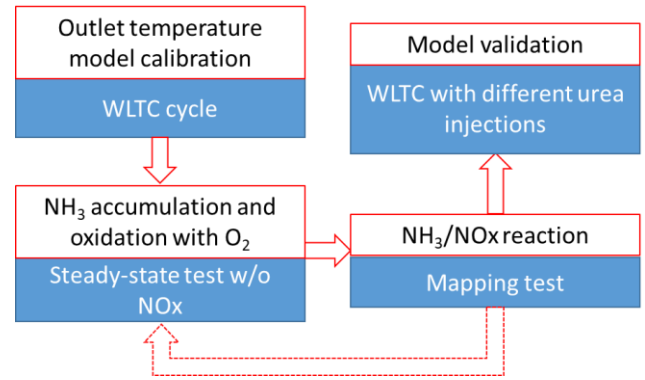
therefore, NOx sensor signal can be expressed as the addition of the NOx concentration and the concentration of NH<sub>3</sub> times the cross-sensitivity factor:

$$X_{NOx, sensor} = X_{NOx, out} + K_{CS}^t X_{NH_3, out} \quad (18)$$

## 3. RESULTS AND DISCUSSION

### 3.1 ASC model calibration and validation

Figure 3 shows the calibration procedure of the ASC and NH<sub>3</sub> cross-sensitivity models. As a first step, the correlation of the temperature prediction at the ASC outlet was calibrated from the inlet gas temperature in a WLTC test in order to account for the more demanding dynamic conditions and a wide temperature range.

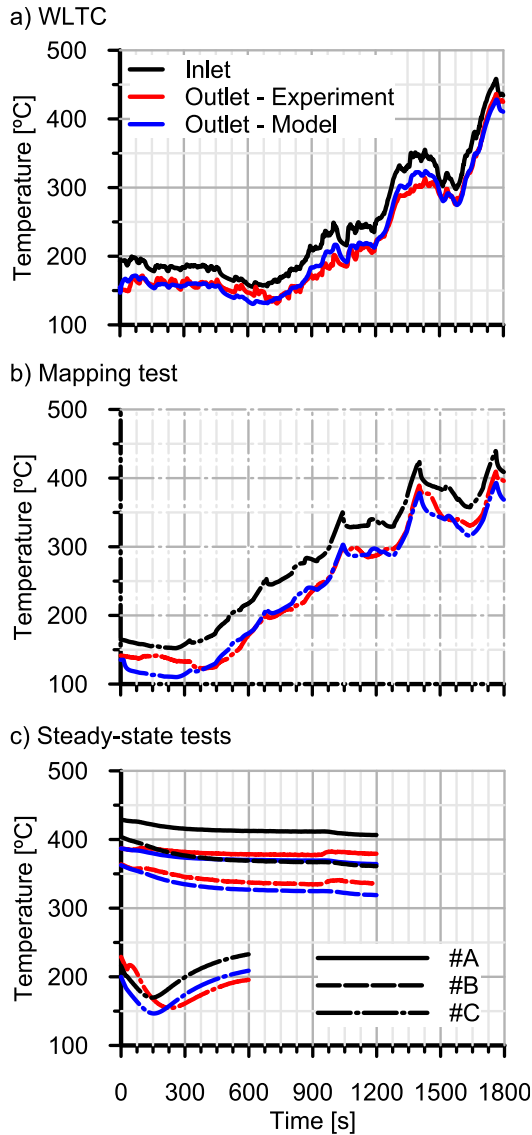


**FIGURE 3: FLOW-CHART OF THE CALIBRATION AND VALIDATION PROCEDURE.**

Figure 4(a) shows the calibration of the WLTC test, which provided the values for constants  $k_{t,1}$  (0.817) and  $k_{t,2}$  (-5.15). As observed, the model was able to capture with good accuracy the ASC outlet gas temperature, which in turn was applied as reaction temperature in the second control volume of the monolith. Figure 5 provides the error analysis of the ASC outlet gas temperature prediction based on the three- $\sigma$  rule [27]. The three- $\sigma$  rule defines three ranges around the mean value. The first one ( $1\sigma$ ) considers the error threshold with a probability of 68.27% to be not exceeded assuming a normal distribution, i.e.  $1\sigma$  represents the half-width interval of one standard deviation; the second range ( $2\sigma$ ) accounts a probability of 95.45% and, finally, the  $3\sigma$  error the 99.73% of points of the whole sample.

According to Figure 5, the error distribution underlines the low magnitude of the error in ASC outlet temperature calculation. The error was less than 10 °C for  $1\sigma$ , while values within a half-width interval of two standard deviations ( $2\sigma$ ) did

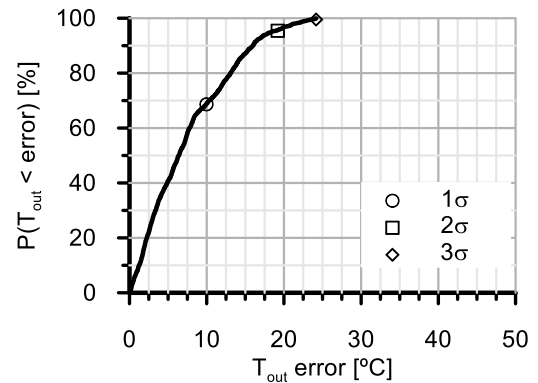
not exceed 20 °C. These low errors in calibration under dynamic operation were, in turn, kept in the prediction provided under different testing conditions, as shown in Figure 4(b), which presents the ASC outlet temperature along the quasi-steady state mapping test discussed next in this Section, and in Figure 4(c), which is dedicated to the steady-state operating points described in Table 3.



**FIGURE 4:** COMPARISON BETWEEN EXPERIMENTAL AND MODELED ASC OUTLET TEMPERATURE: (a) WLTC, (b) MAPPING TEST AND (c) STEADY-STATE TESTS.

The next step of the ASC model calibration was focused on the NH<sub>3</sub> adsorption-desorption and oxidation. Steady-state tests were performed to calibrate the kinetic term of the involved reactions. Table 3 lists the three operating points considered, which were monitored continuously to capture the dynamics in NH<sub>3</sub> slip imposed by the SCRf and the thermal transient. Every

operating point covered a different temperature range, being modified the urea injection amount of the standard ECU strategy in order to feed the ASC with different NH<sub>3</sub> slips from the SCRf.



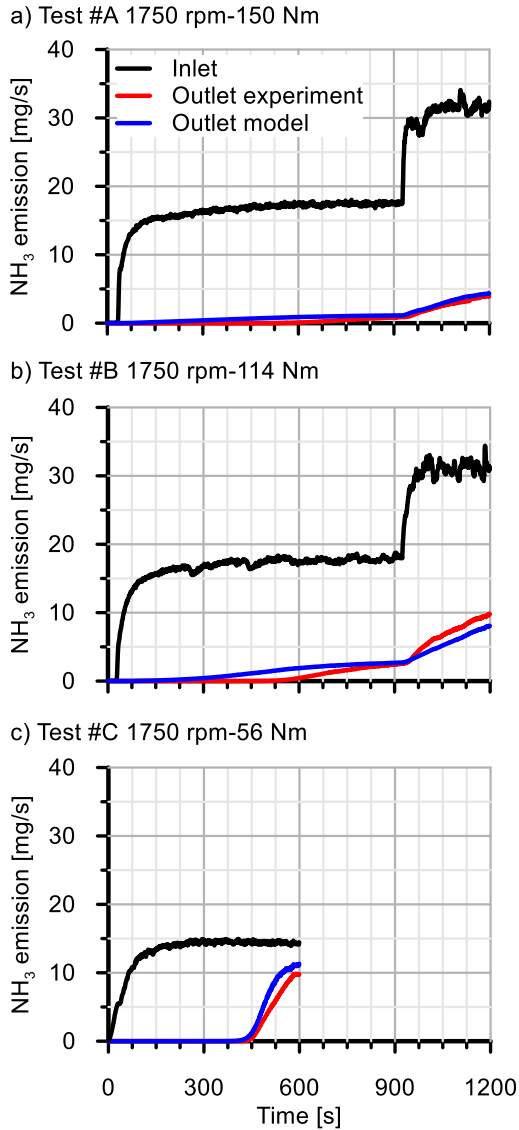
**FIGURE 5:** ASC OUTLET TEMPERATURE ERROR DISTRIBUTION IN WLTC TEST USED IN MODEL CALIBRATION.

**TABLE 3:** STEADY-STATE OPERATING POINTS FOR ASC MODEL CALIBRATION.

Point	Speed / torque	ASC T <sub>in</sub>	Urea injection rate
#A	1750 rpm -150 Nm	~420°C	150 mg/s (0-900 s) 250 mg/s (900 -1500 s)
#B	1750 rpm-114 Nm	~360°C	150 mg/s (0-900 s) 250 mg/s (900 -1500 s)
#C	1750 rpm-56 Nm	~210°C	100 mg/s (0-600 s)

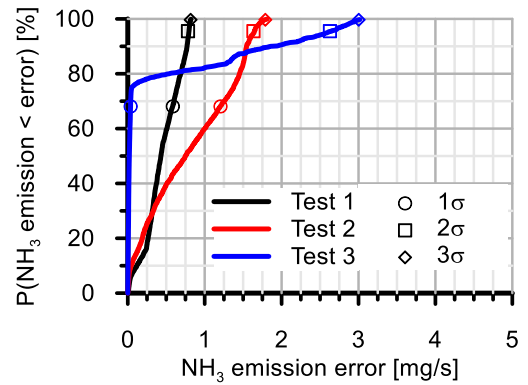
Figure 6 shows the experimental NH<sub>3</sub> mass flow profiles at the inlet and outlet sections of the ASC comparing against the model prediction. As observed, once the SCRf NH<sub>3</sub> slip reached the ASC, a period of NH<sub>3</sub> cumulation within the ASC started without ASC NH<sub>3</sub> slip. This period was shorter as higher the inlet gas temperature (from plot (a) to (c)) because of the progressive weight of the desorption and oxidation rates, which moved the ASC balance towards the slip. In all cases, the model captured with good accuracy the slipped NH<sub>3</sub> mass flow, both in magnitude and dynamics. Only an advance in point #B slip prediction is remarkable (Figure 6(b)). In general terms, the model was very sensitive to the increase in urea injection, i.e. SCRf NH<sub>3</sub> slip, as observed in Figure 6(a) and (b), providing a very accurate prediction of the ASC NH<sub>3</sub> slip fashion.

Figure 7 summarizes the absolute NH<sub>3</sub> outlet mass flow error under these steady-state tests. The 1σ error was kept below 1.2 mg/s in all the tests. This threshold was kept even for 3σ band for point #A and increased just till 1.8 mg/s for point #B. The highest error was obtained at the lowest temperature (point #C), but still very low, ranging between 2.7 mg/s at 2σ and 3.1 mg/s in 3σ condition.

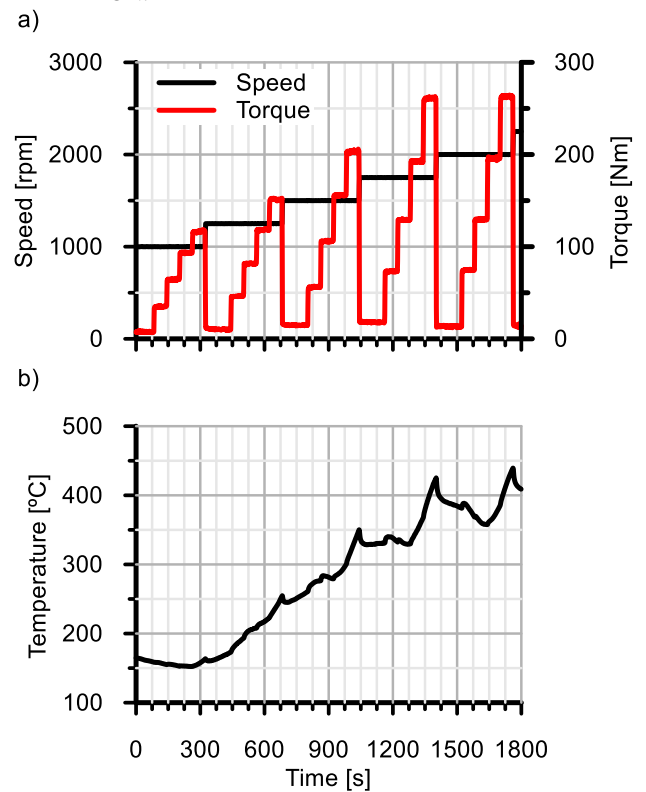


**FIGURE 6:** COMPARISON BETWEEN EXPERIMENTAL AND MODELED ASC NH<sub>3</sub> SLIP UNDER DIFFERENT STEADY-STATE CONDITIONS WITH VARIABLE UREA INJECTION RATE.

Finally, the NO<sub>x</sub> reduction in the ASC model was calibrated assuming NO as representative species and the standard NO reaction, as described in Section 2.3. A mapping test was carried out in quasi-steady-state conditions to calibrate the NO<sub>x</sub> reduction while keeping the NH<sub>3</sub> cumulation and oxidation. This kind of test provided a wide sweep in exhaust gas mass flow, composition and temperature. Figure 8 represents the engine speed and torque profiles defining the test, as well as the ASC inlet temperature.



**FIGURE 7:** OUTLET NH<sub>3</sub> MASS FLOW ERROR DISTRIBUTION IN STEADY-STATE TESTS USED IN MODEL CALIBRATION.

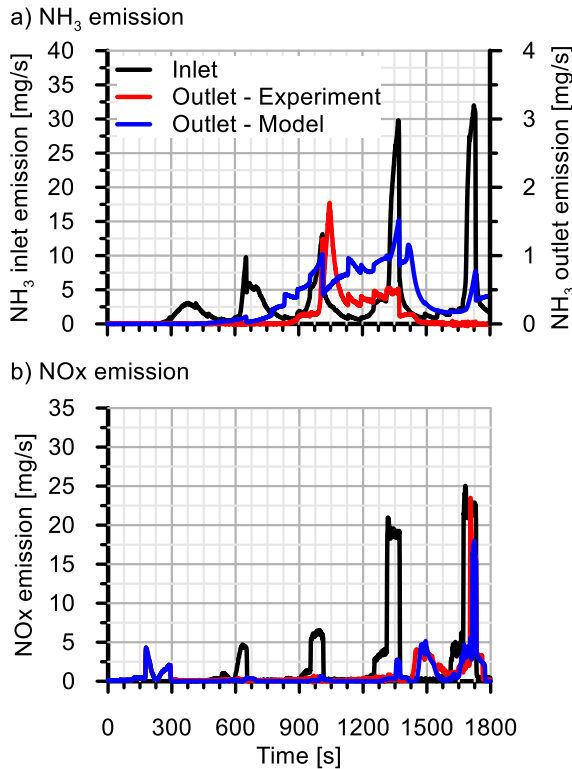


**FIGURE 8:** (a) SPEED AND TORQUE AND (b) ASC INLET GAS TEMPERATURE ALONG THE MAPPING TEST USED AS FINAL STEP OF THE ASC MODEL CALIBRATION PROCEDURE.

Figure 9 shows the comparison between experimental and modeled NH<sub>3</sub> and NO<sub>x</sub> emissions during the mapping test. The model showed good ability to predict the onset and magnitude of the NO<sub>x</sub> and NH<sub>3</sub> slips at the outlet of the ASC. Regarding the NH<sub>3</sub> mass flow, Figure 9(a) shows that the model reproduced the slip that occurred during the period from 900 to 1300 s. On the other hand, Figure 9(b) also evidences the good sensitivity to the NO<sub>x</sub> slip, which was clear during the last phase of the lowest engine speed test (150-300 s) due to the lack of NH<sub>3</sub> in the

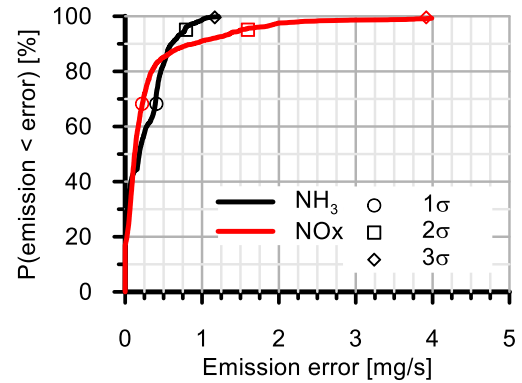
exhaust flow nor in the ASC (previous ASC NH<sub>3</sub> removal conditioning test). During the second and third engine speed tests a very slight NO<sub>x</sub> slip appeared at the highest engine load periods due to the residence time decrease. These slips were identified and well reproduced by the model. Finally, the model also captured the NO<sub>x</sub> slip peaks taking place during the final phase of the test (~1400 s) due to the high NH<sub>3</sub> oxidation rate at the corresponding high engine loads, in which the ASC inlet temperature ranged from 350 to 420 °C, as shown in Figure 8(b).

According to the model trends in dynamic response shown in Figure 9, Figure 10 summarizes the model performance by means of the absolute error distribution in NO<sub>x</sub> and NH<sub>3</sub> tailpipe mass flows. As observed, the 1σ error was less than 0.5 mg/s both for NO<sub>x</sub> and NH<sub>3</sub>. In the case of NH<sub>3</sub>, which is the species of interest for on-board diagnostics proposals, the 2σ error was 0.75 mg/s and remained below 1.25 mg/s for 3σ. Regarding NO<sub>x</sub>, the error was slightly higher, reaching 1.75 mg/s for 2σ and 4 mg/s for the most limiting 3σ case.



**FIGURE 9:** COMPARISON BETWEEN MEASURED AND MODELED NH<sub>3</sub> AND NO<sub>x</sub> EMISSIONS IN MAPPING TESTS.

As a closure of the calibration process, Table 4 shows the kinetic parameters corresponding to the proposed simplified ASC reaction mechanism, whose order of magnitude is in line with those found in the literature [25]. The model accuracy, keeping good response against transient excursions, confirms the potential of reduced order physical-based modelling approaches for control purposes.



**FIGURE 10:** OUTLET NH<sub>3</sub> AND NO<sub>x</sub> EMISSIONS ERROR IN MAPPING TEST.

**TABLE 4:** CALIBRATION OF THE ASC KINETIC PARAMETERS.

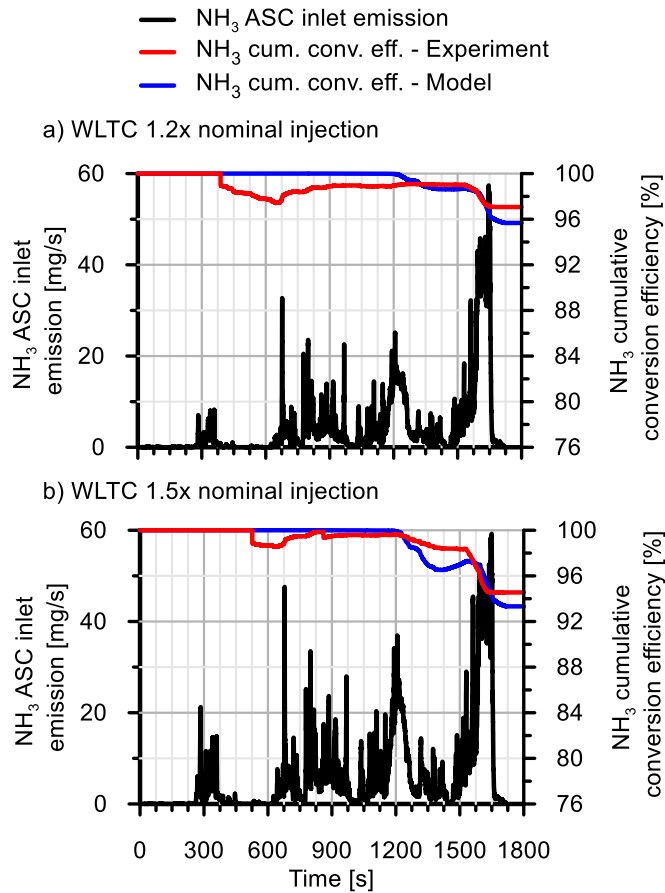
	$A_n$ [-]	$E_a$ [kJ/mol]
R1	$7.4 \times 10^4$	0
R2	$1.21 \times 10^{10}$	63.2
R3	$3.07 \times 10^8$	65.7
R4	$1.51 \times 10^{12}$	143.1
R5	$2.59 \times 10^5$	31

From the calibration, two WLTC tests characterized by different urea injection strategies were used to validate the model prediction ability. In those tests, 1.2x and 1.5 x nominal urea injection were imposed as a way to provide more NH<sub>3</sub> to ASC across the WLTC cycle. The ASC inlet NH<sub>3</sub> mass flow and the resulting experimental and modeled NH<sub>3</sub> cumulative conversion efficiency are shown in Figure 11.

Figure 11 shows how the ASC exhibited a high NH<sub>3</sub> conversion efficiency in both WLTC tests. The low and medium WLTC velocity phases presented an experimental cumulative conversion efficiency higher than 97% for the case of 1.2x nominal injection and 98% for the 1.5x nominal injection strategy. In both cases, the model was close to 100% continuously. Because of the high efficiencies and the reduced NH<sub>3</sub> emission during these phases of the WLTC, the differences between the measured and modeled conversion efficiencies made no difference in the cumulative prediction of the NH<sub>3</sub> emissions at the ASC outlet. However, an increase in NH<sub>3</sub> emissions was observed along with a reduction of conversion efficiency during the high velocity and extra-high velocity phases. These results were produced by a combination of residence time reduction and temperature increase across the ASC. This reduction in conversion efficiency was correctly predicted by the model, being the differences between the cumulative experimental and modeled conversion efficiencies always lower than 2% in both WLTC tests. In this regard, the minimum NH<sub>3</sub> cumulative conversion efficiency achieved



during the extra-high velocity phases in the WLTC with 1.2x nominal injection was 97%, decreasing till 94.5% when the urea injection rate was increased a 50% with respect to the nominal one.



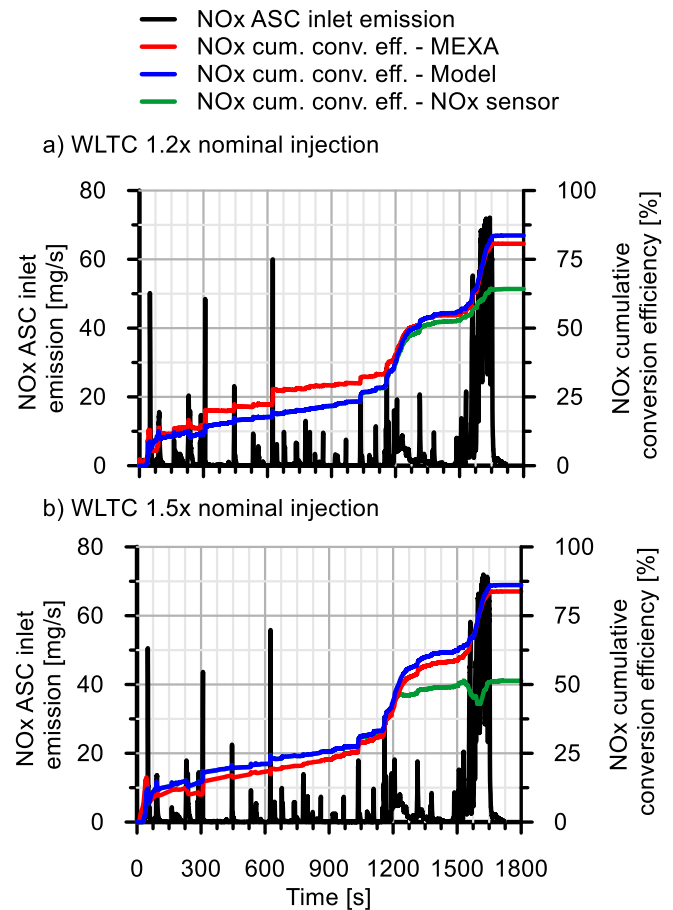
**FIGURE 11:** ASC INLET  $\text{NH}_3$  EMISSION AND EXPERIMENTAL AND MODELED ASC  $\text{NH}_3$  CONVERSION EFFICIENCY IN WLTC WITH (a) 1.2x NOMINAL UREA INJECTION AND (b) 1.5x NOMINAL UREA INJECTION.

### 3.2 APPLICATION OF CROSS-SENSITIVITY FOR NO<sub>x</sub> AND NH<sub>3</sub> ESTIMATION

WLTC tests were used to evaluate the interest of the cross-sensitivity correction of the NO<sub>x</sub> sensor from the NH<sub>3</sub> prediction. The actual NO<sub>x</sub> emission measurement was provided by Horiba MEXA-ONE-FT, whose results were compared with those obtained by the NO<sub>x</sub> sensor and when applied the cross-sensitivity correction.

Figure 12 represents the NO<sub>x</sub> emissions at the ASC inlet and the cumulative NO<sub>x</sub> conversion efficiency corresponding to WLTC tests increasing the nominal urea injection by 20% and 50%. In all cases, for the conversion efficiency calculation, the NO<sub>x</sub> emissions at the ASC inlet provided by the Horiba gas analyzer were used as a baseline. The results evidence that the NO<sub>x</sub> sensor measurement at the ASC outlet was able to capture

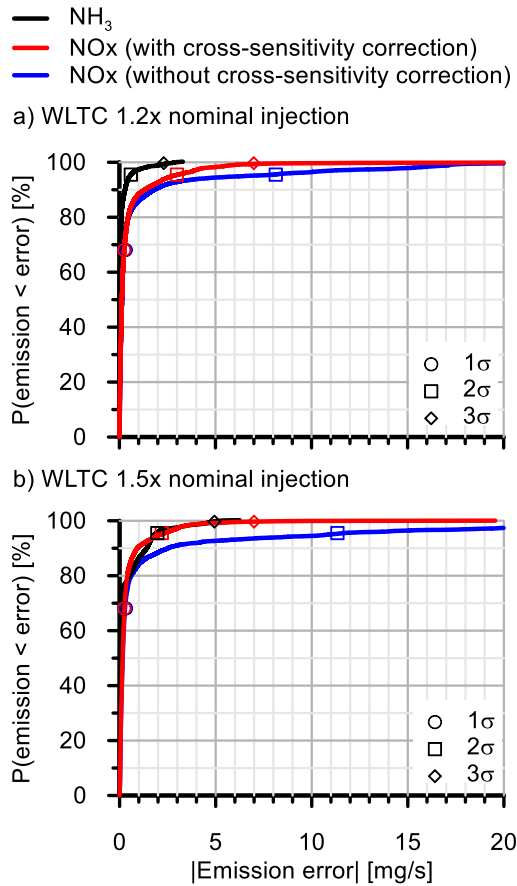
the actual cumulative NO<sub>x</sub> conversion efficiency during the low and medium velocity phases. Along these phases there was not correction from the ASC model since the NH<sub>3</sub> conversion efficiency is 100% till 1200 s, as observed in Figure 11. The deviations in cumulative conversion efficiency between the Horiba MEXA measurement and the NO<sub>x</sub> sensor counterpart appeared along the high and extra-high velocity phases of the WLTC cycle. In fact, the onset of the decrease of the NO<sub>x</sub> sensor accuracy coincided with the NH<sub>3</sub> slip prediction from the ASC model (Figure 11). Therefore, the cross-sensitivity phenomenon led the NO<sub>x</sub> sensor to account for the slipped NH<sub>3</sub> emissions as NO<sub>x</sub>, making the NO<sub>x</sub> signal downstream of the ASC artificially high and reducing the conversion efficiency with respect to the actual one.



**FIGURE 12:** ASC INLET NO<sub>x</sub> EMISSIONS AND COMPARISON BETWEEN EXPERIMENTAL AND MODELED ASC NO<sub>x</sub> CONVERSION EFFICIENCY IN WLTC: (a) 1.2x NOMINAL UREA INJECTION AND (b) 1.5x NOMINAL UREA INJECTION.

The improvement in the prediction of the NO<sub>x</sub> emissions can be also computed in absolute error terms, as depicted in Figure 13, where both NH<sub>3</sub> and NO<sub>x</sub> error distribution are shown. The results shown in Figure 13(a) are dedicated to the

WLTC tests corresponding to 1.2x nominal urea injection whilst Figure 13(b) corresponds to 1.5x nominal urea injection case. The accurate prediction in cumulative NH<sub>3</sub> conversion efficiency is also evidenced in absolute NH<sub>3</sub> emission at the ASC outlet, with errors below 1 mg/s and 2.5 mg/s for 2 $\sigma$  and 3 $\sigma$  respectively. Despite the similar capability to reproduce the cumulative NH<sub>3</sub> conversion efficiency (Figure 11), these absolute errors increased till 2.5 mg/s and 5 mg/s respectively when increasing the urea injection rate by a 50% with respect to the nominal calibration due to the higher NH<sub>3</sub> slip from the SCR during the low to high velocity phases.

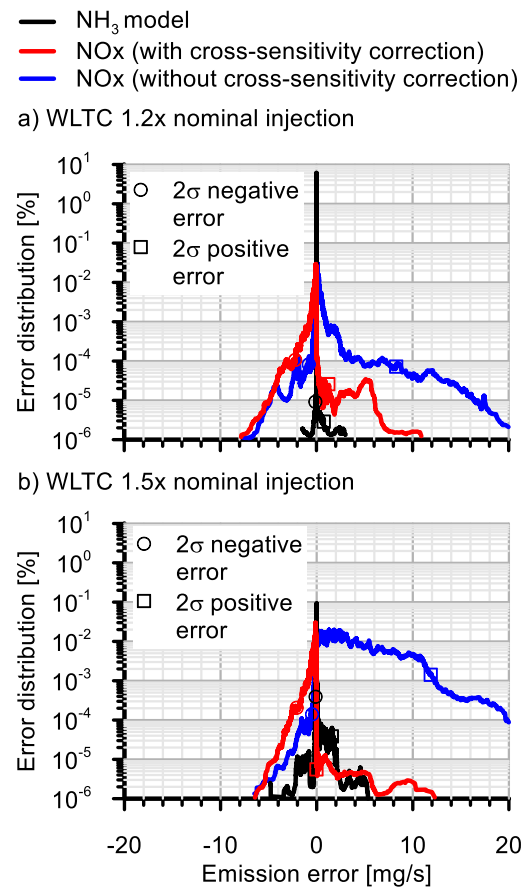


**FIGURE 13:** OUTLET NO<sub>x</sub> AND NH<sub>3</sub> MASS FLOW ABSOLUTE ERROR DISTRIBUTION IN WLTC WITH (a) 1.2x NOMINAL UREA INJECTION AND (b) 1.5x NOMINAL UREA INJECTION.

Nevertheless, this accuracy was high enough to bring a noticeable improvement of the NO<sub>x</sub> sensor accuracy. This is not observed in 1 $\sigma$  due to the lack of NH<sub>3</sub> emission and, hence, no sensor correction during most of the WLTC. However, the 2 $\sigma$  error was reduced from 8.5 mg/s in tailpipe NO<sub>x</sub> emission to 6 mg/s in 2 $\sigma$  and even 7 mg/s in 3 $\sigma$  after NH<sub>3</sub> cross-sensitivity correction in the WLTC test corresponding to 1.2x nominal urea injection. This higher accuracy was even more evident when applying the 1.5x nominal urea injection, providing the same

absolute accuracy in NO<sub>x</sub> emission prediction after NH<sub>3</sub> cross-sensitivity correction than the 1.2x urea injection case despite the very high deviation of the direct NO<sub>x</sub> sensor measurement (2 $\sigma$  above 11 mg/s in NO<sub>x</sub> mass flow error).

Finally, Figure 14 shows the error distribution of the NH<sub>3</sub> mass flow predicted by the model, the direct NO<sub>x</sub> sensor signal and its counterpart when the cross-sensitivity correction is applied. The error distribution shows the model and sensor trends to overestimate or underestimate the emissions. In this sense, the NO<sub>x</sub> sensor error, without any kind of correction, showed a clear trend to overestimate the NO<sub>x</sub> emission due to NH<sub>3</sub> cross-sensitivity issues. In particular, the 2 $\sigma$  of the negative error was -0.7 mg/s while the positive counterpart increased till 8.4 mg/s for the case of the WLTC test corresponding to 1.2x nominal urea injection, which is shown in Figure 14(a). This is even more remarkable when increasing further the urea injection, as shown in Figure 14(b), where the 2 $\sigma$  of the negative error was reduced to -0.4 mg/s while the positive one increased to 11 mg/s. In view of these results, the NO<sub>x</sub> sensor overestimation makes difficult to use this signal for control and diagnostic tasks.



**FIGURE 14:** OUTLET NO<sub>x</sub> AND NH<sub>3</sub> MASS FLOW ERROR DISTRIBUTION IN WLTC WITH (a) 1.2x NOMINAL UREA INJECTION AND (b) 1.5x NOMINAL UREA INJECTION.

Moreover, the error distribution obtained for the model prediction of NH<sub>3</sub> during the WLTC test with 1.2x nominal urea provided a centered error distribution around 0 mg/s. As a result, the correction of cross-sensitivity on the NO<sub>x</sub> sensor signal, provided an almost centered error also for NO<sub>x</sub>. By contrast, the WLTC with 1.5x nominal urea injection showed a slight tendency to overestimate the emission of NH<sub>3</sub>, being the positive 2 $\sigma$  error higher than the negative one. Consequently, the NH<sub>3</sub> overestimation led to the NO<sub>x</sub> underestimation after applying the cross-sensitivity correction.

#### 4. CONCLUSIONS

This work has explored the combined use of control-oriented ASC modeling, based on simplified transport and reaction mechanism, and NO<sub>x</sub> sensor correction, based on cross-sensitivity determination, for the simultaneous prediction of NH<sub>3</sub> and NO<sub>x</sub> emissions at the ASC outlet. The NH<sub>3</sub> slip prediction from the ASC model, which neglects the reactivity limitations caused by bulk gas to washcoat mass transfer and competitiveness between reactions, was used to correct the NO<sub>x</sub> sensor signal to consider the NH<sub>3</sub> cross-sensitivity. The reaction mechanism was also simplified assuming NH<sub>3</sub> oxidation to O<sub>2</sub> and NO as well as the NO<sub>x</sub> reduction, which was represented by the standard SCR reaction. Despite these modeling assumptions, the proposed approach reproduced the NH<sub>3</sub> and NO<sub>x</sub> slips in a wide variety of operating conditions following a calibration procedure that combined steady-state and quasi-steady-state engine operating conditions. The absolute ASC model error was less than 3 mg/s for a half-width interval equal to 2 $\sigma$ , properly predicting the NH<sub>3</sub> conversion efficiency.

The prediction abilities of the ASC and sensor models were checked against WLTC tests in which different urea dosing strategies were imposed, increasing the urea injection rate by up to 20% and 50% with respect to the nominal strategy. The results evidenced an accurate prediction of the NH<sub>3</sub> conversion efficiency along WLTC cycles with high sensitivity to the NH<sub>3</sub> concentration at the ASC inlet and to ASC NH<sub>3</sub> slip appearance at high vehicle velocities due to NH<sub>3</sub> residence time reduction. Complementary, the accurate NH<sub>3</sub> prediction with low computational effort enables the on-board NO<sub>x</sub> signal sensor correction to account for NH<sub>3</sub> cross-sensitivity without the need to add NH<sub>3</sub> sensors. The determination of the cross-sensitivity constant from the estimate of the sensor cell temperature provided a very accurate NO<sub>x</sub> conversion efficiency prediction in the ASC during low NH<sub>3</sub> slip conditions, i.e. almost negligible correction of the NO<sub>x</sub> sensor signal. In parallel, the NO<sub>x</sub> emission during the extra-high velocity WLTC phase was also captured despite the deviations in the original sensor signal providing an accurate NH<sub>3</sub> slip prediction both in magnitude and dynamic terms, i.e., with sensitivity to engine operating conditions and NH<sub>3</sub> concentration resulting from the specific urea injection strategy.

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