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Additional Information

Using momentum flux measurements to determine the injection rate of a Urea Water Solution injector

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Abstract

The Selective Catalytic Reduction (SCR) systems technology allows the transformation of the Nitrous Oxide emissions present in exhaust gases into gaseous nitrogen and water. For a proper operation of the SCR, a urea-water solution (UWS) injector must dose an adequate amount of liquid into the exhaust pipe in order to avoid deposit formation and to guarantee the SCR system efficiency. This task requires the knowledge of the performance of the injector. Then, the goal of this work is to study the hydraulic performance of an UWS injector, by means of measuring the spray momentum flux in order to understand the influence of different variables as injected fluid, injection pressure, counter pressure and cooling temperature of the injector on the flow characteristics. The tested injector was cooled at three different temperatures, 60, 90 and 120 °C, the injection pressure of the UWS was set at 5, 7 and 9 bar, with counter pressures of 750, 900, 1000 and 2000 mbar for the two tested fluids, water and UWS. The measurements were carried out using an experimental facility developed at CMT-Motores Térmicos for the determination of spray momentum flux, where a piezoelectric pressure sensor was located near the nozzle exit of the injector, which measures the impact force of the spray. Additionally, the proposed methodology allowed to determine the injected mass flow, capturing the transient events of the injection, such as the opening and closing stages. Moreover,

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mass flow rate measurements of the injector were performed under the same operating conditions, determining the influence of the injection pressure, cooling temperature, counter pressure and fluid properties. Regarding the pressure, the tendency was as expected, the higher the injection pressure the higher the Momentum flux and flow rate. When the cooling temperature was increased the Momentum flux did not show a clear tendency. For the same conditions water has a higher momentum flux than the UWS due to differences in fluid properties and velocity at the nozzle exit. Additionally, the proposed methodology allowed to determine the injected mass flow, capturing the transient events of the injection, such as the opening and closing stages.

Keywords: Momentum Flux, UWS, Rate of Injection, SCR

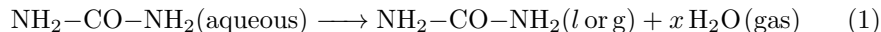
1. Introduction

With the intention of reducing pollutant emissions and complying with existing regulations, Selective Catalytic Reduction (SCR) systems have been incorporated in the after-treatment of exhaust lines [1, 2].

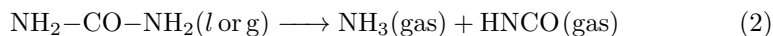
The SCR configuration in current systems require a proper delivery of the Urea-Water Solution (UWS), most commonly known as AdBlue or Diesel Exhaust Fluid (DEF), to have efficient reduction reactions, demanding an accurate fluid dosing and ensuring a correct atomization and evaporation, in order to avoid wall impingement and deposit formation.

Therefore, the UWS injection process needs to be well understood and characterized for suitable injector selection during the design and also for the calibration process [3]. Until a few years ago the information regarding to light duty UWS injection systems was very limited. However, recently, several authors have devoted their research topic to characterize these systems and they have realized the necessity of determining the amount of injected mass [4], since it provides direct information of the unit dosage and because it is an essential parameter for correct initialization of Computational Fluid Dynamics (CFD) modelling [5, 6].

19 Yim et al [7] describe the decomposition of the injected UWS for SCR sys-
20 tems as follows. First the water present in the UWS evaporates, forming pure
21 urea ($\text{CO}(\text{NH}_2)_2$) that can be in liquid or gaseous state:



22 Then the thermolysis of the urea produces ammonia and isocyanic acid
23 (HNCO):



24 Once the gases are inside of the catalyst the isocyanic acid hydrolyses into
25 ammonia and carbon dioxide:



26 Observing equations 1, 2 and 3, injecting incorrect amount of UWS into the
27 exhaust line can cause improper NOx transformation or ammonia slip into the
28 atmosphere [8, 9]. This scenario obliges to experimentally determine the UWS
29 mass flow rate or at least the injected mass per shot. The most used method-
30 ologies for the mass flow determination are the Bosch and the Zeuch method
31 [4, 10]. In general, the measuring principle is based on injecting the fluid into
32 a closed volume and registering the pressure wave generated by a piezoelectric
33 pressure sensor, which is proportional to the injection rate. Both systems are
34 widely used for diesel and gasoline dosing applications, where injection pres-
35 sures are quite high (especially in diesel it can reach 250 MPa). Additionally,
36 the main characteristic of those devices is that the injection is performed into a
37 chamber filled with liquid.

38 However, the direct implementation of those methodologies to UWS injectors
39 is not so simple, since the UWS injection pressures are low in comparison with
40 diesel or gasoline direct injection systems. Moreover, real UWS injection process
41 is in exhaust gas conditions which are considerably different to injecting into

42 liquid and the discharge ambient pressure is low compared to those of diesel and
43 Gasoline Direct Injection (GDI), surrounding the atmospheric pressure.

44 Some authors have implemented another methodology based on the momen-
45 tum flux measurement [11, 12, 13, 14] for the diesel and gasoline spray, injecting
46 into gas and obtaining good results. The fact that this technique allows to mea-
47 sure the evolution of the injection event in a gaseous medium makes it attractive
48 for the application that concerns UWS dosing systems.

49 Currently most estimations of the mass flow rate are determined by CFD
50 modelling of inlet and/or outlet flow [15, 16] or by collecting the injected mass
51 of the injector in a container and assuming uniform injection events [17].

52 Based on the necessity of quantifying the mass flow rate for SCR dosing
53 systems this paper focuses on the implementation of a methodology based on
54 the momentum flux measurements in a UWS injector. The system is tested
55 using UWS and water, which is commonly used in experimental settings due
56 to its easy handling, similar properties and to avoid deposit formation in lab
57 equipment.

58 After the measuring system is configured and validated, the test rig will be
59 used for understanding the effect of different parameters on the evolution of the
60 mass flow rate and injected mass.

61 State of the art UWS dosing systems have a cooling system that prevents
62 the nozzle tip and the fluid from overheating due to the high exhaust gas tem-
63 peratures. The cooling temperature also affects the properties of the injected
64 fluid, even allowing it to reach flash boiling conditions if the cooling fluid is hot
65 enough [18, 19]. The influence on the viscosity and density of the fluid can affect
66 the hydraulic performance of the injector, therefore three cooling temperatures
67 of 60, 90 and 120 °C have been tested.

68 The discharge pressure in the exhaust manifold, especially in real driving
69 conditions, can vary depending on the engine regime and the current height
70 above mean sea level [20, 21]. Hence the chamber pressure is set between 0.75 bar
71 and 2 bar to quantify the effect of discharge pressure on the injector performance,
72 which is known to affect the rate of injection and momentum flux of sprays for

73 Diesel and GDI injectors [14, 22, 23, 24].

74 A sweep of injection pressures of 5, 7 and 9 bar is also performed this is a
75 well known effect [3, 17, 25] and will be used to corroborate the obtained results

76 Finally, the injected mass was also measured using a calibrated precision
77 scale to apply the aforementioned method. The results provided useful infor-
78 mation on the instantaneous mass flow behaviour and allowed the hydraulic
79 characterization of the studied injector.

80 2. Background

81 The main objective of this paper is to validate a method to estimate the rate
82 of injection for a UWS dosing system using momentum flux measurements. A
83 relationship can be established from the definition of both variables:

$$\dot{m} = A \cdot \rho \cdot u \quad (4)$$

$$\dot{M} = A \cdot \rho \cdot u^2 \quad (5)$$

84 Where \dot{m} is the rate of injection, A is the outlet area of the nozzle, ρ is the
85 density of the fluid, u is the velocity of the flow at the nozzle exit and \dot{M} is the
86 momentum flux of the spray.

87 Combining equations 4 and 5 the momentum flux and rate of injection can
88 be related as:

$$\dot{m} = \sqrt{A \cdot \rho \cdot \dot{M}} \quad (6)$$

89 The real mass flux at the hole exit is determined by the velocity profile and
90 the fluid density [26]. The real shape of the velocity profile is experimentally
91 hard to determine but it is possible to define an effective velocity and an effective
92 area in a sense that these are representative of the flow, as shown in figure 1.

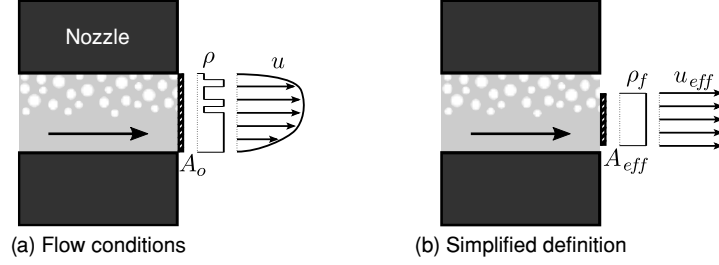


Figure 1: (a) Real Velocity profile, density and area. (b) Effective area, velocity and density in a nozzle.

93 The definition of these parameters is based on the consideration of a simpli-
 94 fied flow, which is characterized by an effective area, smaller than the geometri-
 95 cal area, and with an effective velocity and density (equal to the fluid density)
 96 uniform in all the section. Taking this into account equations 4 and 5 can be
 97 expressed as:

$$\dot{m} = A_{eff} \cdot \rho \cdot u_{eff} \quad (7)$$

$$\dot{M} = A_{eff} \cdot \rho \cdot u_{eff}^2 \quad (8)$$

98 Equations 7 and 8 can be expressed in terms of the velocity u and area A
 99 by means of the discharge coefficient C_d :

$$C_d = \frac{\dot{m}}{A \cdot \rho \cdot u} \quad (9)$$

100 The discharge coefficient can be decomposed in two different coefficients
 101 determined C_A for the area and C_V for the velocity

$$C_d = C_A \cdot C_V \quad (10)$$

$$C_A = \frac{A_{eff}}{A} \quad (11)$$

$$C_V = \frac{u_{eff}}{u} \quad (12)$$

102 Based on this assumption the momentum flux and the mass flow through
 103 the hole could be defined as equation 13 and equation 14 respectively:

$$\dot{M} = C_v^2 \cdot C_A \cdot \rho \cdot A \cdot u^2 \quad (13)$$

$$\dot{m} = C_v \cdot C_A \cdot \rho \cdot A \cdot u \quad (14)$$

Combining equation 13 and equation 14 an expression for the injection rate
 as a function of the momentum flux is obtained as is stated in equation 15:

$$\dot{m} = \sqrt{C_A \cdot A \cdot \rho} \cdot \sqrt{\dot{M}} \quad (15)$$

104 Furthermore, if momentum flux can be determined experimentally, it is pos-
 105 sible to calculate the mass flow directly from equation 15 and the injected mass
 106 from:

$$m_{inj} = \int_0^t \dot{m} \cdot dt \quad (16)$$

By measuring the injected mass, it is possible to compare the calculated
 injected mass with the measured one (Eq. 17) in order to obtain an adjustment
 coefficient K that should take a value near one if all assumptions made are
 correct.

$$\int_0^t \dot{m} \cdot dt = K \cdot m_{exp} \quad (17)$$

Finally, combining equations 15, 16 and 17, the mass flow can be determined
 as:

$$\dot{m} = K \cdot \frac{m_{exp}}{\int_0^t \sqrt{\dot{M}} \cdot dt} \cdot \sqrt{\dot{M}} \quad (18)$$

107 **3. Methodology and Experimental Setup**

108 Momentum flux measurements were performed on a commercial injector
 109 spray using water and urea-water solution (UWS) at a concentration of 32.5%
 110 under different discharge pressures and injector cooling temperatures. The
 111 tested injector for this study is a dosing module from Bosch, which has three

112 orifices with a diameter of 135 μm each. During the experiments, the injector
 113 cooling temperature was set to 60, 90 and 120°C, the discharge pressure to 750,
 114 900, 1000 and 2000 mbar and injection pressures of 5, 7 and 9 bar, in both cases
 115 referring to absolute pressure. A summary of the injector characteristics and
 116 the test conditions is provided in table 1

Table 1: Injector properties and test conditions.

Holes	3
Diameter	135 μm
Injection Pressure (absolute)	5-7-9 bar
Injector cooling temperature	60-90-120 °C
Energizing time	5 ms
Discharge Pressure (absolute)	750, 900, 1000, 2000 mbar
Fluids	Water and UWS

117 Using a calibrated pressure piezoelectric sensor it is possible to measure the
 118 impact force of the spray over a known surface area. The sensor is placed at
 119 a certain distance from the nozzle exit to ensure that the impingement area of
 120 the spray is within the limits of the target, as Figure 2 shows. If the sensor
 121 captures the whole spray and considering the conservation of momentum, the
 122 measured force is equal to the momentum flux at the nozzle exit [27, 28].

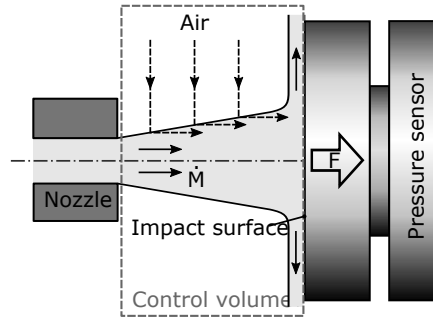


Figure 2: Momentum flux principle

123 The experiments were carried out in a test vessel designed to measure diesel

142 To obtain reliable estimation of the momentum flux, fifty measurements were
 143 performed for each test condition, cleaning thoughtfully the vessel and sensor
 144 after each test to avoid deposit formation on the sensor or the nozzle.

145 Additionally, a scale was used to measure the injected mass using the setup
 146 in Figure 4, where 500 injections of fluid were collected. The conditions for
 147 these experiments were the same used for the momentum flux. The injected
 148 mass corresponds to the integral of the mass flow rate, therefore it will be used
 149 to adjust the curves calculated with the momentum flux measurements.

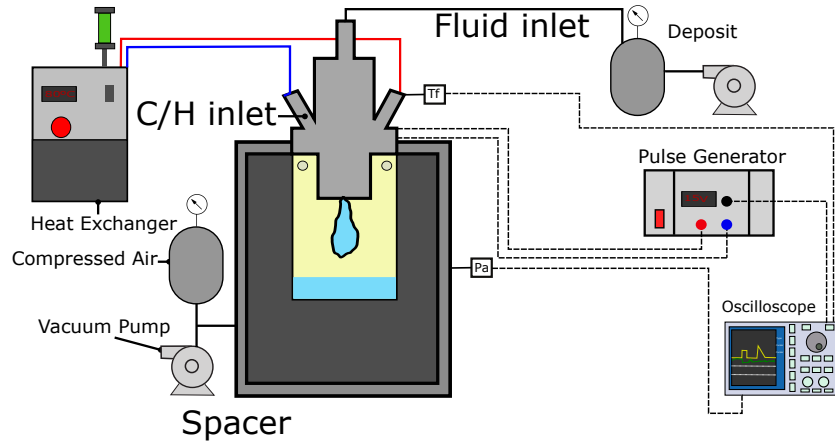


Figure 4: Experimental setup used during the experiments to collect the injected mass

150 The setup in Figure 4 used the same vessel that was employed in the momen-
 151 tum flux measurements, removing the piezoelectric sensor and replacing it with
 152 a lid. The mass was collected using a flask coupled with the injector holder. The
 153 flask has small orifices at the top that allow the pressure be the same in both
 154 the vessel and the flask. The vessel volume is big enough to keep the pressure
 155 level constant after all the injection events (difference between start and finish
 156 below 1%).

157 **4. Results**

158 The results of the measurements of momentum flux and injected mass under
159 different injection pressures, ambient pressures and cooling temperatures are
160 presented and discussed in this section. With the obtained data the Rate of
161 Injection (ROI) of the injector is then determined. Afterwards the discharge
162 coefficient of the nozzle is calculated for both fluids under the studied conditions.

163 *4.1. Momentum Flux*

164 To ensure that the distance from the nozzle to the piezoelectric sensor is
165 enough to capture the whole impingement area and that the momentum flux
166 average value is independent on the sensor position, different distances were
167 tested. In figure 5 the momentum flux signals acquired for distances of 2, 5, 8
168 and 11 mm between the nozzle exit and the sensor are plotted.

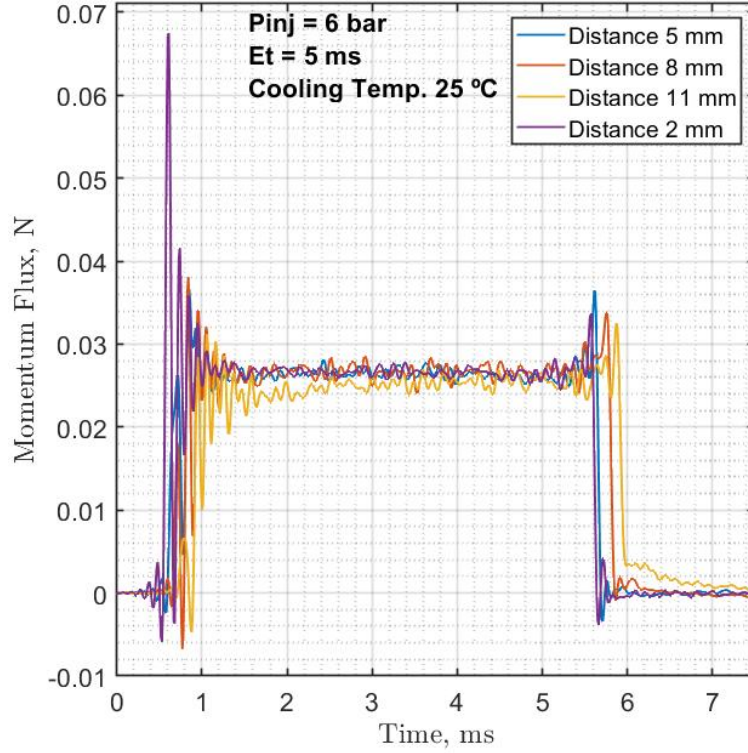


Figure 5: Momentum flux signal for different distances between nozzle and sensor

169 The main difference observed between signals are the starting and ending
 170 phases of the curve, where a displacement to the right due to the longer travel
 171 time (measured from the time after start of energising of the solenoid) of the
 172 spray before hitting the sensor when it is placed further away from the nozzle
 173 tip. The signals from 2, 5 and 8 mm distances are similar in the steady phase
 174 of the signal, meanwhile at 11 mm the signal is lower (on average 8% lower),
 175 which can be attributed to a cross section of the spray greater than the sensor
 176 target and thus not capturing the momentum of the whole plume.

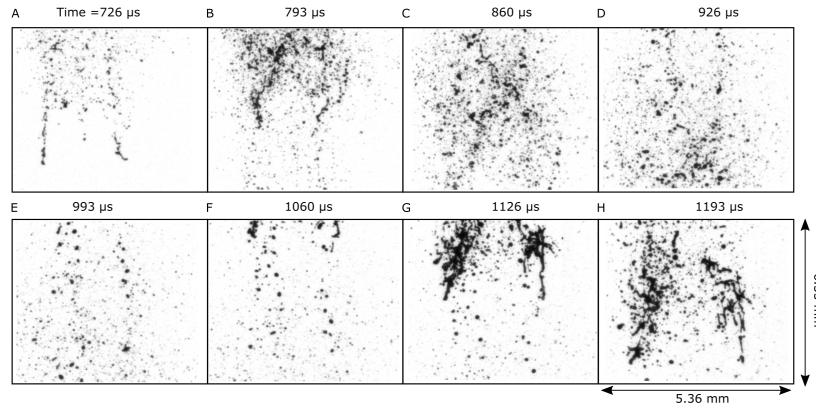


Figure 6: Spray images taken at 4 mm from the hole exit, at the initial stages of the injection event, time measured After Start Of Energising (ASOE)

177 Considering the results shown in Figure 5, it was decided to perform the
 178 measurements with the piezoelectric sensor at a distance of 5 mm from the
 179 nozzle exit because the stabilized signal did not differ in a significant amount
 180 respect to the signal from 2 and 8 mm. From this point forward, all the presented
 181 results correspond to the measurements of the momentum flux with the sensor
 182 at 5 mm from the nozzle exit.

183 The difference in the opening transient of the signals can be attributed to the
 184 packages of fluid leaving the nozzle at the beginning of the injection event, where
 185 the dynamics of the injector plays an important part. Previous visualization
 186 tests images [25] for the initial moments of the injection event are shown in
 187 figure 6, where the aforementioned packages leave the nozzle unsteadily. In
 188 the images it can be observed how droplet quantity and form vary in the first
 189 moments of the injection event, showing the initial bursts where ligaments and
 190 droplets appear increasing its density in the first four instants (A, B, C and
 191 D). Afterwards, the density of packages appears smaller for a few moments (E
 192 and F), until a new burst of packages appear showing different morphology of
 193 ligaments and bigger blobs (G and H) than those observed in the first instant.

194 4.1.1. Effect of the discharge ambient pressure

195 The effect of the ambient pressure and injection pressure over momentum
196 flux is presented for water and UWS. In order to compare the effects of the
197 different conditions over the spray momentum, an average of the steady part of
198 the signal was calculated between the times of 2.5 ms and 5 ms after the start of
199 energizing. Figure 7 shows a momentum flux signal over time for one of the test
200 points and the interval where the averages are calculated is represented with
201 red dashed vertical lines. The reason for selecting this time interval is because
202 the signal is not affected by the transient effects evidenced at the beginning of
203 the injection.

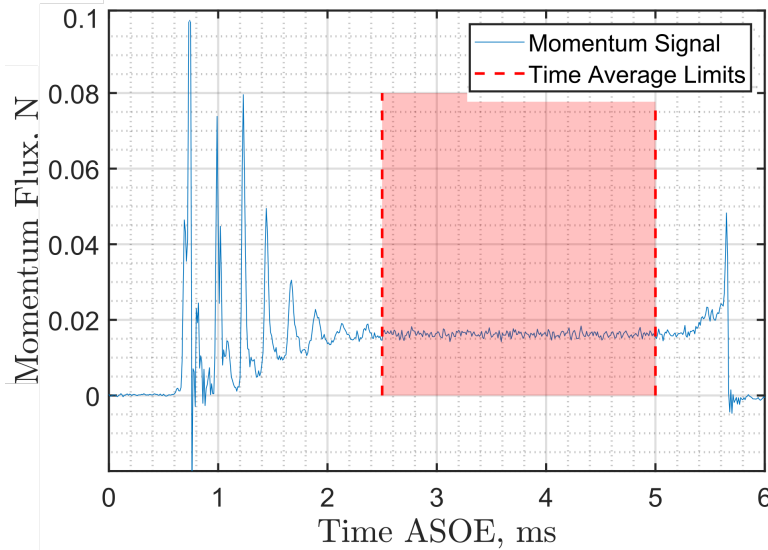


Figure 7: Momentum flux signal for an injection pressure of 5 bar at an ambient pressure of 750 mbar and a cooling temperature of 60 °C in time (ASOE)

204 In figure 8 it is presented the average momentum flux versus the injection
205 pressure, where the measured average value is presented for each tested discharge
206 pressure for both fluids.

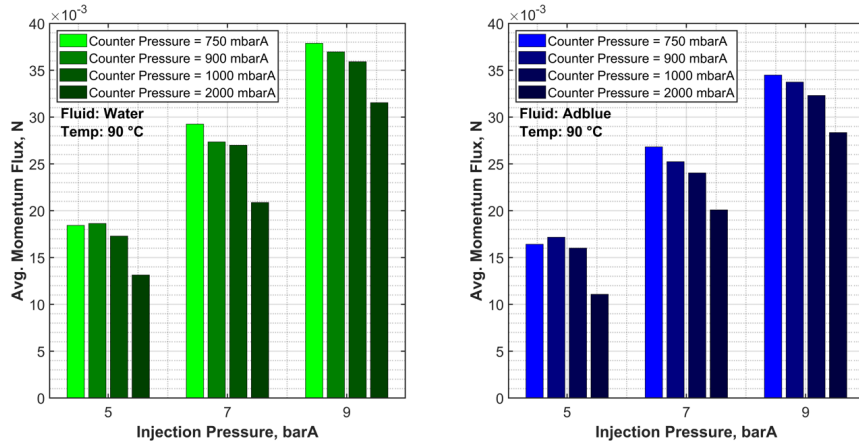


Figure 8: Effect of the discharge ambient pressure on the spray momentum flux for water (left) and UWS (right)

207 A trend towards lower momentum flux as the discharge pressure is increased
 208 is observed. This behaviour is logical considering equation 13, where the mo-
 209 mentum flux depends on the square of the velocity which in turn is proportional
 210 to the square root of the pressure difference between the ambient and the inlet
 211 of the injector. This trend is observed for both fluids, water and UWS.

212 Since the momentum flux of the spray is proportional to the square of the
 213 mass flow, at higher altitudes (where the ambient pressure is lower) the differen-
 214 tial pressure has to be taken into account while dosing into the exhaust stream
 215 to inject the proper amount of fluid and avoid deposit formation or urea slip.

216 4.1.2. Effect of the Cooling temperature

217 Figure 9 show the average momentum flux for the three different cooling
 218 temperatures at the three tested injection pressures. For the UWS at 5 bar
 219 it is observed a reduction of the momentum with higher cooling temperatures,
 220 meanwhile for the pressures of 7 and 9 bar there is not a clear influence of the
 221 temperature over the momentum flux.

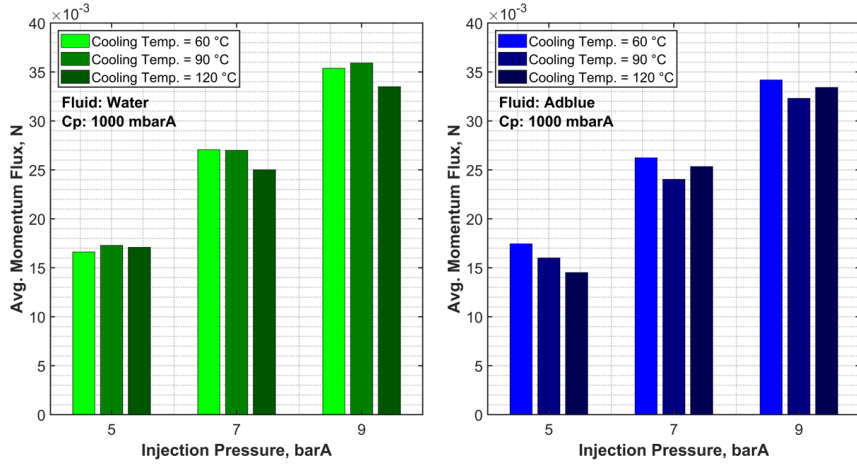


Figure 9: Effect of the cooling temperature over the spray momentum flux for Water (left) and UWS (right)

222 As for the water, there is a little difference at the lowest injection pressure,
 223 meanwhile as the pressure upstream is increased the effect of the cooling
 224 temperature is more evident.

225 Regardless of the fluid, and as reported by Brizi et al [18] for UWS and Ka-
 226 pusta et al [19] for water and UWS, increasing the cooling temperature and the
 227 injection pressure aids in the atomization of the spray. Furthermore, the struc-
 228 ture of the spray changes significantly when the fluid reaches fully developed
 229 flash boiling conditions.

230 These authors also reported that when the flash boiling conditions are set,
 231 the spreading of the spray cone is increased, reaching lower penetration for the
 232 same pressure conditions, better atomization, enhancing evaporation and air
 233 entrainment in the spray. All these factors may have an effect on the spray mo-
 234 mentum, possibly stopping part of the spray from hitting the target or slowing
 235 the spray and thus affecting the measurement.

236 4.1.3. Effect of the injected fluid

237 The average momentum flux for the two tested fluids with a cooling tem-
 238 perature of 90 °C and a counter pressure of 1 bar, for the three tested injection

239 pressures is shown in Figure 10.

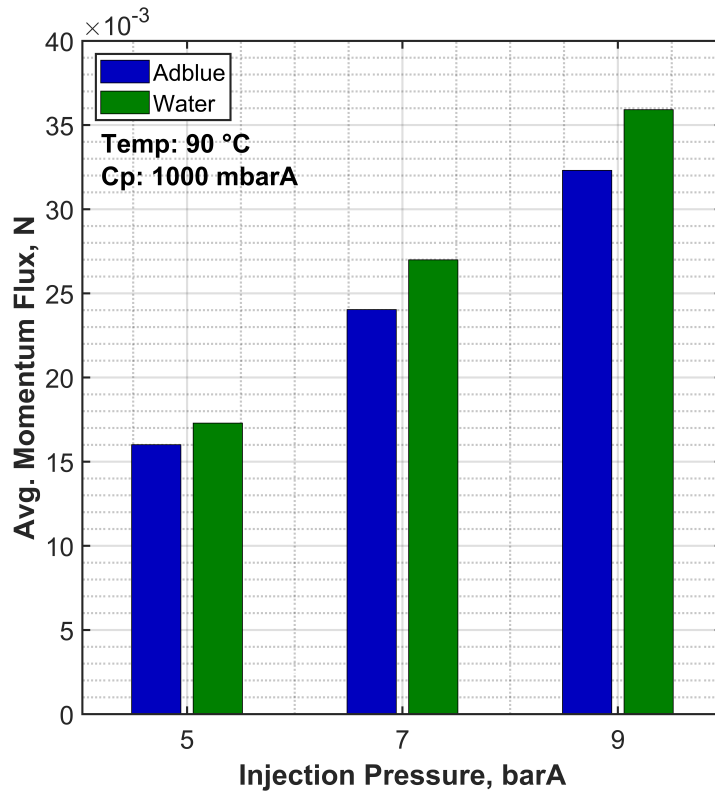


Figure 10: Effect of the injected fluid over the spray momentum flux

240 It is observed how the momentum flux for water is always higher than the
241 UWS, and this results are consistent with the theory and literature. As shown in
242 Equation 13, the spray momentum is proportional to the square of the velocity.
243 Furthermore, Kapusta et al [17] found that for the same test conditions, the
244 spray properties (penetration, spreading angle, unbroken liquid length) change
245 with the injected fluid.

246 These results are of especial importance due to the common use of water
247 as a substitute for UWS during experiments. This means that when water is
248 used as a substitute for UWS some corrections should be done in terms of the
249 momentum quantity.

250 Following this idea, a summary of the momentum flux averaged values is
 251 presented in Figure 11, where the momentum flux is linearly proportional to
 252 the pressure difference (ΔP)

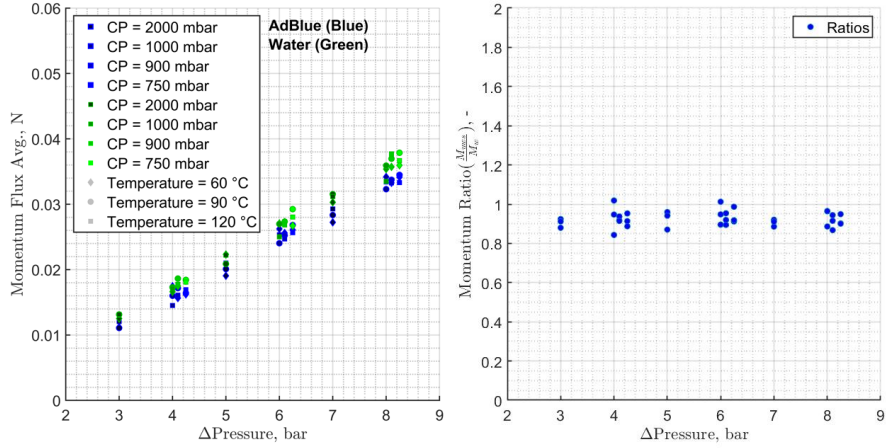


Figure 11: Average Momentum flux for all tested conditions (left) and the ratio of the average momentum flux between UWS and water (right)

253 In the left image a ratio R between the momentum flux of the UWS and the
 254 water is calculated for each test condition using Equation 19.

$$R = \frac{\dot{M}_{uws}}{\dot{M}_{water}} \quad (19)$$

255 The ratios shown in the right side of Figure 11 appear to be similar, with no
 256 clear influence of the injection pressure, cooling temperature or ambient pressure
 257 over the values. This renders possible the correction of the measurements using
 258 the ratio R when water is used as a substitute of UWS in experiments. The
 259 average ratio between all the measurements has a value of $\bar{R} = 0.924$, with an
 260 standard deviation of $s = 0.038$ or 4.17%. The ratio is related to the differences
 261 in the properties of the fluids as will be discussed later.

262 *4.2. Injected mass*

263 The injected mass per shot was determined by collecting the fluid of 500
 264 shots inside of the test vessel at the test conditions and then measuring it
 265 using a scale. The design of the system ensures that most of the fluid remains
 266 inside collector, minimizing the possibility of losses due to evaporation during
 267 the measurement process. Figure 12 show the mass per shot for different fluid
 268 temperatures, injection pressure and back pressure for water (right side) and
 269 UWS (left).

270 It can be observed in both fluids how for similar test conditions the injected
 271 mass per shot has a similar value, noting a linear increase with the square root
 272 of the pressure difference which is in accordance with the theory.

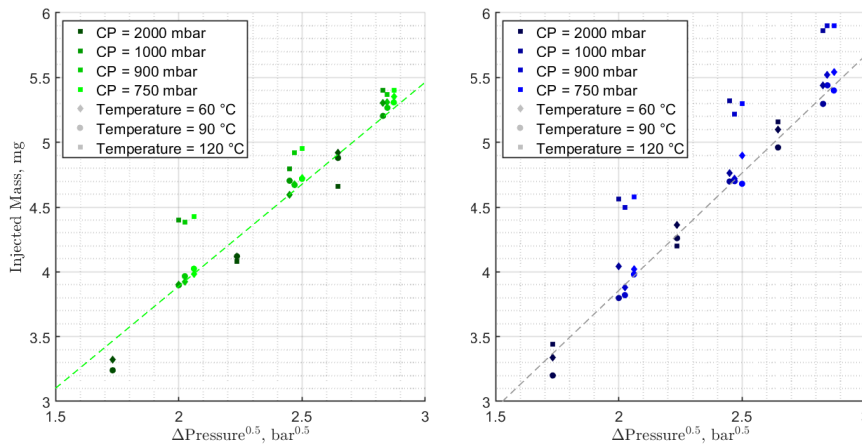


Figure 12: Injected mass for both fluids (water left, UWS right) for all tested conditions

273 The most remarkable aspect of the injected mass is that for the temperature
 274 of 120°C in most conditions is up to 15% higher for both fluids except for the
 275 back pressures of 2 bar, for which the measurements remain similar to other back
 276 pressures and temperatures. This behaviour could be attributed to changes
 277 in the physical properties of the fluid like the viscosity, which increases the
 278 discharge coefficient of the nozzle, together with the flash boiling conditions. To
 279 verify this hypothesis an additional investigation is proposed, using additional

280 tools as CFD to study the internal flow at this temperatures.

281 Brizi [18] observed that under flash boiling conditions and after the main
282 phase of the injection event had finished some fluid was still coming out of the
283 injector. This effect was detected for both liquid and vapour phases under flash
284 boiling conditions, which can explain the increase in the injected mass.

285 *4.3. Rate of injection*

286 With the measurements of momentum flux and injected mass, the rate of
287 injection (ROI) curves can be calculated using the equations 16, 17 and 18. In
288 Figure 13 the calculated rate of injection signals for a counter pressure of 1000
289 mbar are presented for both fluids, showing the ROI for the 3 injection pressures
290 at each fluid temperature.

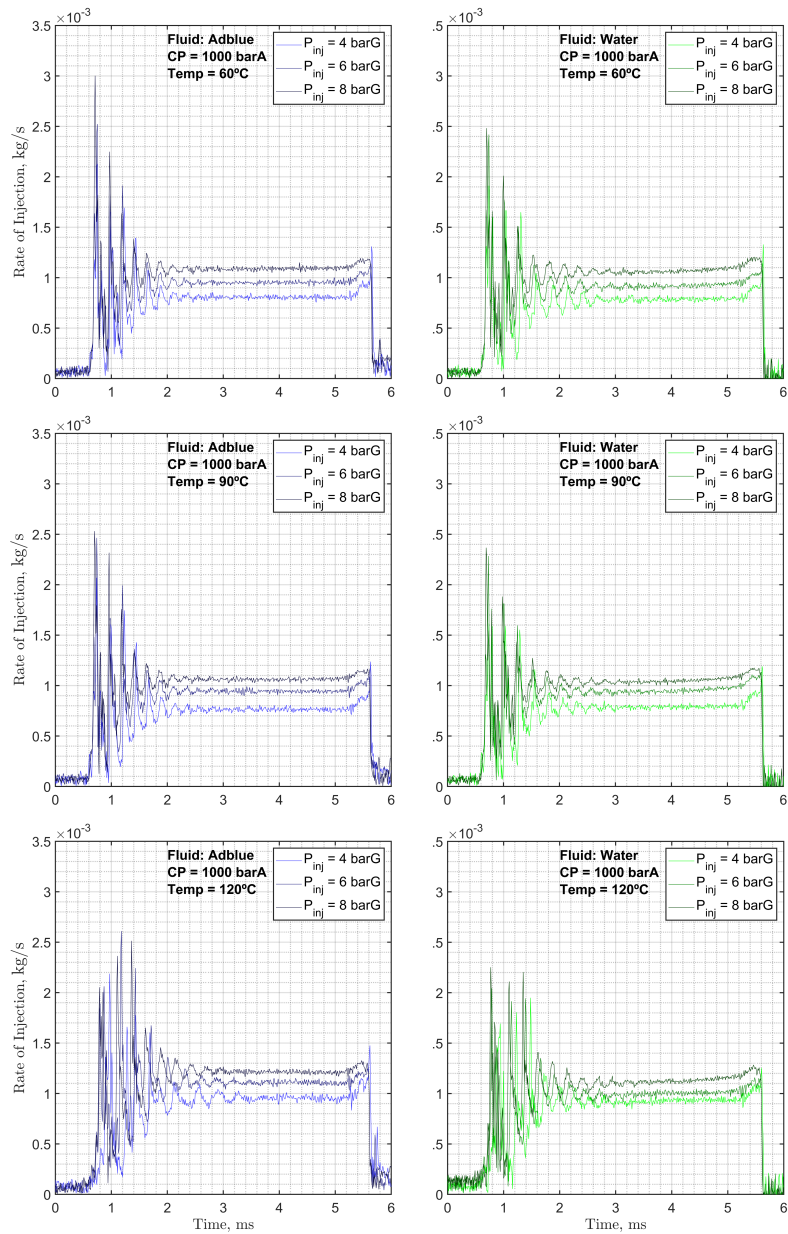


Figure 13: Calculated Rate of injection signals for different temperatures and injection pressure conditions

291

The most noticeable effects seen in the calculated curves are those of the

292 injection pressure, increasing ROI for higher injection pressure levels. A similar
 293 effect is observed for the temperature, increasing the ROI as the temperature
 294 of the fluid is increased to 120°C.

295 Furthermore, the shape of the curves are similar for the fluid temperatures
 296 of 60° and 90°C, meanwhile for the 120°C curves a different and longer opening
 297 transient is observed. This change in the curve could indicate changes in the
 298 internal flow of the nozzle due to the change of density of the fluid or the internal
 299 dynamic behaviour of the injector.

300 Analogous to the momentum flux curves, an average of the ROI value was
 301 calculated using the values comprehended between 2.5 and 5 ms, where the
 302 curve is in a steady state. Figure 14 shows the average value for all the tested
 303 conditions, showing consistency with the injected mass trends.

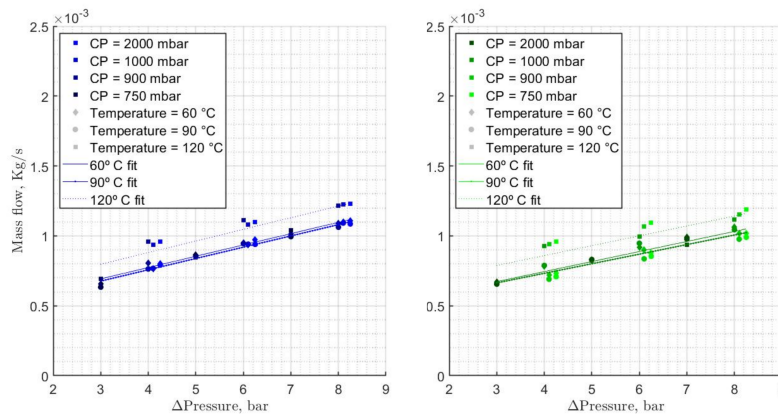


Figure 14: Rate of injection signals for different temperatures and injection pressure conditions

304 The ROI of injection follow a linear trend with the square root of the pressure
 305 difference. As seen before with the injected mass, when the conditions for flash
 306 boiling of the spray are set, the rate of injection is considerable higher (around
 307 20%).

308 The ROI curves have been useful as an input and validation tool for current
 309 CFD models being developed [29] and it is a convenient method to characterize

310 the injector when other known techniques are difficult or impossible to apply.

311 4.4. Nozzle Discharge Coefficient

312 Once the ROI has been calculated from the momentum flux data, it is pos-
313 sible to estimate the discharge coefficient of the nozzle. It is calculated by
314 using the ROI combining Equation 9 and the Bernoulli equation for velocity
315 $u_b = \sqrt{2\Delta P/\rho_f}$ as follows:

$$C_d = \frac{\dot{m}}{A\sqrt{2\Delta P\rho_f}} \quad (20)$$

316 Then, the evolution of the discharge coefficient of the nozzle can be charac-
317 terized in terms of the Reynolds number, which is defined as:

$$Re = \frac{\rho_f u_0 D_0}{\mu_f} \quad (21)$$

318 Where D_0 is the diameter of the orifice, ρ_f is the density of the fluid, u_0 the
319 velocity at the nozzle exit and μ_f the dynamic viscosity of the fluid.

320 To determine the Reynolds number it is required to know the properties of
321 the fluid at the corresponding conditions. The density used for Equations 13,
322 14 and 15 was calculated using the information from [30].

323 The viscosity of the fluid varies widely with the temperature, therefore it was
324 calculated using an exponential decay fit with the data available in the work of
325 Halonen et al [31]. Figure 15 shows the viscosity of water and the data points
326 and fit used to determine this property at different temperatures for UWS.

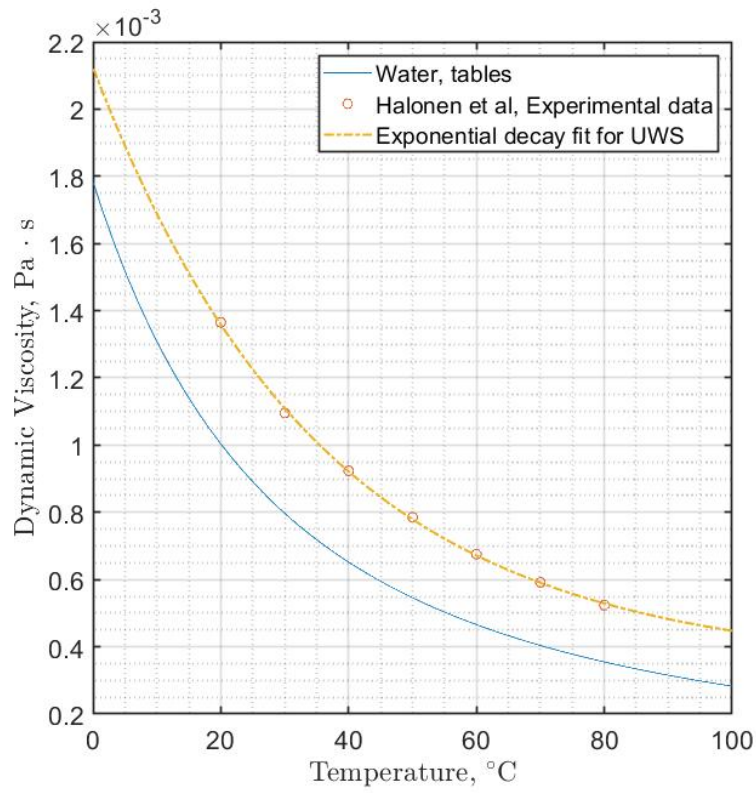


Figure 15: Viscosity of the UWS and water at different temperatures.

327 Figure 16 shows the discharge coefficient C_d versus the Reynolds number
 328 Re for the tested conditions, on the left image the C_d of the UWS and on the
 329 right for water.

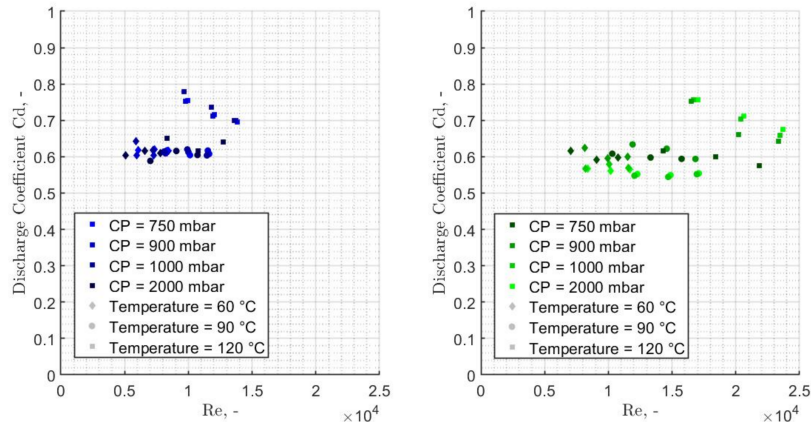


Figure 16: Discharge coefficient vs Reynolds number for each fluid at all the counter pressures and temperature of 60°C and 90°C, for UWS (left) and water (right).

330 In the images we can observe how the discharge coefficient of both fluids is
 331 near 0.6 for the temperatures of 60°and 90°C. Comparing the obtained value for
 332 the SCR dosing unit with other applications in engines, it is similar to the Cd
 333 of GDI injectors with a value near 0.55, but lower than diesel injectors which
 334 usually have a Cd value around 0.8 [14]. The differences can be attributed to a
 335 combination of facts. On one side, the pressures involved in the injection process
 336 of the current application is very little compared to those used in gasoline or
 337 diesel injection. On the other hand, Figure 17 shows the internal geometry of the
 338 nozzle, showing a short L/d combined with a deflection of the flow at the
 339 inlet of the orifices, which can generate some perturbations in the fluid motion.

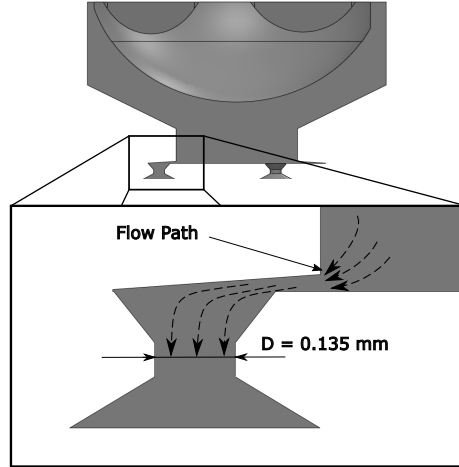


Figure 17: Section view of the internal geometry of the studied injector.

340 Once the fluid temperature is above the flash boiling condition and the am-
 341 bient pressure is below 2 bar, a strange behavior is observed where the discharge
 342 coefficient rises nearly to 0.8 and decreasing towards 0.65 as the Reynolds num-
 343 ber is higher (higher ΔP).

344 These outlier points take higher value due to the difficulty measuring its
 345 momentum flux at flash boiling conditions, where the values are considerably
 346 smaller than the values for lower temperatures at the same ΔP , resulting in
 347 higher injected mass and ROI as shown in Figures 12 and 14.

348 Another notable difference in Figure 16 is the higher range of Reynolds
 349 numbers for water, which can be attributed to the higher exit velocity (higher
 350 momentum flux) than for UWS and to the lower viscosity of the fluid.

351 5. Conclusion

352 A methodology to determine the rate of injection in a SCR dosing unit was
 353 employed obtaining remarking results. Normally an Injection Rate Discharge
 354 Curve indicator device based on the Bosch long tube method would be used to
 355 determine the rate of injection, but the low ΔP and the small amounts of injected

356 mass makes hard to employ this kind of system. In this case, a methodology to
357 measure the rate of injection using the momentum flux measurements becomes
358 useful.

359 The momentum flux of the SCR system injector was measured using water
360 and UWS as fluids. The results shows that the water has higher momentum flux
361 than the UWS for the same testing conditions due to higher velocity of water
362 at the exit of the nozzle.

363 The momentum was affected by the temperature of the fluid and the ambient
364 pressure, showing lower momentum flux as the temperature of the spray was
365 higher and lower momentum for higher ambient pressures.

366 A ratio R between the momentum flux of water and UWS was determined,
367 finding that on average the momentum flux of UWS is 0.924 time the momentum
368 of water.

369 The injected mass was also determined for all the tested conditions, increas-
370 ing linearly with the square root of ΔP . Also finding that under flash boiling
371 conditions the amount of mass injected was nearly 15% higher for both fluids.
372 This can be attributed to the changes in the physical properties of the fluids
373 which increases the discharge coefficient of the nozzle, combined with the effects
374 of the flash boiling conditions.

375 The injected mass and momentum flux were used to determine the Rate
376 Of Injection using Equations. 16, 17 and 18. The ROI also followed a linear
377 behaviour with the square root of ΔP .

378 With the ROI, the discharge coefficients of the nozzle were calculated finding
379 a steady value as the Reynolds number increased for most testing points, except
380 for the points that reached flash boiling conditions.

381 When the flash boiling conditions for the spray are set a higher ROI and
382 Cd were determined for both fluids. The reason behind this increase can be
383 attributed to two factors: the internal behaviour of the nozzle and the changes
384 in the structure of the spray (higher spreading angle) at high temperatures,
385 leading to higher injected mass and probably not capturing the whole spray
386 with the piezoelectric sensor (and thus leading to lower measured momentum

387 flux).

388 Finally, the measuring technique is a useful tool for the hydraulic character-
389 ization of the spray, providing a valid method to accurately determine the ROI
390 relying on the momentum flux measurements and the total injected mass. This
391 is of importance due to the need to determine the ROI, specially when other
392 methodologies cannot be applied, to validate CFD models and accurately dose
393 the UWS, allowing proper reduction of emissions (NOx or Ammonia slip) and
394 minimizing the deposit formation in the exhaust line.

395 **6. CRediT authorship contribution statement**

396 **Raúl Payri:** Supervision, Project administration, Resources, Writing - re-
397 view. **Gabriela Bracho:** Supervision, Conceptualization, Methodology, For-
398 mal analysis, Investigation, Writing - Review and editing. **Pedro Martí-**
399 **Aldaraví:** Writing - review and editing, Formal analysis, Investigation. **Ar-**
400 **mando Moreno:** Conceptualization, Methodology, Formal analysis, Investiga-
401 tion, Writing - original draft.

402 **7. Declaration of Competing Interest**

403 The authors declare that they have no known competing financial interests or
404 personal relationships that could have appeared to influence the work reported
405 in this paper.

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