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Additional Information

1 **Widening the applicability of AnMBR for urban wastewater**
2 **treatment through PDMS membranes for dissolved methane**
3 **capture: Effect of temperature and hydrodynamics.**

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28 **ABSTRACT**

29 AnMBR technology is a promising alternative to achieve future energy-efficiency and
30 environmental-friendly urban wastewater (UWW) treatment. However, the large amount
31 of dissolved methane lost in the effluent represents a potential high environmental impact
32 that hinder the feasibility of this technology for full-scale applications. The use of
33 degassing membranes (DM) to capture the dissolved methane from AnMBR effluents can
34 be considered as an interesting alternative to solve this problem although further research
35 is required to assess the suitability of this emerging technology. The aim of this study was
36 to assess the effect of operating temperature and hydrodynamics on the capture of
37 dissolved methane from AnMBR effluents by DMs. To this aim, a commercial
38 polydimethylsiloxane (PDMS) DM was coupled to an industrial prototype AnMBR
39 (demonstration scale) treating UWW at ambient temperature. Different operating
40 temperatures have been evaluated: 11, 18, 24 and 30 °C. Moreover, the DM was operated
41 at different ratios of liquid flow rate to membrane area ($Q_L:A$) ranging from 22 to 190 Lh⁻¹
42 m⁻² in order to study the resistance of the system to methane permeation. Methane
43 recovery was maximized when temperature raised and $Q_L:A$ was reduced, giving methane
44 recovery efficiencies (MRE) of about 85% at a temperature of 30 °C and a $Q_L:A$ of 25
45 Lh⁻¹m⁻². The study showed that high $Q_L:A$ ratios hinder methane recovery by the
46 perturbation of the DM fibers, being this effect intensified at lower temperatures probably
47 due the higher liquid viscosities. Also, the performed fouling evaluation showed that not
48 significant membrane fouling may be expected in the DM unit at the short-term when
49 treating AnMBR effluents. A resistance-in-series model was proposed to predict the
50 overall mass transfer of the system according to operating temperature and $Q_L:A$, showing
51 that methane capture was controlled by the liquid phase, which represented up to 80-90%
52 of total mass transfer resistance. The energy and environmental evaluation performed in

53 this study revealed that PDMS DMs would enhance energy recovery and environmental
54 feasibility of AnMBR technology for UWW treatment, especially when operating at low
55 temperatures. When MRE was maximized, the combination of AnMBR with DM
56 achieved net energy productions and net greenhouse gas reductions of up to 0.87 kWh
57 and 0.216 kg CO₂-eq per m³ of treated water.

58

59

60 **Keywords**

61 Anaerobic membrane bioreactor (AnMBR); greenhouse gas (GHG) emissions; dissolved
62 methane capture; PDMS degassing membrane; urban wastewater.

63 1. INTRODUCTION

64 Water stress is now a serious and growing problem worldwide and there is an urgent need
65 to apply a new wastewater development model focused on the Circular Economy. In view
66 of the current global energy crisis and climate change, a more energy-efficient and
67 environmentally-friendly technology is required able to generate high-quality reclaimed
68 water. In the wastewater sector, aerobic-based treatments are identified as energy-
69 intensive processes due to the large amount of energy required to oxidize organic waste
70 (Lee *et al.*, 2017), while high biosolid production rates can also be expected in aerobic
71 systems (McCarty *et al.*, 2011). On the other hand, anaerobic processes avoid aeration
72 requirements when transforming biodegradable material into methane. However, due to
73 the lower growth rate of anaerobic microbes, high-rate processes are needed for treating
74 urbane wastewaters (UWW) anaerobically to reduce capital costs (i.e. reducing reactor
75 volume).

76 Anaerobic membrane bioreactors (AnMBRs) have been proposed by several authors as a
77 suitable alternative for high-rate UWW treatment. Thanks to membrane technology,
78 sludge and hydraulic retention times can be decoupled allowing the retention of generated
79 biomass (Giménez *et al.*, 2012; Smith *et al.*, 2012) while producing a high quality effluent
80 (solids-free). Nevertheless, AnMBR systems still present different key issues that restrict
81 their implementation in full-scale UWW treatments (Robles *et al.*, 2018), being one of
82 the main drawbacks the direct greenhouse gas (GHG) emissions produced by stripping
83 dissolved methane from the effluent which raise the carbon footprint and reduce process
84 energy-efficiency (Smith *et al.*, 2012). Indeed, methane losses can reach up to 80% of the
85 total methane production at relatively low operating temperatures (e.g. 15 °C) (Giménez,
86 *et al.*, 2014; Cookney *et al.*, 2016), so that efficient capture of the dissolved methane plays
87 a crucial role in advancing AnMBR technology for UWW treatment.

88 Degassing membranes (DM) are a promising solution for capturing dissolved methane
89 from anaerobic effluents (Crone *et al.*, 2017). This technology avoids the frequent
90 degassing tower operating problems (e.g. flooding, foaming and emulsion) thanks to
91 liquid and gas phase division by membranes (Stanojević *et al.*, 2003). The possibility of
92 operating DMs in the vacuum mode also prevents captured methane dilution
93 (characteristic of sweep gas processes), enhancing the potential energy valorization of
94 recovered methane. In fact, recent studies have showed promising efficiencies for
95 methane recovery from anaerobic effluents on a lab-scale (Bandara *et al.*, 2013; Cookney
96 *et al.*, 2016; Henares *et al.*, 2017), proving the effectivity of DMs for this purpose.
97 Nonetheless, further aspects need to be considered in order to evaluate the feasibility of
98 this technology to support AnMBR technology, finding optimal conditions under which
99 the energy recovery potential of the system is maximized and the GHG emissions are
100 minimized.

101 One of most important issues to take into account is the operating temperature of the
102 system. In anaerobic treatment, anaerobic reactor heating generally represents the major
103 process energy input (Lettinga *et al.*, 2001; Bani *et al.*, 2009), suggesting ambient
104 operation to reduce operating costs (Bandara *et al.*, 2011) and indirect GHG emissions
105 (Bani *et al.*, 2009) when treating low-strength UWWs. In this context, AnMBR can be
106 considered as an attractive option since the membrane allows operating at low/mild
107 temperatures without compromising the effluent quality or process energy balance,
108 reporting even net energy outputs in some cases (Pretel *et al.*, 2015; Stazi and Tomei,
109 2018). Nonetheless, since methane solubility in water increases as the operating
110 temperature decreases, more methane losses are expected under these conditions (Velasco
111 *et al.*, 2018). Therefore, evaluating methane capture efficiency of DMs at different
112 temperatures is imperative to determine the most suitable operating conditions of the

113 combination AnMBR+DM, considering both environmental and energy aspects. On the
114 other hand, since non-porous membranes provide a significant additional resistance for
115 the methane capture, it is necessary to determine the main methane permeation resistance,
116 as well as the conditions under which it is minimized, in order to maximize dissolved
117 methane capture. In this regard, when using different DMs for dissolved gases recovery,
118 Wickramasinghe *et al.* (1992) and Henares *et al.* (2017) showed that the liquid resistance
119 is significantly superior than the membrane resistance or the gas resistance, revealing
120 that the liquid flow rate plays a crucial role in methane permeation. Additionally, large-
121 scale studies are needed to confirm the promising results reported for lab-scale
122 membranes, considering the hydrodynamic changes of industrial DM modules compared
123 to lab-scale DMs. Likewise, intrinsic variations when treating real UWWs such as the
124 interactions among the different dissolved gases present in anaerobic effluents (e.g.
125 carbon dioxide or sulfidic acid) or methane recovery reductions by membrane fouling
126 need to be studied.

127 Therefore, this study aims to evaluate the effect of operating temperature and
128 hydrodynamics on the performance of a commercial PDMS DMs for the capture of
129 dissolved methane from the effluent of an industrial prototype AnMBR (demonstration-
130 scale), which treated the effluent from the pre-treatment step of a full-scale WWTP. To
131 this aim, the system was operated at 4 operating temperatures (11, 18, 24 and 30 °C).
132 Additionally, 8 liquid flow rates (from 22 to 190 Lh⁻¹m⁻²) were tested in order to evaluate
133 the resistance of the DM system to methane permeation at different conditions. Based on
134 the experimental results, the better strategies that maximized methane recovery were
135 determined. On the other hand, a resistance-in-series model was proposed to predict the
136 DM's system methane capture resistance. Finally, the energy and environmental (GHG
137 emissions) feasibility of the combined system (AnMBR+DM) was assessed.

138 2. MATERIALS AND METHODS

139 2.1. Experimental set-up

140 A polydimethylsiloxane (PDMS) hollow-fiber commercial module (PermSelect®,
141 MedArray Inc. USA) was employed as DM for the treatment of the methane-saturated
142 effluent from an AnMBR prototype-plant. The AnMBR prototype-plant consisted of a 40
143 m³ anaerobic bioreactor coupled to three external membrane tanks (0.8 m³ each). The
144 membrane tanks were fitted with an ultrafiltration membrane system (PURON® PSH 41,
145 Koch Membrane Systems, 0.03 µm pore size) giving 123 m² of total filtration area. This
146 AnMBR system was installed in the ‘Alcázar de San Juan’ WWTP (Ciudad Real, Spain)
147 and was fed with effluent from the pre-treatment step of the full-scale WWTP. Further
148 information on this AnMBR system can be found in Jiménez *et al.* (2020). The average
149 AnMBR effluent characteristics and operating conditions during the experimental periods
150 can be found in the Appendix A, Table A1.

151 The DM unit was operated in shell-side mode to avoid lumen clogging-related problems
152 (Sanchis-Perucho *et al.*, 2020) with vacuum applied to the lumen side to provide the
153 driving force. Previous studies have shown the favorable effects of operating PDMS DMs
154 at high transmembrane pressures (TMP) (Cookney *et al.*, 2012; Henares *et al.*, 2017). In
155 fact, the previous results obtained by the system (see Sanchis-Perucho *et al.*, 2020)
156 revealed that net energy recovery can be maximized by increasing TMP. Since the DM
157 unit had a limit shell-side operating pressure of 1 bar, TMP was set to 0.8 bar to avoid
158 operating close to the permitted maximum. Two pressure sensors (UNIK 5000-746-3600,
159 Druck) were fitted to the liquid and gas sides for continuous TMP monitoring and control.
160 The main features of the DM module can be found in the Appendix B, Table B1.

161 The AnMBR+DM combination was operated at ambient temperatures of 11, 18, 24 and
162 30 °C to assess the effect of seasonal temperature dynamics on methane capture efficiency
163 and AnMBR+DM system energy and environmental feasibility. The liquid flow rate to
164 membrane area ($Q_L:A$) ratio was varied from 22 to 190 $Lh^{-1}m^{-2}$ with a stepwise of 24 $Lh^{-1}m^{-2}$. A liquid-flow meter (VX100-45, Vogelsang) was used to measure the applied $Q_L:A$.

166 **2.2. Analytical methods**

167 Duplicate liquid samples from the DM inlet and outlet were collected in 50 mL glass vials
168 and stored at 20 °C with continuous stirring for at least 4 hours to reach gas-liquid
169 thermodynamic equilibrium. The DM unit was operated for at least 5 minutes before the
170 sampling to achieve steady-state conditions. Methane concentration in the head-space of
171 the vials was determined by gas chromatography. Further details on the method used to
172 determine dissolved methane concentrations and calculate the amount of methane
173 recovered can be found in Sanchis-Perucho *et al.* (2020).

174 To evaluate potential fouling issues during DM operation, the concentrations of
175 ammonium, phosphate, total organic carbon (TOC), and total inorganic carbon (TIC)
176 were determined in the DM inlet and outlet streams at different $Q_L:A$ ratios. Ammonium
177 and phosphate concentrations were obtained according to Standard Methods (APHA
178 AWWA WEF, 2012). TOC and total carbon (TC) concentrations were determined by a
179 TOC-VCHS total organic carbon analyzer (Shimazu Corporation), determining the TIC
180 concentration by difference.

2.3. Calculations

2.3.1. Evaluation of DM performance

Methane recovery efficiency (MRE), net energy demand, and GHG emissions in the DM unit were calculated according to the method described in Sanchis-Perucho *et al.* (2020). The AnMBR energy demand was theoretically calculated according to Pretel *et al.* (2016) using data from the AnMBR prototype-plant: equipment, flows, biogas production, operating temperature, etc. AnMBR GHG emissions were calculated considering both energy savings and dissolved methane lost into the effluent.

Liquid velocity (v_L) and Reynolds module (Re) were determined for DM hydrodynamics evaluation. Since the membrane was operated on the shell side, which had an enhanced hydrodynamic structure to improve dissolved gas recovery, v_L and Re were calculated accounting for an equivalent diameter (D_{eq}). A diagram of the commercial DM unit used in this study can be found in the Appendix B, Fig. B1. The DM unit had a central cylindrical diffuser to improve the contact between the liquid and the membrane while reducing the dead zones, so that two different liquid fluxes could be considered in the system: (1) a flux parallel to the fibers across the annular DM section, and (2) a flux perpendicular to the fibers from the cylindrical diffuser to the DM external diameter. Although the fluxes were simultaneous and affected DM hydrodynamics, in order to simplify the calculation both v_L and Re were calculated assuming that the liquid flux was controlled by a single mechanism. According to this simplification, similar v_L and Re values were obtained regardless of the flux considered (data not shown). Since the perpendicular flux requires more factors to be considered (e.g. fiber distribution, number of fibers in each section pass, average distance between fibers, etc.), D_{eq} was estimated with the parallel flux as the dominant mechanism using the following expression:

205
$$D_{eq} = \sqrt{\frac{4 \cdot (V_S - V_{cd})}{\pi \cdot L_w}} \quad eq. (1)$$

206 Where V_S and V_{cd} are the DM unit shell volume and the cylindrical diffuser volume,
 207 respectively, and L_w is the wet fiber length (see Table 1 and Fig. 1).

208 **2.3.2. Theory approach on DMs overall mass transfer coefficient**

209 Dissolved gas capture by DMs can be modeled considering the different involved phases
 210 as an ideal three resistance-in-series system. Defining the total mass flux resistance (R_T)
 211 as the inverse of the overall mass transfer coefficient (K_O), the R_T can then be obtained
 212 from the total of the different resistances involved in the methane mass capture: the liquid
 213 boundary layer (R_L), the permeable non-porous membrane (R_M) and the gas phase
 214 boundary layer (R_G). Considering cylindrical coordinates, the resistance-in-series model
 215 can be expressed as follows:

216
$$R_T = \frac{1}{K_O A_L} = \frac{1}{k_L A_L} + \frac{1}{k_M A_{ml}} + \frac{1}{H^{CH_4}(T) k_G A_G} = R_L + R_M + R_G \quad eq. (2)$$

217 Where k_L , k_M and k_G are the gas mass transfer coefficients in liquid, membrane and gas
 218 phases, respectively, A_L and A_G are the effective membrane area interacting with liquid
 219 and gas phases, respectively, A_{ml} is the logarithmic mean area of the DM and $H^{CH_4}(T)$ is
 220 the Henry's constant for methane. However, unlike the liquid and membrane phases, the
 221 gas boundary layer does not usually represent a significant resistance to mass flux due to
 222 the higher diffusion coefficients in gases than in liquids and membranes (Lu *et al.*, 2008).
 223 *Eq. (2)* is therefore commonly simplified into the following expression:

224
$$\frac{1}{K_O A_L} = \frac{1}{k_L A_L} + \frac{1}{k_m A_{tm}} \quad eq. (3)$$

225 Considering the different described resistances as an isotropic material, the one-
 226 dimensional Fick's first law (steady state) can be used to calculate the gas flux through
 227 the membrane in dissolved gas capture systems:

$$228 \quad J = -D \frac{dc}{dx} \quad eq. (4)$$

229 Where J represents the flux, c the concentration of the diffused compound, x the distance
 230 and D the diffusion coefficient. Applying eq. (4) on the liquid phase, the following
 231 expression can then be obtained:

$$232 \quad J = \frac{D_{CH_4-W}}{t_L} \cdot \Delta c = k_L \cdot \Delta c \quad eq. (5)$$

233 Where D_{CH_4-W} is the methane diffusion coefficient in water and t_L is the thickness of the
 234 liquid phase resistance. Since methane is homogeneously dissolved in the DM's influent,
 235 t_L can be considered as the liquid phase boundary thickness, which should depend on
 236 operating v_L . D_{CH_4-W} can be influenced by both v_L and temperature. The temperature
 237 effect on D_{CH_4-W} can be represented by the equation proposed by Himmelblau (1964):

$$238 \quad D_{CH_4-W} = \exp\left(\frac{-A}{T} + B\right) \cdot 10^{-9} \quad eq. (6)$$

239 Where T is the temperature and A and B are fitting parameters that depend on the
 240 diffusing specie and the medium (Himmelblau, 1964). Alternatively, considering
 241 turbulent liquid conditions in cylindrical pipes, the Linton & Sherwood semi-empirical
 242 expression can be used to estimate k_L :

$$243 \quad \frac{k_L \cdot D_{eq}}{D_{CH_4-W}} = Sh = 0.023 \cdot Re^{0.83} \cdot Sc^{1/3} \quad eq. (7)$$

244 Where Sh and Sc are the Sherwood and Schmidt dimensionless modules, respectively.

245 On the other hand, a similar expression to *eq. (5)* can be obtained when applying Fick's
 246 law to the membrane phase. In non-porous membranes, membrane resistance is usually
 247 modeled by the solubility-diffusion theory (Tremblay *et al.*, 2006), according to which
 248 mass transport through dense membranes is carried out in three steps: (1) gas is dissolved
 249 on the membrane surface, (2) diffused across the membrane, and (3) re-dissolved in the
 250 gas phase. Defining membrane permeability as solubility and diffusivity product (*i.e.*
 251 $P=S \cdot D$) (Tremblay *et al.*, 2006), Fick's first law applied to non-porous membrane systems
 252 can thus be expressed as follows:

$$253 \quad J = \frac{P_{CH_4-PDMS}}{t_M} \cdot \Delta c = \frac{S_{CH_4-PDMS} \cdot D_{CH_4-PDMS}}{t_M} \cdot \Delta c = k_M \cdot \Delta c \quad eq. (8)$$

254 Where t_M is membrane thickness and D_{CH_4-PDMS} , S_{CH_4-PDMS} and P_{CH_4-PDMS} are methane
 255 diffusion, solubility and permeability in PDMS material, respectively. In this case, the
 256 influence of temperature on non-porous membrane permeability can be calculated by the
 257 Van't Hoff–Arrhenius approach (Raharjo *et al.*, 2007a):

$$258 \quad P_{CH_4-PDMS} = P_0 \cdot \exp\left(\frac{-E_P}{R \cdot T}\right) \quad eq. (9)$$

259 Where R is the universal constant of gases ($0.082 \text{ atm L mol}^{-1} \text{ K}^{-1}$), P_0 is the pre-
 260 exponential factor and E_P is the activation energy of permeation. Finally, *eqs. (5)* and *(8)*
 261 can be combined and included in *eq. (3)*, resulting in the following expression which can
 262 be used to predict K_O regarding temperature.

$$263 \quad K_O = \left(\frac{1}{\frac{t_L}{\exp\left(\frac{-A}{T}+B\right) \cdot 10^{-9} \cdot A_L} + \frac{t_M}{P_0 \cdot \exp\left(\frac{-E_P}{RT}\right) \cdot A_{lm}}} \right) \frac{1}{A_L} \quad eq. (10)$$

264 Alternatively, using the turbulent model to estimate k_L , a similar expression can be
 265 obtained:

$$K_O = \left(\frac{1}{\frac{D_{eq}}{0.023 \cdot Re^{0.83} \cdot Sc^{1/3} \cdot D_{CH_4-W} \cdot A_L} + \frac{t_M}{P_0 \cdot \exp\left(\frac{-E_P}{RT}\right) \cdot A_{lm}}} \right) \frac{1}{A_L} \quad eq. (11)$$

2.3.3. Experimental determination of DMs overall mass transfer coefficient

K_O in DMs can be calculated applying a dissolved methane mass balance in the liquid phase (Wickramasinghe *et al.*, 1993):

$$Q_L dc_{CH_4} = J_{CH_4} dA_M \quad eq. (12)$$

Where Q_L is the liquid flow rate pumped through the DM unit, A_M is the membrane area, c_{CH_4} is the dissolved methane concentration in the water and J_{CH_4} is the permeated methane flux, which is perpendicular to the liquid flux. Then, applying Fick's first law in *eq. (12)* and rearranging the expression, the following differential equation is obtained (Wickramasinghe *et al.*, 1993):

$$Q_L \frac{dc_{CH_4}}{dA_M} + K_O(c_{CH_4} - c^*_{CH_4}) = 0 \quad eq. (13)$$

Where $c^*_{CH_4}$ is the membrane-gas interphase methane concentration, which is normally estimated considering equilibrium conditions between $c^*_{CH_4}$ and the methane concentration reached in the gas phase (C_G) (Cookney *et al.*, 2016; Henares *et al.*, 2017):

$$c^*_{CH_4} = H^{CH_4}(T) \cdot c_G \quad eq. (14)$$

Assuming an average constant value for c_G at each operating temperature, *eq. (13)* can be integrated between the influent and effluent methane concentration in the DM, resulting in the following equation:

$$K_O = -\frac{Q_L}{A_M} \ln \left(\frac{c_{CH_4,eff} - c^*_{CH_4}}{c_{CH_4,inf} - c^*_{CH_4}} \right) \quad eq. (15)$$

285 Where $c_{CH_4.inf}$ and $c_{CH_4.eff}$ are the concentrations of dissolved methane in influent and
 286 effluent membrane streams, respectively. Since continuous vacuum was employed to
 287 provide the driving force for the methane capture and k_G was assumed as negligible, the
 288 $c_{CH_4}^*$ reached during DM operations was considered negligible compared to the c_{CH_4}
 289 present in the liquid phase (*i.e.* $c_{CH_4} \gg c_{CH_4}^*$, thus $c_{CH_4} - c_{CH_4}^* \approx c_{CH_4}$). Therefore, *eq.*
 290 (15) can be simplified to obtain *eq.* (16), resulting in an expression on which K_O can be
 291 experimentally modeled for the operating conditions.

$$292 \quad K_O = -\frac{Q_L}{A_M} \ln\left(\frac{c_{CH_4.eff}}{c_{CH_4.inf}}\right) \quad eq. (16)$$

293 The least squares method was used to adjust the theoretical K_O values calculated by *eqs.*
 294 (10) and (11) to that obtained experimentally, estimating the value of the different
 295 parameters (A , B , t_L , P_0 and E_P) for each $Q_L:A$ ratio evaluated.

296 3. RESULTS AND DISCUSSION

297 3.1. Effect of operating conditions on methane recovery

298 Fig. 1 shows the recovered methane fluxes and methane recovery efficiencies reached by
 299 the DM module under the evaluated operating conditions. As expected, temperature
 300 played an important role in methane recovery. According to Fick's first law, methane flux
 301 is controlled by both K_O and the methane concentration gradient. The higher the
 302 temperature the lower the concentration of methane dissolved in the influent but the
 303 higher K_O achieved (see Section 3.2). Due to this competitive effects, two different
 304 dynamics can be observed regarding temperature rise. When low $Q_L:A$ ratios were
 305 applied, lightly lower methane fluxes were reached as temperature raised due the
 306 reduction of the driving force (see Fig. 1a) but when the $Q_L:A$ reached values around 100-

307 $150 \text{ Lh}^{-1}\text{m}^{-2}$, K_O fell thus reducing the methane flux. Over these higher $Q_L:A$ values, the
308 higher methane fluxes achieved at higher temperatures (see Fig. 1b) were due to the early
309 drop in K_O achieved at lower temperatures, hindering methane permeation. These
310 dynamics also influenced MRE; it improved at high temperatures as shown in Fig. 1c. In
311 this case, although in some circumstances higher methane fluxes can be achieved at lower
312 temperatures, the higher K_O values and lower influent dissolved methane concentrations
313 reached at higher temperatures increased the percentage of dissolved methane captured,
314 showing that lower methane emissions can in fact be achieved at higher temperatures.
315 This finding is in agreement with those reported by Cookney *et al.* (2011), who found
316 improved methane recovery efficiencies in the summer period using PDMS membranes.
317 Similarly, Bandara *et al.* (2012) reported slight higher dissolved methane emissions when
318 operating a multi-layer polyethylene DM module in the winter period, although in this
319 case lightly lower methane recovery efficiencies were achieved as temperature raised.

320 Regarding the effect of $Q_L:A$ on MRE, the recovered methane flux increased
321 progressively as $Q_L:A$ was increased from 22 to $118 \text{ Lh}^{-1}\text{m}^{-2}$ (see Fig. 1a). However, a
322 decrease in the recovered methane flux was observed at $Q_L:A$ above $118 \text{ Lh}^{-1}\text{m}^{-2}$ (see Fig.
323 1b). As reported in other studies (Henares *et al.*, 2017; Sanchis-Perucho *et al.*, 2020), this
324 effect is related to a drop in K_O at high operating $Q_L:A$ ratios (see Section 3.2),
325 representing a negative effect on the methane flux through the membrane. On the other
326 hand, as reported in a previous work (Sanchis-Perucho *et al.*, 2020), raising $Q_L:A$
327 negatively affected the MRE due the DM hydraulic retention time reduction (see Fig. 1c).
328 Indeed, similar results were reported by Cookney *et al.* (2016) when operating a dense
329 and micro-porous DM modules. Therefore, it can be concluded that when operating a
330 PDMS DM module, lower dissolved methane emissions are expected at higher
331 temperatures and lower $Q_L:A$ ratios.

3.2. Influence of operating conditions on K_O

As exposed above, since K_O may control the amount of dissolved methane than can be captured from the treated liquid stream, maximizing K_O is necessary to boost DM effectivity. Then, K_O was calculated by *eq.* (16) for the different operating conditions evaluated to determine the most favorable conditions that maximized K_O . As can be seen in Fig. 2, raising the temperature had a favorable effect on K_O . As different in-series resistances are involved in DM methane recovery, temperature is expected to play a crucial role on K_O dynamics since methane solubility and diffusivity in water and PDMS are strongly affected by temperature. On the one hand, methane solubility in water is reduced at higher temperatures and the reduced driving force may decrease the amount of permeated methane, but should not directly affect k_L . In regard of methane diffusion in water, it is expected to increase at higher temperatures (Chen *et al.*, 2018), enhancing k_L and therefore K_O . Thus, it could be assumed that the temperature rise reduced the liquid phase resistance to methane capture. On the other hand, considering gas solubility and diffusivity on PDMS membranes, a direct relationship between temperature and k_M cannot be deduced, since their effect on membrane permeability depends on the treated gas (Pinnau & He, 2004). Regarding methane solubility on PDMS, an increase in temperature reduces gas solubility on the membrane surface (Raharjo *et al.*, 2007b; Favre, 2017), thus reducing k_M . This effect is especially important for heavier gases, such as C_3H_8 (Sadrzadeh *et al.*, 2009), although methane solubility is slightly affected by temperature due to its lower molecular weight (Sadrzadeh *et al.*, 2009). Hence, the negative effect of temperature on k_M may not strongly contribute to K_O . Conversely, a rise in temperature favors gas diffusion through the membrane. According to the free-volume theory (Stern, 1994), this phenomenon is due to an increase in polymeric chain structure mobility as temperature rises, allowing higher free volumes in the membrane structure and improving

357 gas diffusivity (Favre, 2017). Indeed, enhanced methane diffusion has been reported
358 when raising the temperature in PDMS membranes (Raharjo et al., 2007a; Sadrzadeh *et*
359 *al.*, 2009) and improved methane permeability of PDMS membranes has been reported
360 when increasing temperature in pure gas streams (Pinnau & He, 2004; Raharjo et al.,
361 2007a; Sadrzadeh *et al.*, 2009). Hence, it can be concluded that in dissolved methane
362 capture by PDMS membranes a favorable effect on k_M can be achieved when operating
363 at higher temperatures finally increasing K_O .

364 Concerning the effect of $Q_L:A$ on K_O , increasing $Q_L:A$ improved K_O to a maximum value,
365 after which it fell as $Q_L:A$ was raised (see Fig. 2a). As reported in a previous work
366 (Sanchis-Perucho *et al.*, 2020), this phenomenon could be explained by two possible
367 hypotheses: either (1) the appearance of an additional mass transfer resistance or, (2)
368 changes in the membrane hydrodynamic performance. A preliminary membrane fouling
369 and hydrodynamic study was performed to determine the predominant reason why K_O
370 falls at high $Q_L:A$ ratios.

371 **3.2.1. Short-term DM fouling evaluation.**

372 As membrane fouling is one of most important issues in any membrane system, reduction
373 of DM methane recovery capacity by reversible and/or irreversible fouling should be
374 considered. In this respect, AnMBR effluent has a high-quality stream (solid-free
375 permeate), thus reducing the possibility of a biological and/or inorganic cake layer
376 forming on the DM membrane surface. Membrane fouling should therefore be controlled
377 by the partial loss of the useful membrane area for depositing colloidal particles, salt
378 precipitation or soluble compound adsorption on the membrane surface.

379 Table 1 shows the main characteristics of the DM influent and effluent streams. Since the
380 higher the $Q_L:A$ the higher the amount of described pollutants that can reach the

381 membrane surface, fouling propensity could be intensified as $Q_L:A$ raises. However, no
382 relevant changes were seen in the inlet and outlet nutrient concentrations and there were
383 negligible changes in the TIC and TOC concentrations (without considering the captured
384 methane). The results obtained thus seem to indicate that inorganic salt precipitation
385 and/or organic substance adsorption did not contribute a great deal to short-term
386 membrane fouling. Nevertheless, these substances could be deposited quite slowly, which
387 makes their early identification difficult by regular sampling. Further studies are required
388 to assess the possible unfavorable effects of these substances on DM performance and
389 should focus on evaluating long-term fouling and consider integrated DM effluent
390 sampling.

391 Three short-term fouling experiments were also performed. In this case, the DM module
392 was operated for 90 minutes to evaluate the fouling rate under different $Q_L:A$ ratios.
393 Negligible MRE reductions were found during operations, indicating no fouling-related
394 problems (see Fig. 3). This agrees with the results reported by Henares *et al.* (2017), who
395 found not serious fouling problems until about 50 hours when operating a PDMS DM
396 unit in shell-side mode. In addition, Bandara *et al.* (2012) not reported meaningful fouling
397 propensities when operating a multi-layer polyethylene DM module for 18 months,
398 concluding that membrane fouling is neither an important issue in the middle-term.

399 **3.2.2. DM hydrodynamics evaluation**

400 Liquid velocity and Reynolds number were calculated to study the hydrodynamic effects
401 of raising $Q_L:A$. As can be seen in Fig. 2b, K_O declined at Reynolds numbers about 2100
402 - 4000, indicating a transition from laminar to turbulent flow. The K_O decline could thus
403 be controlled in the studied operating conditions by the increasing turbulent flow. As
404 Henares *et al.* (2017) have indicated, DMs can present a critical $Q_L:A$ at which membrane

405 fibers may be less effective. This phenomenon can be explained by the greater shaking,
406 compression and deformation of membrane fibers as $Q_{L:A}$ rises. The dead zones may also
407 increase when raising v_{LS} on high fiber-density DMs (Coockney *et al.*, 2011), especially
408 when operating on the shell side. Moreover, as Coockney *et al.* (2011) suggested, low
409 liquid velocities could help the development of a liquid-phase boundary layer that builds
410 up gas near the membrane surface and the greater turbulence would hinder methane
411 diffusivity through the membrane by reducing or removing this boundary layer.
412 Assuming that the reduced K_O was caused by the change in hydrodynamics, the earlier
413 drop of K_O at lower temperatures could have been caused by greater liquid viscosity. This
414 effect, although it can postpone turbulent flux development, would also result in a higher
415 liquid-fiber friction as $Q_{L:A}$ grows, being able to increase fiber deformation and finally
416 decreasing more intensively the K_O at low temperatures. However, other undesirable
417 effects can also appear when raising $Q_{L:A}$, such as concentration polarization due the
418 increase in concentration gradients that oppose flux. Further research is required to
419 confirm this hypothesis.

420 **3.3. K_O -temperature modeling**

421 The influence of temperature on K_O was first modeled by *eq.* (10). As can be seen in Fig.
422 4, the model accurately fitted the experimental data when operating at $Q_{L:A}$ ratios lower
423 than $100 \text{ Lh}^{-1}\text{m}^{-2}$ but was slightly worse at higher $Q_{L:A}$ ratios. This was mainly attributed
424 to the change in the DM flow conditions as v_L increased (see Fig. 2). In this respect, when
425 analyzing the values obtained for the different equation parameters (see Fig. 5),
426 parameters P_0 and E_P (methane-membrane permeability related parameters) remained
427 nearly invariable as $Q_{L:A}$ was raised. This, as expected, confirms that k_M is not influenced
428 by the applied $Q_{L:A}$. However, a significant increase in parameters A and B (methane-
429 liquid diffusion related parameters) occurred at $Q_{L:A}$ ratios over $100 \text{ Lh}^{-1}\text{m}^{-2}$. Indeed, the

430 values obtained for these parameters when operating at $Q_L:A$ ratios under $100 \text{ Lh}^{-1}\text{m}^{-2}$ can
431 be assumed as constant, achieving values of 1525 ± 289 and 5.24 ± 1.24 for A and B,
432 respectively. These values are similar to those reported for convective methane diffusion
433 in water ($A=1990$; $B=7.11$) (Chen *et al.*, 2018). The proposed model therefore agrees
434 with previous conclusions indicating that for $Q_L:A$ ratios over $100 \text{ Lh}^{-1}\text{m}^{-2}$ the flow inside
435 the DM loses its laminar properties. Moreover, t_L fell slightly when the $Q_L:A$ ratio was
436 over $100 \text{ Lh}^{-1}\text{m}^{-2}$ (from 52.5 ± 1.6 to $43.6 \pm 4.5 \mu\text{m}$) which could represent the reduction in
437 the liquid boundary layer due to increasing flow turbulence as v_L was raised.
438 Nevertheless, although t_L fell by 20%, there was no clear correlation as v_L increased, so
439 that no definite conclusions could be reached.

440 Since changes in the hydrodynamic conditions were not captured by the model proposed
441 in *eq.* (10), an alternative turbulent model was used to represent K_O (*eq.* (11)). However,
442 similar results were achieved in this case (see. Fig. 4), which could indicate that turbulent
443 mass transfer diffusion dynamics were not the main controlling mechanism. Indeed,
444 lower $D_{\text{CH}_4\text{-w}}$ was reached than that expected in laminar conditions for $Q_L:A$ values above
445 $100 \text{ Lh}^{-1}\text{m}^{-2}$ (data not shown). This could indicate that the modeled k_L may be
446 overestimated. As previously commented, disturbances on the fibers caused by the
447 turbulent medium could reduce methane mass transfer. These effects may also be greater
448 at low temperatures by a rise in medium viscosity. To estimate the disturbing effects of
449 liquid flow on membrane fibers, the liquid viscosity was thus selected as the main variable
450 to correct the modeled k_L values. This correction was applied considering a linear
451 relationship between liquid viscosity and the disturbing effects on the membrane fibers,
452 so that *eq.* (10) could be modified as follows:

453
$$K_O = \left(\frac{1}{\frac{t_L}{\left(\exp\left(\frac{-A}{T}+B\right)\cdot 10^{-9}-(a+b\cdot\mu)\right)\cdot A_L} + \frac{t_M}{P_0\cdot\exp\left(\frac{-E_p}{RT}\right)\cdot A_{lm}}} \right) \frac{1}{A_L} \quad eq. (17)$$

454 Where μ is the liquid dynamic viscosity, and a and b are linear fitting parameters. Since
 455 unfavorable effects on k_L should fall on the linear correction, in order to fit eq. (17) at
 456 high $Q_L:A$ ratios, the liquid diffusion parameters (A and B) were fixed to the values
 457 determined in laminar conditions (i.e. 1525 and 5.24 for parameters A and B,
 458 respectively). The least squares method was also used to fit parameters a and b.

459 Eq. (17) properly fitted the experimental data (see Fig. 4), showing that viscosity could
 460 be used to correct the overestimated k_L values. Increasing linear values were achieved for
 461 the parameter a, representing the unfavorable effect of raising $Q_L:A$ on K_O ; while the b
 462 parameter remained around $0.20 - 0.26 \text{ m}^3\cdot\text{N}^{-1}\cdot\text{s}^{-2}$ for the operating range evaluated (see
 463 Fig. 5c). According to this result, since viscosity correction was not necessary for laminar
 464 conditions, the a and b parameter values can be calculated as follows:

465
$$a = \begin{cases} (2.3260 \cdot 10^{-4} \cdot \mu - 5.6046 \cdot 10^{-2})_{Re > 2100} \\ 0_{Re < 2100} \end{cases} \quad eq. (18)$$

466
$$b = \begin{cases} 0.23_{Re > 2100} \\ 0_{Re < 2100} \end{cases} \quad eq. (19)$$

467 According to the proposed model, although R_M cannot be considered negligible, R_T is
 468 mainly controlled by R_L (see Fig. 6), resulting in about 80-90% of the R_T . In this regard,
 469 Wickramasinghe *et al.* (1992) suggested that for oxygen-water separation by micro-
 470 porous membranes, the achieved k_M is significantly higher than k_L . Therefore, k_L
 471 dominates mass transfer in DMs, concluding that K_O is independent of membrane
 472 properties. Henares *et al.* (2017) also reported similar results when operating PDMS
 473 membranes for methane recovery, and concluded that the R_L contributes about 80% of R_T .

474 These authors also indicate that k_M can be positively influenced by the applied vacuum
475 pressure in the permeate. Since the DM unit was operated at high permeate vacuum
476 pressures (TMP = 0.8 bar) k_M could have been significantly improved, thus reducing the
477 influence of R_M on R_T . Nonetheless, since many factors can affect K_O (e.g. temperature,
478 $Q_{L:A}$, flow properties, TMP) further research is required to determine the influence of
479 each partial resistance on R_T and develop strategies to improve mass transfer in DMs.

480 **3.4. Energy balance and environmental impact of the DM unit and AnMBR+DM** 481 **system**

482 The energy recovery and GHG emissions of the DM unit were calculated in order to
483 evaluate the feasibility of this technology for capturing the dissolved methane from
484 anaerobic effluents, thus enhancing AnMBR performance for UWW treatment. Figs. 7a
485 and 7b show the energy recovery and GHG emissions reached by the PDMS DM module
486 under the operating conditions evaluated. As expected, net energy productions were
487 achieved by the DM unit, which is in accordance with the results reported by other authors
488 when using this technology for capturing the dissolved methane from anaerobic effluents
489 (Cookney *et al.*, 2016; Henares *et al.*, 2017). The maximum energy recovery was
490 achieved at the lowest temperature and the lowest $Q_{L:A}$. Temperature affected energy
491 recovery due to its influence on methane flux (see Fig. 1a and 1b), so that for each $Q_{L:A}$
492 the higher the permeated methane flux the higher the energy output. Moreover energy
493 recovery improved as $Q_{L:A}$ decreased due the higher MRE achieved (see Fig. 1c).
494 Similarly, the lowest GHG emission was reached at the lowest $Q_{L:A}$ and the highest
495 temperature due to enhanced MRE under these conditions. However, since raising
496 temperature reduced the influent dissolved methane, the beneficial effects of reducing
497 $Q_{L:A}$ on energy output and GHG emission mitigations are significantly reduced as

498 temperature increases. Maximum energy recoveries of about 0.13 kWh per m³ of treated
499 water were achieved, which were similar to that reported by other authors. Specifically,
500 when operating PDMS DM units, Cookney *et al.* (2012; 2016) and Henares *et al.* (2017)
501 reported maximum energy recoveries of around 0.12 – 0.14 kWh per m³ of treated water.
502 Therefore, the results obtained in this study confirms that these promising results can also
503 be achieved in higher-scale plants.

504 Finally, the total energy recovery and GHG emissions of the combined system
505 (AnMBR+DM) were calculated (energy demands and GHG emissions of the AnMBR
506 prototype plant operated at the temperature ranging studied can be found in the Appendix
507 A, Fig. A1). As show in Figs. 7c and 7d, energy savings can be significantly improved by
508 coupling a DM unit for dissolved methane capture especially at low temperatures and
509 GHG emissions are drastically reduced by the recovery of high-GWP gas. The
510 AnMBR+DM system gave maximum energy recovery and minimum GHG emissions of
511 about 0.18 kWh and 0.070 kg of CO₂-eq per m³ of treated water, respectively in winter
512 (T = 11 °C) and maximum energy recovery of about 0.87 kWh and net GHG emission
513 reductions of up to 0.216 kg CO₂-eq per m³ of treated water in summer (T = 30 °C). Since
514 the average energy demand of conventional activated sludge (CAS) processes is about
515 0.36 kWh per m³ of treated water (Hao *et al.*, 2018), the AnMBR+DM system could be
516 considered as a promising alternative for UWW treatment, being able to recover a
517 significant amount of energy from UWW through the conversion of biodegradable
518 organic carbon into methane. On the other hand, considering an average GHG indirect
519 emissions factor of around 0.3–0.4 kg CO₂-eq per kWh of input energy (Emami *et al.*,
520 2018), indirect GHG emissions of 0.108 – 0.144 kg CO₂-eq per m³ of treated water could
521 be expected from CAS process. Moreover, other indirect GHG and direct GHG emissions
522 (N₂O and CH₄ gas) could significantly increase GHG emissions of CAS process

523 (Parravicini et al., 2016). Therefore, the combination of AnMBR with DMs represents an
524 interesting alternative to significantly reduce the GHG emissions of UWW treatment.
525 Indeed, making allowance of the evolution of climatic change worldwide, all countries
526 are developing new and more demanding GHG emissions policies to confront this crisis
527 (Eskander & Fankhauser, 2020). Unfortunately, the objectives established in the Paris
528 Agreement are not on track to be met (Rogelj et al., 2016), auguring that GHG emissions
529 for 2030 will be significantly higher than the ones required for the 2-°C stabilization path
530 estimated by the united nations (UNEP, 2019). In addition, finding sources of high quality
531 reclaimed water is also a prominent issue in worldwide policies (Jiménez-Benítez *et al.*,
532 2020). Therefore, considering the high quality effluent that AnMBR technology is able
533 to produce for possible water reclamation, and the high energy recovery and low GHG
534 emissions associated to this process after coupling a DM unit for dissolved methane
535 recovery, the combination of AnMBR with DM for UWW treatment may be considered
536 as an attractive option by regulators and policy makers, being able to provide important
537 environmental, economic and social benefits.

538 **4. CONCLUSIONS**

539 The effect of the operating temperature and the hydrodynamics on the performance of a
540 PDMS DM for capturing the dissolved methane from AnMBR effluents was evaluated.
541 Moreover, the energy demand and carbon footprint of the combined system
542 (AnMBR+DM) was assessed. The main findings were as follows:

- 543 • The DM unit showed a high potential for capturing the dissolved methane from
544 the AnMBR system. Dissolved methane recovery was maximized at low $Q_L:A$
545 ratios by the raise of the DM's HRT, achieving maximum methane capture

546 efficiencies of about 79 and 85% when operating at 11 and 30 °C, respectively.
547 Temperature could therefore be considered as not a limiter parameter for methane
548 capture from anaerobic effluents.

549 • The calculated resistance of the DM system to methane permeation showed that
550 K_O was improved at higher temperatures. This effect was attributed to improved
551 methane diffusivity in water and PDMS under these conditions. The
552 hydrodynamic analysis showed that the transition from laminar to turbulent flow
553 reduced K_O . Since short-term fouling propensity was negligible, this effect was
554 attributed to an increase in membrane fibers deformation as $Q_L:A$ was raised.

555 • A theoretical resistance-in-series model was proposed to predict K_O in the DM
556 module used in this study. Adequate predictions were reached under laminar
557 conditions while an empirical correction was suggested under turbulent conditions
558 to achieve properly predictions. According to the model, k_L would control mass
559 flux, representing up to 80-90% of total mass flux resistance.

560 • Using DMs for dissolved methane capture significantly increase energy savings
561 and reduce GHG emissions from AnMBRs. The AnMBR+DM system gave net
562 energy productions and GHG emissions of about 0.18 kWh and 0.070 kg of CO₂-
563 eq per m³ of treated water, respectively, when operating at 11 °C. Net energy
564 productions of about 0.86 kWh and net GHG reductions of up to 0.216 kg CO₂-
565 eq per m³ of treated were achieved when operating at 30 °C.

566 Based on the results achieved in this study, the use of AnMBR technology assisted by
567 PDMS DMs could be considered as a potential alternative for UWW treatment.
568 Nonetheless, important aspects need to be refined before their full-scale implementation,
569 requiring further research:

- 570 • Due to the negative effects observed on K_O when increasing $Q_L:A$, further studies
571 focused on improving DM's hydrodynamics and increasing DM's HRT are
572 suggested in order to improve the methane capture effectivity. Different module
573 configurations, membrane materials or multi-layer membranes could represent
574 interesting options to be evaluated.
- 575 • Since only some hydrodynamic characteristics of the DM module were considered
576 to model K_O , future research considering other DM configurations should be
577 performed to evaluate the viability of the proposed model or to develop advanced
578 models.
- 579 • Due to the low $Q_L:A$ ratios required to maximize the dissolved methane recovery,
580 important economic investments could be expected for the DM unit, although they
581 could be partially counterbalanced by the increased energy recovery and reduced
582 GHG emissions. Therefore, further studies considering all the economic aspects
583 of the proposed alternative as well as deeper environmental evaluations (i.e. life
584 cycle cost and life cycle assessment studies) need to be performed to determine
585 the actual suitability of the AnMBR+DM alternative for UWW treatment.

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Nomenclature

A	Fitting parameter of Himmelblau's equation
a	Fitting parameter of the linear equation proposed in this study to correct the liquid phase mass transfer coefficient under turbulent conditions
A_M	Membrane area
A_G	Effective membrane area interacting with the gas phase
A_L	Effective membrane area interacting with the liquid phase
A_{ml}	Logarithmic mean area of the degassing membrane
AnMBR	Anaerobic membrane bioreactor
B	Fitting parameter of Himmelblau's equation
b	Fitting parameter of the linear equation proposed in this study to correct the liquid phase mass transfer coefficient under turbulent conditions
c	Concentration of the diffused compound
c_{CH_4}	Dissolved methane concentration in the water
c_{CH_4-inf}	Concentration of dissolved methane in the influent membrane stream
c_{CH_4-eff}	Concentration of dissolved methane in the effluent membrane stream
c_G	Methane concentration in the gas phase
$c^*_{CH_4}$	Membrane-gas interphase methane concentration
D	Diffusion coefficient
D_{CH_4-PDMS}	Methane diffusivity in polydimethylsiloxane
D_{CH_4-W}	Methane diffusivity in water
D_{eq}	Equivalent diameter
DM	Degassing membrane
E_P	Fitting parameter of Van't Hoff–Arrhenius's equation
GHG	Greenhouse gas
$H^{CH_4}(T)$	Henry's constant for methane
J	Flux of the diffused compound
J_{CH_4}	Permeated methane flux
k_G	Mass transfer coefficient of the recovered gas in the gas phase
k_L	Mass transfer coefficient of the recovered gas in the liquid phase
k_M	Mass transfer coefficient of the recovered gas in the permeable membrane
K_O	Overall mass transfer coefficient of the system

L_w	Wet fiber length
MRE	methane recovery efficiency
P	Permeability
P_{CH_4-PDMS}	Methane permeability in polydimethylsiloxane
PDMS	Polydimethylsiloxane
P_0	Fitting parameter of Van't Hoff–Arrhenius's equation
Q_L	Liquid flow rate
$Q_{L:A}$	Liquid flow rate to membrane area
R	Universal constant of gases
Re	Reynolds module
R_G	Gas boundary layer resistance
R_L	Liquid boundary layer resistance
R_M	Permeable non-porous membrane resistance
R_T	Total mass flux resistance
S	Solubility coefficient
Sc	Schmidt dimensionless module
S_{CH_4-PDMS}	Methane solubility in polydimethylsiloxane
Sh	Sherwood dimensionless module
T	Temperature
TC	Total carbon
TIC	Total inorganic carbon
t_L	Thickness of the liquid phase resistance
t_M	Membrane thickness
TOC	Total organic carbon
UWW	Urban wastewater
V_{cd}	Cylindrical diffuser volume
V_S	Shell volume
v_L	Liquid velocity
x	Distance between two points
Greek Letters	
μ	Liquid viscosity

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768 **Table and Figure captions**

769 **Table 1.** DM influent and effluent characteristics according to applied $Q_L:A$ ratio (11 °C operating
770 temperature).

771 **Fig. 1.** Methane recovery for the operating conditions studied: (a) Recovered methane flux for a $Q_L:A$
772 ranging from 22 to 118 $Lh^{-1}m^{-2}$, (b) Recovered methane flux for a $Q_L:A$ ranging from 142 to 190 $Lh^{-1}m^{-2}$
773 and (c) Methane recovery efficiency. \square $Q_L:A$ of 22 $Lh^{-1}m^{-2}$; \diamond $Q_L:A$ of 46 $Lh^{-1}m^{-2}$; \triangle $Q_L:A$ of 70 $Lh^{-1}m^{-2}$;
774 \times $Q_L:A$ of 94 $Lh^{-1}m^{-2}$; $-$ $Q_L:A$ of 118 $Lh^{-1}m^{-2}$; \circ $Q_L:A$ of 142 $Lh^{-1}m^{-2}$; $+$ $Q_L:A$ of 166 $Lh^{-1}m^{-2}$; \times $Q_L:A$
775 of 190 $Lh^{-1}m^{-2}$.

776 **Fig. 2.** Influence of temperature and hydrodynamics on the overall mass transfer coefficient (K_o). Influence
777 of: (a) Q_L and v_L , and (b) Reynolds number.

778 **Fig. 3.** Effect of DM operating time and $Q_L:A$ ratio on membrane fouling (11 °C operating temperature).

779 **Fig. 4.** Model validation at $Q_L:A$ of: (a) 22, (b) 46, (c) 70, (d) 94, (e) 118, (f) 142, (g) 166 and (h) 190 $L h^{-1}$
780 m^{-2} . Experimental results shown by dots and model predictions by continuous lines.

781 **Fig. 5.** Fitting parameters of the model as a function of $Q_L:A$ ratio: (a) A and B parameters (*eq. 10*), (b) P_0 ,
782 E_P and t_L parameters (*eq. 10*) and (c) a and b parameters (*eq. 17*). Dotted lines show a linear fit.

783 **Fig. 6.** Evolution of the liquid, membrane and overall mass transfer coefficient calculated from the proposed
784 theoretical model according to temperature and $Q_L:A$ ratio.

785 **Fig. 7.** Influence of temperature and $Q_L:A$ ratio on: (a) DM energy demand, (b) DM GHG emissions, (c)
786 DM+AnMBR system energy demand and (d) DM+AnMBR system GHG emissions. \square $Q_L:A$ of 22 $Lh^{-1}m^{-2}$;
787 \diamond $Q_L:A$ of 46 $Lh^{-1}m^{-2}$; \triangle $Q_L:A$ of 70 $Lh^{-1}m^{-2}$; \times $Q_L:A$ of 94 $Lh^{-1}m^{-2}$; $-$ $Q_L:A$ of 118 $Lh^{-1}m^{-2}$; \circ
788 $Q_L:A$ of 142 $Lh^{-1}m^{-2}$; $+$ $Q_L:A$ of 166 $Lh^{-1}m^{-2}$; \times $Q_L:A$ of 190 $Lh^{-1}m^{-2}$.

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796 **Table 1.** DM influent and effluent characteristics according to applied $Q_L:A$ ratio (11 °C operating
 797 temperature).

Stream	$Q_L:A$ ($Lh^{-1}m^{-2}$)	pH	NH_4^+-N ($mgN L^{-1}$)	$PO_4^{3-}-P$ ($mgP L^{-1}$)	TIC ($mgC L^{-1}$)	TOC* ($mgC L^{-1}$)
Influent	-	7.1 ± 0.3	54.5 ± 0.4	5.0 ± 0.3	273.7 ± 54	64.4 ± 9
	25	7.5 ± 0.2	55.8 ± 1.8	5.5 ± 0.1	268.1 ± 43	54.5 ± 12
	50	7.8 ± 0.3	54.3 ± 0.1	5.2 ± 0.2	n.a.	n.a.
Effluent	95	7.7 ± 0.2	51.9 ± 0.3	4.6 ± 0.3	268.8 ± 61	59.2 ± 15
	140	7.7 ± 0.2	52.0 ± 0.4	5.6 ± 0.7	n.a.	n.a.
	190	7.6 ± 0.3	51.4 ± 1.1	4.8 ± 0.5	268.7 ± 22	57.4 ± 8

798 *TOC concentration excluding dissolved methane.

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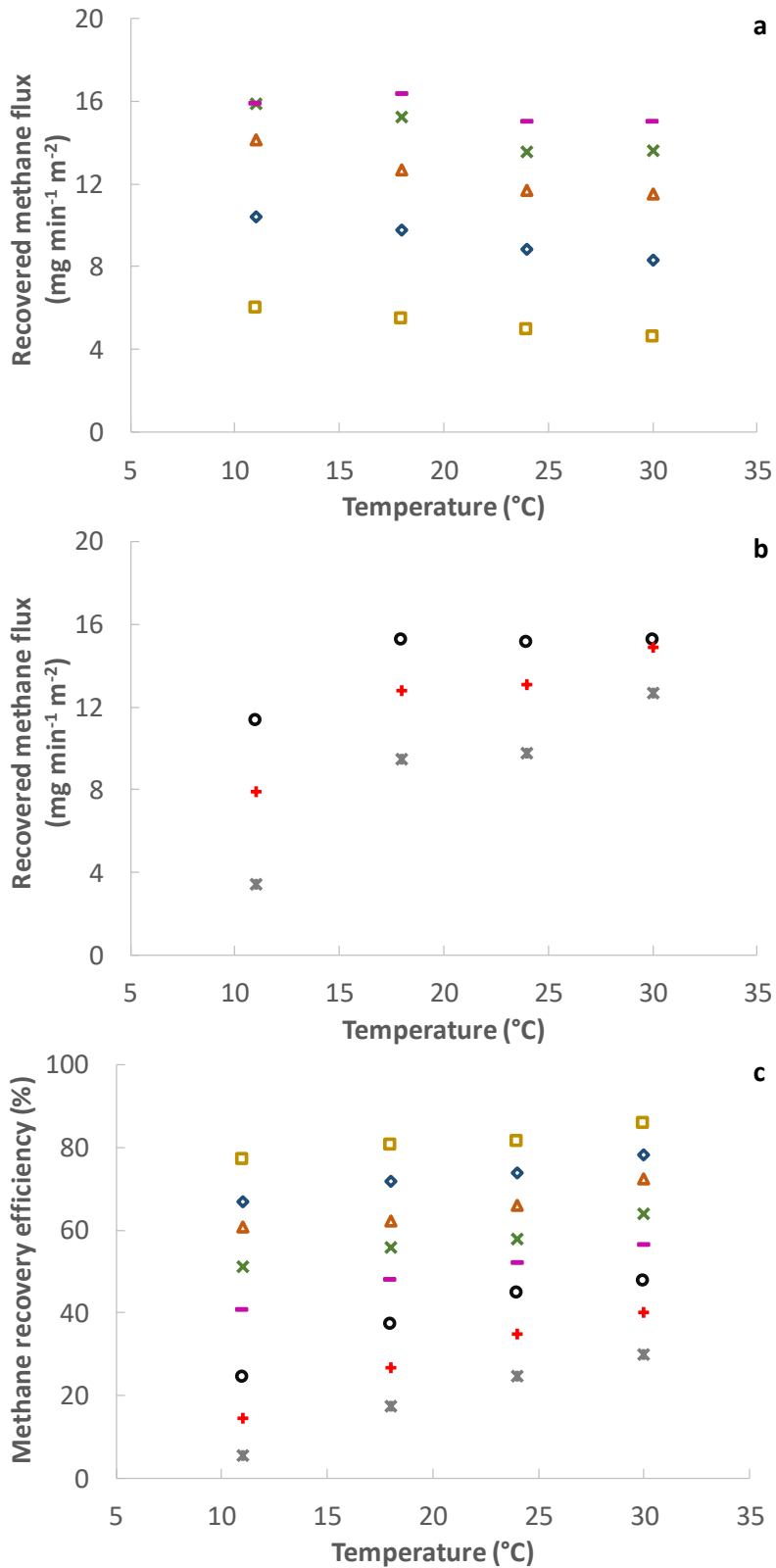
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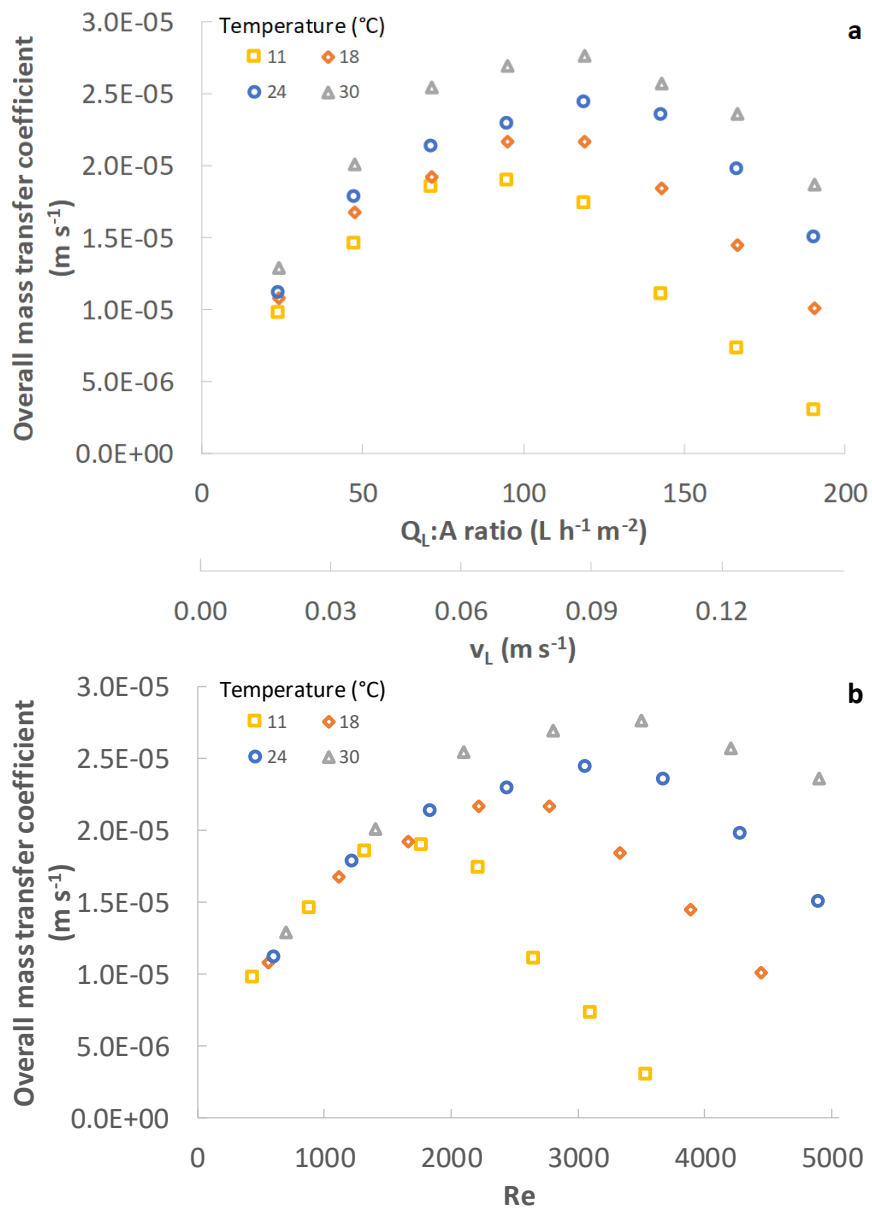
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Fig. 1. Methane recovery for the operating conditions studied: (a) Recovered methane flux for a Q_L:A ranging from 22 to 118 Lh⁻¹m⁻², (b) Recovered methane flux for a Q_L:A ranging from 142 to 190 Lh⁻¹m⁻² and (c) Methane recovery efficiency. \square Q_L:A of 22 Lh⁻¹m⁻²; \diamond Q_L:A of 46 Lh⁻¹m⁻²; \triangle Q_L:A of 70 Lh⁻¹m⁻²; \times Q_L:A of 94 Lh⁻¹m⁻²; $-$ Q_L:A of 118 Lh⁻¹m⁻²; \circ Q_L:A of 142 Lh⁻¹m⁻²; $+$ Q_L:A of 166 Lh⁻¹m⁻²; \times Q_L:A of 190 Lh⁻¹m⁻².



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Fig. 2. Influence of temperature and hydrodynamics on the overall mass transfer coefficient (K_o).

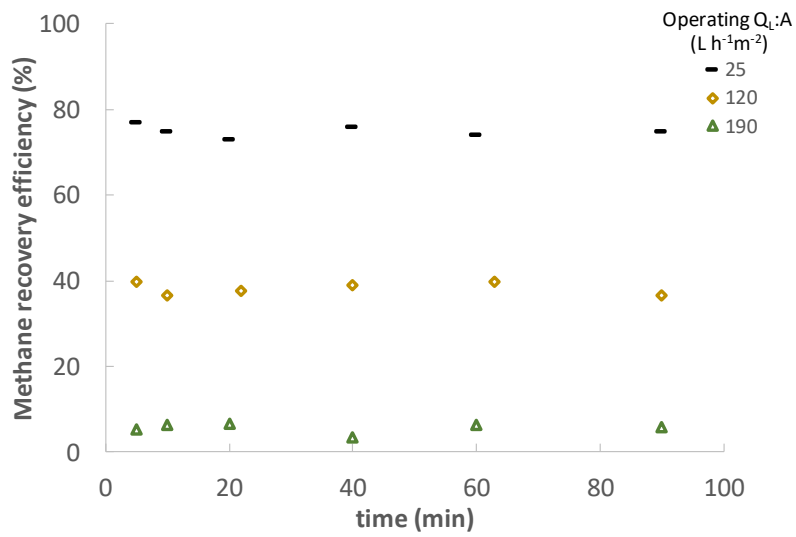
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Influence of: (a) Q_L and v_L , and (b) Reynolds number.

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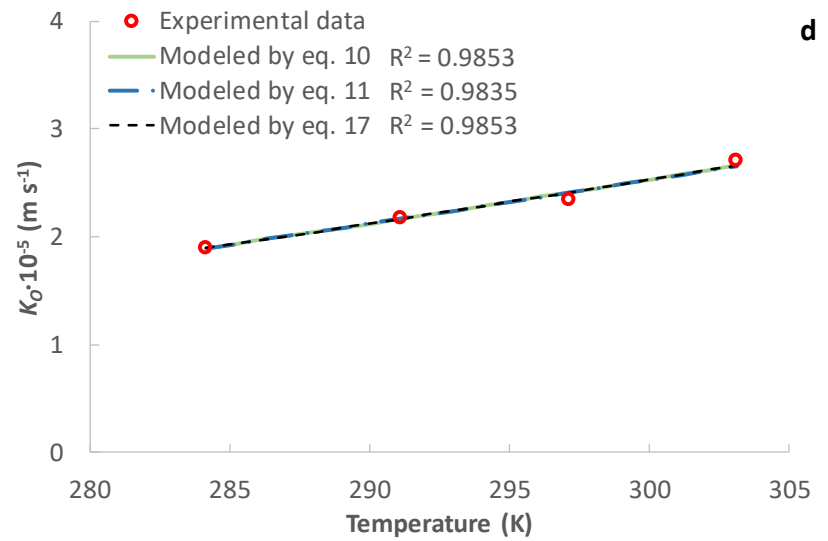
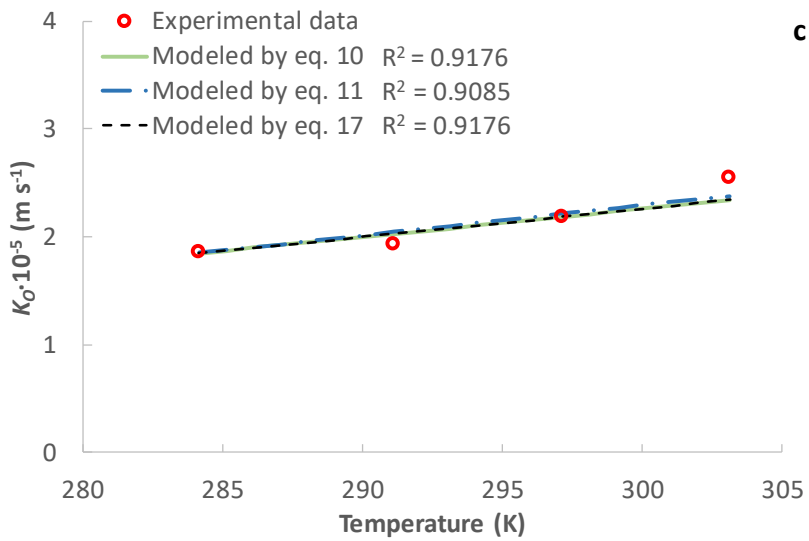
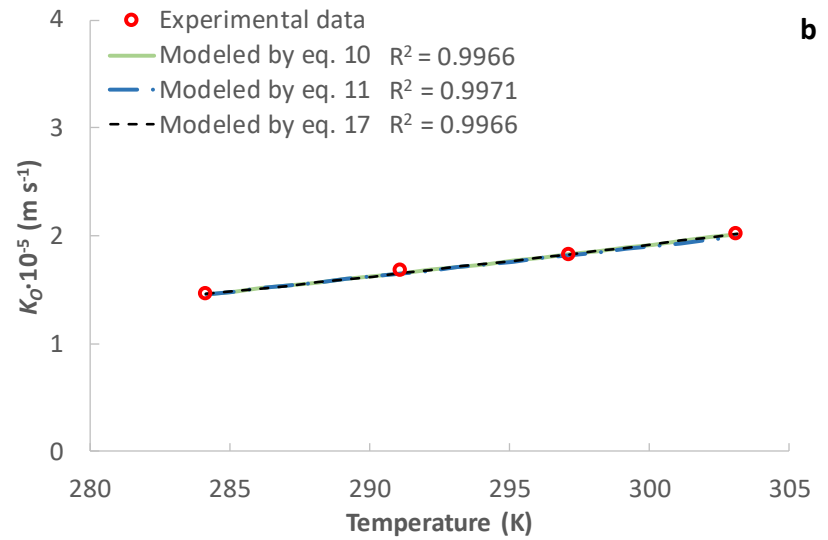
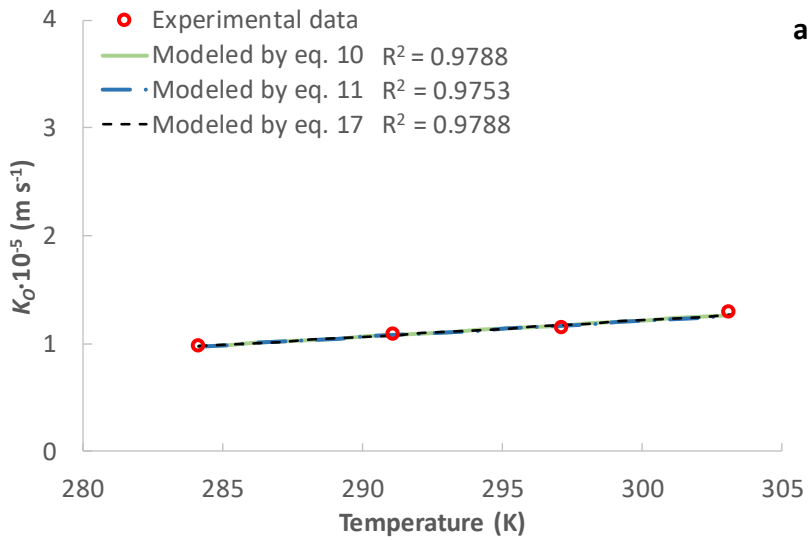
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Fig. 3. Effect of DM operating time and $Q_L:A$ ratio on membrane fouling (11 °C operating temperature).



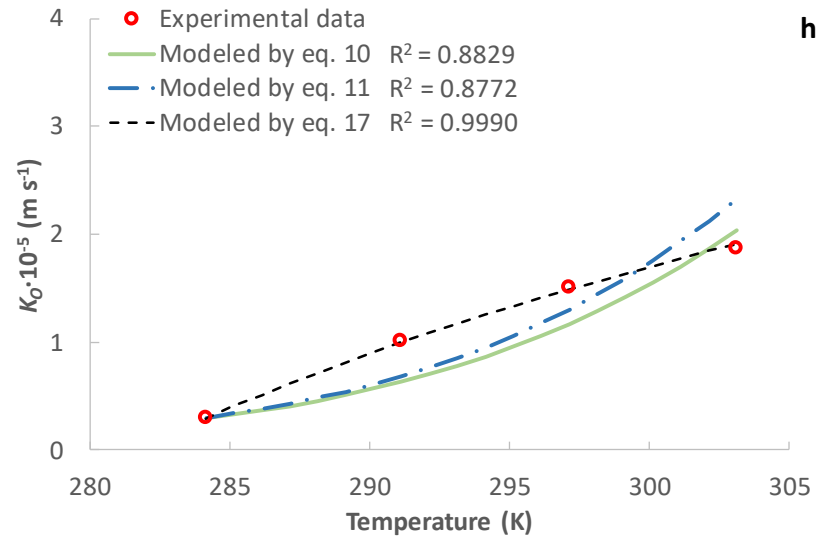
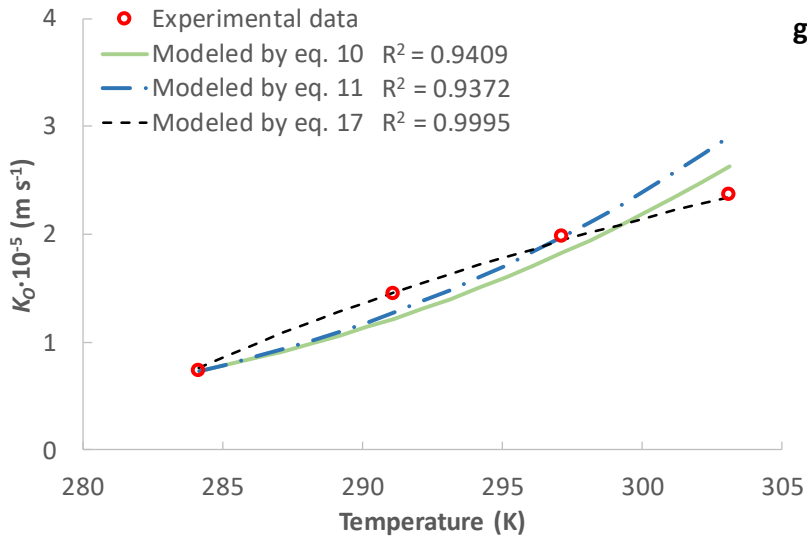
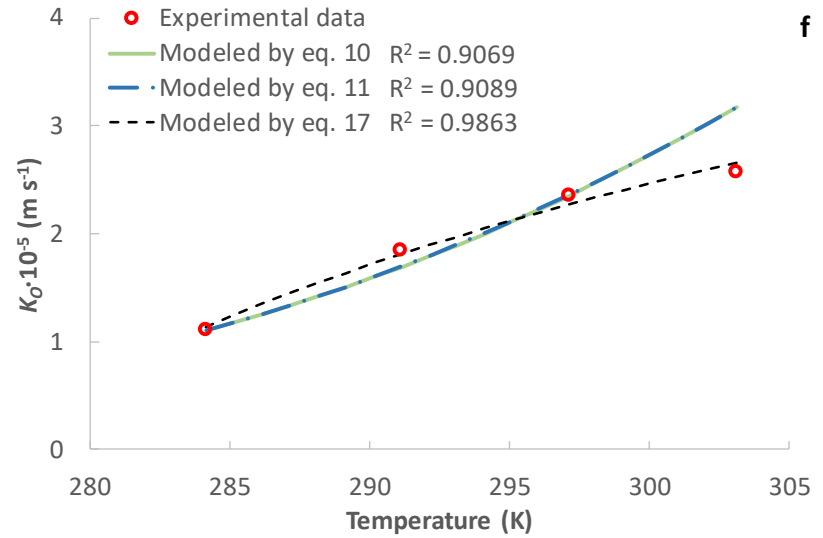
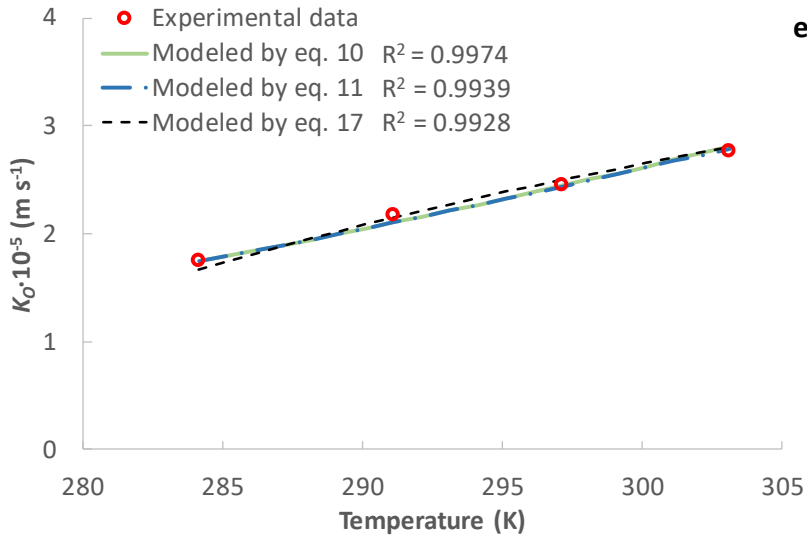
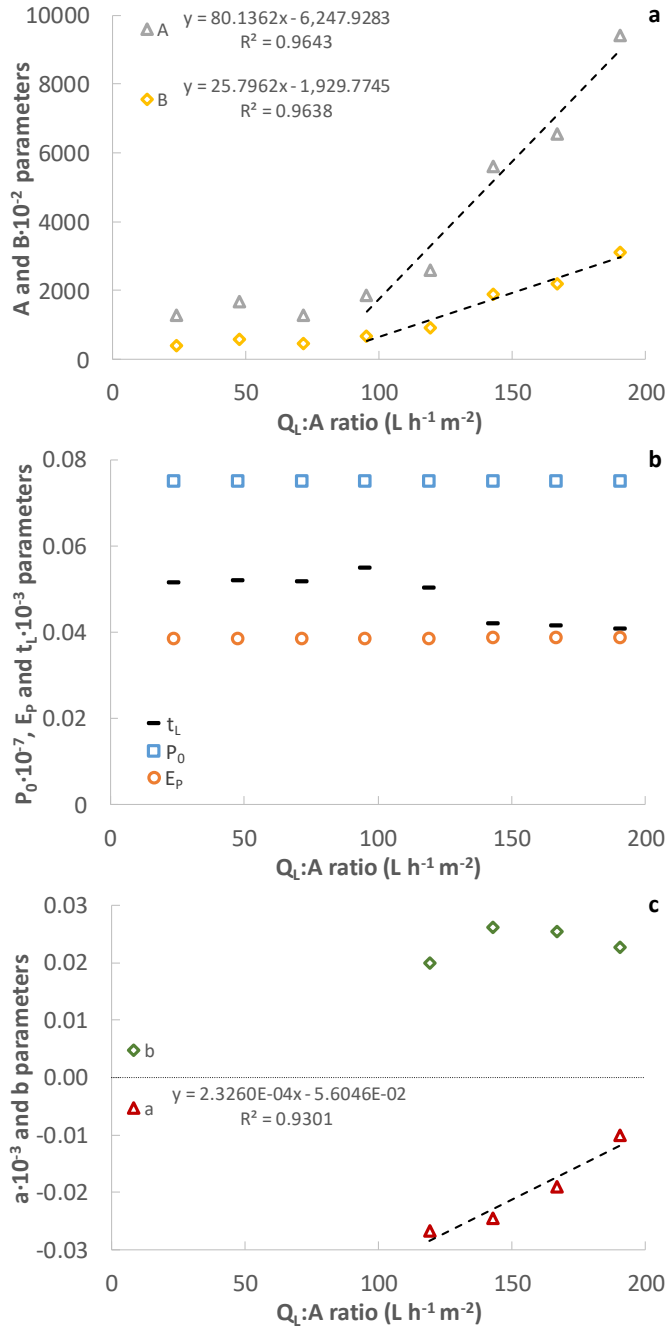


Fig. 4. Model validation at $Q_L:A$ of: (a) 22, (b) 46, (c) 70, (d) 94, (e) 118, (f) 142, (g) 166 and (h) 190 $L h^{-1} m^{-2}$. Experimental results shown by dots and model predictions by continuous lines.



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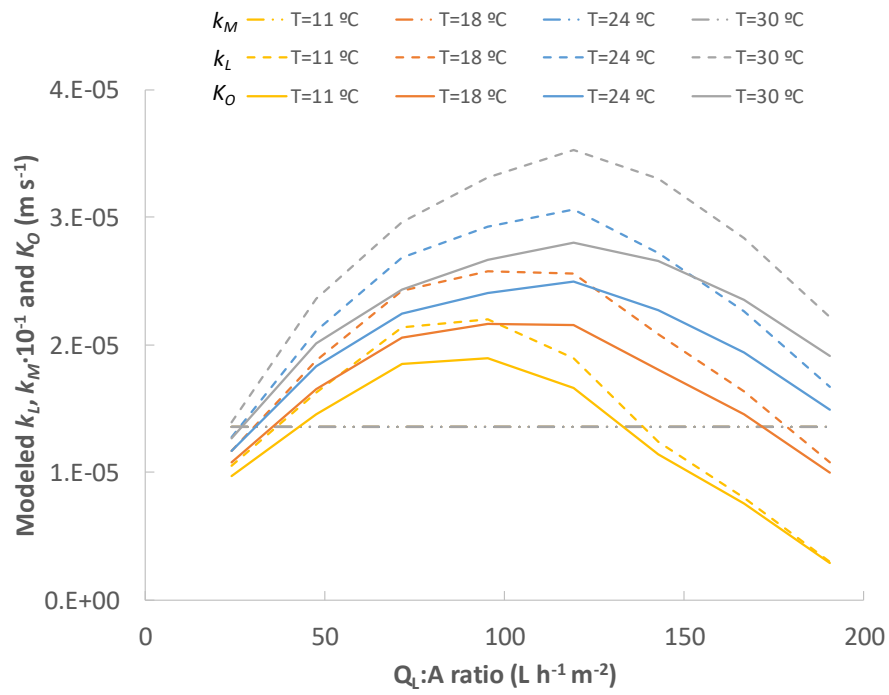
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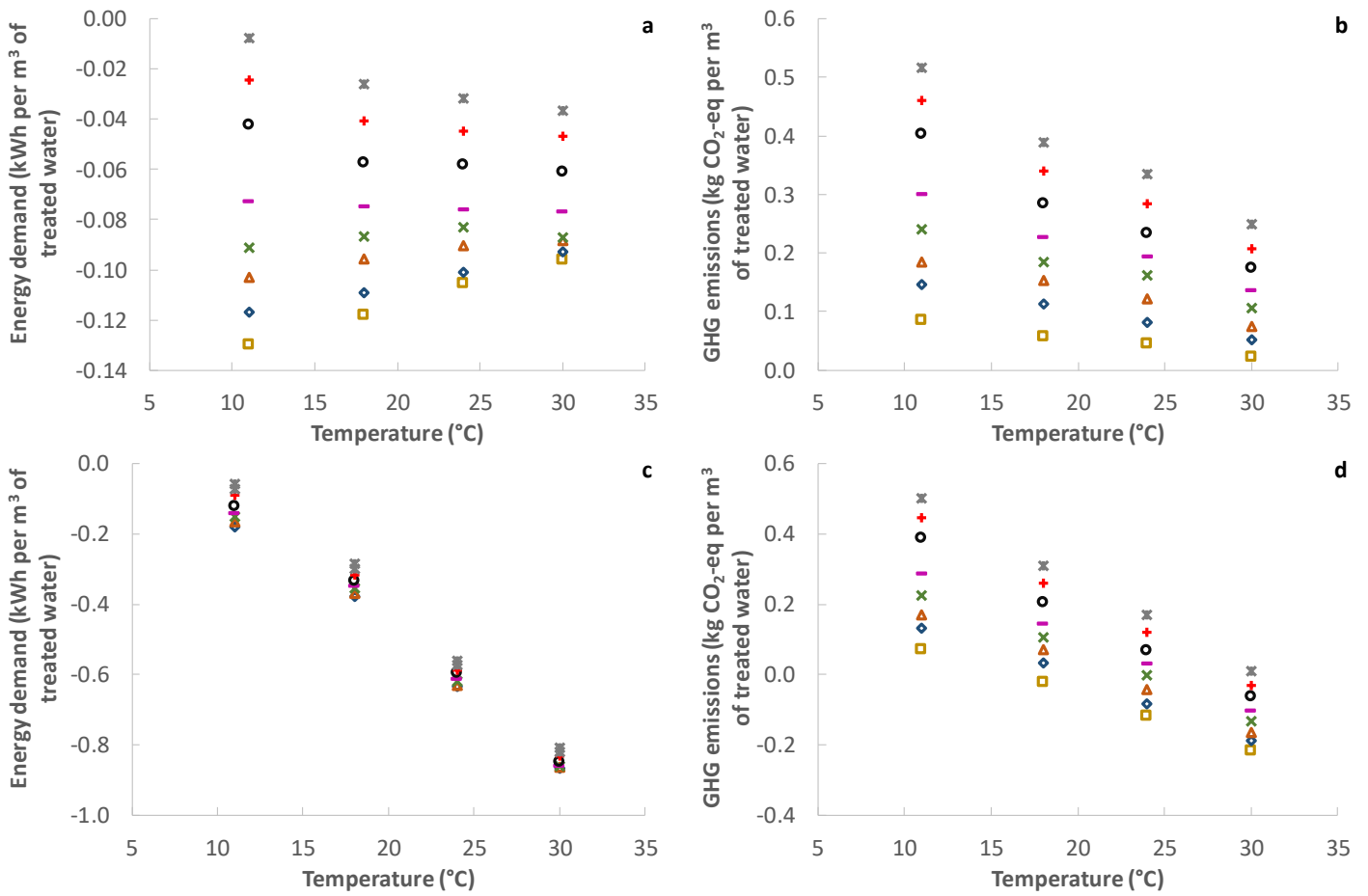
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