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Additional Information

# Study of two dimensional oscillations using a smartphone acceleration sensor: Example of Lissajous curves

Luis Tuset-Sanchis,<sup>†</sup> Juan C. Castro-Palacio ,<sup>‡</sup> José A. Gómez-Tejedor,<sup>¶</sup> Francisco J. Manjón,<sup>§</sup> and Juan A. Monsoriu<sup>\*,||</sup>

*†Escuela Técnica Superior de Ingeniería del Diseño, Camí de Vera s/n, 46022, València,* Spain.

<sup>‡</sup>Department of Chemistry, University of Basel. Klingelbergstrasse 80, CH-4056 Basel, Switzerland.

¶Centro de Biomateriales e Ingeniería Tisular, Universitat Politècnica de València, Camí de Vera s/n, 46022, València, Spain.

§Instituto de Diseño y Fabricación, Universitat Politècnica de València, Camí de Vera s/n, 46022, València, Spain.

|| Centro de Tecnologías Físicas, Universitat Politècnica de València, Camí de Vera s/n, 46022, València, Spain.

E-mail: jmonsori@fis.upv.es

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#### Abstract

The smartphone acceleration sensor is used to study two-dimensional harmonic oscillations. The data recorded by the free Accelerometer Toy Android application is used to determine the periods of oscillation by graphical analysis. Different patterns of the Lissajous curves resulting from the superposition of harmonic motions are illustrated for three experiments. This work introduces an example of how two-dimensional oscillations can be easily studied with a smartphone acceleration sensor.

## 1 Introduction

Many experiments using portable devices in Physics teaching have been recently reported in the literature. Digital cameras,<sup>1</sup> webcams,<sup>2</sup> optical mouse of computers,<sup>3,4</sup> wiimote,<sup>5</sup> and other game console controllers<sup>6</sup> have been included. For instance, by using a simple digital camera,<sup>7,8</sup> a physics experiment can be followed. The recorded videos allow to measure time, distances and positions of objects.

The use of portable devices has been recently extended to the smarphones. Particularly, the acceleration sensor incorporated to the smartphones has been used for the study of single and coupled oscillations at both qualitative and quantitative levels in high schools,<sup>9,10</sup> and in universities,<sup>11,12</sup> respectively. In this work, we extend the use of the smartphone acceleration sensor to the study two-dimensional oscillations.

In fact, most of oscillations in student's everyday life and modern technology are more than one-dimensional. This is a major reason to include two-dimensional oscillation examples in Physics teaching and taking advantage of the possibilities provided by the smartphone acceleration sensor which is a common device of daily use by the students. As an amenable example, we have chosen the study of the Lissajous curves. Several works on Lissajous curves and Physics teaching have been reported in the literature.<sup>13,14</sup> For example, Lissajous curves are used to determine the frequency of a signal by combining them with another signal of known frequency.

So far, the study of two-dimensional oscillations is carried out using somehow tedious experiments. For example, in reference<sup>17</sup> authors use an air table and a puck connected to it by springs. The trajectory of the puck was followed by the trace described by it on a paper, which is later digitalized to extract the information of the trajectory, that is, x(t) and y(t). The introduction of the smartphone acceleration sensor in measuring two- and three- dimensional oscillations represents a major progress in this respect since the instantaneous values of the acceleration are registered by the sensor along its three perpendicular axes. As to the knowledge of the authors, this is the first work on two-dimensional oscillations using the smartphone acceleration sensor.

The outline of the paper is the following. In section II we describe the smartphone acceleration sensor and one of its free Android applications: Accelerometer Toy. In section III, we describe the experimental setup. In section IV, three different arrangements of two-dimensional oscillations are described. In the second and third of these experiments, the resulting mechanical Lissajous curves are shown. Finally, in section VI, some conclusions are drawn.

# 2 The smartphone acceleration sensor and Android application

In our experiments we used the smartphone models Samsung Galaxy S2 with Android 2.1 and LG-E510 with Android version 2.3.4. The mass of the first smartphone is  $(0.1237 \pm 0.0001)$  kg and of the second  $(0.1350 \pm 0.0001)$  kg. The accelerometer sensor is based on three mutually perpendicular silicon circuits, each one oscillating in one direction as a ball hanging on a spring whose movement is restricted to one direction. For the control of the accelerometer sensor the free Android application "Accelerometer Toy ver 1.0.10" is used. This application takes 154 kB of memory and can be downloaded from Google play website.<sup>18</sup> The acceleration components  $a_x$ ,  $a_y$  and  $a_z$ on x, y and z - axes, respectively as a function of time are registered by the sensor. The precision in the measurement of the acceleration and time are  $\delta a = 0.03 \text{ m/s}^2$  and  $\delta t = 0.01 \text{ s}$ , respectively. This application also allows saving the output data to an ASCII file for further analysis. The structure of the ASCII file (Figure 1) is the following. The first column is the order number of the time iteration, the second is the time in miliseconds, and the remaining three columns are the acceleration in x, y and z axes (in m/s<sup>2</sup>), respectively. Once the application is downloaded to the mobile device, a small test can be performed to proof correct working. It can be proved that when the mobile is left quiet on a horizontal surface, the output curves for the acceleration exhibit values very close to zero for x- and y- axes and  $\sim 9.8 \text{ m/s}^2$  for z- axis.

Count	Time	(ms) X	Y	Z
1	0	0,21793	0,14982	9,83469
2	9	0,21793	0,12258	9,74494
3	19	0,17707	0,12258	9,86034
4	29	0,14982	0,12258	9,92445
5	39	0,1362	0,12258	9,86034
6	49	0,17707	0,10896	9,75776
7	59	0,1362	0,12258	9,73211
8	71	0,14982	0,08172	9,80905
9	82	0,14982	0,0681	9,74494
10	92	0,2043	0,04086	9,83469
11	105	0,23155	0,01362	9,83469
12	118	0,21793	0,01362	9,86034
13	126	0,24517	0,01362	9,82187
14	136	0,21793	-0,02724	9,86034
15	147	0,2043	-0,04086	9,80905
16	157	0,2043	-0,05448	9,80905
17	167	0,17707	-0,0681	9,73211
18	177	0,16344	-0,05448	9,69365
19	188	0,10896	-0,09534	9,80905
20	198	0,0681	-0,08172	9,77058
21	208	-0,02724	-0,08172	9,83469
22	218	-0,02724	-0,09534	9,83469
23	228	-0,05448	-0,08172	9,73211

Figure 1: Fragment of the output file of the Accerelometer Toy Android application used for the experiments.

# 3 Experimental setup

The experimental setup includes an air table, a tray to carry the smartphone and four springs. Three arrangements of the springs are used. The table was made up of aluminium with an approximate total cost of  $\sim 40$  euros. The socket for the air supply of this table allows the coupling to conventional air suppliers included in the air tracks kits for basic Physics laboratories. On the other hand, the fact that the experiments can be performed with the students' smartphones makes them more feasible and attractive.

The set-up used for the experiments is shown in Figure 2. The dimensions of the air table and the tray carrying the smartphone are also included. The table is coupled to an air supplier. When the air supplier is on, a thin layer of higher pressure air appear between the tray with the smartphone and the surface on the table allowing the tray to move with almost no friction in two-dimensions. These conditions allow us to study two-dimensional harmonic oscillations by obtaining mechanical Lissajous curves.

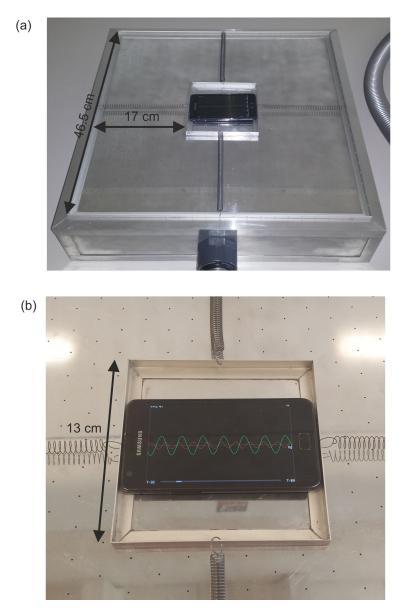


Figure 2: Experimental set-up used for the experiments. In panel (a) a global view of the squared air table is shown. In panel b, the detail of the smartphone and the carrying squared tray are shown. The dimensions of the air table and the tray are indicated on the picture.

# 4 Two dimensional experiments

#### 4.1 Experiment 1

In the following experiment four springs of  $(10.5 \pm 0.1)$  N/m are used, two per each of the x- and y- axes. The mass of the smartphone and the tray together is  $(0.1583 \pm 0.0001)$  kg. After a diagonal shift along y = x curve, the smartphone starts oscillating approximately along this curve. In Figure 3 (panel a) the oscillations of the acceleration along x- and y- axes are shown. The resulting oscillation periods measured directly from the recorded data are in Table 1. In panel b, the curve resulting from the superposition of both harmonic motions is shown. It can be noticed that is almost a straight line, indicating the great similarity in the conditions of oscillations of both axes  $(T_x/T_y \simeq 1)$ .

		$T \pm 0.01$
Experiment 1	х	0.48
	у	0.48
Experiment 2	х	0.27
	У	0.40
Experiment 3	х	0.24
	у	0.33

Table 1: Periods of oscillation from the graphical analysis of the recorded data.

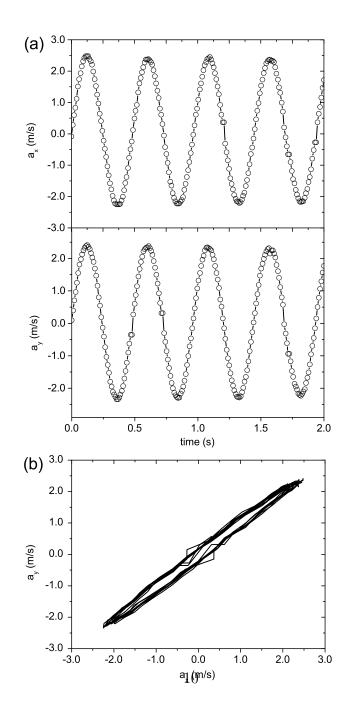


Figure 3: Results for the experiment 1 of the acceleration versus time on the x- and y- axes

#### 4.2 Experiment 2

In the next experiment two springs of  $(46.9 \pm 0.7)$  N/m are used along the x- axis and two of  $(10.5 \pm 0.1)$  N/m along the y- axis. The mass of the smartphone and the tray together is  $(0.1583 \pm 0.0001)$ kg. After a diagonal shift along y = x curve, the system starts oscillating. In Figure 4 (panel a) the oscillations of the acceleration along x and y axes are shown. The periods from the acceleration data are shown in Table 1. In Figure 4 panel b, the curve resulting from the superposition of both harmonic motions is shown. The Lissajous curve corresponding to a ratio between the periods of  $T_x/T_y=0.6752$  $\simeq 2/3$  is shown.

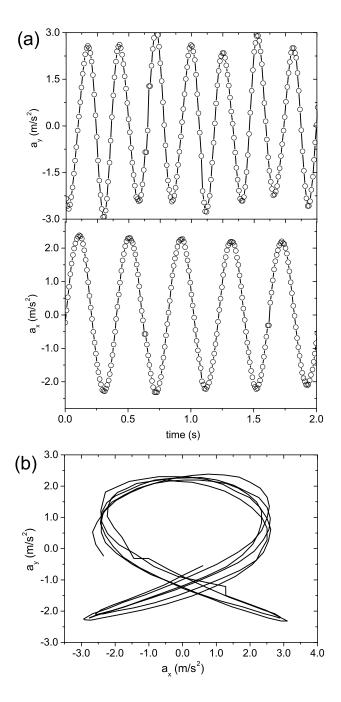


Figure 4: Results for the experiment 2 of the acceleration *versus* time on the x- and y- axes are shown in panel a, and the Lissajous curve from  $a_y = f(a_x)$  in panel b.

#### 4.3 Experiment 3

Finally, in this experiment two springs of  $(20.6 \pm 0.1)$  N/m are used along the x- axis and, two of  $(79.6 \pm 0.7)$  N/m along the y- axis. The mass of the smartphone changes with respect to previous experiments and along with the carrying tray is  $(0.2145 \pm 0.0001)$  kg. A diagonal shift along y = x curve is performed and the system starts oscillating. In Figure 5 panel a, the oscillations of the acceleration along x and y axes are shown. The periods from the acceleration data are shown in Table 1. In Figure 5, panel b, the Lissajous curve corresponding to a ratio between the periods of,  $T_x/T_y = 0.727 \simeq$ 8/11 is shown.

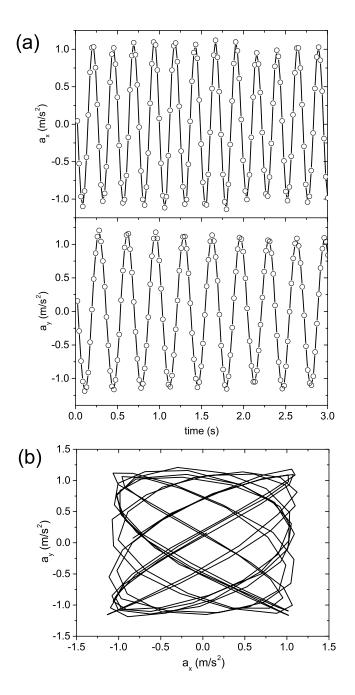


Figure 5: Results for the experiment 3 of the acceleration versus time on the x- and y- axes are shown in panel a, and the Lissajous curve from  $a_y = f(a_x)$  in panel b.

The resulting periods in experiments 2 and 3 differ slightly from the theoretical values expected for small oscillations of a body connected to two springs on single axis,  $T = 2\pi \sqrt{m/k}$ . The springs connected to the body along the perpendicular axis, make influence on these oscillations since components of the elastic force appear on the oscillation direction. This is more stressed the greater is the amplitude of the oscillation. This influences the results in the fact that an effective force constant which is greater than the initial one appears. On the other hand, the resulting frequencies are larger than the expected ones from the theory. The experimental Lissajous curves resulting from experiments 2 and 3 can be tested against the theoretical results (see Figure 6) for  $T_x/T_y \simeq 2/3$  and  $T_x/T_y \simeq 8/11$  respectively (see the virtual laboratory implemented in reference<sup>19</sup>).

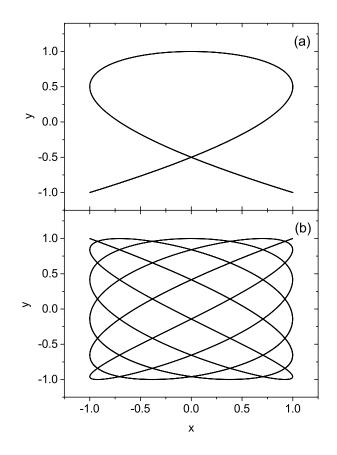


Figure 6: Theoretical Lissajous curves for  $T_x/T_y = 2/3$  in panel a and  $T_x/T_y = 8/11$  in panel b. In both cases an amplitude of 1 arbitrary unit has been considered. The phase difference between x and y oscillations is 0 degrees.

# 5 Conclusions

Two-dimensional harmonic oscillations are studied using an air table and a smartphone acceleration sensor. The instantaneous acceleration data recorded by the sensor are plotted to obtain the periods of oscillation in x- and y- axes. From the data of the harmonic oscillations, Lissajous curves are obtained for a ratio of the periods  $T_x/T_y$  of ~ 2/3 and ~ 8/11, for the second and third experiment, respectively. A very good agreement is obtained between theoretical and experimental results. It is very remarkable the progress that the use of smartphone acceleration sensor represents in the study of two-dimensional oscillations in an easier way than in previous works. Moreover, it is an interesting way to extend the use of the smartphones, a very familiar device for the students, beyond the standard use for communication. We think that Physics concepts whenever linked to popular aspects of the students' everyday life have a clear positive impact on motivation.

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