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Additional Information

# Performance evaluation of a waste heat driven adsorption system for automotive air-conditioning: Part I - Modelling and experimental validation

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## **ABSTRACT**

Adsorption systems driven by engine waste heat are one of the possible alternatives to the conventional automobile air conditioning in terms of energy savings and environmental issues. Assessment of this issue are carried in a two-part study. In this first part I, theoretical and experimental investigations were performed on a two bed, silica gel adsorption chiller for automotive applications. A prototype adsorption system with a total weight of about 86 kg was developed and tested to driven by low-grade waste heat. The single adsorbent bed consisted of three plate-fin heat exchangers connected in parallel. An improved non-equilibrium lumped parameter model was developed to predict the transient performance of the system. The model is fully dynamic and takes into account the mass transfer resistance and pressure drop for each component of the system. The results showed that the model is able to accurately predict the dynamic performance of the system under different operating conditions and configuration modes with a short calculation time. The tested chiller was able to produce an average cooling capacity of about 2.1 kW with a COP of 0.35 at the rated operating conditions. Heat recovery system results in increasing the COP by 43% and the cooling power by 4%.

**Keywords:** Modelling and simulation, Silica-gel, Waste heat recovery, Automotive A/C system, Adsorption chiller.

Nomenclat				
A	area, m <sup>2</sup>	evap	evaporator	
COP	coefficient of performance	HE	heat exchanger	
$C_p$	specific heat, Jkg <sup>-1</sup> k- <sup>1</sup>	i	inlet	
m	mass, kg	1	liquid	
$M_{ads,b}$	total mass of dry adsorbent packed in each bed, kg	out	outlet	
ṁ	mass flow rate, kgs <sup>-1</sup>	Port,i	inlet port	
P	pressure, mbar	Port,o	outlet port	
R	universal gas constant, mbar m³kg-1K-1	sec	secondary	
T	temperature, k	tot	total	
$T_{wi}$	water temperature at the inlet of the bed, K	tot	total	
$T_{wi,HE}$	water temperature at the inlet of the heat exchanger, K	W	water	
$T_{wo}$	water temperature at the outlet of the bed, K	W	uptake, kgkg <sup>-1</sup>	
$T_{wo,HE}$	water temperature at the outlet of the heat exchanger, K	Greek Letters		
$UA_{tot,HE}$	overall thermal conductance of the adsorbent heat exchanger, WK <sup>-1</sup>	ρ	density, kgm <sup>-3</sup>	
V	volume, m <sup>3</sup>	3	effectiveness	
w	uptake, kgkg <sup>-1</sup>	$\Delta h_{\text{ad}}$	enthalpy of adsorption, Jkg-1	
Subscripts		$\tau_{\mathrm{cycle}}$	full cycle time [s]	
b	bed	tot	total	
chill	chilled water	tot	total	
cond	condenser	w	water	
des	desorption	w	uptake, kgkg <sup>-1</sup>	
eq	equilibrium	tot	total	

#### 1 Introduction

Energy savings and environment friendly applications are becoming one of the important topics nowadays due to the rapid population growth and increase in the standard of living. Hazardous gases from automobiles exhausts and chemically synthetic refrigerants used in the conventional vapor-compression refrigeration cycles (VCRC) are the major pollutants of our environment [1]. In addition, transport is considered the major user of primary energy and burns most of the world petroleum. The most widely method for refrigeration and air conditioning systems in different applications is employing VCRC due to its high COP [2, 3]. However, the use of these systems cause a considerable high-grade energy consumption and environmental pollution. This conflicts the concept of sustainable development. Additionally, the negative impacts of VCRS become more pronounced in automotive and transportation applications where the compressor is powered by mechanical energy from the internal combustion engine.

Thermally driven adsorption cooling systems (ACS) use natural working fluids (such as water) and have the ability to be driven by low grade thermal energy such as solar energy and waste heat from automobile engines [4]. They can be considered one of possible

alternative to VCRS in automobile applications in terms of energy savings and environmental issues. The exhaust heat can be used to provide the thermal energy input to the adsorption system. Since, the waste heat usually constitutes 60 to 70% of the total energy used in internal combustion engines (ICE) during energy conversion processes [5, 6].

Various experimental and theoretical studies have been performed on the adsorption cooling systems, most of them are related to the development of mathematical models. Recent developments are focusing on dynamic models which can give a more clear idea about the dynamic behaviour of the transient heat and mass transfer processes in the adsorbent bed and on how to optimize the system operation, especially when the heat-source is variable, as it is the case on vehicles. The majority of researchers propose lumped parameter models [7-16] while some have focused on one dimensional models [17-20]. Two and three-dimensional models can also be found in the literature, [21-25] and [26, 27] respectively. However, the main differences between the different models are generally occur in the simplifying assumptions, numerical solution method, components design and application of the modelled system. A summary survey of experimental and theoretical studies based on adsorption systems driven by engine waste-heat is shown in Table. 1.

**Table 1.** Summary of studies related to the use of engine waste heat (exhaust gases and/or water coolant) to drive adsorption cooling systems

Heat source	Ref.	Heat Source (°C)	Pair	SCP Wkg-1	СОР	Cooling Temp (°C)	Cooling Power (KW)	Application	Study type
Engine waste heat gases	28	210-230	zeolite-water	N/A	0.38	18	3.4	locomotive	Е
	7	350-450	zeolite-water	164-200	0.25	10	6.5-10.0	locomotive	$E^*+T^*$
	29	400	zeolite-water	N/A	0.2-0.3	7	5	locomotive	Е
	8	255-296	zeolite-water	25.7	0.38	10	45	truck	E+T
	30	200-250	zeolite-water	N/A	0.25	3.0-5.0	2.8-4.0	locomotive	Е
	31	325	zeolite 13x –water	180	0.4	0.7-16.2	0.002-0.0105	truck	Е
	32	220-250	zeolite-water	N/A	0.21	5-18	3.0-4.2	locomotive	Е
	9	200	activated carbon– methanol	400	0.25	15-25	0.65	diesel engine	T
	10	250	zeolite-water	N/A	0.436	7-15	2.015	truck	E+T
	11	80-90	zeolite-water	N/A	0.6	10	5	truck	E+T
	33	400-600	zeolite-water	N/A	N/A		2.5	truck	Е
Engine coolant water	12	270-450	zeolite 13x –water	45	0.41	10	N/A	automobile	T
	34	90	activated carbon– ammonia	650-800	0.22	20	1.6-2.0	automobile	Е
	35	87	silica gel–water	208	0.62	12	3.6	automobile	Е
	36	90	N/A	300-600	0.25-0.45	8-14	1-2.3	truck	Е

<sup>\*</sup>E- refers to experimental study and T refers to theoretical study

It can be noted that, Silica gel-water pair can be efficiently used with a maximum desorption temperature of 80-90°C, which is suitable for adsorption systems driven by low temperature heat sources, as it is the case of the engine cooling circuit of automobiles which normally lies between 90-95°C. Systems which have lower heat source temperature have higher COP than those with higher heat source temperature. It may be due to the fact that the heat losses related to the alternate heating cooling of the bed increase by raising the bed's temperature. Few experimental data and calculations on adsorption chillers powered by engine waste-heat with heat recovery system can be found in the open literature [37]. System performance with heat recovery could be improved up to 50% [38-40]. All the existing models contain certain simplifications in the basic equations that result sometimes in numerical instabilities **Douss et al [41]**. Therefore, there is a need for more reliable dynamic models and, in particular, to predict the other components of any sorption systems: evaporator, condenser and other heat exchangers.

In this study, Part I of a two-part study, the work on modelling and testing of a prototype adsorption system powered by engine waste-heat from an automobile engine coolant water is investigated. The system performance was evaluated with and without heat recovery operation. An improved non-equilibrium lumped-parameter model is developed to simulate the dynamic behaviour of the silica gel (Sorbil A)/water adsorption system under different configurations. The model includes each system component in order to simulate the full dynamic behavior of the entire system. In addition, it can be provide sufficient accuracy in the estimation of its instantaneous operation and performance including; the kinetics of the desorption/adsorption processes, the thermal inertia of all the involved components, including the fluid circuits, and the operation of the valves between components. This will allow to understand the non-equilibrium adsorption/desorption process in transient regime.

As a comparison between the proposed model and those existent in the literature is that the flow between the components is based on the pressure difference between them. Also the pressure in the bed is based on a state equation, as well as on mass conversation. This makes the model able to capture the most important characteristics of the dynamics of the system. Moreover, different valve operation strategies or automatic operation (reed valves) could be analyzed with the employed formulation model. However, the developed model has been validated with experimental measurements in dynamic conditions and under different operation strategies such as the inclusion of an interesting heat recovery strategy aimed at reducing alternate heating and cooling losses. The experimental data were obtained at the Energy research Centre of the Netherlands, Petten (ECN).

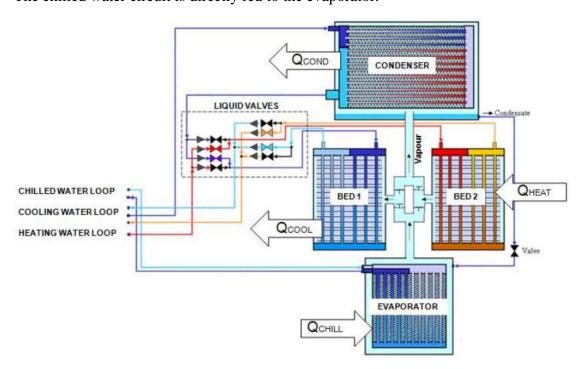
In Part II of this paper, the developed model is used to simulate and optimize the performance of an on-board adsorption system under different real ambient and start-up conditions as well as configurations to obtain comfortable temperatures in the cabin [42].

## 2 Design and description of the adsorption system

The cooling water temperature at the outlet of the engine normally lies between 90-95 °C for cars [4]. A great amount of thermal energy (waste-heat) can be therefore recovered

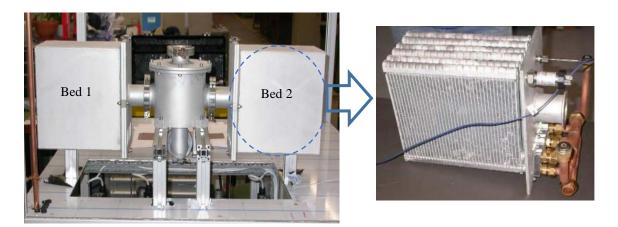
from the engine's coolant loop at those temperatures. In addition, the water temperature could be increased by heat recovery operation from the exhaust gases in order to provide an increased temperature heat source.

TOPMACS project for automotive air conditioning applications [43] where the experimentally tests are performed at the ECN laboratories. The system consists of two sorption beds connected to a condenser and an evaporator, an expansion device and four check valves as shown in Fig. 1. The adsorbent beds operate in counter-phase in order to allow a continuous useful effect: when the first bed is in cooling mode the second one is in regeneration mode. As shown from the figure, the adsorption system in the lab is connected to three secondary water loops for heating, cooling and chilled water. The hot water is sent to one of the two beds, depending on the position of the valves in the liquid circuit. The cooling water is first sent to the condenser and then through the valves to the other bed. The chilled water circuit is directly fed to the evaporator.



**Fig. 1** Schematic diagram of the considered adsorption cooling system, detailed view.

Fig. 2(a) shows a picture of the thermal compressor section of the adsorption system consists of two beds. Each bed has three tube-fin heat exchangers connected in parallel as shown in picture of **Fig. 2(b)**. Physically, the flat tube-fin heat exchanger is constructed by flat channel tubes covered with uniformly spaced flat fins to increase the heat transfer area on the air side which will be employed to increase the heat transfer to the adsorbent. This kind of heat exchangers is available in the market as evaporator for conventional automotive air conditioning systems, therefore they are available at a low cost. In addition these type of HE are made from aluminium, having the advantages of low weight and low thermal capacity (lower heat losses) compared with other types of heat exchangers. The weight of each aluminium heat exchanger (excluding the headers) is approximately 1.012 kg. The fin side of each heat exchanger is filled with approximate 1 kg of silica gel (Sorbil A) grains. The beds are connected to a housing that contains check valves (reed type). The condenser has three heat exchangers (automotive evaporators) connected in parallel and contained in a stainless steel envelope. It has internal reinforcements to withstand the forces of the internal vacuum. On the other hand, the evaporator consists of four tube-fin heat exchangers (automotive heater cores) that lie horizontally in 2 sections on top of each other. Finally, the overall weight of the prototype system is 86 kg, not including the weight of the water in the circuits for heating, cooling and chilling, the refrigerant water in the evaporator, and the thermal insulation.



**Fig. 2 (a)** Two sorption beds connected to the central housing that contains the refrigerant check valves. **(b)** One sorption bed assembly.

In order to assess the performance of the system, the experimental tests have been performed at two different operation (configurations) modes of the liquid valves of the heating and cooling water circuit as shown in **Fig. 3**. i) The first operation mode had no time delay between the switching of the outlet and inlet valves. ii) The second operation mode included a delay time between the switching of the liquid circuit valves in order to decrease the heat losses due to the alternate use of the hot and cooling water flows (heat recovery).

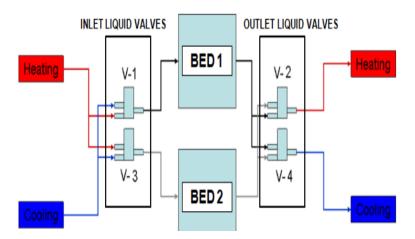


Fig. 3 Layout of the liquid valves of heating and cooling circuits for the two beds system

If the temperature difference between the inlet and outlet is smaller than a predefined value (e.g. 1 K), the inlet valves (V-1 and V-3) will switch. The outlet valves (V-2 and V-4) will switch with a time delay with respect to the inlet valves. The time delay is set to such a value that at the moment of switching the outlet temperatures are almost identical, and within the range of the average temperatures of the heating and cooling water circuit. This time delay prevents hot water remaining inside the hot bed to be sent directly to the cooling circuit, and cooling water remaining in the cold bed to be sent to the heating circuit. The result is that some heat of the water stored in the bed is always returned to the hot water circuit, and the cold water stored in the other bed is sent to the cooling water circuit. In this operation mode a part of the sensible heat contained in the liquid circuits is recovered, with the aim to increase the COP.

# 3 Mathematical modelling

## 3.1 Assumptions

- Uniform temperature distribution in each component at any instant.
- Non-equilibrium conditions at the adsorption/desorption beds.
- The empty space in the adsorbent heat exchanger is filled in with water vapor.
   Consequently, the pressure at the beds depends on the instantaneous mass of vapor contained inside and its temperature.
- Perfect gas behaviour has been assumed.
- The flow of water vapor among the beds, the condenser and the evaporator is governed by the pressure difference between these elements and the position of the valves.
- Liquid water is considered always in thermodynamic equilibrium corresponding to saturation conditions.

## 3.2 Adsorption isotherm and kinetics

The adsorbent material employed was a silica-gel (Sorbsil A) of 0.2 -1.0 mm grain size manufactured by **Ineos Group Limited [44]**. The equilibrium water-uptake of silica gel (Sorbil A)/water pair is correlated by the following equation **[45]**:

$$lnP_{b} = A(w_{eq}) + \frac{B(w_{eq})}{T_{b}}$$
 (1)

where, the parameters A and B are characteristics of the adsorbent/adsorbate interaction and describe a set of isosteres:

$$A(w_{eq}) = a_0 + a_1(w_{eq}) + a_2(w_{eq})^2 + a_3(w_{eq})^3$$
(2)

$$B(w_{eq}) = b_0 + b_1(w_{eq}) + b_2(w_{eq})^2 + b_3(w_{eq})^3$$
(3)

The numerical values of the constants a and b (i = 0, 1, 2, 3) were obtained experimentally for the silica gel/water pair by **Restuccia et al. [46].** 

In practical, the non-equilibrium conditions of the adsorbent material occurs in adsorption systems, so the adsorption rate depends on the difference between the instantaneous uptake

at the bed and the one that would be obtained at the equilibrium conditions ( $w_{eq}$ ) Sakoda et al. [47]:

$$\frac{\mathrm{d}\mathbf{w}_{b}}{\mathrm{d}\mathbf{t}} = \mathbf{k}_{m}(\mathbf{w}_{eq} - \mathbf{w}_{b}) \tag{4}$$

where,  $k_m$  is the overall mass transfer coefficient for Sorbil A/water pair which can be given by:

$$k_{\rm m} = \frac{15D_{\rm s}}{R_{\rm p}^2} \tag{5}$$

where,  $R_p$  is the silica-gel radios and  $D_s$  is the surface diffusivity which is defined by Arrhenius equation as,

$$D_{s} = D_{s0} \exp\left(-\frac{E_{a}}{RT_{b}}\right) \tag{6}$$

Combining Eqs. (5) and (6) in Eq. (4):

$$\frac{dw_b}{dt} = k_1 e^{-k_2/T_b} (w_{eq} - w_b)$$
 (7)

where,  $k_1=15D_{so}/R_p^2$  and  $k_2=E_a/R$  have a constant values which have been taken from **Sakoda et al. [47].** 

Isosteric heat of adsorption ( $\Delta h_{ad}$ ) is not considered constant in the present study, as often occurs in the literature, but depends on the amount of adsorbed water. The isosteric heat of adsorption is extracted experimentally for Sorbil A/water pair [46]:

$$\Delta h_{ad}(W_b) = -(b_0 + b_1 W_b + b_2 W_b^2 + b_3 W_b^3) \frac{R}{M_w}$$
(8)

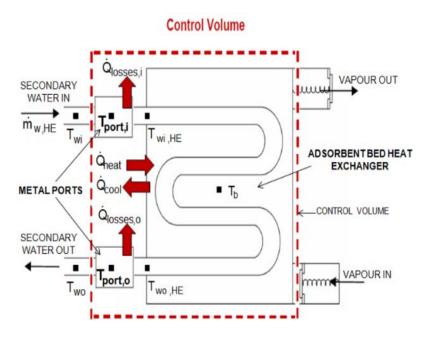
The numerical values of the coefficients b (i = 0, 1, 2, 3) are also given for the present pair.

## 3.3 Mass and energy balance equations

The governing equations are derived from the energy and mass balance and by the corresponding thermodynamic relationships for the different components of the system.

#### 3.3.1 Adsorber and desorber model

**Fig. 4** shows a control volume (red dashed line) for which the energy balance applies on a single adsorbent heat exchanger with inlet and outlet water ports.



**Fig. 4** Single adsorbent bed heat exchanger with the considered control volume (red dashed line)

The energy balance on the adsorbent bed control volume for adsorber/desorber can be described as:

$$C_{\text{HE}} \frac{dT_{\text{b}}}{dt} = m_{\text{ads,HE}} \frac{dw_{\text{b}}}{dt} \Delta h_{\text{ad}} - \left(\frac{n R_{\text{v,i}}}{N_{\text{HE}}}\right) Cp_{\text{v}} (T_{\text{b}} - T_{\text{evap}}) + R_{\text{heat/cool}}$$

$$(9)$$

where,  $C_{HE}$  is the thermal capacity of the adsorbent bed heat exchanger (adsorbent + adsorbate + metal). **Equation (9)** is valid for the bed in adsorption mode as well in desorption mode. However, in desorption mode the term  $\dot{m}_{v,i}Cp_v(T_b-T_{evap})$  in **Eq. (9)** must not be included since the desorbed vapor is assumed to be at the same temperature than the bed. The term on the left-hand side of **Eq. (9)** represents the amount of sensible heat required to heat or cool the bed (including; adsorbent, the adsorbate as well as the metallic parts in the bed) during adsorption or desorption processes. The first tem on the right-hand side refers to the heat due to either the adsorption or desorption process. The second term on the right-hand side represents the sensible heat of the adsorbed vapor, which is the sensible heat required to heat up the vapor from the evaporation temperature up to the bed

temperature during adsorption. Finally, the third term on the right hand side of **Eq.** (9) represents the total amount of heat  $(\dot{Q}_{heat/cool})$  released to the cooling water or provided by the heating water depending on the operation mode of the bed.

An alternative expression to the standard effectiveness NTU formulation has been developed here in order to determine the heat exchanged between the system components and the heat transfer fluid (secondary water) under non-steady conditions. The correlation takes into account the effect of both inlet and outlet temperature differences on the heat flux. The heat transfer  $\dot{Q}_{heat/cool}$  is represented by the following correlation

$$\oint_{\text{heat/cool}} = \varepsilon_{\text{HE}} i \oint_{\text{w,HE}} Cp_{\text{w}} \left[ \alpha (T_{\text{wi,HE}} - T_{\text{b}}) + (1 - \alpha) \left( \frac{T_{\text{wo,HE}} - T_{\text{b}}}{1 - \varepsilon_{\text{HE}}} \right) \right]$$
(10)

where, the parameter  $\alpha$  corresponds to the weighting factor of the temperature difference between the inlet and outlet water temperatures and the temperature of the bed. This parameter was adjusted by comparing the numerical predictions with the experimental results. A value of  $\alpha$  =0.8 (i.e. 80%) of the inlet temperature difference and 20% of the outlet temperature difference was found to produce good results for a wide range of operating conditions. The effectiveness of the adsorbent bed heat exchanger ( $\epsilon_{HE}$ ) is given by:

$$\varepsilon_{\text{HE}} = 1 - \exp(-\frac{UA_{\text{total}, \text{HE}}}{R_{\text{w}, \text{HE}}Cp_{\text{w}}})$$
 (11)

The thermal losses to the inert masses due to the alternate bed heating and cooling have been taken in consideration in the model. The heat transfer from the inlet secondary water to the inlet header and port tube  $\dot{Q}_{losses,i}$  is evaluated with an expression similar to **Eq.** (10) by:

$$\mathbf{E}_{\text{losses,i}} = \epsilon_{\text{port,i}} \mathbf{E}_{\text{w,HE}} \mathbf{C} \mathbf{p}_{\text{w}} \left[ \alpha (\mathbf{T}_{\text{wi}} - \mathbf{T}_{\text{port,i}}) + (1 - \alpha) \frac{\mathbf{T}_{\text{wi,HE}} - \mathbf{T}_{\text{port,i}}}{1 - \epsilon_{\text{port,i}}} \right]$$
(12)

The heat transfer from the outlet secondary water to the outlet header and port tube  $\dot{Q}_{losses,o}$  is given by:

$$\mathbf{E}_{\text{losses,o}} = \varepsilon_{\text{port,o}} \mathbf{E}_{\text{w,HE}} C p_{\text{w}} \left[ \alpha (T_{\text{wo,HE}} - T_{\text{port,o}}) + (1 - \alpha) \frac{T_{\text{wo}} - T_{\text{port,o}}}{1 - \varepsilon_{\text{port,o}}} \right]$$
(13)

where,  $\varepsilon_{port,i}$  and  $\varepsilon_{port,o}$  are the effectiveness of inlet and outlet header and ports respectively. The temperature of the inlet header  $T_{port,i}$  and outlet header  $T_{port,o}$  is given by their corresponding energy conservation equations as:

$$C_{\text{port},i} = \frac{dT_{\text{port},i}}{dt} = \mathcal{E}_{\text{losses},i}$$
 (14)

$$C_{\text{port,o}} = \frac{dT_{\text{port,o}}}{dt} = \mathcal{E}_{\text{losses,o}}$$
 (15)

where,  $C_{\text{port,i}}$  and  $C_{\text{port,o}}$  are the thermal capacity of the inlet and outlet meatal ports of the bed, respectively. As a matter of fact, they are simply evaluated by dividing the total mass of the heat exchanger including the inlet and outlet headers, multiplied by the metal specific heat. In this may it is possible to accurately take into account the total energy employed for the alternate heating and cooling of the total metal mass of the bed.

The temperatures of the secondary water at the inlet of the adsorbent bed heat exchanger  $T_{wi,HE}$  and at the outlet of the heat exchanger  $T_{wo,HE}$  are given by:

$$C_{\text{wport,i}} \frac{dT_{\text{wi,HE}}}{dt} = r \delta_{\text{w,HE}} C p_{\text{w}} (T_{\text{wi}} - T_{\text{wi,HE}}) - \delta_{\text{losses,i}}$$
(16)

$$C_{wHE} \frac{dT_{wo,HE}}{dt} = R_{w,HE} Cp_w (T_{wi,HE} - T_{wo,HE}) - Q_{losses,o}$$
(17)

where,  $C_{wport,i}$  is the thermal capacity of the secondary water inside the inlet header and  $C_{w,HE}$  is the thermal capacity of the secondary water inside the adsorbent heat exchanger.

Finally, the temperature of the secondary water  $(T_{wo})$  leaving the bed (from the outlet header) is given by the following equation:

$$C_{\text{wport,o}} \frac{dT_{\text{wo}}}{dt} = \mathbf{R}_{\text{w,HE}} Cp_{\text{w}} (T_{\text{wo,HE}} - T_{\text{wo}}) - \mathcal{C}_{\text{losses,o}}$$
(18)

where, C<sub>wport,o</sub> is the thermal capacity of the secondary water inside the outlet header.

The continuity equation at the adsorbent bed provides the necessary link between the vapor mass in the bed  $(m_{v,b})$  the uptake variation  $(w_b)$  and the vapor flow rates leaving  $(m_{v,out})$  or entering  $(m_{v,in})$  the bed:

$$\frac{dm_{v,b}}{dt} = -m_{ads,b} \frac{dw_b}{dt} + r \delta_{v,i} - r \delta_{v,o}$$
 (19)

Equilibrium is not assumed in the bed. Therefore, it is necessary to incorporate an equation for the pressure in the bed. The differential equation for the pressure  $(P_b)$  in the adsorbent bed when assumed that non-condensable gases have been totally removed can be expressed in the following way when a perfect gas behaviour is assumed.

$$\frac{dP_{b}}{dt} = P_{b} \left( \frac{1}{T_{b}} \frac{dT_{b}}{dt} + \frac{1}{m_{v,b}} \frac{dm_{v,b}}{dt} \right)$$
 (20)

In order to calculate the vapor flow through the interconnecting pipes and valves and between the sorption beds, the condenser and the evaporator. In practice, vapor velocities must be kept low in order to minimize pressure losses, hence the vapor flow can be considered non-compressible. Therefore, the instantaneous flow rates,  $\dot{m}_{v,in}$  and  $\dot{m}_{v,out}$ , can be calculated as follows:

$$\dot{m}_{v,in} = \begin{cases} = 0 & \text{If } P_b < P_{evap} \\ = A_{evap} \sqrt{2\rho_v(T_{evap}, P_{evap})(P_{evap} - P_b)} & \text{If } P_b \le P_{evap} \end{cases}$$
(21)

$$\dot{m}_{v,out} = \begin{cases} = 0 & \text{If } P_b < P_{cond} \\ = A_{cond} \sqrt{2\rho_v(T_b, P_b)(P_b - P_{cond})} & \text{If } P_b \ge P_{cond} \end{cases}$$
(23)

where, a set of convenient reed valves has been considered to connect the bed with evaporator and condenser. The valves are considered to close instantaneously when the flow is reversed and having a constant effective area  $A_{\text{evap}}$  and  $A_{\text{cond}}$  when the valves are open. A dynamically varying model for the valves could be easily incorporated if a slow motion were detected in experiments.

The above set of equations (9-20) constitutes a system of ODEs for  $w_b$ ,  $T_b$ ,  $T_{port,o}$ ,  $T_{wi,HE}$ ,  $T_{wo,HE}$ ,  $T_{wgi}$ ,  $T_{wo}$ ,  $P_b$  and  $m_{v,b}$  for each bed. Furthermore, it is possible to calculate the refrigerant flow between the sorption beds and the evaporator/condenser according to the operation mode of the bed.

#### 3.3.2 Condenser model

During the desorption process, the condenser is connected to the bed where the refrigerant (desorbed vapor) can be condensed and delivered to the evaporator through an expansion valve. Since the refrigerant comes from the desorber bed as vapor at higher temperature  $T_{cond,i}$  and at the same pressure as in the condenser  $P_{cond}$ , the energy balance equation for the vapor region surrounding the condenser tubes can be expressed as follows:

$$\mathbf{Q}_{c}^{\mathbf{k}} = \mathbf{R}_{cond} \left[ Cp_{v} (T_{cond.i} - T_{cond}) + \Delta h_{fg} (T_{cond}) \right]$$

$$(25)$$

The left-hand side of equation **Eq. (25)** represents the total amount of heat transferred to the cooling water. The first term on the right-hand side represents the sensible heat of the vapor being cooled from the temperature of the refrigerant leaving the bed (desorbed vapor) down to the temperature of condensation. The second term on the right-hand side represents the total amount of latent heat involved in the change of state from saturated vapor to saturated liquid.

The rate of heat released  $(\dot{Q}_c)$  from the refrigerant to the secondary water can again be evaluated by:

The temperature of the secondary water ( $T_{sec,o}$ ) at the outlet of the condenser can be estimated by the following equation:

$$C_{\text{cond}} \frac{dT_{\text{sec,o}}}{dT} = \mathbf{r}_{\text{w,sec}} Cp_{\text{w}} (T_{\text{sec,i}} - T_{\text{sec,o}}) + \mathcal{E}_{c}$$

$$\tag{27}$$

The term on the left-hand side of equation Eq. (27) refers to the energy variation of the metallic tubes and cooling water in the condenser. The first term on the right-hand side represents enthalpy change of the water flow across the condenser. The second term on the right-hand side represents the amount of heat transferred from the cooling water flow to the condenser.

The mass balance equation for the vapor, which links the variation of vapor mass in the condenser with the incoming mass flow from the bed  $(\dot{m}_{v,o})$  and the condensation rate  $(\dot{m}_{cond})$  can be written as

$$\frac{\mathrm{dm}_{v,\mathrm{cond}}}{\mathrm{dt}} = \mathbf{r} \mathbf{8}_{\mathrm{cond,i}} - \mathbf{r} \mathbf{8}_{\mathrm{cond}} \tag{28}$$

where,  $\dot{m}_{con,i}$  is the refrigerant flow entering the condenser which corresponds to the total flow of water vapor desorbed from the bed ( $\dot{m}_{con,i}=\dot{m}_{v,o}$ ).

The mass balance equation for the liquid in the condenser can be written as:

$$\frac{\mathrm{dm}_{\mathrm{l,cond}}}{\mathrm{dt}} = \mathbf{n}_{\mathrm{cond}}^{\mathbf{k}} - \mathbf{n}_{\mathrm{cond,o}}^{\mathbf{k}} \tag{29}$$

where,  $\dot{m}_{l,con}$  is the mass of liquid water in the condenser and  $\dot{m}_{con,o}$  is the refrigerant (liquid water) flow from the condenser to the evaporator.

Hence, the volume of liquid water in the condenser  $(V_{1,cond})$  can be estimated as:

$$\frac{dV_{l,cond}}{dt} = \frac{1}{\rho_w} \frac{dm_{l,cond}}{dt} \rightarrow \frac{dV_{l,cond}}{dt} = \frac{m_{cond}^2 - m_{cond,o}^2}{\rho_w}$$
(30)

The link between the liquid volume  $(V_{1,cond})$  and the volume occupied by the vapor in the condenser  $(V_{v,cond})$  can be expressed by:

$$\frac{dV_{v,cond}}{dt} = -\frac{dV_{l,cond}}{dt} \tag{31}$$

The equation of state for the vapor provides a way to evaluate the variation of the pressure as a function of the variation of the vapor mass, volume and temperature:

$$P_{\text{cond}} = \frac{RT_{\text{cond}}}{V_{\text{v.cond}}} \frac{m_{\text{v,cond}}}{M_{\text{w}}} \to \frac{d}{dt} (P_{\text{cond}}, V_{\text{v,cond}}) = \frac{d}{M_{\text{w}}} \frac{d}{dt} (T_{\text{cond}}, m_{\text{v,cond}})$$
(32)

where,  $M_w$  is the water molar mass [kgmol<sup>-1</sup>]; R is the universal gas constant [mbarm<sup>3</sup>kg<sup>-1</sup>K<sup>-1</sup>];  $m_{v,cond}$  is the water vapor mass in the condenser [kg]; is the volume of water vapor in the condenser [m<sup>3</sup>];  $T_{cond}$  is the temperature in the condenser [K];  $P_{cond}$  is the pressure in condenser [mbar].

Since the refrigerant inside the condenser is in a saturated state, the following equation provides a way to relate the temperature variation with the pressure in the condenser:

$$T_{\text{cond}} = T_{\text{sat}}(P_{\text{cond}}) \rightarrow \frac{dT_{\text{cond}}}{dt} = \frac{dT_{\text{sat}}(P_{\text{cond}})}{dP_{\text{cond}}} \frac{dP_{\text{cond}}}{dt}$$
(33)

By the product rule and replacing **Eq.** (33), the following differential equation for the pressure in the condenser is obtained:

$$\frac{dP_{cond}}{dt} = \frac{\frac{P_{cond}}{m_{v,cond}} \left(\frac{dm_{v,cond}}{dt}\right) - \frac{P_{cond} \left(\frac{dV_{v,cond}}{dt}\right)}{V_{v,cond}}}{1 - \frac{P_{cond}}{T_{cond}} \left(\frac{dT_{sat}}{dP_{cond}}\right)} \tag{34}$$

By solving the set of differential Eqs. (27) to (34) in time, the following unknowns are found for each bed:  $P_{cond}$ ,  $m_{v,cond}$ ,  $V_{v,cond}$  and  $T_{sec,o}$ . Furthermore, it is possible to calculate the condensation rate, the volume of the liquid in the condenser and the temperature in the condenser according to the saturation hypothesis.

#### 3.3.3 Evaporator model

Since the refrigerant enters the evaporator as liquid at higher pressure and temperature  $(P_{cond,o}, T_{cond,o})$ , the energy balance equation for the refrigerant in the evaporator can be given by:

$$\mathbf{g}_{E}^{\mathbf{k}} = \mathbf{g}_{evap} \left[ \Delta h_{fg} (T_{evap}) - Cp_{w} (T_{cond,o} - T_{evap}) \right]$$

$$(35)$$

where,  $\dot{m}_{evap}$  is the evaporation rate,  $T_{evap}$  is the evaporator temperature,  $\Delta_{hfg}$  is the specific heat of vaporization  $T_{evap}$ . The first term on the right-hand side of **Eq.** (35) represents the total amount of latent heat involved in the change of state from saturated liquid to saturated vapor. The second term on the right-hand side represents the sensible heat required to cool down the incoming condensate from the condensation temperature to the evaporation temperature.

The rate of heat provided by the secondary water (i.e. chilled water) to the refrigerant ( $\dot{Q}_E$ ) can be expressed by:

$$\mathbf{E}_{E} = \mathbf{E}_{evap} \mathbf{E}_{w,chill} \mathbf{C} \mathbf{p}_{w} \left[ \alpha (\mathbf{T}_{chill,i} - \mathbf{T}_{evap}) + (1 - \alpha) \frac{\mathbf{T}_{chill,o} - \mathbf{T}_{evap}}{1 - \mathbf{E}_{evap}} \right]$$
(36)

where,  $\varepsilon_{evap}$  is the evaporator effectiveness;  $\dot{m}_{w,chill}$  is the chilled water mass flow [Kgs<sup>-1</sup>];  $Cp_w$  is the specific heat capacity of the water [Jkg<sup>-1</sup>K<sup>-1</sup>];  $T_{chill,i}$  and  $T_{chill,o}$  are the inlet and outlet temperatures of the evaporator secondary water (i.e. chilled water).

The temperature of the chilled water at the outlet of the evaporator  $(T_{chill,o})$  can be estimated by:

$$C_{\text{evap}} \frac{dT_{\text{chill,o}}}{dt} = r \mathbf{A}_{\text{w,chill}} Cp_{\text{w}} (T_{\text{chill,i}} - T_{\text{chill,o}}) - \mathbf{E}_{\text{E}}$$
(37)

The term on the left-hand side of **Eq.** (37) refers to the temporal variation of the internal energy contained in the metal tubes and the water mass in the evaporator. The first term on the right-hand side represents the amount of sensible heat provided by the secondary water. Finally, the second term on the right-hand side of **Eq.** (37) refers to the total amount of heat exchanged with the refrigerant.

The mass balance equation for the vapor, which links the variation of vapor mass in the evaporator with the out coming mass flow from the evaporator ( $\dot{m}_{eva,o}$ ) and the evaporation rate ( $\dot{m}_{evap}$ ) can be written as:

$$\frac{\mathrm{dm}_{\mathrm{v,evap}}}{\mathrm{dt}} = \mathbf{18}_{\mathrm{evap}} - \mathbf{18}_{\mathrm{evap,o}} \tag{38}$$

where,  $\dot{m}_{evap}$  is the evaporation rate, and  $\dot{m}_{evap,o}$  is the refrigerant flow leaving the evaporator which corresponds to the total flow of vapor adsorbed by the bed ( $\dot{m}_{evap,o}=\dot{m}_{v,i}$ ).

The pressure in the evaporator is based on the vapor state equation which provides a way to evaluate the variation of the pressure as a function of the vapor mass  $(m_{v,evap})$ , vapor volume  $(V_{v,evap})$  and temperature  $(T_{evap})$  can be described by:

$$P_{\text{evap}} = \frac{RT_{\text{evap}}}{V_{\text{v,evap}}} \frac{m_{\text{v,evap}}}{M_{\text{w}}} \rightarrow \frac{d}{dt}(P_{\text{evap}}, V_{\text{v,evap}}) = \frac{d}{M_{\text{w}}} \frac{d}{dt}(T_{\text{evap}}, m_{\text{v,evap}})$$
(39)

Since the refrigerant (water vapor) inside the evaporator is in a saturated state. The following equation provides a way to relate the variation of the temperature with the pressure in the evaporator:

$$T_{\text{evap}} = T_{\text{sat}}(P_{\text{evap}}) \to \frac{dT_{\text{evap}}}{dt} = \frac{dT_{\text{sat}}(P_{\text{evap}})}{dP_{\text{evap}}} \frac{dP_{\text{evap}}}{dt}$$
(40)

The differential equation for the pressure in the evaporator can be obtained by:

$$\frac{dP_{\text{evap}}}{dt} = \frac{\frac{P_{\text{evap}}}{m_{\text{v,evap}}} (\frac{dm_{\text{v,evap}}}{dt})}{1 - \frac{P_{\text{evap}}}{T_{\text{evap}}} (\frac{dT_{\text{sat}}}{dP_{\text{evap}}})}$$
(41)

By solving the set of differential equation for each system component of **Eqs.** (37-41) in time, the following unknowns are found for each bed:  $P_{evap}$ ,  $m_{v,evap}$ ,  $V_{v,evap}$ ,  $T_{chill,o}$ . Furthermore, it is possible to calculate the evaporation rate, the volume of the liquid in the evaporator and the temperature in the evaporator accordingly with the saturation hypothesis.

#### 4 Measurement of system performance

The model is able to calculate the amounts of heat exchanged in each component and consequently, the performance of the system. The cooling capacity  $\dot{Q}_{chill}$  is given by the following equation:

$$\mathbf{Q}_{\text{chill}} = \mathbf{R}_{\text{w,chill}} \mathbf{C} \mathbf{p}_{\text{w}} \int_{0}^{t_{\text{cycle}}} (\mathbf{T}_{\text{chill,i}} - \mathbf{T}_{\text{chill,o}}) dt$$
(42)

The condenser capacity  $Q_{cond}$  is given by:

$$\mathbf{\mathcal{E}}_{cond} = -\mathbf{R}_{w,sec} C p_w \int_{0}^{t_{cycle}} (T_{sec,i} - T_{sec,o}) dt$$

$$(43)$$

The heating capacity of the bed Qheat is given by the following equation:

$$\mathbf{Q}_{\text{heat}} = \mathbf{R}_{\text{hw,b}} C p_{\text{w}} \int_{0}^{t_{\text{cycle}}} (T_{\text{hw,i}} - T_{\text{hw,o}}) dt$$

$$\tag{44}$$

The cooling capacity of the bed  $\dot{Q}_{cool}$  is given by the following equation:

$$\mathbf{Q}_{\text{cool}}^{\mathbf{t}} = -\mathbf{M}_{\text{cw,b}} \mathbf{C} \mathbf{p}_{w} \int_{0}^{t_{\text{cycle}}} (\mathbf{T}_{\text{cw,i}} - \mathbf{T}_{\text{cw,o}}) dt$$

$$\tag{45}$$

The performance of the adsorption system is mainly characterized by the cooling capacity of the system (Q<sub>chill</sub>) and the coefficient of performance (COP). The COP is the ratio between the heat extracted by the evaporator and the heat source input to the bed as the following:

$$COP = \frac{\mathcal{E}_{chill}}{\mathcal{E}_{heat}} = \frac{\int_{0}^{t_{cycle}} (\mathbf{n} \mathbf{k} \mathbf{C} \mathbf{p})_{chill} (T_{chill,in} - T_{chill,o}) dt}{\int_{0}^{t_{cycle}} (\mathbf{n} \mathbf{k} \mathbf{C} \mathbf{p})_{des} (T_{hw,in} - T_{hw,o}) dt}$$

$$(46)$$

where, t<sub>cycle</sub> denotes the total cycle time. Experimentally, the cooling capacity and the COP was obtained from the measurements of heat transfer fluid temperatures and mass flow rates at a fixed cycle of 360 s, which is the optimum for the characteristics of the considered system.

The system of first-order ordinary differential equations (ODEs) described above was implemented in MATLAB® as an S-Function and solved dynamically in Simulink® by the solver ode23tb (stiff/TR-BDF2). The solver uses a method from the Runge-Kutta family to solve the system of ODEs and it gives accurate solutions with high speed of convergence. **Fig. 5** shows a simplified structure of the system model with a set of inputs, a set of state variables and a set of outputs.

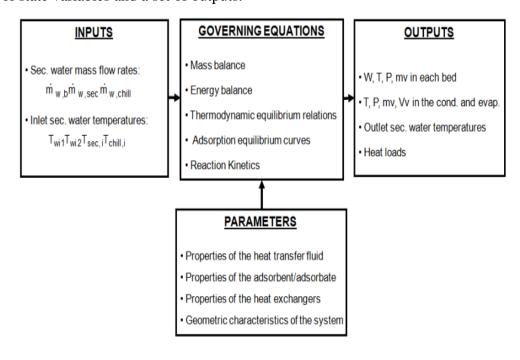


Fig. 5 Simplified structure of the adsorption system model

Furthermore, the model requires several parameters which are constant throughout the simulation the parameters which are related to the thermophysical properties of the water, adsorbent and other components of the system and the parameters which are related to the physical design of the system. The main parameters used in the model are listed in **Table 2.** 

**Table 2.** Values of parameters adopted in the simulation.

Symbol	Value	Units	Observations		
cpw	4182	J Kg <sup>-1</sup> K <sup>-1</sup>	[48]		
$ ho_{ m w}$	1014	$J~Kg^{\text{-}1}K^{\text{-}1}$	[48]		
$h_{\rm w}$	2248	$Wm^{-2}K^{-1}$	[48]		
$C_{\text{pads,o}}$	750	$J~Kg^{\text{-}1}K^{\text{-}1}$	[46]		
$Cp_{\text{met}} \\$	890	$J~Kg^{\text{-}1}K^{\text{-}1}$	[49]		
$k_{\text{met}}$	160	$Wm^{-2}K^{-1}$	[49]		
$\mathbf{k}_1$	0.019	s <sup>-1</sup>	[47]		
$\mathbf{k}_2$	906	K	[47]		
$m_{\rm w,HE}$	0.3276	kg	ECN system prototype		
$m_{\text{w,porti}} \\$	0.0938	kg	Assumed to be 1/3 of $m_{\mbox{\tiny W,HE}}$		
$m_{\text{w,porto}} \\$	0.0938	kg	Assumed to be 1/3 of $m_{\mbox{\tiny W,HE}}$		
$m_{\text{met},\text{HE}}$	1.012	kg	ECN system prototype		
$m_{\text{port},i}$	0.1518	kg	Assumed to be $1/6$ of $m_{\text{met},\text{HE}}$		
$m_{\text{port},o}$	0.1518	kg	Assumed to be $1/6$ of $m_{\text{met},\text{HE}}$		
$m_{\text{ads},\text{HE}}$	1	kg	ECN system prototype		
$N_{H\!E}$	3	-	ECN system prototype		
$V_b$	0.0108	$m^3$	ECN system prototype		
$V_{\text{cond}} \\$	0.0231	$m^3$	ECN system prototype		
$V_{\text{evap}}$	0.0128	$m^3$	ECN system prototype		

**Table 3** shows the standard operating conditions used in the study for both operation modes.

**Table 3.** Nominal operating condition for the two bed adsorption chiller.

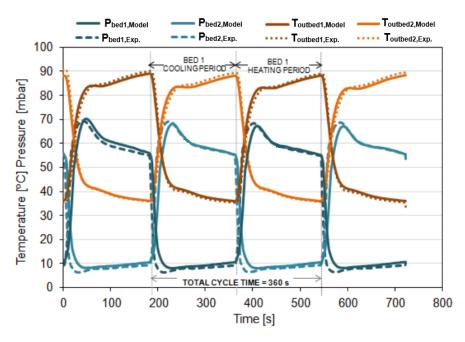
Hot water inlet		Cooling water inlet (cond. + adsorber)			Chilled water inlet		
Temp.	Flow rate	Temp.	Flow rate		Temp.	Flow rate	
[°C]	[kgs <sup>-1</sup> ]	[°C]	[kgs <sup>-1</sup> ]		[°C]	[kgs <sup>-1</sup> ]	
90	0.20	33	0.20		15	0.13	

#### 5 Simulation results and model validation

As mentioned previously, the experimental tests were performed in different operation modes (configurations) include; operation mode without heat recovery and operation mode with heat recovery.

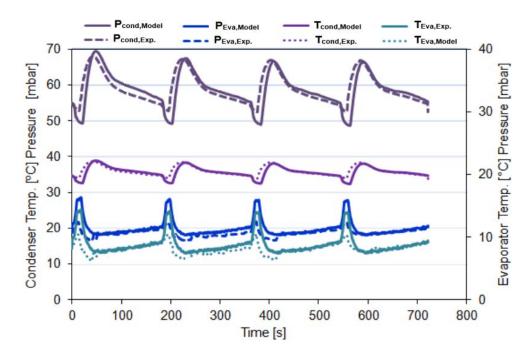
#### 5.1 First operation mode: Tests performed without heat recovery

**Fig. 6** shows a comparison between the simulated and experimental results for the pressure and outlet water temperature profiles of the adsorbent beds at the operating conditions shown in **Table 3**. As it can be observed, the numerical model predicts remarkably well the pressures and outlet water temperatures of adsorbent beds determined from the experimental data. The predicted pressures, however, show some relatively small deviations at the switching region. The main difference being that the experimental pressure reacts faster than the modeled one. This can be due, either to the corresponding temperature and pressure sensor delays, or to the fact that the kinetics of the adsorption/desorption processes are not perfectly taken into account in the model. In any case, overall, the model predicted fairly well the whole dynamics of the system.



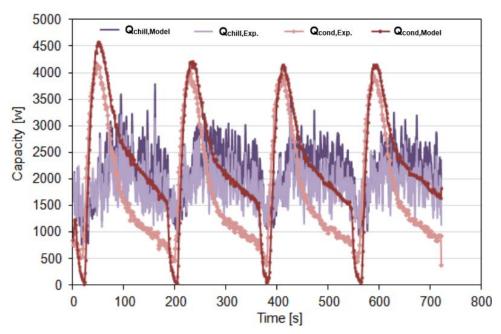
**Fig. 6.** Experimental and model prediction of pressure and outlet temperature of adsorbent beds

**Fig. 7** shows the simulated and experimental results of the temperature and pressure profiles corresponding to the condenser and evaporator. As it can be seen, again, the simulation results show a good agreement with the experimental results regardless the hypothesis assumed in the model, and capturing most of the observed dynamics. A small delay in between the experimental pressure and the calculated one can be also seen.



**Fig. 7.** Comparison between experimental and numerical results of temperature and pressure at condenser and evaporator

In regard to the system performance, **Fig. 8** shows a comparison between the calculated and measured values of the instantaneous evaporator and condenser capacities. As it can be seen, in general, good agreement is observed between experimental and simulated results taking into account the approximate nature of the model and the noise on the performance evaluated from the experimental results. The average cooling capacity at permanent conditions has a value of 2.1 kW. The average condenser capacity was about 2.215 kW.



**Fig. 8.** Comparison between calculated and experimental results for evaporator cooling capacity and condenser capacity

Fig. 9 shows the equilibrium and non-equilibrium uptake evaluated by the model. During the first half cycle time, the adsorbent in the bed is in desorption and the water content of the adsorbent is decreased to about 0.034 kg/kg. In the second half cycle, the adsorbent in the bed is in adsorption and the water content of the adsorbent increases to about 0.088 kg/kg. The beds exchange their roles in the next half cycle and return to the first mode in the third cycle. As it can be seen, the adsorption phase is found to be a bit slower than the desorption one, with a more or less constant difference between the actual uptake and the one which would correspond to equilibrium. Along the desorption period, the difference between equilibrium and actual uptake is higher at the beginning but rapidly decreases with time. It is apparent the difference between the potentially possible uptake difference and the one which is actually obtained, showing the important role of the sorption kinetics on the performance of the system. The agreement in between the instantaneous measured and calculated results as well as the agreement on the prediction of the global performance indirectly validates the employed modeling of the sorption kinetics.

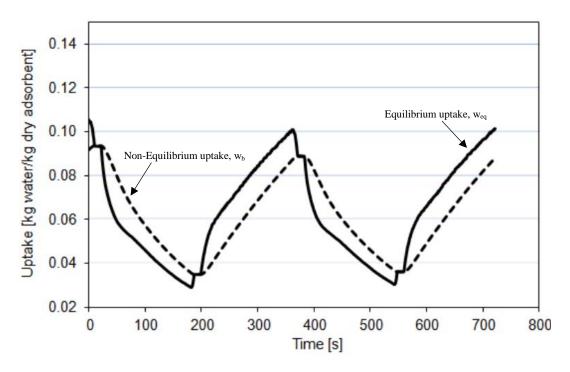
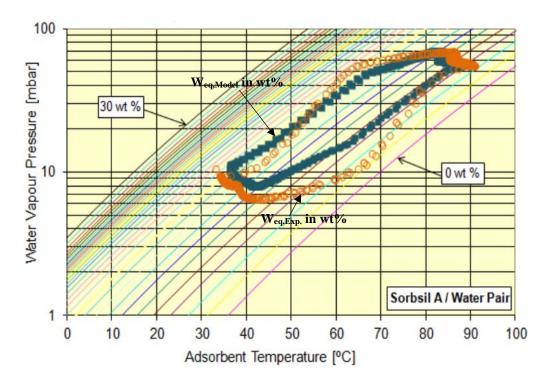


Fig. 9. Equilibrium and non-equilibrium uptake evolution for one bed (desorber)

Finally, Fig. 10 shows the Dühring diagram calculated from the bed pressure and temperature for both measured and calculated data. The equilibrium uptake for the experimental results has been evaluated from the instantaneous recordings of bed pressure and temperature. While the model appears to predict the behavior of the Dühring diagram with reasonable accuracy, the prediction shows some deviations from the experiments particularly during the adsorption period. The main reason for this deviation is the temperature of the bed. However it is difficult to know if the prediction of this temperature is good or not since one must take into account that there is a high uncertainty in the evaluation of the bed temperature, given that the experimental value corresponds only to the readings of a single temperature sensor inserted inside the bed, so the measurements are local. This is the reason why the comparison shown in **Fig. 6** includes the outlet water temperature from the bed instead of the sorbent temperature. The inertia of the temperature measurement together with temperature variation across the sorbent, could explain the differences with the model results and the experimental ones. In any case, the agreement in the total variation of uptake is remarkable. According to the simulation results, the minimum temperature reached by the bed at the end of the adsorption phase was 36 °C,

with a maximum uptake of about 10 wt%, while the maximum temperature reached by the bed at the end of the regeneration phase was 88 °C, with a minimum uptake of about 3 wt %.

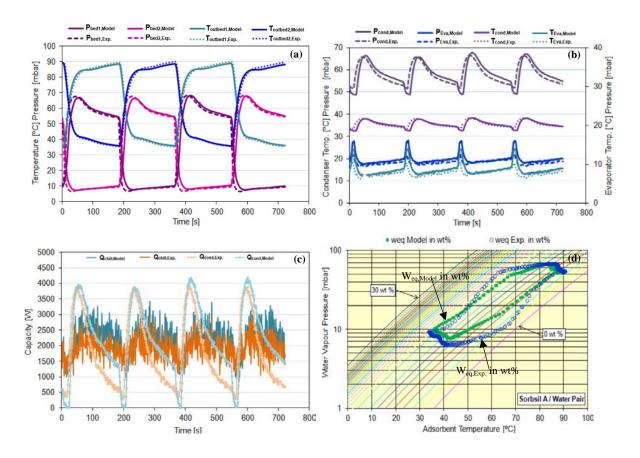


**Fig. 10.** Calculated and measured Dühring diagram of the Silica-gel (Sorbsil A)/water adsorption system at rated conditions

An overall good agreement between calculated and experimental results, this proves that the developed model is an adequate tool to assist the design and optimization of adsorption cooling systems.

# 5.2 Second operation mode: tests performed with heat recovery operation

**Fig. 11(a-d)** shows a comparison between the simulated and experimental results at the above mentioned operating conditions for the first 800 s for different parameters.



**Fig. 11.** Comparison between calculated and measured results - 2<sup>nd</sup> Operation Mode (heat recovery mode): (a) Pressure and outlet temperature profiles of adsorbent beds, (b) Temperature profiles and pressures at condenser and evaporator, (c) Cooling capacity and condenser capacity, (d) Dühring diagram of the Silica gel/water adsorption system at rated conditions

Comparing these results with those obtained previously for the first operation mode (without heat recovery), it can be observed that there are almost no differences in the behavior of the system with the cycle time. The major differences in the system when operating in heat recovery mode are due to the amount of heat that is saved when heating the secondary water, and not due to the operation of the beds. The experimental and simulation results showed a considerable increase in the COP when the heat recovery is performed. Notice that the time delay when switching between inlet and outlet valves of the beds' secondary water circuits is very small (around 20 s).

Again, a good agreement between the simulation and the experimental results with heat recovery operation can be observed, and this further confirms the validity of the proposed model.

#### 6 System performance evaluation

**Table 4** summaries the performance of the proposed system under different operation modes and at the same nominal operating conditions. As it can be seen, clearly, the system with heat recovery provides considerably greater values of COP and a slight positive effect on the evaporator cooling capacity. Both experimental and simulation results show a very similar increase of the coefficient of performance (COP) when the heat recovery is performed, and similar effect on the cooling capacity. This proves again the suitability of the model as a tool to assist the design and optimization of cooling sorption systems.

**Table 4.** System performance at different operation modes

Operation mode	Experimental results		Simulation results		
	Q <sub>chill,Exp.</sub> [kW]	СОР	Q <sub>chill,Model</sub> [kW]	СОР	
1 <sup>st</sup> mode : No heat recovery	1.9	0.31	2.1	0.35	
2 <sup>nd</sup> mode : Heat recovery	2	0.45	2.2	0.50	

Based on the simulation results, the system is able to produce about 2.1 kW of average cooling capacity with COP of 0.35. If the auxiliary heat recovery circuit is considered, the system is able to produce about 2.2 kW of cooling capacity with COP of 0.50. Based on experimental results, the system is able to produce a mean cooling capacity of about 1.9 kW with COP of 0.31 for the second configuration mode, and a mean cooling capacity of 2.0 kW with COP of 0.45 for the second configuration mode.

It is clear that the heat recovery operation has a strong positive effect on the system performance (COP), and a slight positive effect on the cooling capacity. This operation strategy can be considered as a one of the key points to improve the performance of

adsorption systems. However, with heat recovery operation, the system becomes more complex (more piping, valves, and more complicated management).

#### 7 Conclusions

In this first part, Part I of a two-part study, an improved non-equilibrium dynamic model is developed to predict the dynamic performance of a silica gel/water adsorption chiller driven by engine waste heat. The model takes into account the kinetics of the adsorption/desorption processes, the pressure and temperature evaluation at each component of the system as well as the vapor flow in between components. The simulation results were validated against instantaneous experimental measurements realized at ECN laboratory of an adsorption chiller prototype. Different operation modes (configuration) based on the heat recovery operation were tested. The results showed that the system is able to produce an average cooling capacity of 2.1 kW (producing chilled water at 13°C) with COP of 0.35 when optimized for maximum cooling capacity. Both experimental and simulation results showed a considerable increase in the system COP (by about 43%) when the heat recovery operation is performed. A considerably good agreement between simulation and experimental results for both instantaneous and averaged data and for different operation modes were obtained. The developed model has proven to be an adequate tool to assist the design and optimize the operation of adsorption cooling systems. In Part II, the validated model is used to simulate and optimize the performance of an onboard adsorption system (implemented in a car) under different real start-up and ambient conditions to get a comfortable temperature in the automobile cabin.

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